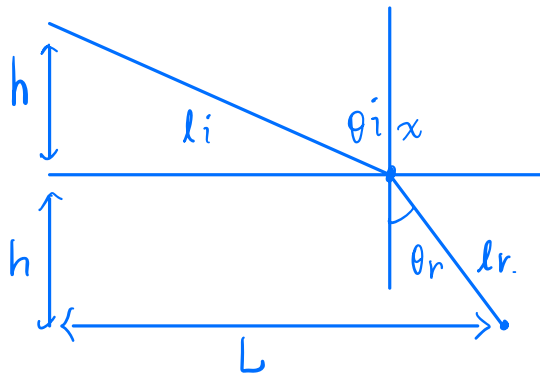


◦ 費馬定理推導折射定律



$$t = \frac{l_i}{v_i} + \frac{l_r}{v_r}$$

$$= \frac{\sqrt{x^2 + h^2}}{\frac{c}{n_i}} + \frac{\sqrt{(L-x)^2 + h^2}}{\frac{c}{n_r}}$$

Find extremum of  $t$ . (According to Fermat's principle)

$$\frac{dt}{dx} = \frac{2x}{\sqrt{x^2 + h^2}} \frac{c}{n_i} + \frac{-2(L-x)}{\sqrt{(L-x)^2 + h^2}} \frac{c}{n_r} = 0$$

$$\boxed{\frac{x}{\sqrt{x^2 + h^2}}} n_i = \boxed{\frac{L-x}{\sqrt{(L-x)^2 + h^2}}} n_r \Rightarrow n_i \sin \theta_i = n_r \sin \theta_r \text{ (Snell's Law)}$$

$\sin \theta_i$                        $\sin \theta_r$