

Team notebook

one more try

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1 Data Structures

1.1 2D BIT With Sparse SegTree

```

int root[maxn], seg[maxn * 100], L[maxn * 100], R[maxn * 100], nxt_id;
int modify(int id, int pos, int val, int l = 1, int r = n) {
    if (!id) {
        id = ++nxt_id;
    }
    if (l == r) {
        seg[id] = val;
        return id;
    }
    int mid = (l + r) / 2;
    if (pos <= mid) {
        L[id] = modify(L[id], pos, val, l, mid);
    } else {
        R[id] = modify(R[id], pos, val, mid + 1, r);
    }
    seg[id] = seg[L[id]] + seg[R[id]];
    return id;
}
int query(int id, int x, int y, int l = 1, int r = n) {
    if (l > y || r < x || !id) {
        return 0;
    }
    if (l >= x && r <= y) {
        return seg[id];
    }
    int mid = (l + r) / 2;
    return query(L[id], x, y, l, mid) + query(R[id], x, y, mid + 1, r);
}
void add(int x, int y) {
    for (; x <= n; x += x & -x) {
        root[x] = modify(root[x], y, 1);
    }
}
int get(int x, int lo, int hi) {
    int ret = 0;
    for (; x > 0; x -= x & -x) {
        ret += query(root[x], lo, hi);
    }
    return ret;
}
int get(int l, int r, int lo, int hi) {
    return get(r, lo, hi) - get(l - 1, lo, hi);
}

```

1.2 2D BIT with ordered_set

```

#include <ext/pb_ds/assoc_container.hpp>

```

```

#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template<class T> using ordered_set = tree<T, null_type, less<T>, rb_tree_tag,
    tree_order_statistics_node_update>;

struct BIT {
    ordered_set<int> f[maxn];
    void add(int i, int val) {
        for(; i <= maxn; i += i & -i)
            f[i].insert(val);
    }
    int get(int i, int lo, int hi) {
        int ret = 0;
        for (; i > 0; i -= i & -i) {
            ret += f[i].order_of_key(hi + 1) - f[i].order_of_key(lo);
        }
        return ret;
    }
    int get(int l, int r, int lo, int hi) {
        return get(r, lo, hi) - get(l - 1, lo, hi);
    }
};

```

1.3 BIT with range updates and point queries

```

/* Description: BIT with range updates and point queries */
#include <bits/stdc++.h>
#define pb push_back
#define all(a) a.begin(), a.end()
#define sz(a) (int)a.size()
#define x first
#define y second
using namespace std;
typedef long long ll;
typedef long double ld;
typedef pair<int, int> pii;
const int maxn = 1e5 + 100;

template<class T, int N>
struct BIT {
    T f[N + 1];
    BIT() {
        memset(f, 0, sizeof f);
    }
    void upd(int pos, T val) {
        for (; pos <= N; pos += pos & -pos)
            f[pos] += val;
    }
    void upd(int l, int r, T val) {
        upd(l, val);
        upd(r + 1, -val);
    }
}

```

```

T query(int pos) {
    T ret = 0;
    for (; pos > 0; pos -= pos & -pos) {
        ret += f[pos];
    }
    return ret;
}

};

int main()
{
    ios_base::sync_with_stdio(false), cin.tie(0);
    BIT<ll, 100000> tree;
    tree.upd(3, 5, 1);
    cout << tree.query(3) << "\n";
    cout << tree.query(4) << "\n";
    cout << tree.query(5) << "\n";
    cout << tree.query(2) << "\n";
    cout << tree.query(6) << "\n";
    return 0;
}

```

1.4 Binary Indexed Tree

```

template<class T, int N>
struct BIT {
    T f[N + 1];
    BIT() {
        memset(f, 0, sizeof f);
    }
    void upd(int pos, T val) {
        for (; pos <= N; pos += pos & -pos)
            f[pos] += val;
    }
    T query(int r) {
        T ret = 0;
        for (; r > 0; r -= r & -r) {
            ret += f[r];
        }
        return ret;
    }
    T query(int l, int r) {
        return query(r) - query(l - 1);
    }
};

```

1.5 DSU

```

template<int N>
struct DSU {

```

```

    int par[N + 1], sz[N + 1];
    DSU() {
        for (int i = 0; i <= N; i++) {
            par[i] = i, sz[i] = 1;
        }
    }
    int root(int v) {
        return v == par[v] ? v : par[v] = root(par[v]);
    }
    bool unite(int a, int b) {
        a = root(a);
        b = root(b);
        if (a == b) {
            return false;
        }
        if (sz[a] < sz[b]) {
            swap(a, b);
        }
        sz[a] += sz[b];
        par[b] = a;
        return true;
    }
};

```

1.6 Lazy SegTree

```

#include <bits/stdc++.h>
#define pb push_back
#define all(a) a.begin(), a.end()
#define sz(a) (int)a.size()
#define x first
#define y second
using namespace std;
typedef long long ll;
typedef long double ld;
typedef pair<int, int> pii;
const int maxn = 1e5 + 100;

template<class T, int N>
struct SegTree {
    T seg[N * 4], lazy[N * 4];
    SegTree() {
        memset(seg, 0, sizeof seg);
        memset(lazy, 0, sizeof lazy);
    }
    void build(T arr[], int id = 1, int l = 0, int r = N - 1) {
        if (r == l) {
            seg[id] = arr[l];
            return;
        }
        int mid = (l + r) / 2;
        build(arr, id * 2, l, mid);

```

```

    build(arr, id * 2 + 1, mid + 1, r);
    seg[id] = seg[id * 2] + seg[id * 2 + 1];
}
void upd(int id, int l, int r, T val) {
    seg[id] += (T)(r - l + 1) * val;
    lazy[id] += val;
}
void shift(int id, int l, int r) {
    int mid = (l + r) / 2;
    upd(id * 2, l, mid, lazy[id]);
    upd(id * 2 + 1, mid + 1, r, lazy[id]);
    lazy[id] = 0;
}
void modify(int x, int y, T val, int id = 1, int l = 0, int r = N - 1) {
    if (l > y || r < x) {
        return;
    }
    if (l >= x && r <= y) {
        upd(id, l, r, val);
        return;
    }
    shift(id, l, r);
    int mid = (l + r) / 2;
    modify(x, y, val, id * 2, l, mid);
    modify(x, y, val, id * 2 + 1, mid + 1, r);
    seg[id] = seg[id * 2] + seg[id * 2 + 1];
}
T query(int x, int y, int id = 1, int l = 0, int r = N - 1) {
    if (l > y || r < x) {
        return 0;
    }
    if (l >= x && r <= y) {
        return seg[id];
    }
    shift(id, l, r);
    int mid = (l + r) / 2;
    return query(x, y, id * 2, l, mid) + query(x, y, id * 2 + 1, mid + 1, r);
}
};

```

1.7 Mergeable Segment Tree

```

/**
https://codeforces.com/contest/911/problem/G
**/
#include <bits/stdc++.h>
#define pb push_back
#define all(a) a.begin(), a.end()
#define sz(a) (int)a.size()
#define x first
#define y second
#define debug(...) cout << "[" << __VA_ARGS__ << ": " << __VA_ARGS__ << "]" \n

```

```

#define rd() abs((int)rng())
using namespace std;
typedef long long ll;
typedef long double ld;
typedef pair<int, int> pii;
const int maxn = 2e5 + 100;
const int mod = 1e9 + 7;
mt19937 rng(chrono::high_resolution_clock::now().time_since_epoch().count());

struct node {
    int l, r;
};
int n, q, ans[maxn], nxt_id;
node tree[maxn * 150];
int root[105];
pii split(int id, int k, int lo = 1, int hi = n) { /// >= goes to the right
    if (!id) {
        return {0, 0};
    }
    if (lo == hi) {
        return (lo >= k ? pii(0, id) : pii(id, 0));
    }
    int other = ++nxt_id;
    int mid = (lo + hi) / 2;
    if (k <= mid) {
        pii p = split(tree[id].l, k, lo, mid);
        tree[id].l = p.y;
        tree[other].l = p.x;
        return {other, id};
    } else {
        pii p = split(tree[id].r, k, mid + 1, hi);
        tree[id].r = p.x;
        tree[other].r = p.y;
        return {id, other};
    }
}
int merge(int a, int b) {
    if (!a) return b;
    if (!b) return a;
    tree[a].l = merge(tree[a].l, tree[b].l);
    tree[a].r = merge(tree[a].r, tree[b].r);
    return a;
}
int ins(int id, int pos, int lo = 1, int hi = n) {
    if (!id) id = ++nxt_id;
    if (lo == hi) return id;
    int mid = (lo + hi) / 2;
    if (pos <= mid) {
        tree[id].l = ins(tree[id].l, pos, lo, mid);
    } else {
        tree[id].r = ins(tree[id].r, pos, mid + 1, hi);
    }
    return id;
}
void go(int id, int x, int lo = 1, int hi = n) {

