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Control Systems Homework 5 Problem 1

```
A1 = [-20, -2, 0, 0; 10, 0, -10, 0; 0, 5, -100, -5; 0, 0, 4, 0];
B1 = [2;0;0;0];
C1 = [0,1,0,0];
D1 = [0];
G1 = ss(A1,B1,C1,D1);
tf(G1)
zpk(G1)
```

```
t1 = 0:0.01:10;
y1 = step(G1,t1);
plot(t1, y1);
xlabel('Time (seconds)');
ylabel('Gain');
```

ans =

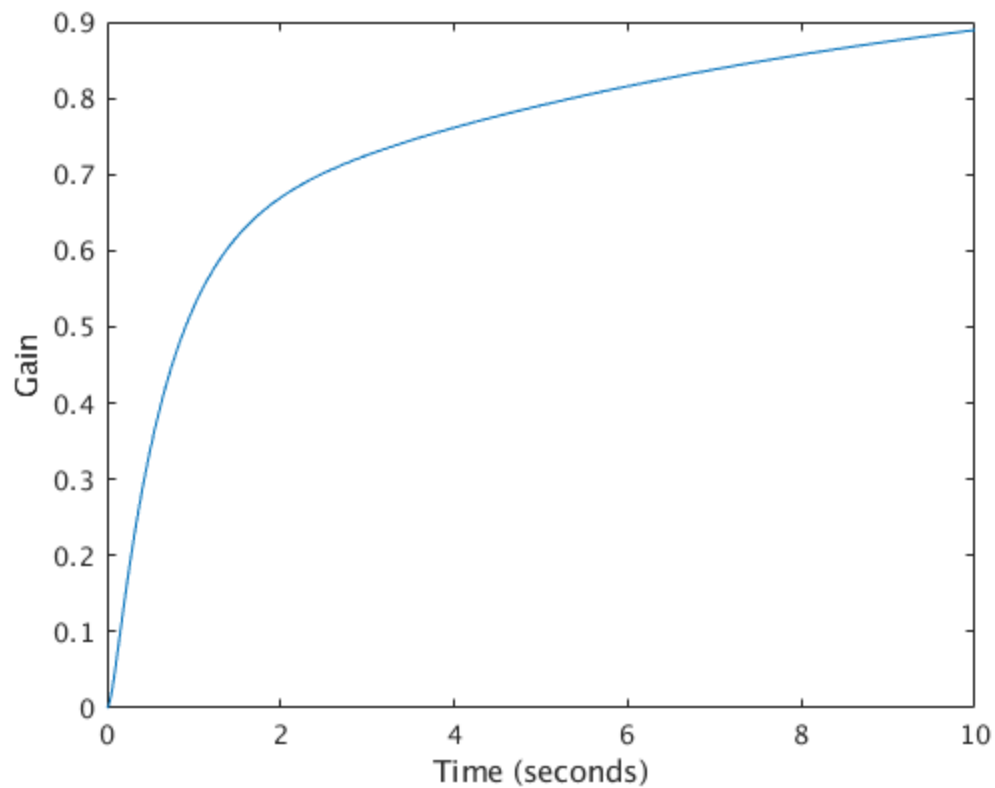
$$\frac{20 s^2 + 2000 s + 400}{s^4 + 120 s^3 + 2090 s^2 + 3400 s + 400}$$

Continuous-time transfer function.

ans =

$$\frac{20 (s+99.8) (s+0.2004)}{(s+99.3) (s+18.91) (s+1.67) (s+0.1276)}$$

Continuous-time zero/pole/gain model.



Control Systems Homework 5 Problem 2

```
A2 = [-20, -2, 0, 0; 10, 0, -10, 0; 0, 5, -100, -5; 0, 0, 4, 0];
B2 = [2;0;0;0];
C2 = [0,0,0,1];
D2 = [0];
G2 = ss(A2,B2,C2,D2);
tf(G2)
zpk(G2)
```

```
t2 = 0:0.01:50;
y2 = step(G2,t2);
figure;
plot(t2, abs(y2));
xlabel('Time (seconds)');
ylabel('Gain');
```

