Team notebook

one more try

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1 Data Structures

1.1 2D BIT With Sparse SegTree

```
int root[maxn], seg[maxn * 100], L[maxn * 100], R[maxn * 100], nxt_id;
int modify(int id, int pos, int val, int l = 1, int r = n) {
   if (!id) {
       id = ++nxt id:
   if (1 == r) {
       seg[id] = val;
       return id:
   int mid = (1 + r) / 2:
   if (pos <= mid) {</pre>
       L[id] = modify(L[id], pos, val, 1, mid);
   } else {
       R[id] = modify(R[id], pos, val, mid + 1, r);
   seg[id] = seg[L[id]] + seg[R[id]];
   return id;
int query(int id, int x, int y, int l = 1, int r = n) {
   if (1 > y || r < x || !id) {</pre>
       return 0;
   if (1 >= x && r <= y) {</pre>
       return seg[id];
   int mid = (1 + r) / 2:
   return query(L[id], x, y, 1, mid) + query(R[id], x, y, mid + 1, r);
void add(int x, int v) {
   for (; x <= n; x += x & -x) {
       root[x] = modify(root[x], y, 1);
}
int get(int x, int lo, int hi) {
   int ret = 0:
   for (; x > 0; x -= x & -x) {
       ret += query(root[x], lo, hi);
   return ret;
}
int get(int 1, int r, int lo, int hi) {
   return get(r, lo, hi) - get(l - 1, lo, hi);
```

1.2 2D BIT with ordered_set

```
#include <ext/pb_ds/assoc_container.hpp>
```

```
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template < class T > using ordered_set = tree < T, null_type, less < T >, rb_tree_tag,
     tree_order_statistics_node_update>;
struct BIT {
   ordered_set<int> f[maxn];
   void add(int i, int val) {
       for(: i <= maxn: i += i & -i)</pre>
           f[i].insert(val);
   int get(int i, int lo, int hi) {
       int ret = 0:
       for (: i > 0: i -= i & -i) {
           ret += f[i].order_of_key(hi + 1) - f[i].order_of_key(lo);
       return ret;
   }
   int get(int 1, int r, int lo, int hi) {
       return get(r, lo, hi) - get(l - 1, lo, hi);
};
```

1.3 BIT with range updates and point queries

```
* Description: BIT with range updates and point queries
#include <bits/stdc++.h>
#define pb push_back
#define all(a) a.begin(), a.end()
#define sz(a) (int)a.size()
#define x first
#define y second
using namespace std;
typedef long long 11;
typedef long double ld:
typedef pair<int, int>pii;
const int maxn = 1e5 + 100;
template < class T. int N>
struct BIT {
   T f[N + 1]:
   BIT() {
       memset(f, 0, sizeof f);
   void upd(int pos, T val) {
       for (; pos <= N; pos += pos & -pos)</pre>
          f[pos] += val;
   void upd(int 1, int r, T val) {
       upd(1, val);
```

```
upd(r + 1, -val);
   T query(int pos) {
       T ret = 0;
       for (; pos > 0; pos -= pos & -pos) {
           ret += f[pos];
       return ret;
};
int main()
    ios_base::sync_with_stdio(false), cin.tie(0);
    BIT<11, 100000> tree;
    tree.upd(3, 5, 1):
    cout << tree.query(3) << "\n";</pre>
    cout << tree.query(4) << "\n";</pre>
    cout << tree.query(5) << "\n";</pre>
    cout << tree.query(2) << "\n";</pre>
    cout << tree.query(6) << "\n";</pre>
    return 0;
```

1.4 Binary Indexed Tree

```
template < class T, int N>
struct BIT {
   T f[N + 1];
   BIT() {
       memset(f, 0, sizeof f);
   void upd(int pos, T val) {
       for (; pos <= N; pos += pos & -pos)</pre>
          f[pos] += val;
   T query(int r) {
       T ret = 0;
       for (; r > 0; r -= r & -r) {
           ret += f[r]:
       }
       return ret:
   T query(int 1, int r) {
       return query(r) - query(1 - 1);
};
```

1.5 DSU

```
template<int N>
struct DSU {
   int par[N + 1], sz[N + 1];
   DSU() {
       for (int i = 0; i <= N; i++) {</pre>
           par[i] = i, sz[i] = 1;
   }
   int root(int v) {
       return v == par[v] ? v : par[v] = root(par[v]);
   bool unite(int a, int b) {
       a = root(a);
       b = root(b);
       if (a == b) {
           return false;
       if (sz[a] < sz[b]) {</pre>
           swap(a, b);
       sz[a] += sz[b]:
       par[b] = a;
       return true;
   }
};
```

1.6 Lazy SegTree

```
#include <bits/stdc++.h>
#define pb push_back
#define all(a) a.begin(), a.end()
#define sz(a) (int)a.size()
#define x first
#define y second
using namespace std;
typedef long long 11;
typedef long double ld;
typedef pair<int, int>pii;
const int maxn = 1e5 + 100;
template < class T, int N>
struct SegTree {
   T \operatorname{seg}[N * 4], \operatorname{lazy}[N * 4];
   SegTree() {
       memset(seg, 0, sizeof seg);
       memset(lazy, 0, sizeof lazy);
   void build(T arr[], int id = 1, int 1 = 0, int r = N - 1) {
       if (r == 1) {
           seg[id] = arr[1];
           return;
```

```
int mid = (1 + r) / 2;
       build(arr, id * 2, 1, mid);
       build(arr, id * 2 + 1, mid + 1, r);
       seg[id] = seg[id * 2] + seg[id * 2 + 1];
   void upd(int id, int 1, int r, T val) {
       seg[id] += (T)(r - 1 + 1) * val:
       lazy[id] += val;
   void shift(int id, int 1, int r) {
       int mid = (1 + r) / 2:
       upd(id * 2, 1, mid, lazy[id]);
       upd(id * 2 + 1, mid + 1, r, lazv[id]):
       lazv[id] = 0:
   void modify(int x, int v, T val, int id = 1, int l = 0, int r = N - 1) {
       if (1 > y || r < x) {
          return;
       }
       if (1 >= x && r <= y) {
          upd(id, 1, r, val);
          return;
       }
       shift(id, 1, r);
       int mid = (1 + r) / 2;
       modify(x, y, val, id * 2, 1, mid);
       modify(x, y, val, id * 2 + 1, mid + 1, r);
       seg[id] = seg[id * 2] + seg[id * 2 + 1];
   T query(int x, int y, int id = 1, int l = 0, int r = N - 1) {
       if (1 > y || r < x) {
          return 0:
       }
       if (1 >= x && r <= v) {
          return seg[id];
       }
       shift(id, l, r):
       int mid = (1 + r) / 2:
       return query(x, y, id * 2, 1, mid) + query(x, y, id * 2 + 1, mid + 1, r);
};
```

1.7 Mergeable Segment Tree

```
/***
https://codeforces.com/contest/911/problem/G
***/
#include <bits/stdc++.h>
#define pb push_back
#define all(a) a.begin(), a.end()
#define sz(a) (int)a.size()
#define x first
```

```
#define v second
#define debug(...) cout << "[" << #__VA_ARGS__ << ": " << __VA_ARGS__ << "]\n"</pre>
#define rd() abs((int)rng())
using namespace std;
typedef long long 11;
typedef long double ld;
typedef pair<int, int>pii;
const int maxn = 2e5 + 100;
const int mod = 1e9 + 7:
mt19937 rng(chrono::high_resolution_clock::now().time_since_epoch().count());
struct node {
   int 1. r:
}:
int n, q, ans[maxn], nxt_id;
node tree[maxn * 150]:
int root[105]:
pii split(int id, int k, int lo = 1, int hi = n) { /// >= goes to the right
   if (!id) {
       return {0, 0};
   if (lo == hi) {
       return (lo >= k ? pii(0, id) : pii(id, 0));
   int other = ++nxt_id;
   int mid = (lo + hi) / 2;
   if (k <= mid) {</pre>
       pii p = split(tree[id].1, k, lo, mid);
       tree[id].1 = p.y;
       tree[other].1 = p.x;
       return {other, id}:
       pii p = split(tree[id].r, k, mid + 1, hi);
       tree[id].r = p.x;
       tree[other].r = p.y;
       return {id, other}:
   }
int merge(int a, int b) {
   if (!a) return b:
   if (!b) return a:
   tree[a].1 = merge(tree[a].1, tree[b].1);
   tree[a].r = merge(tree[a].r, tree[b].r);
   return a:
int ins(int id, int pos, int lo = 1, int hi = n) {
   if (!id) id = ++nxt id:
   if (lo == hi) return id;
   int mid = (lo + hi) / 2;
   if (pos <= mid) {</pre>
       tree[id].l = ins(tree[id].l, pos, lo, mid);
       tree[id].r = ins(tree[id].r, pos, mid + 1, hi);
   return id:
```

```
}
void go(int id, int x, int lo = 1, int hi = n) {
   if (!id) {
       return;
   if (lo == hi) {
       ans[lo] = x;
       return;
   int mid = (lo + hi) / 2:
   go(tree[id].1, x, lo, mid);
   go(tree[id].r, x, mid + 1, hi);
int main()
   ios base::svnc with stdio(false), cin.tie(0):
   cin >> n:
   for (int i = 1; i <= n; i++) {</pre>
       int x;
       cin >> x;
       root[x] = ins(root[x], i);
   }
   cin >> q;
   for (int i = 0; i < q; i++) {</pre>
       int 1, r, x, y;
       cin >> 1 >> r >> x >> y;
       if (x == y) {
           continue; /// DOESNT WORK IF X = Y
       pii a = split(root[x], 1);
       pii b = split(a.y, r + 1);
       root[y] = merge(root[y], b.x);
       root[x] = merge(a.x, b.y);
   for(int i = 1; i <= 100; i++) {</pre>
       go(root[i], i);
   for(int i = 1; i <= n; i++) {</pre>
       cout << ans[i] << " ":
   cout << "\n";
   return 0;
```