```

```

    if (!id) {
        return;
    }
    if (lo == hi) {
        ans[lo] = x;
        return;
    }
    int mid = (lo + hi) / 2;
    go(tree[id].l, x, lo, mid);
    go(tree[id].r, x, mid + 1, hi);
}
int main()
{
    ios_base::sync_with_stdio(false), cin.tie(0);
    cin >> n;
    for (int i = 1; i <= n; i++) {
        int x;
        cin >> x;
        root[x] = ins(root[x], i);
    }
    cin >> q;
    for (int i = 0; i < q; i++) {
        int l, r, x, y;
        cin >> l >> r >> x >> y;
        if (x == y) {
            continue; // DOESNT WORK IF X = Y
        }
        pii a = split(root[x], l);
        pii b = split(a.y, r + 1);
        root[y] = merge(root[y], b.x);
        root[x] = merge(a.x, b.y);
    }
    for (int i = 1; i <= 100; i++) {
        go(root[i], i);
    }
    for (int i = 1; i <= n; i++) {
        cout << ans[i] << " ";
    }
    cout << "\n";
    return 0;
}

```

1.8 Minimum Deque

```

struct MinDeque {
    deque<pii> D;
    int lo, hi;
    MinDeque() {
        lo = 1, hi = 1;
    }
    void ins(int val) {
        while (sz(D) && D.back().x >= val) {

```

```

            D.pop_back();
        }
        D.pb({val, hi++});
    }
    void del() {
        if (sz(D) && D.front().y == lo++) {
            D.pop_front();
        }
    }
    int get() {
        return sz(D) ? D.front().x : mod;
    }
};

```

1.9 Persistent SegTree

```

int root[maxn], seg[maxn * 60], L[maxn * 60], R[maxn * 60], next_id; // required
// size can be different depending on problem
void build(int id = 1, int l = 1, int r = n) {
    if (l == r) {
        return;
    }
    int mid = (l + r) / 2;
    L[id] = ++next_id;
    R[id] = ++next_id;
    build(L[id], l, mid);
    build(R[id], mid + 1, r);
}
int modify(int pos, int delta, int id, int l = 1, int r = n) {
    int new_id = ++next_id;
    seg[new_id] = seg[id] + delta;
    if (l == r) {
        return new_id;
    }
    int mid = (l + r) / 2;
    L[new_id] = L[id];
    R[new_id] = R[id];
    if (pos <= mid) {
        L[new_id] = modify(pos, delta, L[new_id], l, mid);
    } else {
        R[new_id] = modify(pos, delta, R[new_id], mid + 1, r);
    }
    return new_id;
}

```

1.10 Treap

```

/* Description: treap with max heap property */
#include <bits/stdc++.h>
#define pb push_back

```

```

#define all(a) a.begin(), a.end()
#define sz(a) (int)a.size()
#define x first
#define y second
using namespace std;
typedef long long ll;
typedef long double ld;
typedef pair<int, int> pii;
const int maxn = 1e5 + 100;
mt19937 rng(chrono::high_resolution_clock::now().time_since_epoch().count());

struct node {
    int val, pri, sz;
    node *l, *r;

    node(int v) {
        val = v, sz = 1, pri = rng();
        l = r = NULL;
    }

    void recalc() {
        sz = 1 + (l ? l->sz : 0) + (r ? r->sz : 0);
    }
};
typedef node* pnode;

pair<pnode, pnode> split(pnode t, int v) { /// >= v goes to the right
    if (!t) {
        return {t, t};
    }

    if (v <= t->val) {
        auto p = split(t->l, v);
        t->l = p.second;
        t->recalc();
        return {p.first, t};
    } else {
        auto p = split(t->r, v);
        t->r = p.first;
        t->recalc();
        return {t, p.second};
    }
}

pair<pnode, pnode> split_by_order(pnode t, int v) {
    if (!t) {
        return {t, t};
    }
    int tmp = t->l ? t->l->sz : 0;
    if (v <= tmp) {
        auto p = split_by_order(t->l, v);
        t->l = p.second;
        t->recalc();
        return {p.first, t};
    } else {

```

```

        auto p = split_by_order(t->r, v - tmp - 1);
        t->r = p.first;
        t->recalc();
        return {t, p.second};
    }
}

pnode merge(pnode left, pnode right) {
    if (!left) {
        return right;
    }
    if (!right) {
        return left;
    }

    if (left->pri > right->pri) {
        left->r = merge(left->r, right);
        left->recalc();
        return left;
    } else {
        right->l = merge(left, right->l);
        right->recalc();
        return right;
    }
}

pnode ins(pnode x, int v) {
    auto a = split(x, v);
    auto b = split(a.second, v + 1);
    return merge(a.first, merge(new node(v), b.second));
}

pnode del(pnode x, int v) {
    auto a = split(x, v), b = split(a.second, v + 1);
    return merge(a.first, b.second);
}

pnode root;

int order_of_key(int x) {
    auto a = split(root, x);
    int t = a.first ? a.first->sz : 0;
    root = merge(a.first, a.second);
    return t;
}

int find_by_order(int x) {
    auto a = split_by_order(root, x);
    auto b = split_by_order(a.first, x - 1);
    int t = b.second->val;
    root = merge(merge(b.first, b.second), a.second);
    return t;
}

int main()
{

```

```

ios_base::sync_with_stdio(false), cin.tie(0);
int Q;
cin >> Q;
for (int i = 0; i < Q; i++) {
    char c;
    int d;
    cin >> c >> d;
    if (c == 'I') {
        root = ins(root, d);
    } else if (c == 'D') {
        root = del(root, d);
    } else if (c == 'K') {
        if (!root || root->sz < d) {
            cout << "invalid\n";
        } else {
            cout << find_by_order(d) << "\n";
        }
    } else {
        cout << order_of_key(d) << "\n";
    }
}
}

```

2 Geometry

2.1 Convex Hull Trick

```

struct line {
    ll k, b;
    line() = default;
    line(ll kk, ll bb) {
        k = kk;
        b = bb;
    }
    ll eval(ll x) {
        return k * x + b;
    }
};

ld inter(line f, line s) {
    return 1.0 * (s.b - f.b) / (f.k - s.k);
}

int siz, it;
line hull[maxn];
void add(line a) {
    while (siz >= 2 && inter(hull[siz - 1], hull[siz - 2]) >= inter(hull[siz - 2], a)) {
        siz--;
    }
    hull[siz++] = a;
}

// general approach is binary search

```

```

ll get(ll x) {
    // change to < for maximum
    while (it + 1 < siz && hull[it].eval(x) > hull[it + 1].eval(x)) {
        it++;
    }
    return hull[it].eval(x);
}

```

2.2 Convex Hull

```

#include <bits/stdc++.h>
using namespace std;
using ll = long long;
struct point {
    ll x, y;
    point(ll a = 0, ll b = 0) {
        x = a, y = b;
    }
    bool operator<(const point &o) const {
        return make_pair(x, y) < make_pair(o.x, o.y);
    }
    bool operator==(const point& o) const {
        return x == o.x && y == o.y;
    }
    point operator-(const point &b) const {
        return point(x - b.x, y - b.y);
    }
};

ll cross(point a, point b) {
    return a.x * b.y - a.y * b.x;
}

ll cross(point a, point b, point c) {
    return cross(b - a, c - a);
}

vector<point> convex_hull(vector<point>pts) {
    sort(pts.begin(), pts.end());
    pts.erase(unique(pts.begin(), pts.end()), pts.end());
    vector<point>top, bot;
    for (int i = 0; i < pts.size(); ++i) {
        while (bot.size() >= 2 && cross(bot[bot.size() - 2], bot.back(), pts[i])
            <= 0) {
            bot.pop_back();
        }
        bot.push_back(pts[i]);
    }
    bot.pop_back();
    for (int i = pts.size() - 1; i >= 0; --i) {
        while (top.size() >= 2 && cross(top[top.size() - 2], top.back(), pts[i])
            <= 0) {
            top.pop_back();
        }
        top.push_back(pts[i]);
    }
}

```

```

    }
    top.pop_back();
    top.insert(top.end(), bot.begin(), bot.end());
    return top;
}
int main() {
    ios_base::sync_with_stdio(false), cin.tie(0);
    int n;
    cin >> n;
    vector<point>pts;
    for (int i = 0; i < n; i++) {
        point p;
        cin >> p.x >> p.y;
        pts.push_back(p);
    }
    vector<point>hull = convex_hull(pts);
    cout << "-----\n";
    for (point p : hull) {
        cout << p.x << " " << p.y << "\n";
    }
    return 0;
}

