

# Multi-modeling the morphogenesis of transportation networks

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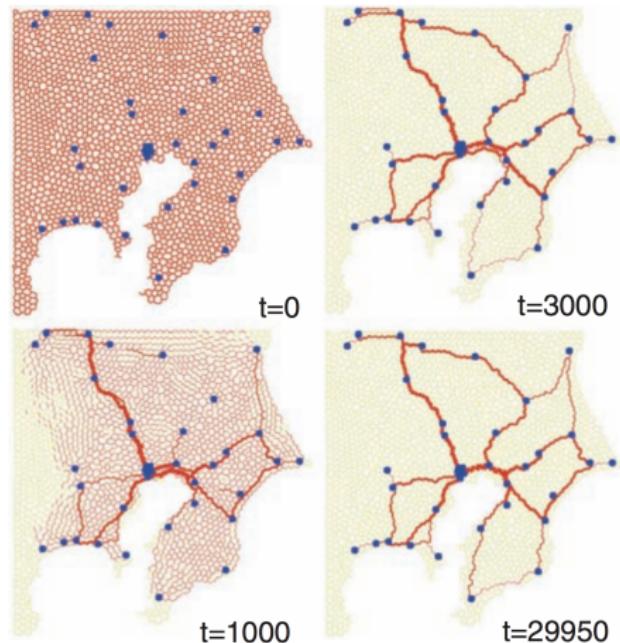
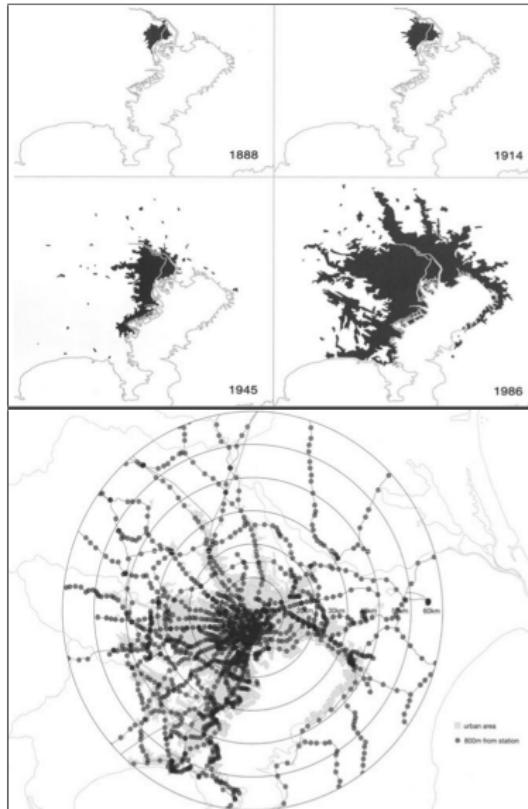
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# Urban growth and network growth



Source: [Tero et al., 2010]

Source:  
[Okata and Murayama, 2011]

# Transportation networks



*Source: OpenStreetMap*

# Morphogenesis of transportation networks

*Is the city alive ?* No

*Is the city ALife ?* Kind of

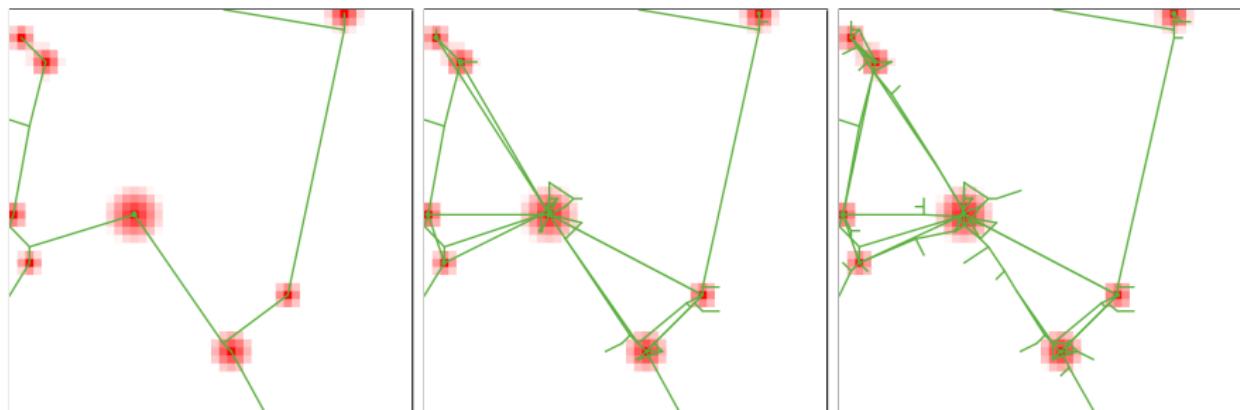
→ Cities (territorial systems) are morphogenetic [Doursat et al., 2012]