1.8 Minimum Deque

```
struct MinDeque {
  deque<pii> D;
  int lo, hi;
  MinDeque() {
    lo = 1, hi = 1;
}
```

```
void ins(int val) {
    while (sz(D) && D.back().x >= val) {
        D.pop_back();
    }
    D.pb({val, hi++});
}
void del() {
    if (sz(D) && D.front().y == lo++) {
        D.pop_front();
    }
}
int get() {
    return sz(D) ? D.front().x : mod;
}
};
```

1.9 Persistent SegTree

```
int root[maxn], seg[maxn * 60], L[maxn * 60], R[maxn * 60], next_id; /// required
    size can be different depending on problem
void build(int id = 1, int l = 1, int r = n) {
   if (1 == r) {
       return:
   int mid = (1 + r) / 2:
   L[id] = ++next id:
   R[id] = ++next_id;
   build(L[id]. 1. mid):
   build(R[id], mid + 1, r):
int modify(int pos, int delta, int id, int l = 1, int r = n) {
   int new_id = ++next_id;
   seg[new_id] = seg[id] + delta;
   if (1 == r) {
       return new_id;
   int mid = (1 + r) / 2;
   L[new_id] = L[id];
   R[new_id] = R[id];
   if (pos <= mid) {</pre>
       L[new_id] = modify(pos, delta, L[new_id], 1, mid);
       R[new_id] = modify(pos, delta, R[new_id], mid + 1, r);
   return new_id;
```

1.10 Treap

```
int tmp = t->1 ? t->1->sz : 0;
* Source:
    https://github.com/bqi343/USACO/blob/master/Implementations/09%20-%20Range%20Queries%20(2)115(3%8e-120)BBET%20(4)/Treap.cpp
* Description: treap with max heap property
                                                                                                    auto p = split_by_order(t->1, v);
* Verification: http://www.spoj.com/problems/ORDERSET/
                                                                                                    t->1 = p.second;
                                                                                                    t->recalc();
#include <bits/stdc++.h>
                                                                                                    return {p.first, t};
#define pb push_back
#define all(a) a.begin(), a.end()
                                                                                                    auto p = split_by_order(t->r, v - tmp - 1);
#define sz(a) (int)a.size()
                                                                                                    t->r = p.first;
#define x first
                                                                                                    t->recalc();
#define y second
                                                                                                    return {t, p.second};
using namespace std;
                                                                                                }
typedef long long 11;
                                                                                            }
typedef long double ld;
typedef pair<int, int>pii;
                                                                                             pnode merge(pnode left, pnode right) {
const int maxn = 1e5 + 100:
                                                                                                if (!left) {
mt19937 rng(chrono::high_resolution_clock::now().time_since_epoch().count());
                                                                                                    return right;
struct node {
                                                                                                if (!right) {
   int val, pri, sz;
                                                                                                    return left;
   node *1, *r;
   node(int v) {
                                                                                                if (left->pri > right->pri) {
       val = v, sz = 1, pri = rng();
                                                                                                    left->r = merge(left->r, right);
       1 = r = NULL;
                                                                                                    left->recalc();
   }
                                                                                                    return left;
                                                                                                } else {
                                                                                                    right->l = merge(left, right->l);
   void recalc() {
       sz = 1 + (1 ? 1->sz : 0) + (r ? r->sz : 0);
                                                                                                    right->recalc();
                                                                                                    return right;
                                                                                                }
typedef node* pnode;
pair<pnode, pnode> split(pnode t, int v) { /// >= v goes to the right
                                                                                            pnode ins(pnode x, int v) {
                                                                                                auto a = split(x, v);
   if (!t) {
                                                                                                auto b = split(a.second, v + 1);
       return {t, t};
                                                                                                return merge(a.first, merge(new node(v), b.second));
                                                                                            }
   if (v <= t->val) {
       auto p = split(t->1, v);
                                                                                            pnode del(pnode x, int v) {
                                                                                                auto a = split(x, v), b = split(a.second, v + 1);
       t->1 = p.second;
       t->recalc();
                                                                                                return merge(a.first, b.second);
       return {p.first, t};
   } else {
       auto p = split(t->r, v);
                                                                                            pnode root;
       t\rightarrow r = p.first;
       t->recalc();
                                                                                            int order_of_key(int x) {
       return {t, p.second};
                                                                                                auto a = split(root, x);
                                                                                                int t = a.first ? a.first->sz : 0;
                                                                                                root = merge(a.first, a.second);
                                                                                                return t;
pair<pnode, pnode> split_by_order(pnode t, int v) {
   if (!t) {
       return {t, t};
                                                                                             int find_by_order(int x) {
                                                                                                auto a = split_by_order(root, x);
```

```
auto b = split_by_order(a.first, x - 1);
   int t = b.second->val;
   root = merge(merge(b.first, b.second), a.second);
}
int main()
{
   ios_base::sync_with_stdio(false), cin.tie(0);
   int 0:
   cin >> 0:
   for (int i = 0; i < Q; i++) {</pre>
       char c;
       int d:
       cin >> c >> d:
       if (c == 'I') {
           root = ins(root, d):
       } else if (c == 'D') {
           root = del(root, d);
       } else if (c == 'K') {
           if (!root || root->sz < d) {</pre>
               cout << "invalid\n";</pre>
           } else {
               cout << find_by_order(d) << "\n";</pre>
       } else {
           cout << order_of_key(d) << "\n";</pre>
       }
   }
}
```

2 Geometry

2.1 Convex Hull Trick

```
struct line {
    ll k, b;
    line() = default;
    line(ll kk, ll bb) {
        k = kk;
        b = bb;
    }
    ll eval(ll x) {
        return k * x + b;
    }
};
Id inter(line f, line s) {
    return 1.0 * (s.b - f.b) / (f.k - s.k);
}
int siz, it;
line hull[maxn];
void add(line a) {
```

2.2 Convex Hull

```
/*
* Source:
     https://en.wikibooks.org/wiki/Algorithm_Implementation/Geometry/Convex_hull/Monotone
* Description: NlogN Convex Hull
#include <bits/stdc++.h>
using namespace std;
using ll = long long;
struct point {
   11 x, y;
   point(11 a = 0, 11 b = 0) {
       x = a, y = b;
   bool operator<(const point &o) const {</pre>
       return make_pair(x, y) < make_pair(o.x, o.y);</pre>
   bool operator==(const point& o) const {
       return x == o.x && y == o.y;
   point operator-(const point &b) const {
       return point(x - b.x, y - b.y);
}:
11 cross(point a, point b) {
   return a.x * b.y - a.y * b.x;
11 cross(point a, point b, point c) {
   return cross(b - a, c - a);
vector<point> convex_hull(vector<point>pts) {
   sort(pts.begin(), pts.end());
   pts.erase(unique(pts.begin(), pts.end()), pts.end());
   vector<point>top, bot;
    for (int i = 0; i < pts.size(); ++i) {</pre>
```

```
while (bot.size() >= 2 && cross(bot[bot.size() - 2], bot.back(), pts[i])
           bot.pop_back();
       bot.push_back(pts[i]);
   bot.pop_back();
   for (int i = pts.size() - 1; i >= 0; --i) {
       while (top.size() >= 2 && cross(top[top.size() - 2], top.back(), pts[i])
            <= 0) {
           top.pop_back();
       }
       top.push_back(pts[i]);
   top.pop_back();
   top.insert(top.end(), bot.begin(), bot.end());
   return top;
}
int main() {
   ios_base::sync_with_stdio(false), cin.tie(0);
   int n;
   cin >> n;
   vector<point>pts;
   for (int i = 0; i < n; i++) {</pre>
       point p;
       cin >> p.x >> p.y;
       pts.push_back(p);
   vector<point>hull = convex_hull(pts);
   cout << "----\n":
   for (point p : hull) {
       cout << p.x << " " << p.y << "\n";
   }
   return 0:
}
```

