Simulation of ALICE Project

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1 Introduction

ALICE_Simulation is a computer program that simulates the ALICE experiment that has been conducted at CERN since 1993, which consists of analyzing the collisions occurring between particles at very high energies⁽¹⁾. Those particles would create different particles following a probability distribution (Table1).

Particle Type	Probability
π^+	40%
π^-	40%
k^+	5.0%
k^-	5.0%
P^+	4.5%
P^-	4.5%
k^*	1.0%

Table 1: The table shows the probability of obtaining a specific particle from a collision of high energy particles

In the simulation, we generated a finite amount of particles from the collision of the flux in the particle accelerator, each with a proper momentum, mass, and resulting energy, to maintain the conservation of those properties. The goal of the experiment is to detect the existence of Kaon 0 (k^*) , a very rare particle that decays into either a Positive Pion (π^+) and Negative Kaon (k^-) or a Negative Pion (π^-) and Positive Kaon (k^+) , after only $5.2 \times 10^{-8} s$. We stored the data of momentum, energy, charge, and invariant mass of all the particles to detect the presence of differences that could indicate the existence of the Kaon.

The program we implemented stores the information about the particles and generates histograms from which we studied the system.

2 Code Structure

The code's division into different files and folders has the background idea of making it more orderly. There are eight files for the simulation program (one main file: mainE.cpp, one libraries file: library.hpp, three header files: ParticleType.hpp, ResonanceType.hpp, Particle.hpp, and three source files: ParticleType.cpp, ResonanceType.cpp, Particle.cpp) and one for the data analysis (analysis.C). The header

files contain the classes implemented for the proper functioning of the simulation, whereas the source files contain the implementation of the methods defined in the headers.

ParticleType Class

The class ParticleType creates a homonymous type that contains the name, the mass, and the charge of a particular particle, respectively as a std::string, a double, and an integer. This class has five methods, two of which are virtual.

ResonanceType Class

The ResonanceType class is a derived class from ParticleType and, in addition to the base class items, contains the information about the width of the particle as a double. The type defined with the name of this class creates a particle with a width, contrary to what happens to a ParticleType object, in which the width of the particle is always zero. This class has two methods, both of them are the override of the already existing virtual methods in the base class.

Particle Class

The class Particle is the one that allows the creation of a particle giving it a random momentum and making it decay into other particles if necessary. It also creates a set of particle type, each with a proper index as an identifier. The variables in this class are three momentum components (fPx, fPy, fPz), an array of ParticleType and its dimension (fParticleType, fMaxNumParticleType), an index of particle type (fNParticleType), and a numeric code proper of each particle type (fIndex). This class has, several methods, including some static, meanning they are accessible from the main without defining an object.

3 Generation

In the simulation, there had been 100000 collision events, each using a set of 100 particles. The particles resulting from the collisions were Positive Pions (π^+) , Negative Pions (π^-) , Positive Kaons (k^+) , Negative Kaons (k^-) , Protons (p^+) , Antiprotons (p^-) , and Resonance Kaons (k^*) , generated randomly using a uniform distribution and the probability shown in Table 1. The module of the momentum of the particles comes from an exponential distribution with a mean of 1. Its direction drives from the cartesian components:

$$\begin{cases} p_x = |p| \cdot \cos \theta \cdot \cos \phi \\ p_y = |p| \cdot \cos \theta \cdot \sin \phi \\ p_z = |p| \cdot \sin \theta \end{cases}$$
 (1)

Where the azimuthal angle theta (θ) and the polar angle phi (ϕ) are generated using a uniform random distribution respectively from 0 to π and the second from 0 to 2π . In the case that a Resonance Kaon is created from the collision of particles, it deacys into eather a Positive Pion and a Negative Kaon or a Negative Pion and a Positive Kaon with the same probability. The momentum of these new two particles comes from a normal distribution.

4 Analysis

The generation of particle types is compatible with the theoretical calculation as shown in Table. 2

Particle Type	Entries	Error	Theo. Ent.
π^+	4000250	2000	$4.0 \cdot 10^{6}$
π^-	3998440	2000	$4.0 \cdot 10^{6}$
k^+	500727	707	$5.0 \cdot 10^{5}$
k^-	499365	707	$5.0 \cdot 10^{5}$
P^+	450417	671	$4.5 \cdot 10^{5}$
P^-	450536	671	$4.5 \cdot 10^{5}$
k^*	100264	317	$1.0 \cdot 10^{5}$

Table 2: The table shows the entries from the simulation with the respective error calculated using root, and the theoretical entries calculated taking the percentage of each particle type from the total amount of particles.

The angles and momentum distributions are fitting to the relative uniform and exponential distribution as shown in table 3.

Distribution	Fit's Parameters	χ^2	D.O.F.	Reduced χ^2
Polar Angles (pol0)	9999 ± 3	973.8	999	0.9748
Azimutal Angols (pol0)	9999 ± 3	902.8	999	0.9037
Momentum (expo)	$9939 \pm 3) \cdot 10^{-4}$	959.2	998	0.9961

Table 3: The table shows the results of the fits from the histograms of the angles and the momentum.

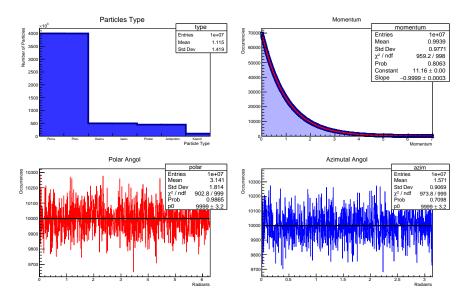


Figure 1: The image shows the fit between the uniform distribution compared with the histograms of the angles randomly generated and the histogram of the momentum with the exponential distribution.