```

2.3 Dynamic Convex Hull Trick

```

bool Q;
struct Line {
    mutable ll k, m, p;
    bool operator<(const Line& o) const {
        return Q ? p < o.p : k < o.k;
    }
};

struct LineContainer : multiset<Line> {
    // (for doubles, use inf = 1/.0, div(a,b) = a/b)
    const ll inf = LLONG_MAX;
    ll div(ll a, ll b) { // floored division
        return a / b - ((a ^ b) < 0 && a % b); }
    bool isect(iterator x, iterator y) {
        if (y == end()) { x->p = inf; return false; }
        if (x->k == y->k) x->p = x->m > y->m ? inf : -inf;
        else x->p = div(y->m - x->m, x->k - y->k);
        return x->p >= y->p;
    }
    void add(ll k, ll m) {
        auto z = insert({k, m, 0}), y = z++, x = y;
        while (isect(y, z)) z = erase(z);
        if (x != begin() && isect(--x, y)) isect(x, y = erase(y));
        while ((y = x) != begin() && (--x)->p >= y->p)
            isect(x, erase(y));
    }
    ll query(ll x) {

```

```

        assert(!empty());
        Q = 1; auto l = *lower_bound({0,0,x}); Q = 0;
        return l.k * x + l.m;
    }
};

```

2.4 Point

```

const ld eps = 1e-9;
int sgn(ld a) {
    return (a > 0) - (a < 0);
}
struct point {
    // Use ll everywhere instead of ld if coordinates are always integers
    ld x, y;
    point(ld a = 0, ld b = 0) {
        x = a, y = b;
    }
    bool operator==(const point& o) const {
        return x == o.x && y == o.y;
    }
    point operator+(const point &b) const {
        return point(x + b.x, y + b.y);
    }
    point operator-(const point &b) const {
        return point(x - b.x, y - b.y);
    }
    point operator*(const ld &a) const {
        return point(x * a, y * a);
    }
    point operator/(const ld &a) const {
        return point(x / a, y / a);
    }
    ld vlensq() {
        return x * x + y * y;
    }
    ld vlen() {
        return sqrtl(vlensq());
    }
    point perp() const {
        return point(-y, x);
    }
};
ld dot(point a, point b) {
    return a.x * b.x + a.y * b.y;
}
ld cross(point a, point b) {
    return a.x * b.y - a.y * b.x;
}
point proj(point v, point u) {
    // projection of v onto u
    return u * (dot(v, u) / dot(u, u));
}

```



```

}
// check if line segments AB and CD intersect
bool isect(point a, point b, point c, point d) {
    int A = sgn(cross(c - a, d - a));
    int B = sgn(cross(c - b, d - b));
    if (A * B != 0 && A == B) {
        return false;
    }
    int C = sgn(cross(a - c, b - c));
    int D = sgn(cross(a - d, b - d));
    if (C * D != 0 && C == D) {
        return false;
    }
    return true;
}
// intersection point of line segments AB and CD
point inter(point a, point b, point c, point d) {
    point ab = b - a;
    point cd = d - c;
    ld top = cross(a, ab) - cross(c, ab);
    ld bot = cross(cd, ab);
    // if(cd.x * top % bot != 0) // FLOATING POINT - CHANGE TO DOUBLE IF NECESSARY
    // return point(mod, mod);
    // if(cd.y * top % bot != 0) // FLOATING POINT - CHANGE TO DOUBLE IF NECESSARY
    // return point(mod, mod);
    ld X = c.x + cd.x * top / bot;
    ld Y = c.y + cd.y * top / bot;
    // or alternatively (works with doubles)
    // return c + cd * (top / bot)
    return point(X, Y);
}
// checks if circles with centers a, b and radiuses r1, r2 intersect
// intersection points are written to parameter out
bool circleInter(point a, point b, double r1, double r2, pair<point, point>* out) {
    if (a == b) { assert(r1 != r2); return false; }
    point vec = b - a;
    double d2 = vec.vlensq(), sum = r1+r2, dif = r1-r2,
    p = (d2 + r1*r1 - r2*r2)/(d2*2), h2 = r1*r1 - p*p*d2;
    if (sum*sum < d2 || dif*dif > d2) return false;
    point mid = a + vec*p, per = vec.perp() * sqrt(fmax(0, h2) / d2);
    *out = {mid + per, mid - per};
    return true;
}
// point in polygon
bool insidePoly(point p, vector<point>poly) {
    point mx = {-1e9, -1e9};
    for (point pp : poly) {
        if (pp.x > mx.x) {
            mx = pp;
        }
    }
    mx.x++;
    int cnt = 0;
    for (int i = 0; i < poly.size(); i++) {
        point a = poly[i];

```

```

        point b = poly[(i + 1) % poly.size()];
        if (isect(p, mx, a, b)) {
            cnt++;
        }
    }
    return cnt == 1;
}
// normalize vector
point toUnitVec(point vec) {
    return vec / vec.vlen();
}
// get unit vector that is orthogonal to given vector
point getUnitOrthog(point vec) {
    if (abs(vec.x) < eps || abs(vec.y) < eps) {
        swap(vec.x, vec.y);
        return toUnitVec(vec);
    }
    point orthog(1, 0);
    orthog.y = -orthog.x * vec.x / vec.y;
    return toUnitVec(orthog);
}

```

2.5 Rotational Sweep

```

#include <bits/stdc++.h>
#define pb push_back
#define all(a) a.begin(), a.end()
#define sz(a) (int)a.size()
#define x first
#define y second
#define debug(...) ["<<#__VA_ARGS__<<": "<<__VA_ARGS__<<"]
using namespace std;
typedef long long ll;
typedef long double ld;
typedef pair<int, int> pii;
const int maxn = 1e6 + 100;
const int mod = 1e9 + 7;
mt19937 rng(chrono::high_resolution_clock::now().time_since_epoch().count());
struct point
{
    ll x, y;
    point() {}
    point(ll a, ll b)
    {
        x=a;
        y=b;
    }
    point operator+(const point &o)
    {
        return point(x+o.x, y+o.y);
    }
    point operator-(const point &o)

```

```

    {
        return point(x-o.x, y-o.y);
    }
};
ll cross(point a, point b)
{
    return a.x*b.y-a.y*b.x;
}
int n;
ll ans;
vector<point>v;
void sweep(int id) {
    vector<point>u;
    for(int i = 0; i < n; i++) {
        if(i != id) {
            u.push_back(v[i]);
        }
    }
    point p = v[id];
    sort(u.begin(), u.end(), [&](point a, point b) {
        if((a.y >= p.y) != (b.y >= p.y)) {
            return a.y >= p.y;
        }
        return cross(a - p, b - p) < 0;
    });
    int r = 0, cnt = 0;
    for(int l = 0; l < u.size(); l++) {
        if (l > 0) {
            cnt--;
        }
        int rr = (r + 1) % u.size();
        while (cnt != n - 2 && cross(u[l] - p, u[rr] - p) <= 0) {
            cnt++;
            rr = (rr + 1) % u.size();
        }
        r = rr - 1;
        ll R = (r - l + u.size()) % u.size(), L = n - R - 2;
        ans += R * (R - 1) / 2 * L * (L - 1) / 2;
    }
}
int main()
{
    ios_base::sync_with_stdio(false), cin.tie(0);
    cin >> n;
    v.resize(n);
    for(int i = 0; i < n; i++)
        cin >> v[i].x >> v[i].y;
    for(int i = 0; i < n; i++)
        sweep(i);
    cout << ans / 2 << "\n";
    return 0;
}

```

3 Graphs

3.1 2-Edge Connected Components

```

/* Description: Finding 2-edge connected components using Tarjan's algorithm and
DSU */
#include <bits/stdc++.h>
#define pb push_back
using namespace std;
typedef long long ll;
typedef long double ld;
const int maxn = 3e5 + 100;
int n, m, val[maxn], low[maxn], timer = 1, par[maxn], sz[maxn], vis[maxn];
vector<int> adj[maxn], g[maxn];
vector<pair<int, int>> bridges;
int root(int v) {
    return v == par[v] ? v : par[v] = root(par[v]);
}
void unite(int a, int b) {
    a = root(a), b = root(b);
    if (a == b) {
        return;
    }
    if (sz[a] < sz[b]) {
        swap(a, b);
    }
    par[b] = a;
    sz[a] += sz[b];
}
void tarjan(int v, int p = -1) {
    val[v] = low[v] = timer++;
    for (auto to : adj[v]) {
        if (to == p) {
            continue;
        }
        if (!val[to]) {
            tarjan(to, v);
            low[v] = min(low[v], low[to]);
            if (low[to] > val[v]) {
                bridges.push_back({v, to});
            } else {
                unite(v, to);
            }
        } else {
            low[v] = min(low[v], val[to]);
        }
    }
}
void construct() {
    for (pair<int, int> p : bridges) {
        int a = root(p.first), b = root(p.second);
        g[a].push_back(b);
        g[b].push_back(a);
    }
}