ans =

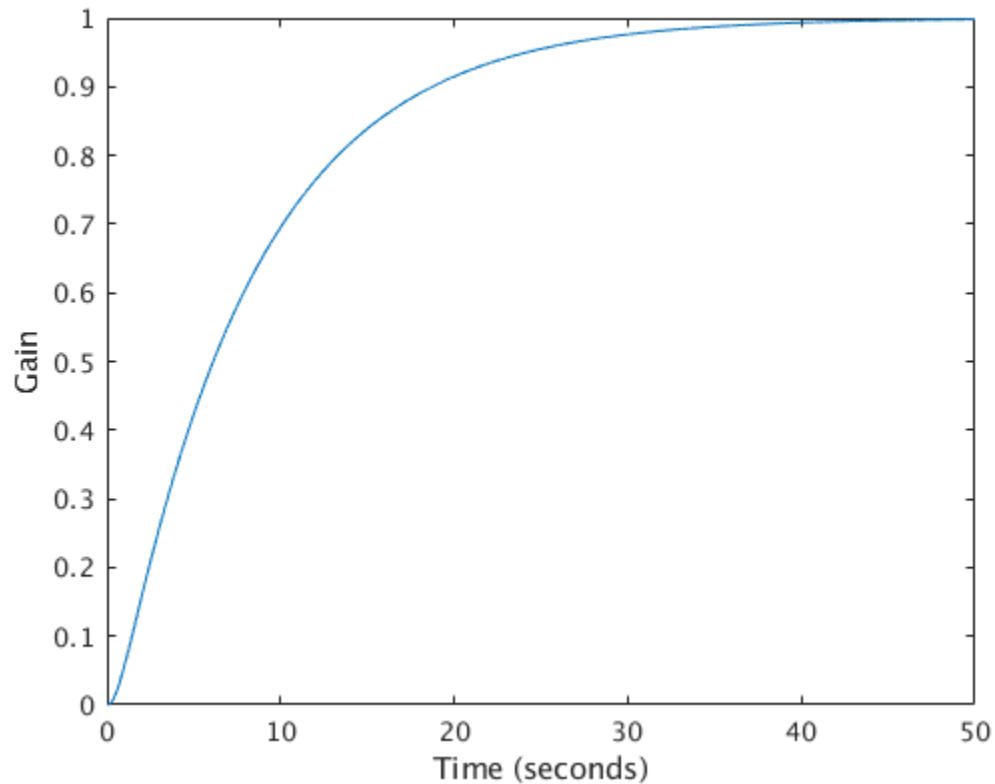
$$\frac{400}{s^4 + 120 s^3 + 2090 s^2 + 3400 s + 400}$$

Continuous-time transfer function.

`ans =`

$$\frac{400}{(s+99.3)(s+18.91)(s+1.67)(s+0.1276)}$$

Continuous-time zero/pole/gain model.



Control Systems Homework 5 Problem 3

```
A3 = [0, -10, 0, 0; 100, -0.2, -100, 0; 0, 5, 0, 5; 0, 0, -50, -83.33];
B3 = [10;0;0;0];
C3 = [0,1,0,0];
D3 = [0];
G3 = ss(A3,B3,C3,D3);
tf(G3)
zpk(G3)

t3 = 0:0.01:10;
y3 = step(G3,t3);
figure;
plot(t3, abs(y3));
xlabel('Time (seconds)');
```

```
ylabel('Gain');
```

```
ans =
```

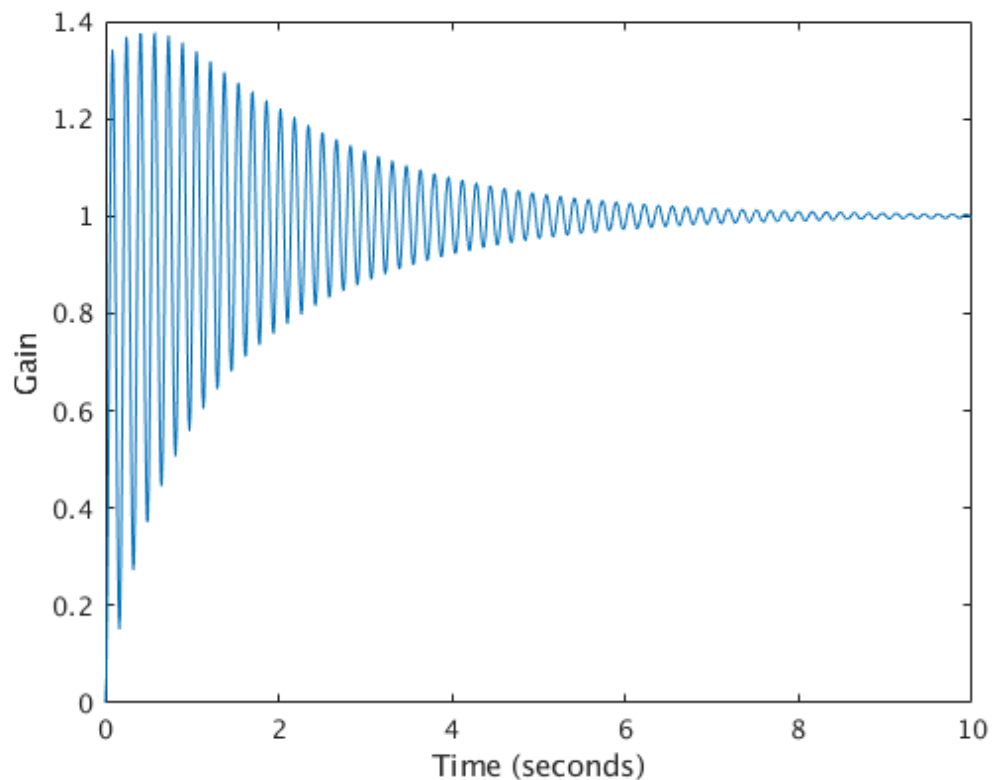
$$\frac{1000 s^2 + 83330 s + 2.5e05}{s^4 + 83.53 s^3 + 1767 s^2 + 1.25e05 s + 2.5e05}$$