2.3 Dynamic Convex Hull Trick

```
bool Q;
struct Line {
    mutable ll k, m, p;
    bool operator<(const Line& o) const {
        return Q ? p < o.p : k < o.k;
    }
};
struct LineContainer : multiset<Line> {
    // (for doubles, use inf = 1/.0, div(a,b) = a/b)
    const ll inf = LLONG_MAX;
    ll div(ll a, ll b) { // floored division
        return a / b - ((a ^ b) < 0 && a % b); }
    bool isect(iterator x, iterator y) {</pre>
```

```
if (y == end()) { x->p = inf; return false; }
       if (x->k == y->k) x->p = x->m > y->m ? inf : -inf;
       else x->p = div(y->m - x->m, x->k - y->k);
       return x->p >= y->p;
   void add(ll k, ll m) {
       auto z = insert(\{k, m, 0\}), y = z++, x = y;
       while (isect(y, z)) z = erase(z);
       if (x != begin() \&\& isect(--x, y)) isect(x, y = erase(y));
       while ((y = x) != begin() && (--x)->p >= y->p)
           isect(x, erase(y));
   11 query(11 x) {
       assert(!empty());
       Q = 1; auto l = *lower_bound({0,0,x}); Q = 0;
       return 1.k * x + 1.m:
   }
};
```

2.4 Point

```
const ld eps = 1e-9:
int sgn(ld a) {
   return (a > 0) - (a < 0);
struct point {
   // Use 11 everywhere instead of 1d if coordinates are always integers
   point(ld a = 0, ld b = 0) {
       x = a, y = b;
   bool operator==(const point& o) const {
       return x == o.x && y == o.y;
   point operator+(const point &b) const {
       return point(x + b.x, y + b.y);
   point operator-(const point &b) const {
       return point(x - b.x, y - b.y);
   point operator*(const ld &a) const {
       return point(x * a, y * a);
   point operator/(const ld &a) const {
       return point(x / a, y / a);
   ld vlensq() {
       return x * x + y * y;
   ld vlen() {
       return sqrtl(vlensq());
```

```
point perp() const {
       return point(-y, x);
};
ld dot(point a, point b) {
   return a.x * b.x + a.y * b.y;
ld cross(point a, point b) {
   return a.x * b.v - a.v * b.x:
point proj(point v, point u) {
   // projection of v onto u
   return u * (dot(v, u) / dot(u, u)):
// check if line segments AB and CD intersect
bool isect(point a, point b, point c, point d) {
   int A = sgn(cross(c - a, d - a));
   int B = sgn(cross(c - b, d - b));
   if (A * B != 0 && A == B) {
       return false:
   int C = sgn(cross(a - c, b - c));
   int D = sgn(cross(a - d, b - d));
   if (C * D != 0 && C == D) {
       return false;
   return true;
// intersection point of line segments AB and CD
point inter(point a, point b, point c, point d) {
   point ab = b - a;
   point cd = d - c;
   ld top = cross(a, ab) - cross(c, ab);
   ld bot = cross(cd, ab):
   // if(cd.x * top % bot != 0) // FLOATING POINT - CHANGE TO DOUBLE IF NECESSARY
   // return point(mod, mod);
   // if(cd.v * top % bot != 0) // FLOATING POINT - CHANGE TO DOUBLE IF NECESSARY
   // return point(mod, mod);
   1d X = c.x + cd.x * top / bot:
   1d Y = c.y + cd.y * top / bot;
   // or alternatively (works with doubles)
   // return c + cd * (top / bot)
   return point(X, Y);
}
// checks if circles with centers a, b and radiuses r1, r2 intersect
// intersection points are written to parameter out
bool circleInter(point a, point b,double r1,double r2,pair<point, point>* out) {
   if (a == b) { assert(r1 != r2); return false; }
   point vec = b - a;
   double d2 = vec.vlensq(), sum = r1+r2, dif = r1-r2,
         p = (d2 + r1*r1 - r2*r2)/(d2*2), h2 = r1*r1 - p*p*d2;
   if (sum*sum < d2 || dif*dif > d2) return false;
   point mid = a + vec*p, per = vec.perp() * sqrt(fmax(0, h2) / d2);
   *out = {mid + per, mid - per};
   return true:
```

```
// point in polygon
bool insidePoly(point p, vector<point>poly) {
   point mx = \{-1e9, -1e9\};
   for (point pp : poly) {
       if (pp.x > mx.x) {
          mx = pp;
   mx.x++;
   int cnt = 0;
   for (int i = 0; i < poly.size(); i++) {</pre>
       point a = poly[i];
       point b = poly[(i + 1) % poly.size()];
       if (isect(p, mx, a, b)) {
           cnt++:
   return cnt == 1;
// normalize vector
point toUnitVec(point vec) {
   return vec / vec.vlen();
// get unit vector that is orthogonal to given vector
point getUnitOrthog(point vec) {
   if (abs(vec.x) < eps || abs(vec.y) < eps) {</pre>
       swap(vec.x, vec.y);
       return toUnitVec(vec):
   point orthog(1, 0);
   orthog.y = -orthog.x * vec.x / vec.y;
   return toUnitVec(orthog);
/*
Geometry notes:
Pick's theorem:
If a polygon has all integer coordinates then the area A is
A = i + b / 2 - 1
where i is the number of integer points interior to the polygon
b is the number of integer points on the boundary
Shoelace formula:
1/2 * (x1*y2 - x2*y1 + x2*y3 - x3*y2 + ... + xn*y1 - x1*yn)
*/
```

2.5 Rotational Sweep

```
/***
https://codeforces.com/contest/1025/problem/F
```

```
***/
#include <bits/stdc++.h>
using namespace std;
typedef long long 11;
typedef long double ld;
struct point {
   11 x, y;
   point(l1 a = 0, l1 b = 0) {
       x = a, y = b;
   point operator+(const point &o) {
       return point(x + o.x, y + o.y);
   point operator-(const point &o) {
       return point(x - o.x, y - o.y);
};
11 dot(point a, point b) {
   return a.x * b.x + a.y * b.y;
11 cross(point a, point b) {
   return a.x * b.y - a.y * b.x;
}
int n;
ll ans;
vector<point> v;
void sweep(int id) {
   vector<point>u;
   for(int i = 0; i < n; i++) {</pre>
       if(i != id) {
           u.push_back(v[i]);
       }
   }
   point p = v[id];
   sort(u.begin(), u.end(), [&](point a, point b) {
       if((a.y >= p.y) != (b.y >= p.y)) {
           return a.y >= p.y;
       }
       return cross(a - p, b - p) < 0;
   });
   int r = 0, cnt = 0;
   for(int 1 = 0; 1 < u.size(); 1++) {</pre>
       if (1 > 0) {
           cnt--;
       int rr = (r + 1) % u.size();
       while (cnt != n - 2 && cross(u[1] - p, u[rr] - p) <= 0) {</pre>
           rr = (rr + 1) % u.size();
       }
       11 R = (r - 1 + u.size()) % u.size(), L = n - R - 2;
       ans += R * (R - 1) / 2 * L * (L - 1) / 2:
}
```

```
int main()
{
    ios_base::sync_with_stdio(false), cin.tie(0);
    cin >> n;
    v.resize(n);
    for(int i = 0; i < n; i++) {
        cin >> v[i].x >> v[i].y;
    }
    for(int i = 0; i < n; i++) {
        sweep(i);
    }
    cout << ans / 2 << "\n";
    return 0;
}</pre>
```