**Research objective:** *Understand the morphogenesis of transportation networks (road network), taking into account multiple concurrent processes through multi-modeling*

# Road network generation algorithm

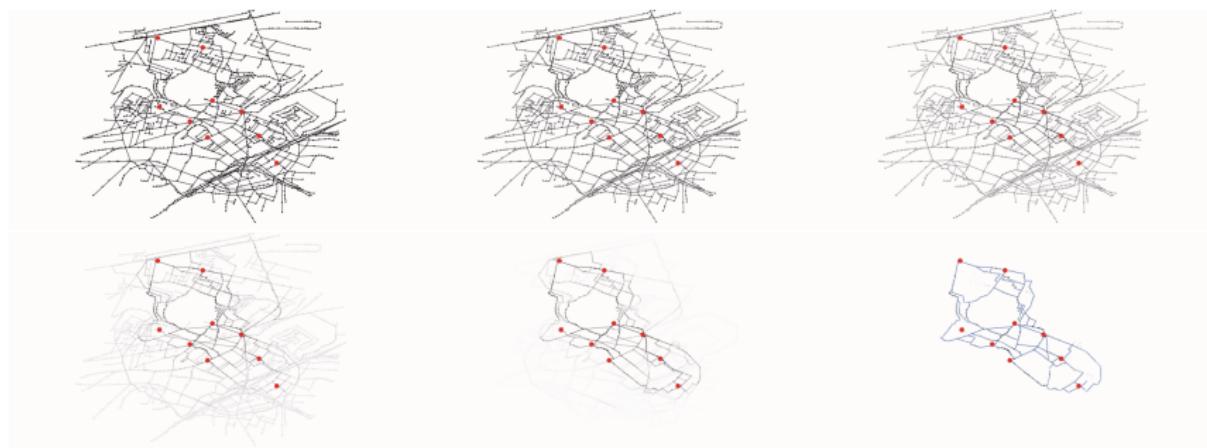
At each time step, with a fixed population density:

- ① Add new nodes preferentially to population and connect them
- ② Variable heuristic for new links, among: nothing, random, gravity-based deterministic breakdown, gravity-based random breakdown (from [Schmitt, 2014]), cost-benefits (from [Louf et al., 2013]), biological network generation (based on [Tero et al., 2010])