Continuous-time transfer function.

```
ans =
```

$$\frac{1000 (s+3.117) (s+80.21)}{(s+80.42) (s+2.053) (s^2 + 1.06s + 1514)}$$

Continuous-time zero/pole/gain model.



Control Systems Homework 5 Problem 4

```
C4 = 0.01; R41 = 10; R42 = 100;  
A4 = [-1/(C4*R42), -1/(C4*R41), 0; 1/(C4*R41), -1/(C4*R42), -1/  
(C4*R41); 0, 1/(C4*R41), -1/(C4*R42)-1/(C4*R41)];
```

```

B4 = [1/(C4*R41); 0; 0];
C4 = [0,0,1];
D4 = [0];
G4 = ss(A4,B4,C4,D4);
tf(G4)
zpk(G4)

t4 = 0:0.01:2;
y4 = step(G4,t4);
figure;
plot(t4, abs(y4));
xlabel('Time (seconds)');
ylabel('Gain');

```

```
ans =
```

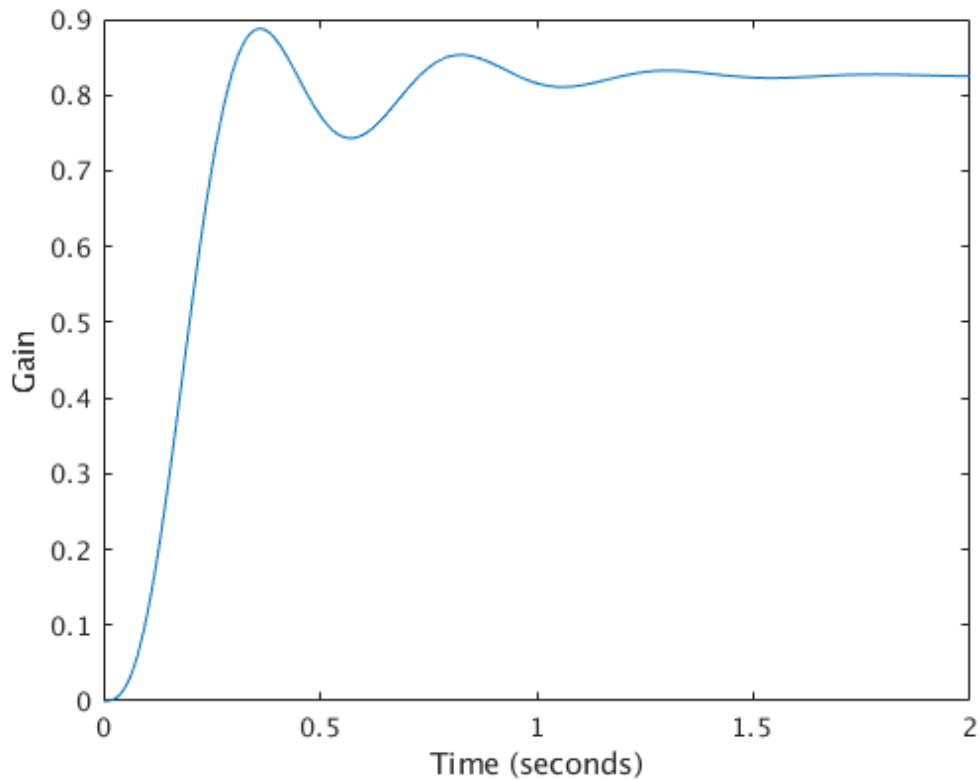
$$\frac{1000}{s^3 + 13 s^2 + 223 s + 1211}$$

Continuous-time transfer function.

```
ans =
```

$$\frac{1000}{(s+6.698) (s^2 + 6.302s + 180.8)}$$

Continuous-time zero/pole/gain model.