```

```

}
int main() {
    ios_base::sync_with_stdio(false), cin.tie(0);
    int n, m;
    cin >> n >> m;
    for (int i = 1; i <= n; i++) {
        par[i] = i, sz[i] = 1;
    }
    for (int i = 0; i < m; i++) {
        int a, b;
        cin >> a >> b;
        adj[a].push_back(b);
        adj[b].push_back(a);
    }
    tarjan(1);
    construct();
    int v = 1, d = 0;
    for (int i = 1; i <= n; i++) {
        if (!g[i].empty()) {
            v = i;
        }
    }
    queue<pair<int, int>> Q;
    Q.push({v, 0});
    vis[v] = 1;
    while (!Q.empty()) {
        v = Q.front().first;
        d = Q.front().second;
        Q.pop();
        for (auto to : g[v]) {
            if (!vis[to]) {
                vis[to] = 1;
                Q.push({to, d + 1});
            }
        }
    }
    Q.push({v, 0});
    for (int i = 0; i < maxn; i++) {
        vis[i] = 0;
    }
    vis[v] = 1;
    while (!Q.empty()) {
        v = Q.front().first;
        d = Q.front().second;
        Q.pop();
        for (auto to : g[v]) {
            if (!vis[to]) {
                vis[to] = 1;
                Q.push({to, d + 1});
            }
        }
    }
    cout << d << "\n";
    return 0;
}

```

3.2 Bipartite Matching

```

int n;
bool vis[maxn];
int match[maxn];
vector<int>adj[maxn];
bool dfs(int v) {
    if (vis[v]) {
        return false;
    }
    vis[v] = true;
    for (int to : adj[v]) {
        if (match[to] == -1 || dfs(match[to])) {
            match[v] = to, match[to] = v;
            return true;
        }
    }
    return false;
}
void matching() {
    memset(match, -1, sizeof match);
    while (true) {
        memset(vis, 0, sizeof vis);
        bool found = false;
        for (int i = 1; i <= n; i++) {
            if (!vis[i] && match[i] == -1) {
                found |= dfs(i);
            }
        }
        if (!found) {
            break;
        }
    }
}

```

3.3 Dijkstra

```

ll D[maxn];
vector<pii> adj[maxn];
void Dijkstra(int st) {
    fill(D, D + maxn, LLONG_MAX);
    priority_queue<pii, vector<pii>, greater<pii>> Q;
    Q.push({D[st] = 0, st});
    while (!Q.empty()) {
        pii v = Q.top();
        Q.pop();
        if (D[v.y] < v.x) {
            continue;
        }
        for (auto to : adj[v.y]) {
            if (v.x + to.y < D[to.x]) {

```

```

        Q.push({D[to.x] = v.x + to.y, to.x});
    }
}
}
}

```

3.4 Dinic

```

struct edge {
    int to, flow, cap;
};
vector<edge> edges;
vector<int> adj[maxn];
void add_edge(int a, int b, int cap) {
    edge ab = {b, 0, cap};
    edge ba = {a, 0, 0};
    adj[a].push_back(edges.size());
    edges.push_back(ab);
    adj[b].push_back(edges.size());
    edges.push_back(ba);
}
int vis[maxn], ptr[maxn], level[maxn], s, t;
bool bfs() {
    queue<int> Q;
    Q.push(s);
    while (!Q.empty()) {
        int v = Q.front();
        Q.pop();
        for (int id : adj[v]) {
            edge e = edges[id];
            if (e.cap - e.flow < 1) {
                continue;
            }
            if (level[e.to] != -1) {
                continue;
            }
            level[e.to] = level[v] + 1;
            Q.push(e.to);
        }
    }
    return level[t] != -1;
}
int dfs(int v, int pushed) {
    if (pushed == 0) {
        return 0;
    }
    if (v == t) {
        return pushed;
    }
    for (int &j = ptr[v]; j < adj[v].size(); j++) {
        edge e = edges[adj[v][j]];
        if (level[v] + 1 != level[e.to] || e.cap - e.flow < 1) {

```

```

            continue;
        }
        int tr = dfs(e.to, min(pushed, e.cap - e.flow));
        if (tr == 0) {
            continue;
        }
        edges[adj[v][j]].flow += tr;
        edges[adj[v][j] ^ 1].flow -= tr;
        return tr;
    }
    return 0;
}
int max_flow() {
    int flow = 0;
    while (true) {
        memset(level, -1, sizeof level);
        level[s] = 0;
        if (!bfs()) {
            break;
        }
        memset(ptr, 0, sizeof ptr);
        while (int pushed = dfs(s, mod)) {
            flow += pushed;
        }
    }
    return flow;
}

```

3.5 Edmonds-Karp

```

struct edge {
    int to, flow, cap, cost;
};
vector<edge> edges;
vector<int> adj[maxn];
void add_edge(int a, int b, int cap) {
    adj[a].push_back(edges.size());
    edges.push_back({b, 0, cap});
    adj[b].push_back(edges.size());
    edges.push_back({a, 0, 0});
}
int vis[maxn], pid[maxn], s, t;
int bfs() {
    queue<pair<int, int>> Q;
    vis[s] = 1;
    Q.push({s, mod});
    while (!Q.empty()) {
        int v, flow;
        tie(v, flow) = Q.front();
        Q.pop();
        if (v == t) {
            return flow;

```

```

    }
    for (int j : adj[v]) {
        edge e = edges[j];
        if (!vis[e.to] && e.cap - e.flow > 0) {
            vis[e.to] = 1;
            pid[e.to] = j;
            Q.push({e.to, min(e.cap - e.flow, flow)});
        }
    }
}
return 0;
}
int max_flow() {
    int maxflow = 0;
    while (true) {
        memset(vis, 0, sizeof vis);
        int cur_flow = bfs();
        if (cur_flow == 0) {
            break;
        }
        maxflow += cur_flow;
        int v = t;
        while (v != s) {
            int j = pid[v];
            edges[j].flow += cur_flow;
            edges[j ^ 1].flow -= cur_flow;
            v = edges[j ^ 1].to;
        }
    }
    return maxflow;
}
}

```

3.6 Eulerian Tour

```

int n, m, even;
set<int> adj[maxn];
vector<int> tour;
void dfs(int v) {
    for (auto it = adj[v].begin(); adj[v].size() > 0;) {
        int to = *it;
        it = adj[v].erase(it);
        adj[to].erase(v);
        dfs(to);
    }
    tour.push_back(v);
}
int main() {
    ios_base::sync_with_stdio(false), cin.tie(0);
    cin >> n >> m;
    for (int i = 0; i < m; i++) {
        int a, b;
        cin >> a >> b;
    }
}

```

```

adj[a].insert(b);
adj[b].insert(a);
}
for (int i = 1; i <= n; i++) {
    if (adj[i].size() % 2 == 0) {
        ++even;
    }
}
if (even != n && even != n - 2) {
    /// no tour exists
    return 0;
}
int start = 1;
if (even == n - 2) {
    for (int i = 1; i <= n; i++) {
        if (adj[i].size() % 2 == 1) {
            start = i;
            break;
        }
    }
}
dfs(start);
for (int v : tour) {
    cout << v << " ";
}
cout << "\n";
return 0;
}

```

3.7 Hungarian

```

template<class T> bool ckmin(T& a, const T& b) { return a > b ? a = b, 1 : 0; }
template<class T> bool ckmax(T& a, const T& b) { return a < b ? a = b, 1 : 0; }

int hungarian(const vector<vector<int>> &a) {
    int n = sz(a) - 1, m = sz(a[0]) - 1; // jobs 1..n, workers 1..m
    vector<int> u(n + 1), v(m + 1); // potentials
    vector<int> p(m + 1); // p[j] -> job picked by worker j
    for (int i = 1; i <= n; i++) { // find alternating path with job i
        p[0] = i; int j0 = 0; // add "dummy" worker 0
        vector<int> dist(m + 1, INT_MAX), pre(m + 1, -1); // prev vertex on shortest path
        vector<bool> done(m + 1, false);
        do { // dijkstra
            done[j0] = true; // fix dist[j0], update dists from j0
            int i0 = p[j0], j1;
            int delta = INT_MAX;
            for (int j = 1; j <= m; j++)
                if (!done[j]) {
                    auto cur = a[i0][j] - u[i0] - v[j];
                    if (ckmin(dist[j], cur))
                        pre[j] = j0;
                }
        } while (j0);
    }
}