3 Graphs

3.1 2-Edge Connected Components

```
/*
 * Description: Finding 2-edge connected components using Tarjan's algorithm and
 * Verification: https://codeforces.com/contest/1000/problem/E
#include <bits/stdc++.h>
#define pb push_back
using namespace std;
typedef long long 11;
typedef long double ld;
const int maxn = 3e5 + 100;
int n, m, val[maxn], low[maxn], timer = 1, par[maxn], sz[maxn], vis[maxn];
vector<int> adj[maxn], g[maxn];
vector<pair<int, int>> bridges;
int root(int v) {
   return v == par[v] ? v : par[v] = root(par[v]);
void unite(int a, int b) {
   a = root(a), b = root(b):
   if (a == b) {
       return:
   if (sz[a] < sz[b]) {
       swap(a, b);
   par[b] = a;
   sz[a] += sz[b];
void tarjan(int v, int p = -1) {
   val[v] = low[v] = timer++;
   for (auto to : adj[v]) {
       if (to == p) {
           continue:
```

```
}
       if (!val[to]) {
           tarjan(to, v);
           low[v] = min(low[v], low[to]);
           if (low[to] > val[v]) {
               bridges.push_back({v, to});
           } else {
               unite(v, to);
       } else {
           low[v] = min(low[v], val[to]);
   }
void construct() {
   for (pair<int, int> p : bridges) {
       int a = root(p.first), b = root(p.second);
       g[a].push_back(b);
       g[b].push_back(a);
int main() {
   ios_base::sync_with_stdio(false), cin.tie(0);
   int n, m;
   cin >> n >> m;
   for (int i = 1; i <= n; i++) {</pre>
       par[i] = i, sz[i] = 1;
   for (int i = 0; i < m; i++) {</pre>
       int a, b;
       cin >> a >> b;
       adi[a].push back(b):
       adj[b].push_back(a);
   tarjan(1);
   construct();
   int v = 1, d = 0:
   for (int i = 1; i <= n; i++) {</pre>
       if (!g[i].empty()) {
          v = i:
       }
   }
   queue<pair<int, int>> Q;
   Q.push({v, 0});
   vis[v] = 1;
   while (!Q.empty()) {
       v = Q.front().first;
       d = Q.front().second;
       Q.pop();
       for (auto to : g[v]) {
          if (!vis[to]) {
               vis[to] = 1;
               Q.push(\{to, d + 1\});
       }
```

```
Q.push({v, 0});
for (int i = 0; i < maxn; i++) {</pre>
   vis[i] = 0;
vis[v] = 1;
while (!Q.empty()) {
   v = Q.front().first;
   d = Q.front().second;
   Q.pop();
   for (auto to : g[v]) {
       if (!vis[to]) {
           vis[to] = 1:
           Q.push(\{to, d + 1\});
       }
   }
}
cout << d << "\n":
return 0;
```

3.2 Bipartite Matching

```
int n;
bool vis[maxn];
int match[maxn];
vector<int>adj[maxn];
bool dfs(int v) {
   if (vis[v]) {
       return false;
   vis[v] = true;
   for (int to : adj[v]) {
       if (match[to] == -1 || dfs(match[to])) {
           match[v] = to, match[to] = v;
           return true;
   return false;
void matching() {
   memset(match, -1, sizeof match);
   while (true) {
       memset(vis, 0, sizeof vis);
       bool found = false;
       for (int i = 1; i <= n; i++) {</pre>
           if (!vis[i] && match[i] == -1) {
              found |= dfs(i);
          }
       if (!found) {
           break;
```

```
}
}
}
```

3.3 Dijkstra

```
11 D[maxn];
vector<pii> adj[maxn];
void Dijkstra(int st) {
   fill(D, D + maxn, LLONG_MAX);
   priority_queue<pii, vector<pii>, greater<pii>> Q;
   Q.push({D[st] = 0, st});
   while (!Q.empty()) {
       pii v = Q.top();
       Q.pop();
       if (D[v.y] < v.x) {
           continue;
       for (auto to : adi[v.v]) {
          if (v.x + to.y < D[to.x]) {
              Q.push(\{D[to.x] = v.x + to.y, to.x\});
       }
   }
}
```

3.4 Dinic

```
struct edge {
   int to, flow, cap;
vector<edge> edges;
vector<int> adi[maxn];
void add_edge(int a, int b, int cap) {
   edge ab = \{b, 0, cap\};
   edge ba = \{a, 0, 0\};
   adj[a].push_back(edges.size());
   edges.push_back(ab);
   adj[b].push_back(edges.size());
   edges.push_back(ba);
}
int vis[maxn], ptr[maxn], level[maxn], s, t;
bool bfs() {
   queue<int> Q;
   Q.push(s);
   while (!Q.empty()) {
       int v = Q.front();
       Q.pop();
       for (int id : adj[v]) {
           edge e = edges[id];
```

```
if (e.cap - e.flow < 1) {</pre>
               continue;
           if (level[e.to] != -1) {
               continue;
           level[e.to] = level[v] + 1;
           Q.push(e.to);
   return level[t] != -1;
int dfs(int v, int pushed) {
   if (pushed == 0) {
       return 0:
   if (v == t) {
       return pushed;
   for (int &j = ptr[v]; j < adj[v].size(); j++) {</pre>
       edge e = edges[adi[v][i]];
       if (level[v] + 1 != level[e.to] || e.cap - e.flow < 1) {</pre>
           continue;
       int tr = dfs(e.to, min(pushed, e.cap - e.flow));
       if (tr == 0) {
           continue;
       edges[adj[v][j]].flow += tr;
       edges[adj[v][j] ^ 1].flow -= tr;
       return tr;
   }
   return 0;
int max_flow() {
   int flow = 0;
   while (true) {
       memset(level, -1, sizeof level);
       level[s] = 0:
       if (!bfs()) {
           break;
       memset(ptr, 0, sizeof ptr);
       while (int pushed = dfs(s, mod)) {
           flow += pushed;
       }
   }
   return flow;
```

3.5 Edmonds-Karp

```
struct edge {
   int to, flow, cap, cost;
vector<edge> edges;
vector<int> adj[maxn];
void add_edge(int a, int b, int cap) {
   adj[a].push_back(edges.size());
   edges.push_back({b, 0, cap});
   adj[b].push_back(edges.size());
   edges.push_back({a, 0, 0});
}
int vis[maxn], pid[maxn], s, t;
int bfs() {
   queue<pair<int, int>> Q;
   vis[s] = 1;
   Q.push({s, mod});
   while (!Q.empty()) {
       int v, flow;
       tie(v, flow) = Q.front();
       Q.pop();
       if (v == t) {
           return flow;
       }
       for (int j : adj[v]) {
           edge e = edges[j];
          if (!vis[e.to] && e.cap - e.flow > 0) {
              vis[e.to] = 1;
              pid[e.to] = j;
              Q.push({e.to, min(e.cap - e.flow, flow)});
       }
   }
   return 0;
int max_flow() {
   int maxflow = 0;
   while (true) {
       memset(vis, 0, sizeof vis);
       int cur flow = bfs():
       if (cur flow == 0) {
           break;
       }
       maxflow += cur_flow;
       int v = t;
       while (v != s) {
          int j = pid[v];
           edges[j].flow += cur_flow;
           edges[j ^ 1].flow -= cur_flow;
          v = edges[j ^ 1].to;
       }
   }
   return maxflow;
```

3.6 Eulerian Tour

```
int n, m, even;
set<int> adj[maxn];
vector<int> tour:
void dfs(int v) {
   for (auto it = adj[v].begin(); adj[v].size() > 0;) {
       int to = *it;
       it = adj[v].erase(it);
       adj[to].erase(v);
       dfs(to);
   }
   tour.push_back(v);
int main() {
   ios_base::sync_with_stdio(false), cin.tie(0);
   cin >> n >> m;
   for (int i = 0: i < m: i++) {</pre>
       int a. b:
       cin >> a >> b;
       adj[a].insert(b);
       adj[b].insert(a);
   }
   for (int i = 1; i <= n; i++) {
       if (adi[i].size() % 2 == 0) {
           ++even:
   if (even != n && even != n - 2) {
       /// no tour exists
       return 0;
   }
   int start = 1;
   if (even == n - 2) {
       for (int i = 1; i <= n; i++) {
           if (adj[i].size() % 2 == 1) {
              start = i;
              break;
          }
       }
   dfs(start);
   for (int v : tour) {
       cout << v << " ";
   cout << "\n":
   return 0;
```