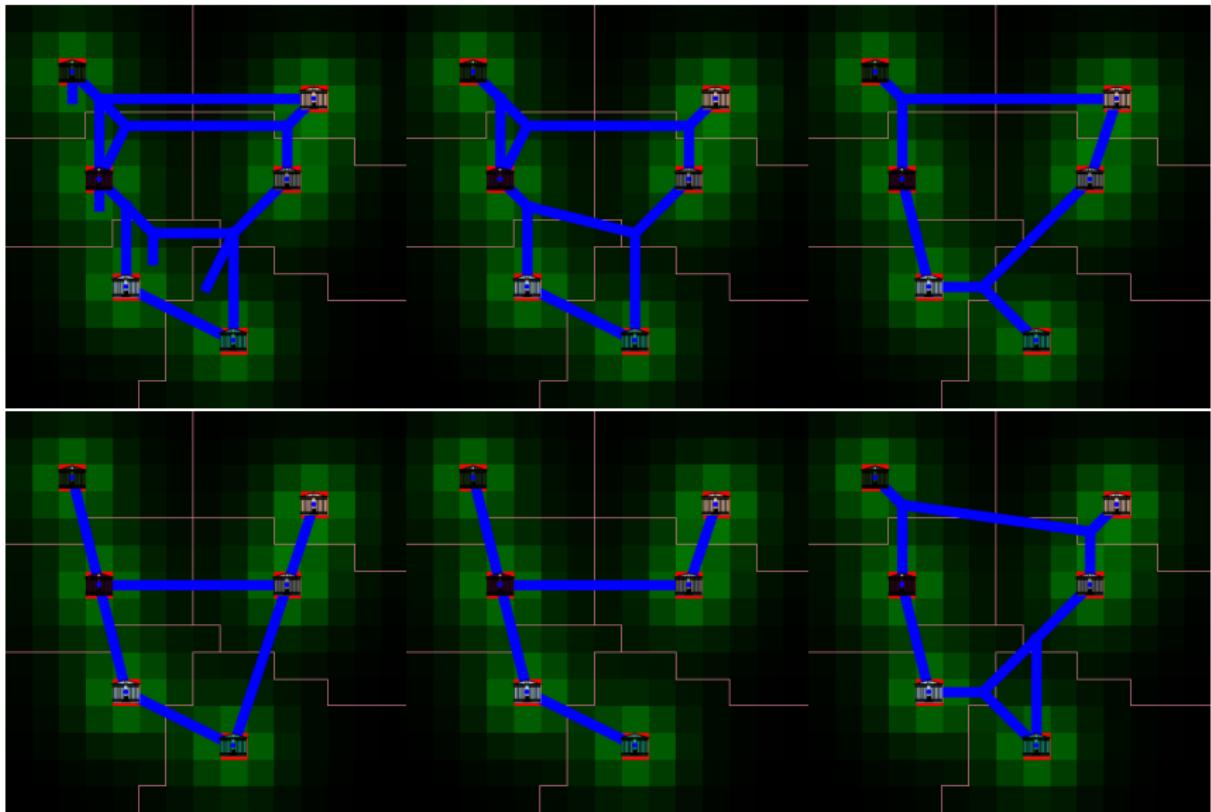
# Biological network generation

Model studied by [Tero et al., 2010] : exploration and reinforcement by a slime mould searching for resources



*Application to the design of optimal bus routes*

# Application: generating synthetic networks

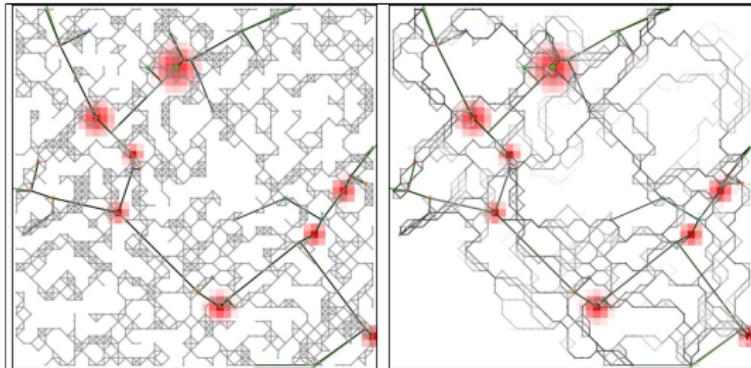


*Generation of Pareto optimal (cost/robustness) transportation networks:  
transportation scenarios for a land-use model*