```

```

        if (ckmin(delta, dist[j]))
            j1 = j;
    }
    for(int j = 0; j <= m; j++) { // subtract constant from all edges going
        // from done -> not done vertices, lowers all
        // remaining dists by constant
        if (done[j])
            u[p[j]] += delta, v[j] -= delta;
        else
            dist[j] -= delta;
    }
    j0 = j1;
} while (p[j0]); // potentials adjusted so that all edge weights are
// non-negative
// perfect matching has zero weight and
// costs of augmenting paths do not change
while (j0) { // update jobs picked by workers on alternating path
    int j1 = pre[j0];
    p[j0] = p[j1];
    j0 = j1;
}
}
return -v[0]; // min cost
}

```

3.8 Min Cost Max Flow

```

struct edge {
    int to, flow, cap, cost;
    edge(int a = 0, int b = 0, int c = 0, int d = 0) {
        to = a, flow = b, cap = c, cost = d;
    }
};
vector<edge> edges;
vector<int> adj[maxn];
void add_edge(int a, int b, int cap, int cost) {
    edge ab(b, 0, cap, cost);
    edge ba(a, 0, 0, -cost);
    adj[a].push_back(edges.size());
    edges.push_back(ab);
    adj[b].push_back(edges.size());
    edges.push_back(ba);
}
int vis[maxn], pid[maxn], s, t;
int dist[maxn];
pii dijkstra() {
    priority_queue<pair<int, pii>, vector<pair<int, pii>>, greater<pair<int,
        pii>>> Q;
    vis[s] = 1;
    Q.push({0, {s, mod}});
    while (!Q.empty()) {
        int v, flow, w;

```

```

        pair<int, pii> p = Q.top();
        Q.pop();
        w = p.x;
        v = p.y.x;
        flow = p.y.y;
        if (dist[v] < w) {
            continue;
        }
        if (v == t) {
            return make_pair(w, flow);
        }
        for (int j : adj[v]) {
            edge e = edges[j];
            if (!vis[e.to] && e.cap - e.flow > 0) {
                if (w + e.cost < dist[e.to]) {
                    dist[e.to] = w + e.cost;
                    pid[e.to] = j;
                    Q.push({dist[e.to], {e.to, min(e.cap - e.flow, flow)}});
                }
            }
        }
    }
    return make_pair(0, 0);
}
pii max_flow() {
    int maxflow = 0, mincost = 0;
    while (true) {
        fill(dist, dist + maxn, mod);
        pii cur_flow = dijkstra();
        if (cur_flow.y == 0) {
            break;
        }
        maxflow += cur_flow.y;
        mincost += cur_flow.x;
        int v = t;
        while (v != s) {
            int j = pid[v];
            edges[j].flow += cur_flow.y;
            edges[j ^ 1].flow -= cur_flow.y;
            v = edges[j ^ 1].to;
        }
    }
    return make_pair(mincost, maxflow);
}

```

3.9 Tarjan SCC

```

int val[maxn], low[maxn], scc[maxn], siz[maxn], tim, onStack[maxn], cnt;
stack<int> st;
void tarjan(int v) {
    low[v] = val[v] = tim++;
    onStack[v] = 1;

```

```

st.push(v);
for (int to : adj[v]) {
    if (val[to] == 0) {
        tarjan(to);
        low[v] = min(low[v], low[to]);
    } else if (onStack[to]) {
        low[v] = min(low[v], val[to]);
    }
}
if (low[v] == val[v]) {
    cnt++;
    while (true) {
        int u = st.top();
        st.pop();
        onStack[u] = 0;
        scc[u] = cnt;
        ++siz[cnt];
        if (u == v) {
            break;
        }
    }
}
}
}

```

4 Math

4.1 Basis

```

/* Basis of vectors modulo 2 (for xor related problems) */
ll basis[62];
void add(ll a) {
    for (int bit = 61; bit >= 0; bit--) {
        if (a >> bit & 1) {
            if (basis[bit]) {
                a ^= basis[bit];
            } else {
                basis[bit] = a;
                return;
            }
        }
    }
}

```

4.2 Big Integer

```

#include <bits/stdc++.h>
#define pb push_back
#define all(a) a.begin(), a.end()
#define sz(a) (int)a.size()

```

```

#define x first
#define y second
using namespace std;
typedef long long ll;
typedef long double ld;
typedef pair<int, int> pii;
const int maxn = 1e5 + 100;
const ll base = 1e18;
const int SZ = 300;
struct BigInt {
    vector<ll> digs;
    bool neg;
    BigInt() {
        digs.assign(SZ, 0);
        neg = false;
    }
    BigInt(ll num) {
        digs.assign(SZ, 0);
        neg = (num < 0);
        digs[0] = abs(num);
    }
    BigInt &operator=(const ll &b) {
        return *this = BigInt(b);
    }
    BigInt &operator=(const BigInt &b) {
        for (int i = 0; i < SZ; i++) {
            digs[i] = b.digs[i];
        }
        neg = b.neg;
        return *this;
    }
};
bool operator<(const BigInt &a, const BigInt &b) {
    if (a.neg != b.neg) return a.neg;
    for (int i = SZ - 1; i >= 0; i--) {
        if (a.digs[i] != b.digs[i]) {
            return (a.digs[i] < b.digs[i]) ^ (a.neg);
        }
    }
    return false;
}
bool operator==(const BigInt &a, const BigInt &b) {
    return !(a < b) && !(b < a);
}
bool operator>(const BigInt &a, const BigInt &b) {
    return b < a;
}
ostream &operator<<(ostream &out, const BigInt &a) {
    if (a.neg) out << "-";
    bool flag = false;
    for (int i = SZ - 1; i >= 0; i--) {
        if (a.digs[i] > 0 || flag) {
            if (flag) {
                out << setw(18) << setfill('0') << a.digs[i];
            } else {

```

```

        out << a.digs[i];
    }
    flag = true;
}
return out;
}

BigInt operator+(const BigInt &a, const BigInt &b) {
    if (a.neg != b.neg) {
        BigInt aa = a, bb = b;
        if (aa.neg) swap(aa, bb);
        BigInt c;
        bb.neg = false;
        c.neg = (aa < bb);
        if (aa < bb) swap(aa, bb);
        ll borrow = 0;
        for (int i = 0; i < SZ; i++) {
            c.digs[i] = aa.digs[i] - bb.digs[i] - borrow;
            if (c.digs[i] < 0) {
                c.digs[i] += base, borrow = 1;
            } else {
                borrow = 0;
            }
        }
        return c;
    } else {
        ll carry = 0;
        BigInt c;
        for (int i = 0; i < SZ; i++) {
            c.digs[i] = a.digs[i] + b.digs[i] + carry;
            if (c.digs[i] >= base) {
                c.digs[i] -= base, carry = 1;
            } else {
                carry = 0;
            }
        }
        c.neg = a.neg;
        return c;
    }
}

BigInt operator+=(BigInt &a, const BigInt &b) {
    return a = a + b;
}

BigInt operator-(BigInt &a, BigInt &b) {
    b.neg ^= true;
    BigInt c = a + b;
    b.neg ^= true;
    return c;
}

BigInt operator-=(BigInt &a, BigInt &b) {
    return a = a - b;
}

BigInt max(BigInt a, BigInt b) {
    if (a > b) {
        return a;
    } else {

```

```

        return b;
    }
}

BigInt min(BigInt a, BigInt b) {
    if (a < b) {
        return a;
    } else {
        return b;
    }
}

int main() {
    ios_base::sync_with_stdio(false), cin.tie(0);
    BigInt a, b;
    ll aa, bb;
    cin >> aa >> bb;
    a = BigInt(aa), b = BigInt(bb);
    cout << "a+b " << a + b << "\n";
    cout << "a-b " << a - b << "\n";
    BigInt c = a;
    c += b;
    cout << "a+=b " << c << "\n";
    c = b;
    c += a;
    cout << "b+=a " << c << "\n";
    cout << "a<b " << (a < b) << "\n";
    cout << "a>b " << (a > b) << "\n";
    cout << "a==b " << (a == b) << "\n";
    cout << "max(a, b) " << max(a, b) << "\n";
    cout << "min(a, b) " << min(a, b) << "\n";
    return 0;
}