Control Systems Homework 5 Problem 5

```

C5 = 0.01; R51 = 10; R52 = 100;
A5 = [-1/(C5*R52), -1/(C5*R51), 0, 0, 0, 0, 0, 0, 0, 0; ...
      1/(C5*R51), -1/(C5*R52), -1/(C5*R51), 0, 0, 0, 0, 0, 0, 0; ...
      0, 1/(C5*R51), -1/(C5*R52), -1/(C5*R51), 0, 0, 0, 0, 0, 0; ...
      0, 0, 1/(C5*R51), -1/(C5*R52), -1/(C5*R51), 0, 0, 0, 0, 0; ...
      0, 0, 0, 1/(C5*R51), -1/(C5*R52), -1/(C5*R51), 0, 0, 0, 0; ...
      0, 0, 0, 0, 1/(C5*R51), -1/(C5*R52), -1/(C5*R51), 0, 0, 0; ...
      0, 0, 0, 0, 0, 1/(C5*R51), -1/(C5*R52), -1/(C5*R51), 0, 0; ...
      0, 0, 0, 0, 0, 0, 1/(C5*R51), -1/(C5*R52), -1/(C5*R51), 0; ...
      0, 0, 0, 0, 0, 0, 0, 1/(C5*R51), -1/(C5*R52), -1/(C5*R51); ...
      0, 0, 0, 0, 0, 0, 0, 0, 1/(C5*R51), -1/(C5*R52) - 1/(C5*R51)];
B5 = [(1/(C5*R51)); 0; 0; 0; 0; 0; 0; 0; 0; 0];
C5 = [0,0,0,0,0,0,0,0,0,1];
D5 = [0];
G5 = ss(A5,B5,C5,D5);

```

```
tf(G5)
zpk(G5)

t5 = 0:0.01:3;
y5 = step(G5,t5);
figure;
plot(t5, abs(y5));
xlabel('Time (seconds)');
ylabel('Gain');
```

```
ans =
```

1e10

$s^{10} + 20 s^9 + 1035 s^8 + 1.568e04 s^7 + 3.623e05 s^6 + 4e06 s^5$

$+ 5.004e07 s^4 + 3.669e08 s^3 + 2.335e09 s^2 + 8.752e09 s$

+

1.674e10

Continuous-time transfer function.

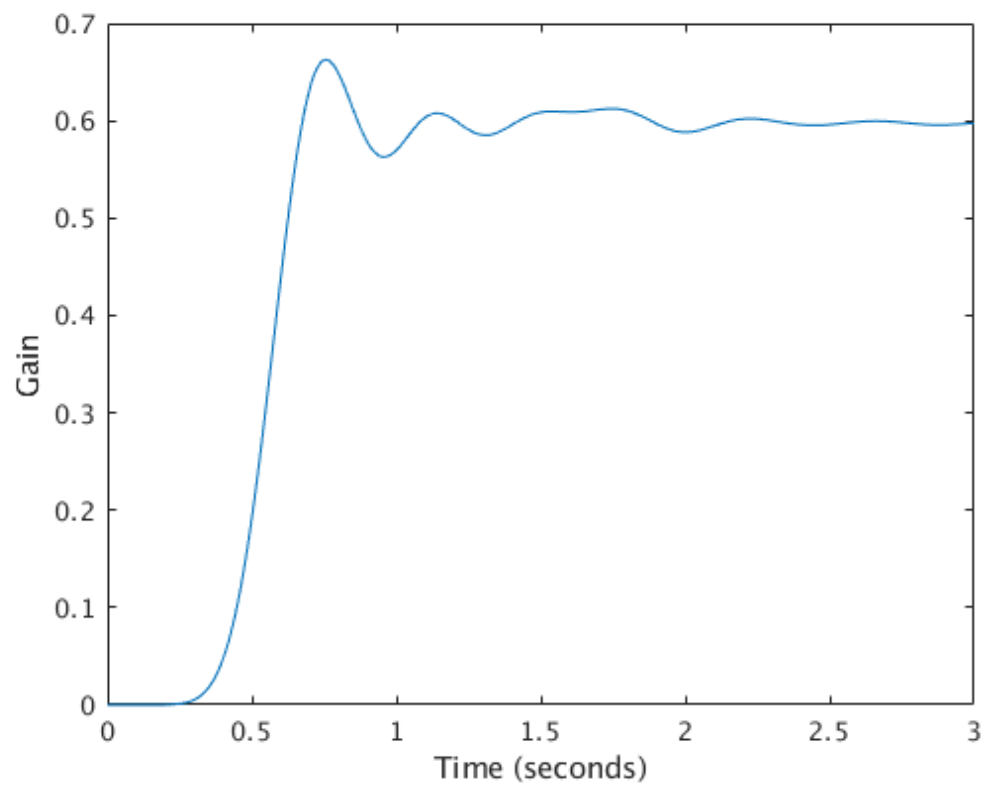
```
ans =
```

1e+10

$(s^2 + 6.74s + 16.56) (s^2 + 4.863s + 62.3) (s^2 + 3.547s + 160.5)$

$(s^2 + 2.68s + 275.8) (s^2 + 2.17s + 366.7)$

Continuous-time zero/pole/gain model.



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