3.7 Hungarian

template < class T > bool ckmin(T& a, const T& b) { return a > b ? a = b, 1 : 0; }

```
template < class T > bool ckmax(T& a, const T& b) { return a < b ? a = b, 1 : 0; }
int hungarian(const vector<vector<int> >& a) {
   int n = sz(a) - 1, m = sz(a[0]) - 1; // jobs 1..n, workers 1..m
   vector\langle int \rangle u(n + 1), v(m + 1); // potentials
   vector<int> p(m + 1); // p[j] -> job picked by worker j
   for(int i = 1; i <= n; i++) { // find alternating path with job i</pre>
       p[0] = i; int j0 = 0; // add "dummy" worker 0
       vector<int> dist(m + 1,INT_MAX), pre(m + 1,-1); // prev vertex on shortest
            path
       vector<bool> done(m + 1, false);
       do { // dijkstra
           done[j0] = true; // fix dist[j0], update dists from j0
           int i0 = p[j0], j1;
          int delta = INT_MAX;
          for(int i = 1: i <= m: i++)</pre>
              if (!done[j]) {
                  auto cur = a[i0][j] - u[i0]-v[j];
                  if (ckmin(dist[j], cur))
                      pre[j] = j0;
                  if (ckmin(delta, dist[j]))
                      i1 = i;
           for(int j = 0; j <= m; j++) { // subtract constant from all edges going</pre>
              // from done -> not done vertices, lowers all
              // remaining dists by constant
              if (done[i])
                  u[p[j]] += delta, v[j] -= delta;
                  dist[i] -= delta:
          }
       } while (p[j0]); // potentials adjusted so that all edge weights are
            non-negative
       // perfect matching has zero weight and
       // costs of augmenting paths do not change
       while (i0) { // update jobs picked by workers on alternating path
          int j1 = pre[j0];
          p[j0] = p[j1];
          j0 = j1;
       }
   }
   return -v[0]; // min cost
```

3.8 Min Cost Max Flow

```
struct edge {
   int to, flow, cap, cost;
   edge(int a = 0, int b = 0, int c = 0, int d = 0) {
      to = a, flow = b, cap = c, cost = d;
   }
```

```
vector<edge> edges;
vector<int> adj[maxn];
void add_edge(int a, int b, int cap, int cost) {
   edge ab(b, 0, cap, cost);
   edge ba(a, 0, 0, -cost);
   adj[a].push_back(edges.size());
   edges.push_back(ab);
   adj[b].push_back(edges.size());
   edges.push_back(ba);
int vis[maxn], pid[maxn], s, t;
int dist[maxn]:
pii dijkstra() {
   priority_queue<pair<int, pii>, vector<pair<int, pii>>, greater<pair<int,</pre>
        pii>>> 0:
   vis[s] = 1:
   Q.push({0, {s, mod}});
   while (!Q.empty()) {
       int v, flow, w;
       pair<int, pii> p = Q.top();
       Q.pop();
       w = p.x;
       v = p.y.x;
       flow = p.y.y;
       if (dist[v] < w) {</pre>
           continue;
       if (v == t) {
          return make_pair(w, flow);
       for (int j : adj[v]) {
           edge e = edges[j];
          if (!vis[e.to] && e.cap - e.flow > 0) {
              if (w + e.cost < dist[e.to]) {</pre>
                  dist[e.to] = w + e.cost:
                  pid[e.to] = i:
                  Q.push({dist[e.to], {e.to, min(e.cap - e.flow, flow)}});
          }
       }
   }
   return make_pair(0, 0);
pii max_flow() {
   int maxflow = 0, mincost = 0;
   while (true) {
       fill(dist, dist + maxn, mod);
       pii cur_flow = dijkstra();
       if (cur_flow.y == 0) {
          break;
       maxflow += cur flow.v:
       mincost += cur_flow.x;
       int v = t:
```

```
while (v != s) {
    int j = pid[v];
    edges[j].flow += cur_flow.y;
    edges[j ^ 1].flow -= cur_flow.y;
    v = edges[j ^ 1].to;
}
return make_pair(mincost, maxflow);
```

3.9 Tarjan SCC

```
int val[maxn], low[maxn], scc[maxn], siz[maxn], tim, onStack[maxn], cnt;
stack<int> st:
void tarjan(int v) {
   low[v] = val[v] = tim++;
   onStack[v] = 1;
   st.push(v);
   for (int to : adj[v]) {
       if (val[to] == 0) {
           tarjan(to);
          low[v] = min(low[v], low[to]);
       } else if (onStack[to]) {
          low[v] = min(low[v], val[to]);
       }
   if (low[v] == val[v]) {
       cnt++:
       while (true) {
          int u = st.top();
           st.pop();
          onStack[u] = 0;
          scc[u] = cnt;
          ++siz[cnt]:
          if (u == v) {
              break;
       }
   }
```

4 Math

4.1 Basis

```
// Basis of vectors modulo 2 (for xor related problems)
// https://codeforces.com/blog/entry/68953
ll basis[62];
```

```
void add(ll a) {
   for (int bit = 61; bit >= 0; bit--) {
      if (a >> bit & 1) {
        if (basis[bit]) {
            a ^= basis[bit];
      } else {
            basis[bit] = a;
            return;
      }
   }
}
```

4.2 Big Integer

```
* Description: Big Integer struct
#include <bits/stdc++.h>
#define pb push_back
#define all(a) a.begin(), a.end()
#define sz(a) (int)a.size()
#define x first
#define y second
using namespace std;
typedef long long 11;
typedef long double ld;
typedef pair<int, int> pii;
const int maxn = 1e5 + 100;
const ll base = 1e18;
const int SZ = 300;
struct BigInt {
   vector<ll> digs;
   bool neg;
   BigInt() {
       digs.assign(SZ, 0);
       neg = false;
   BigInt(ll num) {
       digs.assign(SZ, 0);
       neg = (num < 0);
       digs[0] = abs(num);
   BigInt &operator=(const 11 &b) {
       return *this = BigInt(b);
   BigInt &operator=(const BigInt &b) {
       for (int i = 0; i < SZ; i++) {</pre>
          digs[i] = b.digs[i];
       neg = b.neg;
       return *this:
```

```
};
bool operator<(const BigInt &a, const BigInt &b) {</pre>
   if (a.neg != b.neg) return a.neg;
   for (int i = SZ - 1; i >= 0; i--) {
       if (a.digs[i] != b.digs[i]) {
           return (a.digs[i] < b.digs[i]) ^ (a.neg);</pre>
       }
   return false;
bool operator==(const BigInt &a, const BigInt &b) {
   return !(a < b) && !(b < a):
bool operator>(const BigInt &a, const BigInt &b) {
   return b < a:
ostream &operator<<(ostream &out, const BigInt &a) {
   if (a.neg) out << "-";</pre>
   bool flag = false;
   for (int i = SZ - 1; i >= 0; i--)
       if (a.digs[i] > 0 || flag) {
           if (flag) {
               out << setw(18) << setfill('0') << a.digs[i];
           } else {
               out << a.digs[i];</pre>
           flag = true;
       }
   return out;
BigInt operator+(const BigInt &a, const BigInt &b) {
   if (a.neg != b.neg) {
       BigInt aa = a. bb = b:
       if (aa.neg) swap(aa, bb);
       BigInt c;
       bb.neg = false:
       c.neg = (aa < bb);
       if (aa < bb) swap(aa, bb):
       11 borrow = 0:
       for (int i = 0; i < SZ; i++) {</pre>
           c.digs[i] = aa.digs[i] - bb.digs[i] - borrow;
           if (c.digs[i] < 0) {</pre>
               c.digs[i] += base, borrow = 1;
           } else {
              borrow = 0;
       }
       return c;
   } else {
       11 carry = 0;
       BigInt c;
       for (int i = 0: i < SZ: i++) {
           c.digs[i] = a.digs[i] + b.digs[i] + carry;
           if (c.digs[i] >= base) {
```

```
c.digs[i] -= base, carry = 1;
          } else {
               carry = 0;
       c.neg = a.neg;
       return c;
BigInt operator+=(BigInt &a, const BigInt &b) {
   return a = a + b:
BigInt operator-(BigInt &a, BigInt &b) {
    b.neg ^= true:
   BigInt c = a + b;
   b.neg ^= true:
   return c;
BigInt operator-=(BigInt &a, BigInt &b) {
   return a = a - b;
BigInt max(BigInt a, BigInt b) {
   if (a > b) {
       return a;
   } else {
       return b;
BigInt min(BigInt a, BigInt b) {
   if (a < b) {
       return a:
   } else {
       return b;
}
int main() {
   ios_base::sync_with_stdio(false), cin.tie(0);
   BigInt a, b;
   ll aa. bb:
    cin >> aa >> bb:
   a = BigInt(aa), b = BigInt(bb);
    cout << "a+b " << a + b << "\n";
   cout << "a-b " << a - b << "\n";
   BigInt c = a;
   c += b;
   cout << "a+=b " << c << "\n";
   c = b:
    cout << "b+=a " << c << "\n";
    cout << "a<b " << (a < b) << "\n";
   cout << "a>b " << (a > b) << "\n";
   cout << "a==b" << (a == b) << "\n":
   cout << "max(a, b) " << max(a, b) << "\n";</pre>
   cout << "min(a, b) " << min(a, b) << "\n";</pre>
   return 0:
```