```

4.3 Extended Euclidean Algorithm

```

const ll mod = 1e9 + 7;
ll gcd(ll a, ll b, ll &x, ll &y) {
    if (b == 0) {
        x = 1, y = 0;
        return a;
    }
    ll x1, y1;
    ll ret = gcd(b, a % b, x1, y1);
    x = y1;
    y = x1 - (a / b) * y1;
    return ret;
}

ll modinv(ll a) {
    ll x, y;
    gcd(a, mod, x, y);
    return (x % mod + mod) % mod;
}

```

4.4 FFT

```
#define rep(i, a, b) for(int i = a; i < (b); ++i)
#define all(x) begin(x), end(x)
#define sz(x) (int)(x).size()
typedef long long ll;
typedef pair<int, int> pii;
typedef vector<int> vi;
typedef complex<double> C;
typedef vector<double> vd;

void fft(vector<C>& a) {
    int n = sz(a), L = 31 - __builtin_clz(n);
    static vector<complex<long double>> R(2, 1);
    static vector<C> rt(2, 1); // (~ 10% faster if double)
    for (static int k = 2; k < n; k *= 2) {
        R.resize(n); rt.resize(n);
        auto x = polar(1.0L, acos(-1.0L) / k);
        rep(i, k, 2*k) rt[i] = R[i] = i&1 ? R[i/2] * x : R[i/2];
    }
    vi rev(n);
    rep(i, 0, n) rev[i] = (rev[i / 2] | (i & 1) << L) / 2;
    rep(i, 0, n) if (i < rev[i]) swap(a[i], a[rev[i]]);
    for (int k = 1; k < n; k *= 2)
        for (int i = 0; i < n; i += 2 * k) rep(j, 0, k) {
            // C z = rt[j+k] * a[i+j+k]; // (25% faster if hand-rolled) ///
            include-line
            auto x = (double *)&rt[j+k], y = (double *)&a[i+j+k]; /// exclude-line
            C z(x[0]*y[0] - x[1]*y[1], x[0]*y[1] + x[1]*y[0]); /// exclude-line
            a[i + j + k] = a[i + j] - z;
            a[i + j] += z;
        }
    }
    // conv(a, b) = c, where c[x] = Sum_over_i (a[i] * b[x - i])
    // rounding is safe if (Sum(a_i^2) + Sum(b_i^2)) * log_2(N) < 9 * 10^14 (in
    // practice 10^16)
    vd conv(const vd& a, const vd& b) {
        if (a.empty() || b.empty()) return {};
        vd res(sz(a) + sz(b) - 1);
        int L = 32 - __builtin_clz(sz(res)), n = 1 << L;
        vector<C> in(n), out(n);
        copy(all(a), begin(in));
        rep(i, 0, sz(b)) in[i].imag(b[i]);
        fft(in);
        for (C& x : in) x *= x;
        rep(i, 0, n) out[i] = in[-i & (n - 1)] - conj(in[i]);
        fft(out);
        rep(i, 0, sz(res)) res[i] = imag(out[i]) / (4 * n);
        return res;
    }
}
```

4.5 Fraction

```
/*
 * Description: Fraction struct
 */
#include <bits/stdc++.h>
#define pb push_back
#define all(a) a.begin(), a.end()
#define sz(a) (int)a.size()
#define x first
#define y second
using namespace std;
typedef long long ll;
typedef long double ld;
typedef pair<int, int> pii;
const int maxn = 1e5 + 100;
struct fraction {
    ll sk, v;
    fraction() {
        sk = 0, v = 1;
    }
    fraction(ll _sk, ll _v) {
        sk = _sk, v = _v;
        ll dbd = __gcd(sk, v);
        sk /= dbd, v /= dbd;
        if (v < 0) sk *= -1, v *= -1;
    }
};
fraction abs(fraction f) { return fraction(abs(f.sk), f.v); }
bool operator<(const fraction &a, const fraction &b) { return a.sk * b.v < b.sk * a.v; }
bool operator>(const fraction &a, const fraction &b) { return a.sk * b.v > b.sk * a.v; }
bool operator==(const fraction &a, const fraction &b) { return a.sk == b.sk && a.v == b.v; }
bool operator!=(const fraction &a, const fraction &b) { return !(a == b); }
fraction operator+(const fraction &a, const fraction &b) { return fraction(a.sk * b.v + b.sk * a.v, a.v * b.v); }
fraction operator-(const fraction &a, const fraction &b) { return fraction(a.sk * b.v - b.sk * a.v, a.v * b.v); }
fraction operator*(const fraction &a, const fraction &b) { return fraction(a.sk * b.sk, a.v * b.v); }
fraction operator/(const fraction &a, const fraction &b) { return fraction(a.sk * b.v, a.v * b.sk); }
fraction operator+=(fraction &a, const fraction &b) { return a = a + b; }
fraction operator-=(fraction &a, const fraction &b) { return a = a - b; }
fraction operator*=(fraction &a, const fraction &b) { return a = a * b; }
fraction operator/=(fraction &a, const fraction &b) { return a = a / b; }
ostream &operator<<(ostream &strm, const fraction &a) {
    if (a.v == 1)
        strm << a.sk;
    else
        strm << a.sk << "/" << a.v;
    return strm;
}
```

```

}
int main() {
    ios_base::sync_with_stdio(false), cin.tie(0);
    int q, w, e, r;
    cin >> q >> w >> e >> r;
    fraction a(q, w);
    fraction b(e, r);
    cout << "< " << (a < b) << "\n";
    cout << "> " << (a > b) << "\n";
    cout << "==" << (a == b) << "\n";
    cout << "!=" << (a != b) << "\n";
    cout << "+" << (a + b) << "\n";
    cout << "-" << (a - b) << "\n";
    cout << "*" << (a * b) << "\n";
    cout << "/" << (a / b) << "\n";
    return 0;
}

```

4.6 Gauss

```

const double EPS = 1e-9;
const int INF = 2; // it doesn't actually have to be infinity or a big number

```

```

int gauss(vector<vector<double>> a, vector<double>& ans) {
    int n = (int)a.size();
    int m = (int)a[0].size() - 1;

    vector<int> where(m, -1);
    for (int col = 0, row = 0; col < m && row < n; ++col) {
        int sel = row;
        for (int i = row; i < n; ++i)
            if (abs(a[i][col]) > abs(a[sel][col]))
                sel = i;
        if (abs(a[sel][col]) < EPS)
            continue;
        for (int i = col; i <= m; ++i)
            swap(a[sel][i], a[row][i]);
        where[col] = row;

        for (int i = 0; i < n; ++i)
            if (i != row) {
                double c = a[i][col] / a[row][col];
                for (int j = col; j <= m; ++j)
                    a[i][j] -= a[row][j] * c;
            }
        ++row;
    }

    ans.assign(m, 0);
    for (int i = 0; i < m; ++i)
        if (where[i] != -1)
            ans[i] = a[where[i]][m] / a[where[i]][i];
}

```

```

for (int i = 0; i < n; ++i) {
    double sum = 0;
    for (int j = 0; j < m; ++j)
        sum += ans[j] * a[i][j];
    if (abs(sum - a[i][m]) > EPS)
        return 0;
}

for (int i = 0; i < m; ++i)
    if (where[i] == -1)
        return INF;
return 1;
}

vector<int> GaussModulo(vector<vector<int>> mat) {
    for (int i = 0; i < mat.size(); i++) {
        int val = mat[i][i];
        int mul = modinv(val);
        for (int k = 0; k < mat[i].size(); k++)
            mat[i][k] = 1ll * mat[i][k] * mul % mod;
        for (int j = 0; j < mat.size(); j++)
            if (i != j) {
                int times = mat[j][i];
                for (int k = 0; k < mat[j].size(); k++)
                    mat[j][k] = (mat[j][k] - 1ll * times * mat[i][k] % mod + mod) %
                        mod;
            }
    }
    vector<int> ret;
    for (int i = 0; i < mat.size(); i++) {
        ret.push_back(mat[i].back());
    }
    return ret;
}

```

4.7 Matrix Struct

```

int add(int a, int b) {
    int c = a + b;
    if (c > mod) {
        c -= mod;
    }
    return c;
}

int mul(int a, int b) {
    1l c = (1l)a * b;
    c %= mod;
    return (int)c;
}

struct matrix {
    int N, M;
    vector<vector<int>> mat;
}