It is possible to analyze these phenomena by looking at the histograms of the invariant mass, because its definition contains both the momentum and the energy of the particles, it is, therefore, conserved in the collision. The construction of the invariant mass histogram consist of counting the number of particles per mass invariant value, and to detect the resonance Kaon. We considered the histogram only for Pion and Kaon with different charges and we compared it with the histogram of the Pion and Kaon with the same charges. Because the resonance Kaon decays very quickly into those two particles with opposite charges, there should be a little "bump" in the first of those two histograms. A second approach consists of comparing the two histograms of the invariant mass of all the particles with the same charge and opposite charges.

Subtracting the two pairs of histograms gives, in both cases, a bell shape, fitting a normal distribution with mean being the mass of the resonance Kaon and sigma its error, should appear in the canvas. Comparing the results with the testing histogram of the decay, filled during the simulation, fitting a normal distribution, gives a value that stands inside the error.

In conclusion, from the previous considerations, we had been able to detect the presence

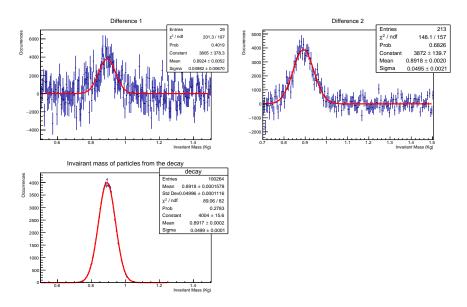


Figure 2: The image shows the histograms of the invariant mass calculated in the three different ways all of them fitted suing a normal distribution.

of a resonance Kaon and the result of the simulated experiment has been summarized in table 4.

Distribution	Mean	Sigma	Amplitude	χ^2
Inv. Mass. Decay	0.8917 ± 0.0002	4004 ± 15	999	1.086
Inv. Mass. Charges	0.8924 ± 0.0052	3805 ± 378	999	1.021
Inv. Mass. Kaon-Pion	0.8918 ± 0.0020	3872 ± 140	998	0.9433

Table 4: The table summarize the result of the fit of all the histograms.

Word Citation

1. Alice Experiment. CERN. https://home.cern/science/experiments/alice . November $29^{th},\,2021.$

Appendix

Code

4.1 ParticleType.hpp

```
1
   #ifndef PARTICLETYPE_HPP
   #define PARTICLETYPE_HPP
   #include <string>
  class ParticleType {
   private:
    const std::string fName;
9
    const double fMass;
10
    const int fCharge;
11
public:
13
     //Constructor
     ParticleType(std::string Name, double Mass, int Charge);
     //Getters
17
     std::string GetParticleName() const;
18
     double GetParticleMass() const;
19
     int GetParticleCharge() const;
20
     virtual double GetParticleWidth() const;
21
22
    //Printer
23
     virtual void Print() const;
   #endif
27
28
```

4.2 ParticleType.cpp

```
1
# #include <iostream >
3 #include <string>
4 #include "ParticleType.hpp"
6
  //Class ParticleType
  //-----
   //Constructor
  ParticleType::ParticleType(std::string Name, double Mass, int Charge):
  fName(Name),
  fMass(Mass),
fCharge(Charge)
  {}
13
14
15 //Getters
16 std::string ParticleType::GetParticleName() const { return fName; }
double ParticleType::GetParticleMass() const { return fMass; }
int ParticleType::GetParticleCharge() const { return fCharge; }
double ParticleType::GetParticleWidth() const { return 0; }
```

```
20
21
22
  //Printer
  void ParticleType::Print() const {
23
    std::cout << "Particle's Name: "<<fName << '\n';</pre>
24
    std::cout << "Particle's Mass: "<<fMass << '\n';</pre>
    std::cout << "Particle's Charge: "<<fCharge << '\n';</pre>
    std::cout << "----" << '\n';
27
28 }
  //----
29
30
```

4.3 ResonanceType.hpp

```
1
   #ifndef RESONANCETYPE_HPP
   #define RESONANCETYPE_HPP
3
  #include <string>
  #include "../ParticleType/ParticleType.hpp"
  class ResonanceType: public ParticleType {
9
   private:
    const double fWidth;
10
  public:
11
12
    //Constructor
13
    ResonanceType(std::string Name, double Mass, int Charge, double Width
14
15
    //Pritner
17
     void Print() const;
18
    //Getter
19
     double GetParticleWidth() const;
20
21 };
22
   #endif
23
24
```

4.4 ResonanceType.cpp

```
1
#include <iostream>
#include <string>
# #include "ResonanceType.hpp"
6
7 //Class ResonanceType
8 //----
  //Constructor
9
ResonanceType::ResonanceType(std::string Name, double Mass, int Charge,
     double Width):
ParticleType(Name, Mass, Charge),
  fWidth(Width)
{}
12
13
14
```