}

4.3 Extended Euclidean Algorithm

```
const ll mod = 1e9 + 7;
ll gcd(ll a, ll b, ll &x, ll &y) {
    if (b == 0) {
        x = 1, y = 0;
        return a;
    }
    ll x1, y1;
    ll ret = gcd(b, a % b, x1, y1);
    x = y1;
    y = x1 - (a / b) * y1;
    return ret;
}
ll modinv(ll a) {
    ll x, y;
    gcd(a, mod, x, y);
    return (x % mod + mod) % mod;
}
```

4.4 FFT

```
#define rep(i, a, b) for(int i = a; i < (b); ++i)
#define all(x) begin(x), end(x)
#define sz(x) (int)(x).size()
typedef long long 11;
typedef pair<int, int> pii;
typedef vector<int> vi;
typedef complex<double> C;
typedef vector<double> vd;
void fft(vector<C>& a) {
   int n = sz(a), L = 31 - builtin clz(n):
   static vector<complex<long double>> R(2, 1);
   static vector<C> rt(2, 1); // (^ 10% faster if double)
   for (static int k = 2: k < n: k *= 2) {
      R.resize(n): rt.resize(n):
       auto x = polar(1.0L, acos(-1.0L) / k);
       rep(i,k,2*k) rt[i] = R[i] = i&1 ? R[i/2] * x : R[i/2];
   vi rev(n):
   rep(i,0,n) rev[i] = (rev[i / 2] | (i & 1) << L) / 2;
   rep(i,0,n) if (i < rev[i]) swap(a[i], a[rev[i]]);
   for (int k = 1; k < n; k *= 2)
       for (int i = 0; i < n; i += 2 * k) rep(j,0,k) {
          // C z = rt[j+k] * a[i+j+k]; // (25\% faster if hand-rolled) ///
               include-line
          auto x = (double *)&rt[j+k], y = (double *)&a[i+j+k]; /// exclude-line
```

```
C z(x[0]*y[0] - x[1]*y[1], x[0]*y[1] + x[1]*y[0]);
                                                                  /// exclude-line
          a[i + j + k] = a[i + j] - z;
          a[i + j] += z;
// conv(a, b) = c, where c[x] = Sum_over_i (a[i] * b[x - i])
// rounding is safe if (Sum(a_i^2) + Sum(b_i^2)) * log_2(N) < 9 * 10^14 (in
    practice 10^16)
vd conv(const vd& a, const vd& b) {
   if (a.empty() || b.empty()) return {};
   vd res(sz(a) + sz(b) - 1);
   int L = 32 - __builtin_clz(sz(res)), n = 1 << L;</pre>
   vector<C> in(n), out(n):
   copy(all(a), begin(in));
   rep(i,0,sz(b)) in[i].imag(b[i]);
   fft(in):
   for (C& x : in) x *= x;
   rep(i,0,n) out[i] = in[-i & (n-1)] - conj(in[i]);
   rep(i,0,sz(res)) res[i] = imag(out[i]) / (4 * n);
   return res;
```

4.5 Fraction

```
* Description: Fraction struct
#include <bits/stdc++.h>
#define pb push_back
#define all(a) a.begin(), a.end()
#define sz(a) (int)a.size()
#define x first
#define y second
using namespace std;
typedef long long 11;
typedef long double ld:
typedef pair<int, int> pii;
const int maxn = 1e5 + 100;
struct fraction {
   ll sk. v:
   fraction() {
       sk = 0, v = 1:
   fraction(ll _sk, ll _v) {
       sk = _sk, v = _v;
       11 \text{ dbd} = \_\_gcd(sk, v);
       sk /= dbd, v /= dbd;
       if (v < 0) sk *= -1, v *= -1;
};
fraction abs(fraction f) { return fraction(abs(f.sk), f.v); }
```

```
bool operator<(const fraction &a, const fraction &b) { return a.sk * b.v < b.sk *
     a.v: }
bool operator>(const fraction &a, const fraction &b) { return a.sk * b.v > b.sk *
     a.v: }
bool operator == (const fraction &a, const fraction &b) { return a.sk == b.sk &&
     a.v == b.v: }
bool operator!=(const fraction &a, const fraction &b) { return !(a == b); }
fraction operator+(const fraction &a, const fraction &b) { return fraction(a.sk *
     b.v + b.sk * a.v. a.v * b.v): }
fraction operator+=(fraction &a, const fraction &b) { return a = a + b; }
fraction operator-(const fraction &a, const fraction &b) { return fraction(a.sk *
     b.v - b.sk * a.v. a.v * b.v): }
fraction operator == (fraction &a. const fraction &b) { return a = a - b; }
fraction operator*(const fraction &a. const fraction &b) { return fraction(a.sk *
    b.sk. a.v * b.v): }
fraction operator*=(fraction &a. const fraction &b) { return a = a * b; }
fraction operator*(int a, const fraction &b) { return fraction(a * b.sk, b.v); }
fraction operator*(const fraction &a, int b) { return fraction(a.sk * b, a.v); }
fraction operator/(const fraction &a, const fraction &b) { return fraction(a.sk *
    b.v. a.v * b.sk): 
fraction operator/=(fraction &a, const fraction &b) { return a = a / b; }
ostream &operator << (ostream &strm, const fraction &a) {
   if (a.v == 1)
       strm << a.sk;
   else
       strm << a.sk << "/" << a.v;
   return strm;
int main() {
   ios_base::sync_with_stdio(false), cin.tie(0);
   int a. w. e. r:
   cin >> q >> w >> e >> r;
   fraction a(q, w);
   fraction b(e, r):
   cout << "< " << (a < b) << "\n";
   cout << "> " << (a > b) << "\n";
   cout << "== " << (a == b) << "\n":
   cout << "!= " << (a != b) << "\n";
   cout << "+ " << (a + b) << "\n":
   cout << "- " << (a - b) << "\n":
   cout << "* " << (a * b) << "\n":
   cout << "/ " << (a / b) << "\n";
   return 0;
```

4.6 Gauss

```
const double EPS = 1e-9;
const int INF = 2; // it doesn't actually have to be infinity or a big number
int gauss(vector<vector<double> > a, vector<double>& ans) {
  int n = (int)a.size();
```

```
int m = (int)a[0].size() - 1;
    vector<int> where(m, -1);
    for (int col = 0, row = 0; col < m && row < n; ++col) {</pre>
        int sel = row;
        for (int i = row; i < n; ++i)</pre>
           if (abs(a[i][col]) > abs(a[sel][col]))
               sel = i:
        if (abs(a[sel][col]) < EPS)</pre>
           continue;
        for (int i = col; i <= m; ++i)</pre>
           swap(a[sel][i], a[row][i]);
        where[col] = row:
        for (int i = 0; i < n; ++i)</pre>
           if (i != row) {
               double c = a[i][col] / a[row][col]:
               for (int j = col; j <= m; ++j)</pre>
                   a[i][i] -= a[row][i] * c;
           }
        ++row;
    }
    ans.assign(m, 0);
    for (int i = 0; i < m; ++i)</pre>
       if (where[i] != -1)
           ans[i] = a[where[i]][m] / a[where[i]][i];
    for (int i = 0; i < n; ++i) {</pre>
       double sum = 0:
        for (int j = 0; j < m; ++j)
           sum += ans[j] * a[i][j];
       if (abs(sum - a[i][m]) > EPS)
           return 0:
    for (int i = 0: i < m: ++i)</pre>
       if (where[i] == -1)
           return INF;
    return 1:
}
vector<int> GaussModulo(vector<vector<int>> mat) {
   for (int i = 0; i < mat.size(); i++) {</pre>
       int val = mat[i][i];
        int mul = modinv(val);
        for (int k = 0; k < mat[i].size(); k++)</pre>
           mat[i][k] = 1ll * mat[i][k] * mul % mod;
        for (int j = 0; j < mat.size(); j++)</pre>
           if (i != j) {
               int times = mat[j][i];
               for (int k = 0; k < mat[j].size(); k++)</pre>
                   mat[j][k] = (mat[j][k] - 111 * times * mat[i][k] % mod + mod) %
                        mod.
           }
    }
```

```
vector<int> ret;
for (int i = 0; i < mat.size(); i++) {
    ret.push_back(mat[i].back());
}
return ret;
}</pre>
```