# Biological Network generation

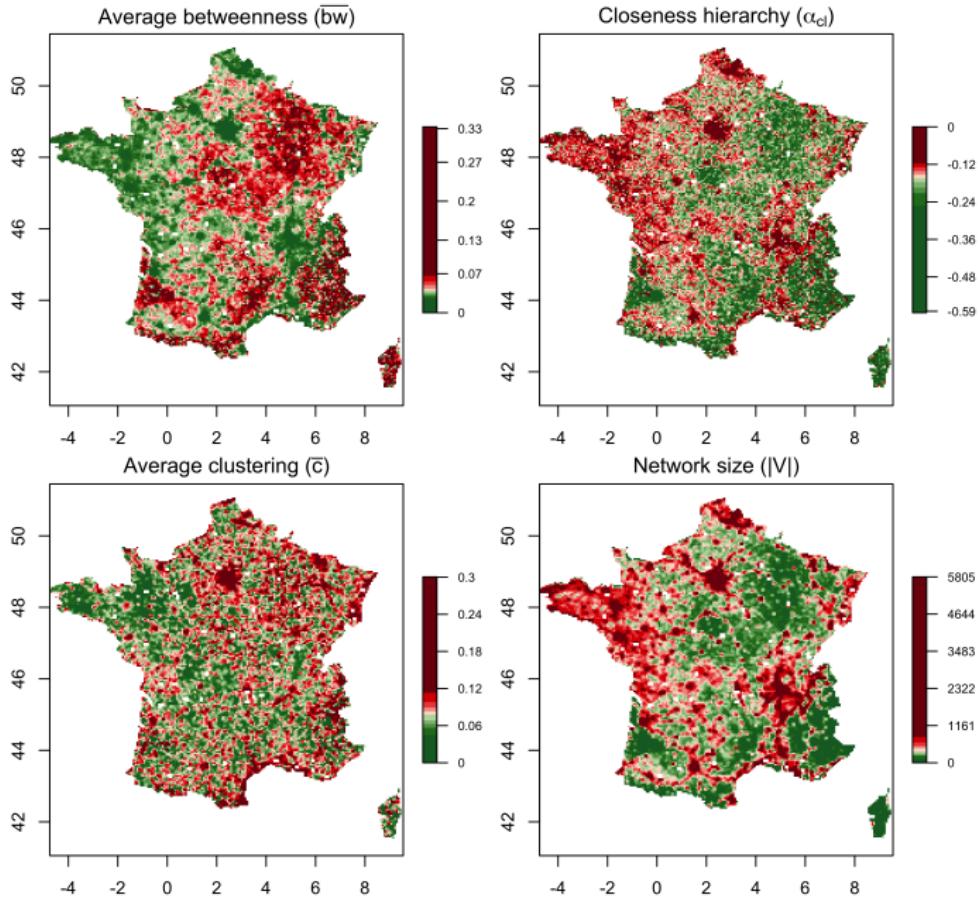
Adding new links with biological heuristic:

- ① Create network of potential new links, with existing network and randomly sampled diagonal lattice
- ② Iterate for  $k$  increasing ( $k \in \{1, 2, 4\}$  in practice) :
  - Using population distribution, iterate  $k \cdot n_b$  times the slime mould model to compute new link capacities
  - Delete links with capacity under  $\theta_d$
  - Keep the largest connected component
- ③ Planarize and simplify final network