4.5 Particle.hpp

```
1
   #ifndef PARTICLE_HPP
   #define PARTICLE_HPP
3
   #include <string>
5
   #include <vector>
6
   #include "../ParticleType/ParticleType.hpp"
   enum class PL{Electron, Positron, Proton, Antiproton, PionPlus,
    PionMinus, PionO, KaonPlus, KaonMinus, KaonO};
  class Particle {
11
  private:
12
     double fPx;
13
    double fPy;
14
15
     double fPz;
16
     static const int fMaxNumParticleType = 10;
17
18
     static ParticleType* fParticleType[fMaxNumParticleType];
19
     static int fNParticleType;
     int fIndex;
20
21
     static int FindParticle(std::string PTBF); //Particle To Be Found
22
23
     void Boost(double bx, double by, double bz);
24
25
26
   public:
27
28
     Particle(std::string name, double Px, double Py, double Pz);
29
     Particle() = default;
     static void AddParticle(std::string name , double mass , int charge ,
30
     double with=0);
     static void AddParticle(PL particle);
31
32
     int GetIndex() const;
33
     int GetCharge() const;
34
     std::string GetName() const;
35
     double GetPx() const;
36
37
     double GetPy() const;
38
     double GetPz() const;
39
     double GetMass() const;
40
     double GetMomentum() const;
41
    double GetTotalEnergy() const;
    double GetInvMass(Particle& p) const;
42
double GetTrasMomentum() const;
```

```
44
     void SetIndex(std::string);
45
     void SetIndex(int index);
46
     void SetMomentum(double x, double y, double z);
47
48
     static void PrintTable();
49
     void PrintParticle() const;
50
51
     static void ParticleFeatures(PL& particle, int const N);
52
53
     int Decay2body(Particle &dau1,Particle &dau2) const;
54
55
56
   };
57
58
   #endif
```