4.7 Matrix Struct

```
int add(int a, int b) {
   int c = a + b:
   if (c > mod) {
       c -= mod:
   return c;
int mul(int a, int b) {
   11 c = (11)a * b;
   c %= mod:
   return (int)c;
struct matrix {
   int N, M;
   vector<vector<int>> mat;
   matrix(int n, int m) {
       N = n, M = m;
       mat = vector<vector<int>>(N, vector<int>(M, 0));
   }
   void ident() {
       for (int i = 0; i < N; i++) {</pre>
           for (int j = 0; j < N; j++) {
               mat[i][j] = (i == j);
       }
   matrix(vector<vector<int> > arr) {
       N = arr.size(), M = arr[0].size();
       mat = vector<vector<int> >(N, vector<int>(M, 0));
       for (int i = 0; i < N; i++) {</pre>
           for (int j = 0; j < M; j++) {</pre>
               mat[i][j] = arr[i][j];
       }
   }
   matrix operator*(const matrix &o) {
       matrix ret(N, o.M);
       for (int i = 0; i < ret.N; i++) {</pre>
           for (int j = 0; j < ret.M; j++) {</pre>
              for (int k = 0; k < M; k++) {
                  ret.mat[i][j] = add(ret.mat[i][j], mul(mat[i][k], o.mat[k][j]));
           }
```

```
}
    return ret;
}

matrix pwr(matrix a, ll pw) {
    matrix ret(a);
    ret.ident();
    while (pw > 0) {
        if (pw & 1) {
            ret = ret * a;
        }
        a = a * a;
        pw >>= 1;
    }

return ret;
}
```

4.8 Modulo operations

```
typedef long long ll;
const ll mod = 1e9 + 7;
ll pwr(ll num, ll pw) {
    ll ret = 1;
    while (pw > 0) {
        if (pw & 1) {
            ret = (ret * num) % mod;
        }
        num = (num * num) % mod;
        pw >>= 1;
    }
    return ret;
}
ll modinv(ll a) { return pwr(a, mod - 2); }
ll add(ll a, ll b) { return (a + b) % mod; }
ll sub(ll a, ll b) { return (a - b + mod) % mod; }
ll mul(ll a, ll b) { return (a * b) % mod; }
```

5 Misc

5.1 Custom Vector

```
/*
 * Source: https://codeforces.com/blog/entry/70472?#comment-549341
 * Description: Implementation of vector with negative indexing
 */
#include <bits/stdc++.h>
using namespace std;

template<class T>
```

```
struct MyVector {
    int offset;
    vector<T> vec_;
    MyVector(int n, int off, T &&values = T()) {
       vec_.resize(n, values);
       offset = off;
    T& operator[](int i) {
       i += offset;
       assert(0 <= i && i < (int)vec_.size());</pre>
       return vec_[i];
};
int main()
{
    ios_base::sync_with_stdio(false), cin.tie(0);
    // Example usage
    MyVector < MyVector < int > dp(10 + 1, 5, MyVector < int > (8 + 1, 4));
    for (int i = -5; i <= 5; i++) {</pre>
       for (int j = -4; j <= 4; j++) {
           dp[i][j] = i * j;
       }
   }
    for (int i = -5; i <= 5; i++) {
       for (int j = -4; j \le 4; j++) {
           cout << i << " " << j << " " << dp[i][j] << "\n";
       }
   }
   return 0;
}
```

6 Notes

6.1 Notes

```
/*
---
Pick's theorem:

If a polygon has all integer coordinates then the area A is A = i + b / 2 - 1
where i is the number of integer points interior to the polygon b is the number of integer points on the boundary
---
Shoelace formula:
1/2 * (x1*y2 - x2*y1 + x2*y3 - x3*y2 + ... + xn*y1 - x1*yn)
---
Euler's formula:
```

```
For a connected planar graph with v vertices, e edges and f faces (including
    outer)
v - e + f = 2
*/
```

7 Strings

7.1 Bitset Trie

```
template <int N>
struct trie {
   int t[N + 1][2], nxt = 1;
   trie() {
       memset(t, 0, sizeof t);
   void ins(string s) {
       int cur = 0:
       for (int i = 0; i < s.size(); ++i) {</pre>
           int bit = s[i] - '0';
           if (!t[cur][bit]) {
               t[cur][bit] = nxt++;
           cur = t[cur][bit];
       }
   }
   bool fnd(string s) {
       int cur = 0;
       for (int i = 0; i < s.size(); ++i) {</pre>
           int bit = s[i] - '0';
           if (!t[cur][bit]) {
               return false;
           cur = t[cur][bit];
       return true;
};
```

7.2 Hashing

```
/*
Works, but might be a little slow
https://judge.yosupo.jp/submission/80957
*/
bool is_prime(int a) {
   if (a == 1) {
```

```
return false;
   if (a % 2 == 0) {
       return a == 2;
   for (int i = 3; i * i <= a; i += 2) {
       if (a % i == 0) {
          return false;
   return true;
int pwr(int a, int pw, int MOD) {
   <u>int</u> ret = 1:
   while (pw > 0) {
       if (pw & 1) {
          ret = 111 * ret * a % MOD;
       a = 111 * a * a % MOD;
       pw >>= 1;
   return ret;
}
int modinv(int a, int MOD) {
   return pwr(a, MOD - 2, MOD);
}
struct hashing {
   vector<vector<int> >ha:
   vector<vector<int> >rha;
   static vector<vector<int> >pw;
   static vector<vector<int> >inv_pw;
   static vector<int>mods:
   static vector<int>BASE_INV;
   static int BASE;
   static int M:
   int N;
   static vector<int>zero vector(int len) {
       vector<int>ret;
       for (int i = 0; i < len; i++) {</pre>
           ret.push_back(0);
       }
       return ret;
   }
   struct hash {
       vector<int>h;
       int len;
       hash() {
           h = zero_vector(M);
           len = 0;
       }
```

```
hash(vector<int>h, int len) {
   this -> h = h;
   this->len = len;
bool operator==(const hash& b) const {
   return h == b.h && len == b.len;
hash operator-(const hash& b) {
   hash c:
   c.h = h:
   for (int j = 0; j < M; j++) {</pre>
       c.h[i] = b.h[i]:
       if (c.h[j] < 0) {
           c.h[j] += mods[j];
       c.h[j] = 1ll * c.h[j] * inv_pw[b.len][j] % mods[j];
   c.len = len - b.len;
   return c;
hash operator-=(const hash& b) {
   hash c = *this;
   c = c - b;
   this->h = c.h;
   this->len = c.len;
   return *this;
}
hash operator+(const hash& b) {
   hash c:
   c.h = h:
   for (int j = 0; j < M; j++) {</pre>
       c.h[j] += 111 * pw[len][j] * b.h[j] % mods[j];
       if (c.h[j] >= mods[j]) {
           c.h[j] -= mods[j];
   }
   c.len = len + b.len;
   return c;
}
hash operator+=(const hash& b) {
   hash c = *this;
   c = c + b;
   this \rightarrow h = c.h:
   this->len = c.len;
   return *this:
```

```
}
   bool operator<(const hash& b) const {</pre>
       for (int i = 0; i < M; i++) {</pre>
           if (h[i] != b.h[i]) {
               return h[i] < b.h[i];</pre>
           }
       return len < b.len:
   }
};
hashing(string s) {
   if (M == 0 || BASE == 0) {
       cerr << "Initialize mods and base before creating a hashing instance!";</pre>
       exit(1):
   }
    init_string(s);
static void init_base() {
  mt19937 rng(chrono::steady_clock::now().time_since_epoch().count());
   uniform_int_distribution<>distrib(3, (int)1e9);
   while (true) {
       BASE = distrib(rng);
       if (is_prime(BASE)) {
           break;
       }
   }
static void init mods(vector<int>new mods) {
   mods = new mods:
   M = (int)mods.size():
   BASE_INV = vector<int>(M);
   for (int j = 0; j < M; j++) {</pre>
       BASE INV[i] = modinv(BASE, mods[i]):
   }
static void init_pows(int MAX_POW) {
   pw = vector<vector<int> >(MAX_POW + 1, vector<int>(M));
   inv_pw = vector<vector<int> >(MAX_POW + 1, vector<int>(M));
   for (int i = 0; i <= MAX_POW; i++) {</pre>
       for (int j = 0; j < M; j++) {</pre>
           if (i == 0) {
               pw[i][j] = 1;
               inv_pw[i][j] = 1;
               pw[i][j] = 111 * pw[i - 1][j] * BASE % mods[j];
               inv_pw[i][j] = 1ll * inv_pw[i - 1][j] * BASE_INV[j] % mods[j];
           }
       }
   }
```

```
}
   void init_string(string s) {
       N = (int)s.size();
       ha = vector<vector<int> >(N, vector<int>(M));
       rha = vector<vector<int> >(N, vector<int>(M));
       init_pows(N * 2);
       for (int i = 0; i < N; i++) {</pre>
          for (int j = 0; j < M; j++) {</pre>
              ha[i][j] = 111 * pw[i][j] * (s[i] - 'a' + 1) % mods[j];
              rha[i][j] = 111 * pw[i][j] * (s[N - i - 1] - 'a' + 1) % mods[j];
              if (i > 0) {
                  ha[i][j] += ha[i - 1][j];
                  if (ha[i][j] >= mods[j]) {
                      ha[i][i] -= mods[i];
                  rha[i][j] += rha[i - 1][j];
                  if (rha[i][j] >= mods[j]) {
                      rha[i][j] -= mods[j];
             }
          }
      }
   hash get_hash(int i, int j, bool reverse) {
       if (i > j) {
           return hash();
       hash pref_i, pref_j;
       if (reverse) {
           i = N - i - 1:
           j = N - j - 1;
           swap(i, j);
           pref i = (i == 0 ? hash() : hash(rha[i - 1], i));
          pref_j = hash(rha[j], j + 1);
           pref_i = (i == 0 ? hash() : hash(ha[i - 1], i));
           pref_j = hash(ha[j], j + 1);
       return pref_j - pref_i;
};
vector<vector<int> > hashing::pw;
vector<vector<int> > hashing::inv_pw;
vector<int> hashing::mods;
vector<int> hashing::BASE_INV;
int hashing::BASE;
```