```

```

matrix(int n, int m) {
    N = n, M = m;
    mat = vector<vector<int>>(N, vector<int>(M, 0));
}

void ident() {
    for (int i = 0; i < N; i++) {
        for (int j = 0; j < N; j++) {
            mat[i][j] = (i == j);
        }
    }
}

matrix(vector<vector<int>> arr) {
    N = arr.size(), M = arr[0].size();
    mat = vector<vector<int>>(N, vector<int>(M, 0));
    for (int i = 0; i < N; i++) {
        for (int j = 0; j < M; j++) {
            mat[i][j] = arr[i][j];
        }
    }
}

matrix operator*(const matrix &o) {
    matrix ret(N, o.M);
    for (int i = 0; i < ret.N; i++) {
        for (int j = 0; j < ret.M; j++) {
            for (int k = 0; k < M; k++) {
                ret.mat[i][j] = add(ret.mat[i][j], mul(mat[i][k], o.mat[k][j]));
            }
        }
    }
    return ret;
}

};

matrix pwr(matrix a, ll pw) {
    matrix ret(a);
    ret.ident();
    while (pw > 0) {
        if (pw & 1) {
            ret = ret * a;
        }
        a = a * a;
        pw >>= 1;
    }
    return ret;
}

```

4.8 Modulo operations

```

typedef long long ll;
const ll mod = 1e9 + 7;
ll pwr(ll num, ll pw) {
    ll ret = 1;
    while (pw > 0) {

```

```

        if (pw & 1) {
            ret = (ret * num) % mod;
        }
        num = (num * num) % mod;
        pw >>= 1;
    }
    return ret;
}

ll modinv(ll a) { return pwr(a, mod - 2); }
ll add(ll a, ll b) { return (a + b) % mod; }
ll sub(ll a, ll b) { return (a - b + mod) % mod; }
ll mul(ll a, ll b) { return (a * b) % mod; }

```

5 Misc

5.1 Custom Vector

```

/* Description: Implementation of vector with negative indexing */
#include <bits/stdc++.h>
using namespace std;

template<class T>
struct MyVector {
    int offset;
    vector<T> vec_;

    MyVector(int n, int off, T &&values = T()) {
        vec_.resize(n, values);
        offset = off;
    }

    T& operator[](int i) {
        i += offset;
        assert(0 <= i && i < (int)vec_.size());
        return vec_[i];
    }
};

int main()
{
    ios_base::sync_with_stdio(false), cin.tie(0);
    // Example usage
    MyVector<MyVector<int>> dp(10 + 1, 5, MyVector<int>(8 + 1, 4));

    for (int i = -5; i <= 5; i++) {
        for (int j = -4; j <= 4; j++) {
            dp[i][j] = i * j;
        }
    }

    for (int i = -5; i <= 5; i++) {
        for (int j = -4; j <= 4; j++) {

```

```

        cout << i << " " << j << " " << dp[i][j] << "\n";
    }
}
return 0;
}

```

6 Notes

6.1 Notes

```

/*
---
Pick's theorem:
If a polygon has all integer coordinates then the area A is
 $A = i + b / 2 - 1$ 
where i is the number of integer points interior to the polygon
b is the number of integer points on the boundary
---
Shoelace formula:
 $1/2 * (x1*y2 - x2*y1 + x2*y3 - x3*y2 + ... + xn*y1 - x1*yn)$ 
---
Euler's formula:
For a connected planar graph with v vertices, e edges and f faces (including
outer)
 $v - e + f = 2$ 
*/

```

7 Strings

7.1 Bitset Trie

```

template <int N>
struct trie {
    int t[N + 1][2], nxt = 1;

    trie() {
        memset(t, 0, sizeof t);
    }

    void ins(string s) {
        int cur = 0;
        for (int i = 0; i < s.size(); ++i) {
            int bit = s[i] - '0';
            if (!t[cur][bit]) {
                t[cur][bit] = nxt++;
            }
            cur = t[cur][bit];
        }
    }
}

```

```

bool find(string s) {
    int cur = 0;
    for (int i = 0; i < s.size(); ++i) {
        int bit = s[i] - '0';
        if (!t[cur][bit]) {
            return false;
        }
        cur = t[cur][bit];
    }
    return true;
}
};

```

7.2 Hashing

```

/*
Works, but might be a little slow
https://judge.yosupo.jp/submission/80957
*/
bool is_prime(int a) {
    if (a == 1) {
        return false;
    }
    if (a % 2 == 0) {
        return a == 2;
    }
    for (int i = 3; i * i <= a; i += 2) {
        if (a % i == 0) {
            return false;
        }
    }
    return true;
}

int pwr(int a, int pw, int MOD) {
    int ret = 1;
    while (pw > 0) {
        if (pw & 1) {
            ret = 1ll * ret * a % MOD;
        }
        a = 1ll * a * a % MOD;
        pw >>= 1;
    }
    return ret;
}

int modinv(int a, int MOD) {
    return pwr(a, MOD - 2, MOD);
}

struct hashing {
    vector<vector<int>> >ha;
}

```

```

vector<vector<int>> >rha;
static vector<vector<int>> >pw;
static vector<vector<int>> >inv_pw;
static vector<int>>mods;
static vector<int>>BASE_INV;
static int BASE;
static int M;
int N;

static vector<int>>zero_vector(int len) {
    vector<int>>ret;
    for (int i = 0; i < len; i++) {
        ret.push_back(0);
    }
    return ret;
}

struct hash {
    vector<int>>h;
    int len;

    hash() {
        h = zero_vector(M);
        len = 0;
    }

    hash(vector<int>>h, int len) {
        this->h = h;
        this->len = len;
    }

    bool operator==(const hash& b) const {
        return h == b.h && len == b.len;
    }

    hash operator-(const hash& b) {
        hash c;
        c.h = h;

        for (int j = 0; j < M; j++) {
            c.h[j] -= b.h[j];
            if (c.h[j] < 0) {
                c.h[j] += mods[j];
            }
            c.h[j] = 111 * c.h[j] * inv_pw[b.len][j] % mods[j];
        }

        c.len = len - b.len;
        return c;
    }

    hash operator+=(const hash& b) {
        hash c = *this;
        c = c + b;
        this->h = c.h;
        this->len = c.len;
    }
};

```

```

        this->len = c.len;
        return *this;
    }

    hash operator+(const hash& b) {
        hash c;
        c.h = h;

        for (int j = 0; j < M; j++) {
            c.h[j] += 111 * pw[len][j] * b.h[j] % mods[j];
            if (c.h[j] >= mods[j]) {
                c.h[j] -= mods[j];
            }
        }

        c.len = len + b.len;
        return c;
    }

    hash operator+=(const hash& b) {
        hash c = *this;
        c = c + b;
        this->h = c.h;
        this->len = c.len;
        return *this;
    }

    bool operator<(const hash& b) const {
        for (int i = 0; i < M; i++) {
            if (h[i] != b.h[i]) {
                return h[i] < b.h[i];
            }
        }
        return len < b.len;
    }
};

hashing(string s) {
    if (M == 0 || BASE == 0) {
        cerr << "Initialize mods and base before creating a hashing instance!";
        exit(1);
    }
    init_string(s);
}

static void init_base() {
    mt19937 rng(chrono::steady_clock::now().time_since_epoch().count());
    uniform_int_distribution<>distrib(3, (int)1e9);
    while (true) {
        BASE = distrib(rng);
        if (is_prime(BASE)) {
            break;
        }
    }
}

```

```

static void init_mods(vector<int> new_mods) {
    mods = new_mods;
    M = (int)mods.size();
    BASE_INV = vector<int>(M);
    for (int j = 0; j < M; j++) {
        BASE_INV[j] = modinv(BASE, mods[j]);
    }
}

static void init_pows(int MAX_POW) {
    pw = vector<vector<int>> >(MAX_POW + 1, vector<int>(M));
    inv_pw = vector<vector<int>> >(MAX_POW + 1, vector<int>(M));

    for (int i = 0; i <= MAX_POW; i++) {
        for (int j = 0; j < M; j++) {
            if (i == 0) {
                pw[i][j] = 1;
                inv_pw[i][j] = 1;
            } else {
                pw[i][j] = 11l * pw[i - 1][j] * BASE % mods[j];
                inv_pw[i][j] = 11l * inv_pw[i - 1][j] * BASE_INV[j] % mods[j];
            }
        }
    }
}

void init_string(string s) {
    N = (int)s.size();

    ha = vector<vector<int>> >(N, vector<int>(M));
    rha = vector<vector<int>> >(N, vector<int>(M));

    init_pows(N * 2);

    for (int i = 0; i < N; i++) {
        for (int j = 0; j < M; j++) {
            ha[i][j] = 11l * pw[i][j] * (s[i] - 'a' + 1) % mods[j];
            rha[i][j] = 11l * pw[i][j] * (s[N - i - 1] - 'a' + 1) % mods[j];

            if (i > 0) {
                ha[i][j] += ha[i - 1][j];
                if (ha[i][j] >= mods[j]) {
                    ha[i][j] -= mods[j];
                }
                rha[i][j] += rha[i - 1][j];
                if (rha[i][j] >= mods[j]) {
                    rha[i][j] -= mods[j];
                }
            }
        }
    }
}

hash get_hash(int i, int j, bool reverse) {

