

VAE loss

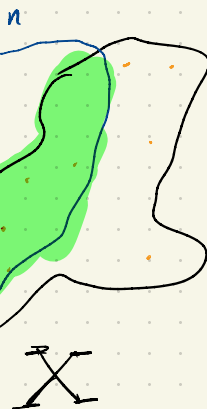
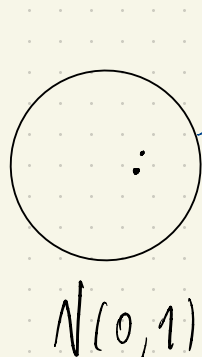
z

\times

$$L = \|x_i - \bar{x}_i\|_2 + \mathbb{E} L(P(z), N(0, 1))$$

$$D(x) \rightarrow [0, 1]$$

$$G: z \rightarrow x$$



$$L_D = -\mathbb{E}_{x \sim X} \log_2 D(x) - \mathbb{E}_{z \sim N(0, 1)} (1 - \log_2 D(G(z)))$$

$$L_G = \mathbb{E}_{z \sim N(0,1)} (1 - \log_2 D(G(z)))$$

$$L(G, D) = \min_D \max_G - \mathbb{E}_{x \sim X} \log_2 D(x) - \mathbb{E}_{z \sim N(0,1)} (1 - \log_2 D(G(z)))$$

$$\begin{array}{l} 1) L \xrightarrow{D} \min \\ 2) L \xrightarrow{G} \max \end{array} \quad \left. \begin{array}{l} \times 5 \quad \bar{x} + f \\ \times 1 \quad \bar{x} + f \end{array} \right\}$$

$$- \int_X P(x) \log_2 D(x) dx - \int_Z P_z(z) (1 - \log_2 D(G(z))) dz$$

$$- \int_X P(x) \log_2 D(x) dx - \int_X q(x) (1 - \log_2 D(x)) dx =$$

$$= - \int_X [P(x) \log_2 D(x) + q(x) (1 - \log_2 D(x))] dx$$

$$D^*(x) = \frac{p(x)}{p(x) + q(x)} = \frac{1}{2}$$

$$- \int_x \left(p(x) \log_2 \frac{p(x)}{p(x) + q(x)} + q(x) \log_2 \frac{q(x)}{p(x) + q(x)} \right) dx =$$

$$= \left[KL(p(x) \parallel \frac{p(x) + q(x)}{2}) + \right. \\ \left. + KL(q(x) \parallel \frac{p(x) + q(x)}{2}) \right]$$

$$JS(p \parallel q) = KL(p(x) \parallel \frac{p(x) + q(x)}{2}) + \\ + KL(q(x) \parallel \frac{p(x) + q(x)}{2})$$

$$I = -\log p(x),$$

$$H(p) = E I = - \int_x p(x) \log p(x) dx$$

$$KL(P \parallel q) = \mathbb{E}(I_p(x) - I_q(x)) =$$

$$= \int_x P(x) [-\log P(x) + \log q(x)] =$$

$$= - \int_x P(x) \log \frac{P(x)}{q(x)}.$$

$$KL(P \parallel q) = \mathbb{E}_{x \sim P} \log_2 \frac{q(x)}{P(x)}$$

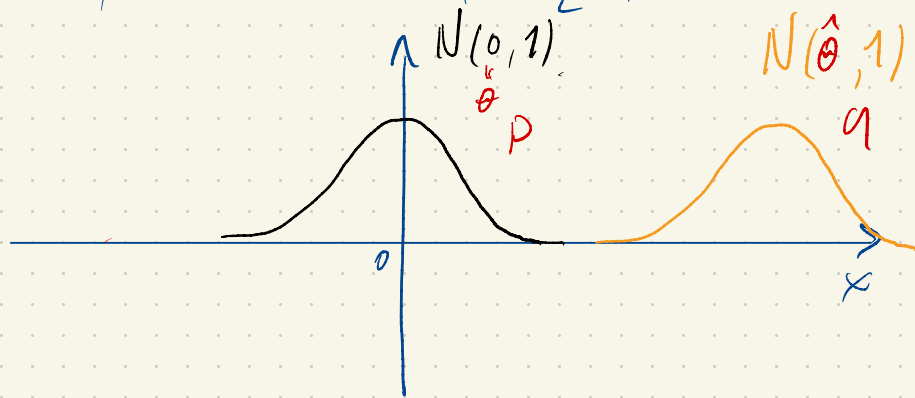
$\theta = \hat{\theta} = 0 \quad KL(P \parallel q) = 0$
 $\theta = 100 \sim \infty$