4.6 Particle.cpp

```
1
   #include "../../libraries/library.hpp"
   #include <string>
  #include <iostream>
  #include <cstdlib>
   #include <cmath>
   #include <random>
  int Particle::fNParticleType = 0;
10
ParticleType* Particle::fParticleType[fMaxNumParticleType];
int Particle::FindParticle(std::string PTBF) {
14
15
    int i = 0;
     for(; i < fNParticleType; ++i) {</pre>
16
      std::string ParticleName = fParticleType[i]->GetParticleName();
17
       if(ParticleName == PTBF) { return i; }
18
       else if (fNParticleType == 0) { return 0; }
19
20
     }
21
     return 10;
22
23
  void Particle::AddParticle(std::string name, double mass, int charge,
24
    double width) {
     int const N = fNParticleType;
25
     int chack = FindParticle(name);
26
     if(N < fMaxNumParticleType && chack==10) {</pre>
27
       if (width!=0) {
28
         fParticleType[N] = new ResonanceType(name, mass, charge, width);
29
30
         ++fNParticleType;
31
32
         fParticleType[N] = new ParticleType (name, mass, charge);
33
         ++fNParticleType;
       }
34
35
     } else {
       std::cout << "!! -- The particle Does alreay excist -- !! " << '\n
36
```

```
37
38
39
   int Particle::Decay2body(Particle &dau1,Particle &dau2) const {
40
     if(GetMass() == 0.0){
41
        printf("Decayment cannot be preformed if mass is zero\n");
42
        return 1;
43
     }
44
45
     double massMot = GetMass();
46
     double massDau1 = dau1.GetMass();
47
     double massDau2 = dau2.GetMass();
48
49
     if(fIndex < 10){ // add width effect</pre>
50
51
       // gaussian random numbers
52
53
       float x1, x2, w, y1, y2;
54
55
       double invnum = 1./RAND_MAX;
56
       do {
57
         x1 = 2.0 * rand()*invnum - 1.0;
58
         x2 = 2.0 * rand()*invnum - 1.0;
59
          w = x1 * x1 + x2 * x2;
60
61
       } while ( w >= 1.0 );
62
63
       w = sqrt((-2.0 * log(w)) / w);
64
       y1 = x1 * w;
       y2 = x2 * w;
65
       massMot += fParticleType[fIndex]->GetParticleWidth() * y1;
66
67
     if(massMot < massDau1 + massDau2){</pre>
68
       printf("Decayment cannot be preformed because mass is too low in
69
     this channel\n");
       return 2;
70
71
     double pout = sqrt((massMot*massMot - (massDau1+massDau2)*(massDau1+
     massDau2))*(massMot*massMot - (massDau1-massDau2)*(massDau1-massDau2))
     )/massMot *0.5;
73
     double norm = 2*M_PI/RAND_MAX;
74
     double phi = rand()*norm;
     double theta = rand()*norm*0.5 - M_PI/2.;
75
     dau1.SetMomentum(pout*sin(theta)*cos(phi),pout*sin(theta)*sin(phi),
76
     pout*cos(theta));
     dau2.SetMomentum(-pout*sin(theta)*cos(phi),-pout*sin(theta)*sin(phi)
     ,-pout*cos(theta));
     double energy = sqrt(fPx*fPx + fPy*fPy + fPz*fPz + massMot*massMot);
78
     double bx = fPx/energy;
79
     double by = fPy/energy;
80
     double bz = fPz/energy;
81
     dau1.Boost(bx,by,bz);
82
     dau2.Boost(bx,by,bz);
83
     return 0;
84
   }
85
86
   void Particle::Boost(double bx, double by, double bz)
87
88 {
     double energy = GetTotalEnergy();
90 //Boost this Lorentz vector
```

```
double b2 = bx*bx + by*by + bz*bz;
91
      double gamma = 1.0 / sqrt(1.0 - b2);
92
      double bp = bx*fPx + by*fPy + bz*fPz;
93
      double gamma2 = b2 > 0 ? (gamma - 1.0)/b2 : 0.0;
94
95
      fPx += gamma2*bp*bx + gamma*bx*energy;
96
     fPy += gamma2*bp*by + gamma*by*energy;
97
     fPz += gamma2*bp*bz + gamma*bz*energy;
98
   7
99
100
   101
   Particle::Particle(std::string name, double Px = 0, double Py = 0,
     double Pz = 0):
   fPx(Px),
103
104
   fPy(Py),
   fPz(Pz),
   fIndex (FindParticle(name))
   { if(fIndex == 10) { std::cout << "!! -- This Type of Particle does not
      Excist -- !!" << '\n'; } }</pre>
108
    109
   int Particle::GetIndex() const { return fIndex; }
110
111
   int Particle::GetCharge() const {return fParticleType[fIndex]->
112
     GetParticleCharge(); }
113
114
   std::string Particle::GetName() const {return fParticleType[fIndex]->
     GetParticleName();}
115
   double Particle::GetPx() const { return fPx; }
116
117
   double Particle::GetPy() const { return fPy; }
118
119
   double Particle::GetPz() const { return fPz; }
120
121
   double Particle::GetMass() const {
122
     return (fParticleType[fIndex]->GetParticleMass());
123
124
125
126
   double Particle::GetMomentum() const {
127
    return (fPx*fPx + fPy*fPy + fPz*fPz);
128
129
   double Particle::GetTrasMomentum() const {
130
     return fPx*fPx + fPy*fPy;
131
132
133
   double Particle::GetTotalEnergy() const {
134
     double m = GetMass();
135
     double p2 = GetMomentum();
136
137
     return sqrt(m*m + p2);
   }
138
139
   double Particle::GetInvMass(Particle& p) const {
140
     double E1 = GetTotalEnergy();
141
     double E2 = p.GetTotalEnergy();
142
     double Psum = (fPx+p.GetPx())*(fPx+p.GetPx())+(fPy+p.GetPy())*(fPy+p.
143
     GetPy())+(fPz+p.GetPz())*(fPz+p.GetPz());
double M = sqrt((E1+ E2)*(E1+ E2) - Psum);
```

```
145
   return M;
146
147
   148
    void Particle::SetIndex(std::string type) {
149
      const int index = FindParticle(type);