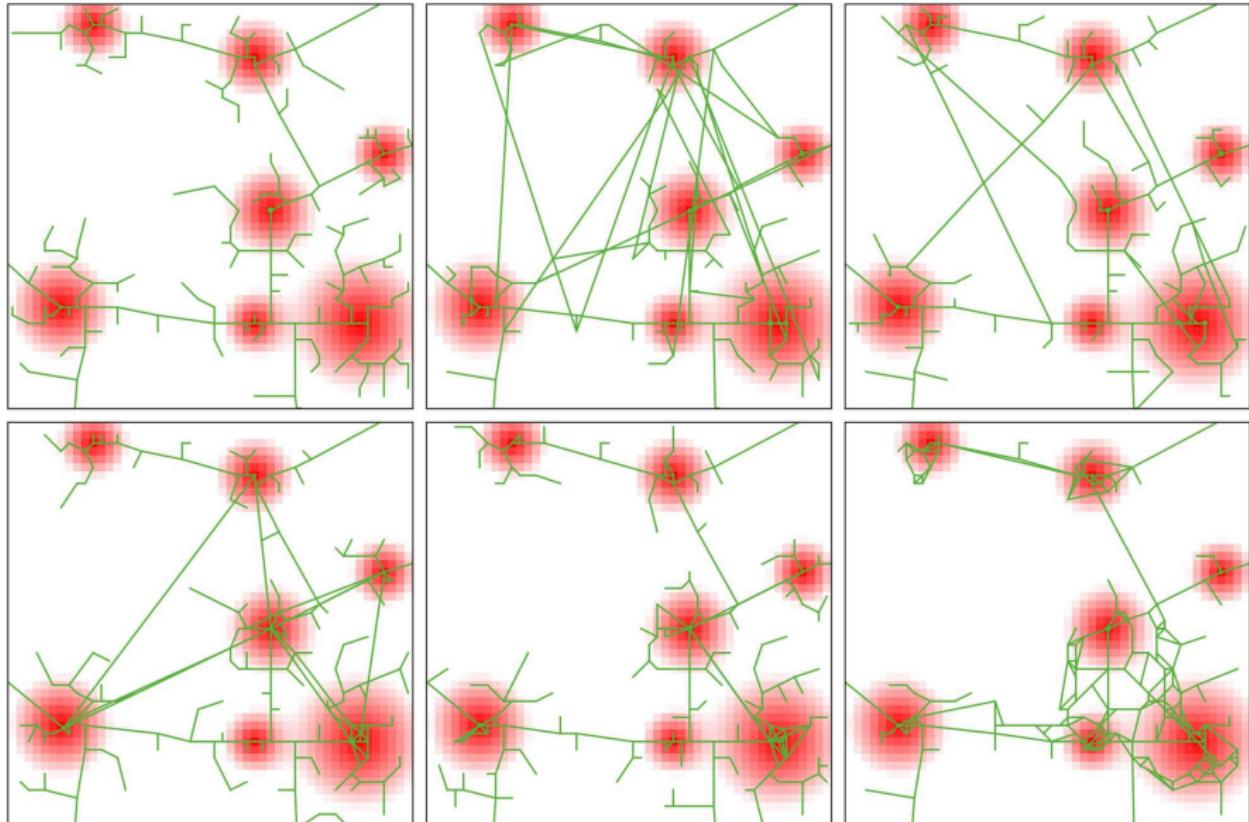


Intermediate stage for biological network generation

# Empirical Data : network indicators

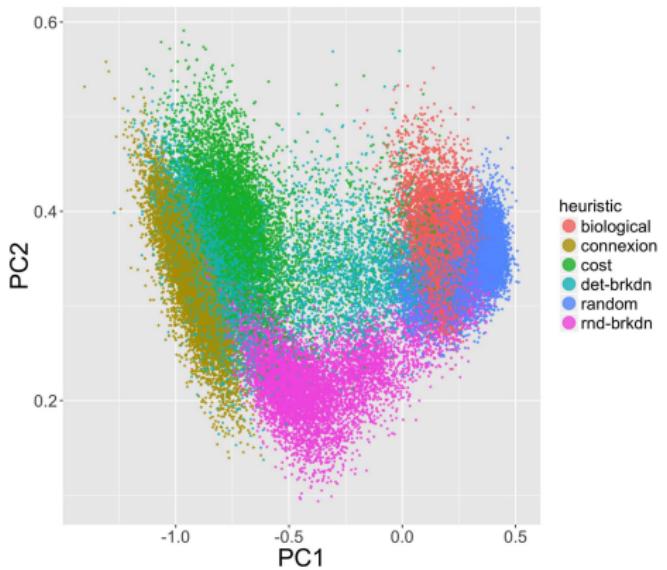


## Example of generated networks



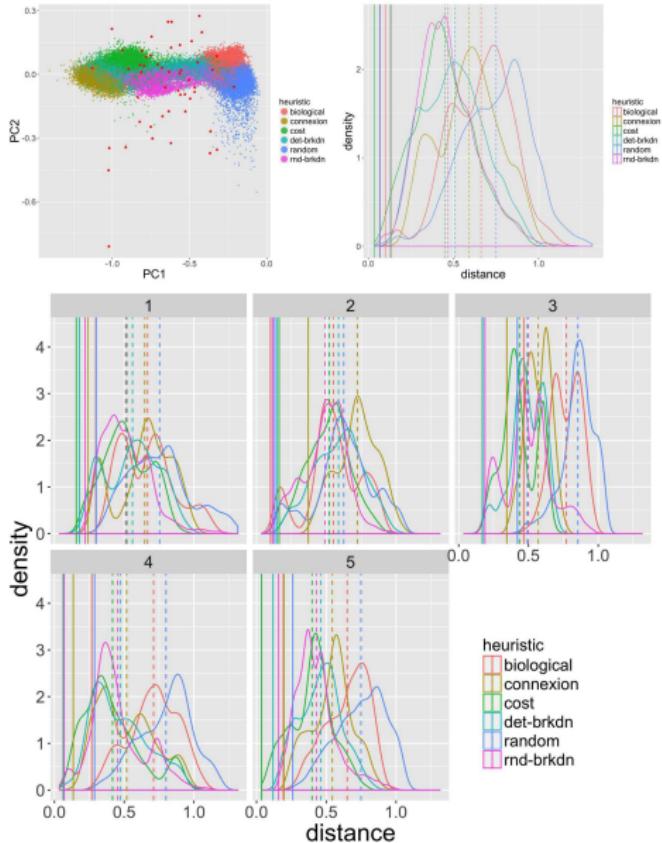
*In order: connection; random; deterministic breakdown; random breakdown;  
cost-driven; biological.*

# Feasible space of network indicators



Feasible spaces by network heuristic

# Distance to real networks



Distribution of distances to topologies of real networks

# Discussion

## Implications

- Complementary of various processes to cover the feasible space and produce existing topologies.
- 

## Developments

- Dynamical calibration requires (quasi-inexistent) data.
- Targeted calibrations to establish potential correspondances between processes and network topology.
- Compare network generation heuristics in a “fair” way (correcting for additional parameters, open question for models of simulation).

# Conclusion

- Several road network morphogenesis processes explored: **need for more coupling and comparison of models.**
- With more refined urban characteristics and other dimensions ? **Need for more interdisciplinarity.**

## Related works

Raimbault, J., Banos, A., & Doursat, R. (2014). A hybrid network/grid model of urban morphogenesis and optimization. Proceedings of 4th ICCSA 2014. arXiv:1612.08552.