int hashing::M;

7.3 Hashing2

```
#include <iostream>
#include <vector>
using namespace std;
typedef long long 11;
struct RollingHash {
   static const 11 mod0 = 1000000123, mod1 = 1000000007;
   static const 11 base0 = 137, base1 = 163;
   vector<ll> po0, po1;
   vector<ll> hsh0, hsh1;
   void init(string str) {
       if (!po0.size()) po0 = po1 = {1};
       hsh0 = {base0}, hsh1 = {base1};
       for (int i = 0; i < (int)str.size(); i++) {</pre>
           if (str[i] >= 'A' && str[i] <= 'Z') str[i] += 'a'-'A':
           hsh0.push_back((hsh0.back() * base0 % mod0 + str[i]) % mod0);
           hsh1.push_back((hsh1.back() * base1 % mod1 + str[i]) % mod1);
       }
   }
   pair<11,11> cut(int 1, int r) {
       while (po0.size() <= r+1) {</pre>
           po0.push_back(po0.back() * base0 % mod0);
           po1.push_back(po1.back() * base1 % mod1);
       }
       return make_pair((hsh0[r+1]+mod0-(hsh0[1]*po0[r-1+1]%mod0))%mod0,
                       (hsh1[r+1]+mod1-(hsh1[l]*po1[r-l+1]%mod1))%mod1);
   }
} rh;
```

7.4 KMP

```
/*
 * Source: KACTL
 * Description: Linear time string matching
 */
#include <bits/stdc++.h>
#define pb push_back
#define all(a) a.begin(), a.end()
#define sz(a) (int)a.size()
#define x first
```

```
#define y second
using namespace std;
typedef long long 11;
typedef long double ld;
typedef pair<int, int> pii;
const int maxn = 1e5 + 100;
vector<int> build_lps(string s) {
   vector<int> lps(sz(s), 0);
   for (int i = 1; i < sz(s); ++i) {
       int id = lps[i - 1];
       while (id && s[i] != s[id]) {
           id = lps[id - 1];
       lps[i] = id + (s[i] == s[id]);
   return lps;
}
vector<int> KMP(string s, string pat) {
   vector<int> lps = build_lps(pat + '\0' + s), res;
   for (int i = 0; i < sz(lps); ++i) {</pre>
       if (lps[i] == sz(pat)) {
           res.pb(i - 2 * sz(pat));
   }
   return res;
int main() {
   ios_base::sync_with_stdio(false), cin.tie(0);
   string s, pat;
   cin >> s >> pat;
   vector<int> res = KMP(s, pat);
   for (auto aa : res) {
       cout << aa << " ";
   cout << "\n";
   return 0;
```

7.5 SuffixArray

```
vector<int> sort_cyclic_shifts(string const& s) {
   int n = s.size();
   const int alphabet = 256;
   vector<int> p(n), c(n), cnt(max(alphabet, n), 0);
   for (int i = 0; i < n; i++)
        cnt[s[i]]++;
   for (int i = 1; i < alphabet; i++)
        cnt[i] += cnt[i - 1];
   for (int i = 0; i < n; i++)
        p[--cnt[s[i]]] = i;
   c[p[0]] = 0;
   int classes = 1;</pre>
```

```
for (int i = 1; i < n; i++) {</pre>
       if (s[p[i]] != s[p[i - 1]])
           classes++;
       c[p[i]] = classes - 1;
   vector<int> pn(n), cn(n);
   for (int h = 0; (1 << h) < n; ++h) {
       for (int i = 0; i < n; i++) {</pre>
           pn[i] = p[i] - (1 << h);
           if (pn[i] < 0)</pre>
               pn[i] += n;
       fill(cnt.begin(), cnt.begin() + classes, 0);
       for (int i = 0; i < n; i++)
           cnt[c[pn[i]]]++;
       for (int i = 1: i < classes: i++)</pre>
           cnt[i] += cnt[i - 1]:
       for (int i = n - 1; i >= 0; i--)
           p[--cnt[c[pn[i]]]] = pn[i];
       cn[p[0]] = 0;
       classes = 1;
       for (int i = 1; i < n; i++) {</pre>
           pair<int, int> cur = {c[p[i]], c[(p[i] + (1 << h)) % n]};</pre>
           pair < int, int > prev = \{c[p[i - 1]], c[(p[i - 1] + (1 << h)) % n]\};
           if (cur != prev)
               ++classes;
           cn[p[i]] = classes - 1;
       }
       c.swap(cn);
   return p;
vector<int> suffix_array_construction(string s) {
   vector<int> sorted_shifts = sort_cyclic_shifts(s);
   sorted_shifts.erase(sorted_shifts.begin());
   return sorted shifts:
```

8 Trees

8.1 Centroid Decomposition

```
/*
 * Description: Centroid Decomposition on trees
 * Verification: http://codeforces.com/contest/321/problem/C
 */
#include <bits/stdc++.h>
#define push_back push_back
#define all(a) a.begin(), a.end()
#define sz(a) (int)a.size()
#define x first
```

```
#define y second
using namespace std;
typedef long long 11;
typedef long double ld;
typedef pair<int, int> pii;
const int maxn = 1e5 + 100;
vector<int> adj[maxn];
int n, sub[maxn], par[maxn];
bool vis[maxn]:
char ans[maxn]:
void dfs(int v) {
   sub[v] = 1:
   for (auto to : adj[v]) {
       if (!vis[to] && to != par[v]) {
          par[to] = v;
           dfs(to):
           sub[v] += sub[to];
int get_centroid(int v) {
   par[v] = 0;
   dfs(v);
   int sz = sub[v];
   while (true) {
       pii mx = \{0, 0\};
       for (auto to : adj[v]) {
           if (!vis[to] && par[v] != to) {
              mx = max(mx, {sub[to], to});
       if (mx.first * 2 > sz) {
           v = mx.second:
       } else {
           return v;
   }
void solve(int v. int level = 0) {
   v = get centroid(v):
   vis[v] = true;
   ans[v] = (char)(level + 'A');
   for (auto to : adj[v]) {
       if (!vis[to]) {
           solve(to, level + 1);
   }
}
int main() {
   ios_base::sync_with_stdio(false), cin.tie(0);
   cin >> n;
   for (int i = 0; i < n - 1; i++) {</pre>
       int a. b:
       cin >> a >> b;
       adj[a].push_back(b);
```

```
adj[b].push_back(a);
}
solve(1);
for (int i = 1; i <= n; i++) {
    cout << ans[i] << " ";
}
cout << "\n";
return 0;
}</pre>
```

8.2 Lowest Common Ancestor

```
for (int to : adj[v]) {
       if (to != p) {
          dfs(to, v);
int lca(int a, int b) {
   if (dep[a] < dep[b]) {</pre>
       swap(a, b);
   for (int i = 17; i >= 0; i--) {
       if (dep[anc[a][i]] >= dep[b]) {
          a = anc[a][i];
   if (a == b) {
       return a;
   for (int i = 17; i >= 0; i--) {
       if (anc[a][i] != anc[b][i]) {
          a = anc[a][i], b = anc[b][i];
   }
   return anc[a][0];
int getDist(int v, int u) {
   return dep[v] + dep[u] - 2 * dep[lca(v, u)];
```