      if (10 != index) {
       fIndex = index;
152
     }
153
   }
154
   void Particle::SetIndex(int index) {
156
     if(index < fNParticleType) {</pre>
157
       fIndex = index;
158
     }
159
   }
160
161
   void Particle::SetMomentum(double x, double y, double z) {
162
     fPx = x;
163
     fPy = y;
164
     fPz = z;
165
166
167
   168
169
   void Particle::PrintTable() {
170
     for(int i = 0; i < fNParticleType; ++i) {</pre>
171
       fParticleType[i]->Print();
     }
172
   }
173
174
   void Particle::PrintParticle() const {
175
     std::cout << "Particle index: " << fIndex << '\n';</pre>
176
     std::cout << "Particle name: "<< fParticleType[fIndex]->
177
     GetParticleName() << '\n';</pre>
     std::cout << "Px: "<< fPx << '\n';
178
     std::cout << "Py: "<< fPy << '\n';
179
      std::cout << "Pz: "<< fPz << '\n';
                                           ----" << '\n';
     std::cout << "-----
181
182
183
   184
   void Particle::ParticleFeatures(PL& particle, int const N) {
185
     int check;
186
     switch (particle) {
187
       case (PL::Electron):
188
          check = FindParticle("Electron");
189
          if (check == 10) {
190
           fParticleType[N] = new ParticleType ("Electron", 0.0005109, -1)
191
           ++fNParticleType;
192
         } else {
193
           std::cout << "!! -- The particle Does alreay excist -- !! " <<
194
      '\n';
         }
195
       break;
196
       case (PL::Proton) :
197
         check = FindParticle("Proton");
198
         if(check == 10) {
199
           fParticleType[N] = new ParticleType ("Proton", 0.938327, +1);
```

```
++fNParticleType;
201
           } else {
202
             std::cout << "!! -- The particle Does alreay excist -- !! " <<
203
       '\n';
           }
204
         break;
205
         case (PL::Positron) :
206
           check = FindParticle("Positron");
207
           if (check == 10) {
208
             fParticleType[N] = new ParticleType ("Positron", 0.0005109, +1)
209
             ++fNParticleType;
           } else {
211
             std::cout << "!! -- The particle Does alreay excist -- !! " <<
212
       '\n';
          }
213
        break;
214
         case (PL::PionMinus):
215
          check = FindParticle("Pion-");
216
           if(check == 10) {
217
             fParticleType[N] = new ParticleType ("Pion-", 0.13957, +1);
218
             ++fNParticleType;
219
           } else {
220
             std::cout << "!! -- The particle Does alreay excist -- !! " <<
221
       '\n';
222
         break;
224
         case (PL::PionPlus) :
           check = FindParticle("Pion+");
225
           if(check == 10) {
226
             fParticleType[N] = new ParticleType ("Pion+", 0.13957, -1);
227
             ++fNParticleType;
228
           } else {
229
             std::cout << "!! -- The particle Does alreay excist -- !! " <<
230
       '\n';
          }
231
         break;
         case (PL::Pion0) :
233
           check = FindParticle("Pion0");
234
235
           if(check == 10) {
             fParticleType[N] = new ParticleType ("Pion0", 0.1350, 0);
236
             ++fNParticleType;
           } else {
238
             std::cout << "!! -- The particle Does alreay excist -- !! " <<
239
       '\n';
           }
240
         break;
241
         case (PL::KaonPlus) :
242
           check = FindParticle("Kaon+");
243
           if(check == 10) {
244
             fParticleType[N] = new ParticleType ("Kaon+", 0.49367, +1);
245
             ++fNParticleType;
246
           } else {
247
             std::cout << "!! -- The particle Does alreay excist -- !! " <<
       '\n';
          }
249
250
         break;
         case (PL::KaonMinus) :
251
          check = FindParticle("Kaon-");
```

```
if (check == 10) {
253
             fParticleType[N] = new ParticleType ("Kaon-", 0.49367, -1);
254
255
             ++fNParticleType;
256
             std::cout << "!! -- The particle Does alreay excist -- !! " <<
257
       '\n';
           }
258
259
         break;
         case (PL::Kaon0) :
260
           check = FindParticle("Kaon0");
261
           if (check == 10) {
262
             fParticleType[N] = new ResonanceType ("Kaono", 0.89166, 0,
263
      0.05);
             ++fNParticleType;
264
265
           } else {
             std::cout << "!! -- The particle Does alreay excist -- !! " <<
       '\n';
267
          }
        break;
268
        case (PL::Antiproton) :
269
           check = FindParticle("Antiproton");
           if (check == 10) {
271
             fParticleType[N] = new ParticleType ("Antiproton", 0.93827, -1)
272
273
             ++fNParticleType;
274
          } else {
             std::cout << "!! -- The particle Does alreay excist -- !! " <<
       '\n';
          }
276
277
        break;
        default:
278
          std::cout << "!! -- Particle not in the list, add it using the</pre>
279
      standard AddParticle -- !!" << '\n';
280
281
282
    void Particle::AddParticle(PL particle) {
      int const N = fNParticleType;
285
      ParticleFeatures(particle, N);
286
    }
287
```