$$KL(Q \parallel P) = \mathbb{E}_{x \sim q} \log_2 \frac{P(x)}{q(x)}$$

$\theta = \hat{\theta} \quad KL(Q \parallel P) = 0$
 ∞

$$JS(P, q) = KL(P \parallel \frac{P+q}{2}) + KL(q \parallel \frac{P+q}{2})$$

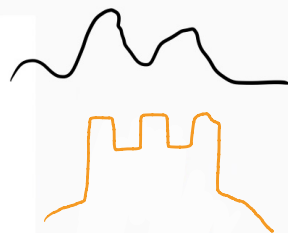
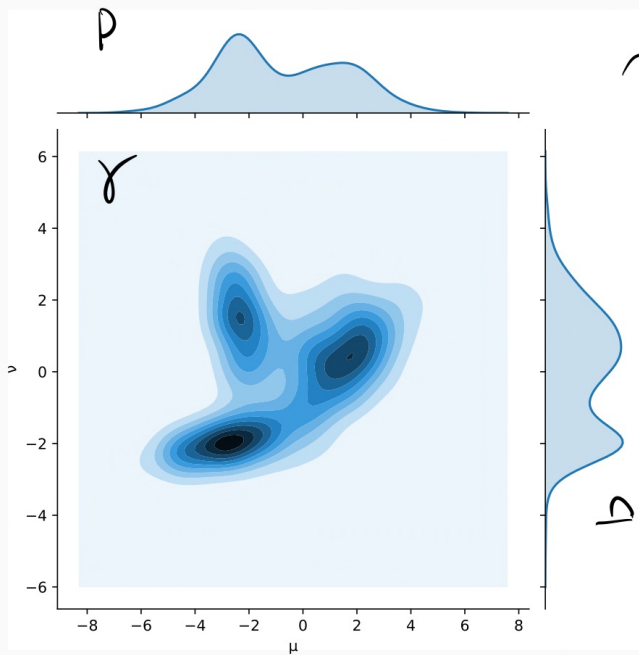
$\theta = \hat{\theta} = 0$
 $\theta = 100$
 $\stackrel{2}{\sim} \text{const}$



$$W(P, q) = \|\hat{\theta} - \hat{\theta}\|_2$$

$$W(p, q) = \inf_{x, y \sim \gamma} \mathbb{E} \|x - y\|_2$$

wasserstein



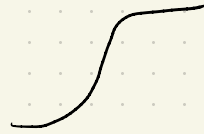
$$W(p, q) = \sup_f \left(\mathbb{E}_{x \sim p} f(x) - \mathbb{E}_{x \sim q} f(x) \right),$$

zge f funkcijska $p - q$ ϵ
 $K=1$

$$\forall x, y. |f(x) - f(y)| \leq K |x - y| \quad K=1$$

x ; $\sin(x)$,

$\sigma(x)$. $\tanh(x)$.



$\text{ReLU}(x)$. $-?$

$\max(0, x)$.

f - dnn.

$f_{\theta}(x)$ $\|\nabla_x f_{\theta}(x)\|$.

$$\left[\|\|\nabla_x f_{\theta}(x)\| - 1\|_2 \right]$$

$$L_D = -\mathbb{E}_{x \sim p} f_{\theta_f}(x) + \mathbb{E}_{x \sim q} f_{\theta_f}(x) \quad (1).$$

$$L_G = -\mathbb{E}_{x \sim q} f_{\theta_f}(x) = -\mathbb{E}_{z \sim N} f_{\theta_f}(G_{\theta_g}(z)) \quad (2)$$

f - critic.

optim = Adam (G.parameters())

optim.step()