```

```

        if (i > j) {
            return hash();
        }

        hash pref_i, pref_j;
        if (reverse) {
            i = N - i - 1;
            j = N - j - 1;
            swap(i, j);
            pref_i = (i == 0 ? hash() : hash(rha[i - 1], i));
            pref_j = hash(rha[j], j + 1);
        } else {
            pref_i = (i == 0 ? hash() : hash(ha[i - 1], i));
            pref_j = hash(ha[j], j + 1);
        }

        return pref_j - pref_i;
    }
};

vector<vector<int>> > hashing::pw;
vector<vector<int>> > hashing::inv_pw;
vector<int> hashing::mods;
vector<int> hashing::BASE_INV;
int hashing::BASE;
int hashing::M;

```

7.3 Hashing2

```

#include <iostream>
#include <vector>
using namespace std;

typedef long long ll;

struct RollingHash {
    static const ll mod0 = 1000000123, mod1 = 1000000007;
    static const ll base0 = 137, base1 = 163;

    vector<ll> po0, po1;
    vector<ll> hsh0, hsh1;

    void init(string str) {
        if (!po0.size()) po0 = po1 = {1};
        hsh0 = {base0}, hsh1 = {base1};

        for (int i = 0; i < (int)str.size(); i++) {
            if (str[i] >= 'A' && str[i] <= 'Z') str[i] += 'a' - 'A';
            hsh0.push_back((hsh0.back() * base0 % mod0 + str[i]) % mod0);
            hsh1.push_back((hsh1.back() * base1 % mod1 + str[i]) % mod1);
        }
    }
}

```

```

pair<ll,ll> cut(int l, int r) {
    while (po0.size() <= r+1) {
        po0.push_back(po0.back() * base0 % mod0);
        po1.push_back(po1.back() * base1 % mod1);
    }

    return make_pair((hsh0[r+1]+mod0-(hsh0[l]*po0[r-l+1]%mod0))%mod0,
                    (hsh1[r+1]+mod1-(hsh1[l]*po1[r-l+1]%mod1))%mod1);
}
} rh;

```

7.4 KMP

```

/* Description: Linear time string matching */
#include <bits/stdc++.h>
#define pb push_back
#define all(a) a.begin(), a.end()
#define sz(a) (int)a.size()
#define x first
#define y second
using namespace std;
typedef long long ll;
typedef long double ld;
typedef pair<int, int> pii;
const int maxn = 1e5 + 100;
vector<int> build_lps(string s) {
    vector<int> lps(sz(s), 0);
    for (int i = 1; i < sz(s); ++i) {
        int id = lps[i - 1];
        while (id && s[i] != s[id]) {
            id = lps[id - 1];
        }
        lps[i] = id + (s[i] == s[id]);
    }
    return lps;
}
vector<int> KMP(string s, string pat) {
    vector<int> lps = build_lps(pat + '\0' + s), res;
    for (int i = 0; i < sz(lps); ++i) {
        if (lps[i] == sz(pat)) {
            res.pb(i - 2 * sz(pat));
        }
    }
    return res;
}
int main() {
    ios_base::sync_with_stdio(false), cin.tie(0);
    string s, pat;
    cin >> s >> pat;
    vector<int> res = KMP(s, pat);
    for (auto aa : res) {

```

```

        cout << aa << " ";
    }
    cout << "\n";
    return 0;
}

```

7.5 SuffixArray

```

vector<int> sort_cyclic_shifts(string const& s) {
    int n = s.size();
    const int alphabet = 256;
    vector<int> p(n), c(n), cnt(max(alphabet, n), 0);
    for (int i = 0; i < n; i++)
        cnt[s[i]]++;
    for (int i = 1; i < alphabet; i++)
        cnt[i] += cnt[i - 1];
    for (int i = 0; i < n; i++)
        p[--cnt[s[i]]] = i;
    c[p[0]] = 0;
    int classes = 1;
    for (int i = 1; i < n; i++) {
        if (s[p[i]] != s[p[i - 1]])
            classes++;
        c[p[i]] = classes - 1;
    }
    vector<int> pn(n), cn(n);
    for (int h = 0; (1 << h) < n; ++h) {
        for (int i = 0; i < n; i++) {
            pn[i] = p[i] - (1 << h);
            if (pn[i] < 0)
                pn[i] += n;
        }
        fill(cnt.begin(), cnt.begin() + classes, 0);
        for (int i = 0; i < n; i++)
            cnt[c[pn[i]]]++;
        for (int i = 1; i < classes; i++)
            cnt[i] += cnt[i - 1];
        for (int i = n - 1; i >= 0; i--)
            p[--cnt[c[pn[i]]]] = pn[i];
        cn[p[0]] = 0;
        classes = 1;
        for (int i = 1; i < n; i++) {
            pair<int, int> cur = {c[p[i]], c[(p[i] + (1 << h)) % n]};
            pair<int, int> prev = {c[p[i - 1]], c[(p[i - 1] + (1 << h)) % n]};
            if (cur != prev)
                ++classes;
            cn[p[i]] = classes - 1;
        }
        c.swap(cn);
    }
    return p;
}

```

```
vector<int> suffix_array_construction(string s) {
    s += "$";
    vector<int> sorted_shifts = sort_cyclic_shifts(s);
    sorted_shifts.erase(sorted_shifts.begin());
    return sorted_shifts;
}
```

8 Trees

8.1 Centroid Decomposition

/* Description: Centroid Decomposition on trees */

```
#include <bits/stdc++.h>
#define push_back push_back
#define all(a) a.begin(), a.end()
#define sz(a) (int)a.size()
#define x first
#define y second
using namespace std;
typedef long long ll;
typedef long double ld;
typedef pair<int, int> pii;
const int maxn = 1e5 + 100;
vector<int> adj[maxn];
int n, sub[maxn], par[maxn];
bool vis[maxn];
char ans[maxn];
void dfs(int v) {
    sub[v] = 1;
    for (auto to : adj[v]) {
        if (!vis[to] && to != par[v]) {
            par[to] = v;
            dfs(to);
            sub[v] += sub[to];
        }
    }
}
int get_centroid(int v) {
    par[v] = 0;
    dfs(v);
    int sz = sub[v];
    while (true) {
        pii mx = {0, 0};
        for (auto to : adj[v]) {
            if (!vis[to] && par[v] != to) {
                mx = max(mx, {sub[to], to});
            }
        }
        if (mx.first * 2 > sz) {
            v = mx.second;
        } else {
            return v;
        }
    }
}
```

```

    }
}
void solve(int v, int level = 0) {
    v = get_centroid(v);
    vis[v] = true;
    ans[v] = (char)(level + 'A');
    for (auto to : adj[v]) {
        if (!vis[to]) {
            solve(to, level + 1);
        }
    }
}
int main() {
    ios_base::sync_with_stdio(false), cin.tie(0);
    cin >> n;
    for (int i = 0; i < n - 1; i++) {
        int a, b;
        cin >> a >> b;
        adj[a].push_back(b);
        adj[b].push_back(a);
    }
    solve(1);
    for (int i = 1; i <= n; i++) {
        cout << ans[i] << " ";
    }
    cout << "\n";
    return 0;
}
```

8.2 Lowest Common Ancestor

/* Description: Offline Lowest Common Ancestor with NlogN preprocessing and logN query using binary lifting */

```
const int maxn = 1e5 + 100;
const int maxlog = 20;
int dep[maxn], anc[maxn][maxlog];
vector<int> adj[maxn];
void dfs(int v, int p = 0) {
    dep[v] = dep[p] + 1;
    anc[v][0] = p;
    for (int i = 1; i < 18; i++) {
        anc[v][i] = anc[anc[v][i - 1]][i - 1];
    }
    for (int to : adj[v]) {
        if (to != p) {
            dfs(to, v);
        }
    }
}
int lca(int a, int b) {
    if (dep[a] < dep[b]) {
```



```
    swap(a, b);
}
for (int i = 17; i >= 0; i--) {
    if (dep[anc[a][i]] >= dep[b]) {
        a = anc[a][i];
    }
}
if (a == b) {
    return a;
}
for (int i = 17; i >= 0; i--) {
```

```
    if (anc[a][i] != anc[b][i]) {
        a = anc[a][i], b = anc[b][i];
    }
}
return anc[a][0];
}
int getDist(int v, int u) {
    return dep[v] + dep[u] - 2 * dep[lca(v, u)];
}
```