4.7 mainE.cpp

```
#include "../libraries/library.hpp"
   #include <iostream>
   #include <cmath>
   void ProgressionBar(int Progression) {
   double n = (Progression/5.22E8);
   std::cout << "[";
9
     int pos = 70 * n;
10
     for (int i = 0; i < 70; ++i) {</pre>
          if (i < pos) std::cout << "=";</pre>
11
          else if (i == pos) std::cout << ">";
12
          else std::cout << " ";</pre>
13
14
```

```
std::cout << "] " << int(n * 100.0) << " %\r";
15
     std::cout.flush();
16
17
18
19
   int main() {
   double const pi = 3.1415926535;
20
   int progression = 0;
   TRandom* Random = new TRandom();
22
   Random ->SetSeed(0);
23
24
   Particle::AddParticle(PL::PionPlus);
25
   Particle::AddParticle(PL::PionMinus);
26
   Particle::AddParticle(PL::KaonPlus);
27
  Particle::AddParticle(PL::KaonMinus);
28
29 Particle::AddParticle(PL::Proton);
  Particle::AddParticle(PL::Antiproton);
   Particle::AddParticle(PL::Kaon0);
31
32
   TH1F* type = new TH1F("type", "Particles Type", 7, 0, 7);
33
   type->GetXaxis()->TAxis::SetBinLabel(1, "Pion+");
34
   type->GetXaxis()->TAxis::SetBinLabel(2, "Pion-");
35
   type->GetXaxis()->TAxis::SetBinLabel(3, "Kaon+");
36
   type->GetXaxis()->TAxis::SetBinLabel(4, "kaon-");
37
   type->GetXaxis()->TAxis::SetBinLabel(5, "Proton");
38
   type->GetXaxis()->TAxis::SetBinLabel(6, "Antiproton");
39
   type->GetXaxis()->TAxis::SetBinLabel(7, "Kaon0");
40
42
   TH1F* momentum = new TH1F("momentum", "Momentum", 1000, 0, 7);
   TH1F* tmomentum = new TH1F("tmomentum", "Transversal Momentum", 1000,
43
     0, 7);
   TH1F* invmass = new TH1F("invmass", "Invarian Mass", 1000, 0, 5);
44
   TH1F* energy = new TH1F("energy", "Energy", 1000, 0, 7);
45
   TH1F* azim = new TH1F("azim", "Azimutal Angol", 1000, 0, pi);
46
   TH1F* polar = new TH1F("polar", "Polar Angol", 1000, 0, 2*pi);
47
   TH1F* invmassdis = new TH1F("invmassdis", "Invariant Mass opposite
48
     charges", 1000, 0, 5);
   TH1F* invmasscon = new TH1F("invmasscon", "Invariant Mass same charges"
     , 1000, 0, 5);
   TH1F* invppkmpmkp = new TH1F("invppkmpmkp", "Invariant Mass pion+/kaon-
50
      & pion-/kaon+", 1000, 0, 5);
51
   //invariant (i) mass (m) of pion (p) plus (p) and kaon (k) minus (m) or
      pion (p) minus (m) and kaon (k) plus (p)
52
   //i-m-p-p-k-m-p-m-k-p
   invppkmpmkp ->SetLineColor(kRed);
53
   TH1F* invppkppmkm = new TH1F("invppkppmkm", "Invariant Mass pion+/kaon+
54
      & pion-/kaon-", 1000, 0, 5);
   //invariant (i) mass (m) of pion (p) minus (m) and kaon (k) plus (p) or
55
      pion (p) minus (m) and kaon (k) minus (k)
   //i-m-p-p-k-p-p-m-k-m
   invppkppmkm ->SetLineColor(kBlue);
57
   TH1F* decay = new TH1F("decay", "Invairant mass of particles from the
58
     decay", 1000, 0, 5);
59
   invmass->Sumw2();
60
   invmassdis->Sumw2();
61
62 invmasscon->Sumw2();
invppkmpmkp->Sumw2();
64 invppkppmkm ->Sumw2();
65 decay->Sumw2();
```

```
66
    int const N = 100;
67
    int const extra = 20;
68
69
    Particle Particella[N+extra];
70
    for(int i = 0; i < 1E5; ++i) {</pre>
71
      int ExtraCounter = 0;
72
      for(int j = 0; j < (N); ++j) {
73
74
        double phi = 2*pi*Random->Uniform(0.0,1.0);
75
        double theta = pi*Random->Uniform(0.0,1.0);
76
77
        azim->Fill(theta);
78
79
        polar ->Fill(phi);
80
        double P = Random -> Exp(1.0);
81
82
        double Px = P*cos(phi)*cos(theta);
83
        double Py = P*cos(phi)*sin(theta);
84
        double Pz = P*sin(phi);
85
86
        Particella[j].SetMomentum(Px, Py, Pz);
87
88
        89
90
        double prob = Random -> Uniform (0.0,100.0);
91
        if(prob<40) {
93
          Particella[j].SetIndex("Pion+");
        } else if (prob<80) {</pre>
94
          Particella[j].SetIndex("Pion-");
95
        } else if (prob<85) {</pre>
96
          Particella[j].SetIndex("Kaon+");
97
        } else if (prob<90) {</pre>
98
          Particella[j].SetIndex("Kaon-");
99
        } else if (prob<94.5) {</pre>
100
          Particella[j].SetIndex("Proton");
101
        } else if (prob<99) {</pre>
          Particella[j].SetIndex("Antiproton");
        } else {
105
          Particella[j].SetIndex("Kaon0");
106
          int c = ExtraCounter + N;
          double chance = Random -> Uniform (0.0,1.0);
107
          if(chance < 0.5) {
108
             Particella[c].SetIndex("Pion+");
109
            Particella[c+1].SetIndex("Kaon-");
110
          } else {
111
             Particella[c].SetIndex("Pion-");
112
             Particella[c+1].SetIndex("Kaon+");
113
114
          int check = Particella[j].Decay2body(Particella[c], Particella[c
115
      +1]):
          if (check != 0) return check;
116
          double MassInvCondition = Particella[c].GetInvMass(Particella[c
117
      +1]);
          decay ->Fill (MassInvCondition);
118
          ExtraCounter = ExtraCounter +2;
119
120
        int index = Particella[j].GetIndex();
121
        type->Fill(index);
```

```
double PTModule = sqrt(Particella[j].GetTrasMomentum());
123
        tmomentum ->Fill(PTModule);
124
125
        double PModule = sqrt(Particella[j].GetMomentum());
        momentum ->Fill(PModule);
126
        double Energy = Particella[j].GetTotalEnergy();
127
        energy->Fill(Energy);
        ++progression;
129
      }
130
131
      double MassInv;
     for(int k = 0; k <N+ExtraCounter; ++k) {</pre>
132
       for(int h = k+1 ; h<N+ExtraCounter; ++h){</pre>
133
         MassInv = Particella[k].GetInvMass(Particella[h]);
134
         invmass ->Fill(MassInv);
135
         if ((Particella[k].GetCharge() * Particella[h].GetCharge()) < 0) {</pre>
136
           double MassInvCondition = Particella[k].GetInvMass(Particella[h
137
      ]);
           invmassdis->Fill(MassInvCondition);
138
         } else if((Particella[k].GetCharge() * Particella[h].GetCharge())
139
      > 0) {
           double MassInvCondition = Particella[k].GetInvMass(Particella[h
140
      ]);
           invmasscon ->Fill(MassInvCondition);
141
         }
142
         if (Particella[k].GetName() == "Pion+" && Particella[h].GetName()
143
      == "Kaon-") {
           double MassInvCondition = Particella[k].GetInvMass(Particella[h
144
      ]);
145
            invppkmpmkp ->Fill(MassInvCondition);
         } else if(Particella[k].GetName() == "Pion-" && Particella[h].
146
      GetName() == "Kaon+") {
            double MassInvCondition = Particella[k].GetInvMass(Particella[h
147
      ]);
            invppkmpmkp ->Fill(MassInvCondition);
148
         } else if (Particella[k].GetName() == "Pion+" && Particella[h].
149
      GetName() == "Kaon+") {
           double MassInvCondition = Particella[k].GetInvMass(Particella[h
150
      ]);
            invppkppmkm ->Fill(MassInvCondition);
         } else if(Particella[k].GetName() == "Pion-" && Particella[h].
      GetName() == "Kaon-") {
           double MassInvCondition = Particella[k].GetInvMass(Particella[h
      1):
           invppkppmkm ->Fill(MassInvCondition);
154
          ++progression;
156
157
158
      ProgressionBar(progression);
159
160
161
    TCanvas *canv1 = new TCanvas("canv1", "Type");
162
163
    type->Draw();
    TCanvas *canv2 = new TCanvas("canv2", "Momentum");
164
    canv2->Divide(1,2);
165
   canv2 -> cd(1);
166
    momentum ->Draw();
167
    canv2->cd(2);
168
    tmomentum ->Draw();
TCanvas *canv12 = new TCanvas("canv12", "energy");
```

```
energy ->Draw();
171
    TCanvas *canv4 = new TCanvas("canv4", "invMass");
172
173
    invmass -> Draw();
    TCanvas *canv5 = new TCanvas("canv5", "polarAngle");
    polar -> Draw();
    TCanvas *canv6 = new TCanvas("canv6", "azimutalAngle");
    azim->Draw();
    TCanvas *canv7 = new TCanvas("canv7", "Invariant Mass opposite charges"
     );
    invmassdis ->Draw("histo");
179
    TCanvas *canv8 = new TCanvas("canv8", "invariant Mass same charges");
180
    invmasscon -> Draw("histo");
181
    TCanvas *canv9 = new TCanvas("canv9", "Invariant Mass of pion and kaon"
182
     );
    canv9->Divide(1,2);
183
    canv9 -> cd(1);
    invppkppmkm ->Draw("histo");
186 canv9->cd(2);
    invppkmpmkp ->Draw("histo");
187
    TCanvas *canv10 = new TCanvas("canv10", "Invariant Mass pion+/kaon+ &
188
     pion-/kaon-");
    invppkppmkm ->Draw("histo");
189
    invppkmpmkp ->Draw("histo same");
190
    TCanvas *canv11 = new TCanvas("canv11", "Decay");
191
192
    decay -> Draw("histo");
193
    canv1->Print("../histograms/type.pdf");
    canv2->Print("../histograms/Momentums.pdf");
195
    canv12->Print("../histograms/energy.pdf");
196
    canv4->Print("../histograms/invMass.pdf");
197
    canv5->Print("../histograms/polarAngle.pdf");
198
    canv6->Print("../histograms/azimutalAngle.pdf");
199
    canv7->Print("../histograms/invmassdis.pdf");
200
    canv8->Print("../histograms/invmasscon.pdf");
201
    canv9->Print("../histograms/invppkmpmkp.pdf");
202
    canv10->Print("../histograms/invppkppmkm.pdf");
    canv11->Print("../histograms/decay.pdf");
205
    TFile* RFile = new TFile("ALICE_Simulation.root", "RECREATE");
206
    RFile->cd();
207
208
    type->Write();
    momentum ->Write();
209
    tmomentum ->Write();
    energy->Write();
211
    invmass->Write();
212
    polar -> Write();
213
214
    azim->Write();
    invmassdis->Write();
215
    invmasscon->Write();
   invppkmpmkp->Write();
217
   invppkppmkm ->Write();
218
    decay->Write();
219
   RFile -> ls();
220
    RFile -> Close();
221
222
223
   return 0;
224
    }
225
226
```

4.8 library.hpp

```
#ifndef LIBRARY_HPP
   #define LIBRARY_HPP
   #include "../script/ParticleType/ParticleType.hpp"
5
   #include "../script/ResonanceType/ResonanceType.hpp"
6
   #include "../script/Particle/Particle.hpp"
   #include "TRandom.h"
8
   #include "TAxis.h"
9
   #include "TH1.h"
10
   #include "TCanvas.h"
11
   #include "TFile.h"
13
   #endif
14
15
```

4.9 analysis.C

```
1
2
   void setStyle() {
    gROOT->SetStyle("Modern");
3
    gStyle->SetPalette(56);
4
    gStyle->SetOptFit(111);
5
6
   // Function that checks the generation of the values ///////
   void Checks() {
11
     int optarg = 1111;
12
13
     // Check of the generaation of particles ///////
14
     double particleProb[7];
15
16
     particleProb[0] = 0.4;
17
     particleProb[1] = 0.4;
18
     particleProb[2] = 0.05;
19
     particleProb[3] = 0.05;
20
21
     particleProb[4] = 0.045;
22
     particleProb[5] = 0.045;
     particleProb[6] = 0.01;
23
24
     TFile* c = new TFile("Alice_Simulation.root", "read");
25
     TH1F* type = (TH1F*)c->Get("type");
26
27
     cout << "Bin Content - Error - Theo. Val.\n";</pre>
     cout << " -----\n ";
28
     for(int i=1; i<8; ++i) {</pre>
29
      cout << type -> GetBinContent(i) << " - " << type -> GetBinError(i) << " - " <<</pre>
30
     particleProb[i-1]*1E7<< '\n';
       cout << " -----\n ";
31
32
33
     // CCheck of the shape of the momentum //////
34
     TCanvas* c1 = new TCanvas("c1", "Momento");
35
     TH1F* Mom = (TH1F*)c->Get("momentum");
36
```

```
Mom -> SetFillColorAlpha(kBlue, 0.3);
38
     Mom -> SetLineWidth(6);
39
     Mom -> Draw();
40
     c1->Print("../fit/Momentumfit.pdf");
41
     gPad->Update();
42
     TPaveStats* ft = (TPaveStats*)Mom->FindObject("stats");
43
     ft->SetOptFit(optarg);
44
     cout << " -----
45
     cout << Mom -> GetMean() << " - " << Mom -> GetRMS() << " - " << 1 << '\n';
46
     cout << " -----\n":
47
48
     // Cheack of the angles ////////////////
49
     TCanvas* c2 = new TCanvas("c2", "Angoli");
50
51
     c2->Divide(1,2);
52
     c2 -> cd(1);
53
     TH1F* Pol = (TH1F*)c->Get("polar");
54
     Pol -> Fit ("pol0");
55
     TF1* f1 = Pol->GetFunction("pol0");
56
     f1->SetLineColor(kBlack);
57
     Pol->SetLineColor(kRed);
58
     Pol -> Draw();
59
     gPad -> Update();
60
     TPaveStats* ft1 = (TPaveStats*)Pol->GetListOfFunctions()->FindObject(
61
     "stats");
     ft1->SetOptFit(optarg);
62
63
     gStyle -> SetStatW(.2);
64
     gStyle->SetStatH(.4);
65
     c2 -> cd(2);
66
     TH1F* azim = (TH1F*)c->Get("azim");
67
     azim ->Fit("pol0");
68
     TF1* f2 = azim->GetFunction("pol0");
69
     f2->SetLineColor(kBlack);
70
     azim -> SetLineColor(kBlue);
71
     azim ->Draw();
72
     gPad->Update();
73
     TPaveStats* ft5 = (TPaveStats*)azim->FindObject("stats");
74
     ft5->SetOptFit(optarg);
75
76
     c2->Print("../fit/anglesfit.pdf");
77
     // Check the entrance for each histogram
78
79
     TH1F* tmom = (TH1F*)c->Get("tmomentum");
80
     TH1F* imass = (TH1F*)c->Get("invmass");
81
     TH1F* en = (TH1F*)c->Get("energy");
82
     TH1F* imd = (TH1F*)c->Get("invmassdis");
83
     TH1F* imc = (TH1F*)c->Get("invmasscon");
84
     TH1F* inv1 = (TH1F*)c->Get("invppkmpmkp");
85
     TH1F* inv2 = (TH1F*)c->Get("invppkppmkm");
86
     TH1F* dec = (TH1F*)c->Get("decay");
87
88
     cout << " -----\n ";
89
     cout << "Entries Momentum: "<< Mom->GetEntries() << " - "<< 1E7 << '\n';</pre>
90
91
     cout << " -----\n ";
92
     cout << "Entries tMoment: " << tmom -> GetEntries () << " - " << 1E7 << '\n';
93
     cout << "----\n";
```

```
cout << "Entries invariant mass: "<< imass->GetEntries() << " - " << 1E5</pre>
96
     *101*100/2<<'\n';
97
      cout << " ---- \ n ";
98
      cout << "Entries energy: " << en -> GetEntries() << " - " << 1E7 << '\n';</pre>
99
      cout << "Entries invariant mass opposite: " << imd->GetEntries() << " - "</pre>
102
     <<1E5*101*100*0.495/2<<'\n';
      cout << "----\n":
104
     cout << "Entries invariant mass concord: " << imc -> GetEntries () << " - "</pre>
     <<1E5*101*100*0.495/2<<'\n';
106
      cout << " ---- \n ";
107
      cout << "Entries invariant mass 1: "<< inv1->GetEntries() << " - " << 1E5</pre>
     *101*100<<'\n';
109
     cout << "----\n":
110
     cout << "Entries invariant mass 2: "<< inv2->GetEntries() << " - " << 1E5</pre>
111
     *101*100<<'\n';
112
     cout << " -----\n ";
113
      cout < "Entries decay: " << dec -> GetEntries () << " - " << 1E7 *0.01 << '\n';
114
115
116
      cout<<"Entries azimutal angles: "<< azim->GetEntries()<<" - "<<1E7<<'</pre>
117
118
      cout << " -----\n ";
119
      cout << "Entries polar angles: "<< Pol->GetEntries() << " - " << 1E7 << '\n</pre>
120
121
122
123
124
   // Function that analyze the function for the detection of the
    Resonance Kaon ////////
127
128
   void analysis() {
     int optarg = 1111;
129
      TColor* myYellow = gROOT->GetColor(10);
130
      TFile* f = new TFile("Alice_Simulation.root", "read");
131
132
      TCanvas* c3 = new TCanvas("c3", "Cariche");
133
      TH1F* Im1 = (TH1F*)f->Get("invmassdis");
134
      TH1F* Im2 = (TH1F*)f->Get("invmasscon");
      TH1F* diff1 = new TH1F("diff1","Difference 1", 1000, 0, 5);
     diff1->Add(Im1,Im2, -1, 1);
diff1->Fit("gaus","","",0.5, 1.5);
137
138
      diff1->SetAxisRange(0.5, 1.5);
139
     diff1->Draw();
140
      gPad->Update();
141
     TPaveStats* ft2 = (TPaveStats*)diff1->FindObject("stats");
142
     c3->Print("../fit/Cariche_fit.pdf");
143
     ft2->SetOptFit(optarg);
144
     ft2->SetOptStat(10);
146
```

```
TCanvas* c4 = new TCanvas("c4", "Pioni e Kaoni");
147
      TH1F* Im3 = (TH1F*)f->Get("invppkmpmkp");
148
      TH1F* Im4 = (TH1F*)f->Get("invppkppmkm");
149
      TH1F* diff2 = new TH1F("diff2", "Difference 2", 1000, 0, 5);
150
      diff2->Add(Im3,Im4, 1, -1);
diff2->Fit("gaus","","",0.7, 1.5);
151
      diff2->SetAxisRange(0.7, 1.5);
153
      diff2->Draw();
154
      gPad->Update();
155
      TPaveStats* ft3 = (TPaveStats*)diff2->FindObject("stats");
156
      c4->Print("../fit/pion_kaon_fit.pdf");
157
      ft3->SetOptFit(optarg);
158
159
      ft3->SetOptStat(10);
160
      TCanvas* c5 = new TCanvas("c5", "Decadimento Kaoni");
161
162
      TH1F* kaon = (TH1F*)f->Get("decay");
      kaon->Fit("gaus","","",0.5, 1.25);
163
164
      kaon->SetAxisRange(0.5, 1.5);
      kaon -> Draw();
165
      gPad->Update();
166
      TPaveStats* ft4 = (TPaveStats*)kaon->FindObject("stats");
167
      ft4->SetOptFit(optarg);
168
      c5->Print("../fit/decay_fit.pdf");
169
170
      ft4->SetOptStat(2211);
171
172
```