Raimbault, J. (2017). Calibration of a Density-based Model of Urban Morphogenesis. arXiv preprint arXiv:1708.06743.

Raimbault, J. (2018). An Urban Morphogenesis Model Capturing Interactions between Networks and Territories. arXiv preprint arXiv:1805.05195.

**Open repository** (code, data and results) at

<https://github.com/JusteRaimbault/CityNetwork>

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# Reserve Slides

# Biological network morphogenesis model

Model studied by [Tero et al., 2010]: exploration and reinforcement by a slime mould searching for resources

Settings :

- Initial homogeneous network of tubes  $ij$  of length  $L_{ij}$ , variable diameter  $D_{ij}$ , carrying a flow  $Q_{ij}$ .
- Nodes  $i$  with a pressure  $p_i$ .
- $N$  nodes are origin/destination points : randomly at each step one becomes source  $p_{i+} = l_0$  and one other sink  $p_{i-} = -l_0$

# Biological network evolution

At each iteration :

- ① Determination of flows with Kirchoff's law (electrostatic analogy) :  
Ohm's law  $Q_{ij} = \frac{D_{ij}}{L_{ij}} \cdot (p_i - p_j)$  and conservation of flows  
 $\sum_{j \rightarrow i} Q_{ij} = 0, \sum_{j \rightarrow i_{\pm}} Q_{i_{\pm}j} = \pm I_0$
- ② Evolution of diameters ( $\gamma$  reinforcement parameter) by

$$\frac{dD_{ij}}{dt} = \frac{|Q_{ij}|^\gamma}{1 + |Q_{ij}|^\gamma} - D_{ij}$$

- Extraction of the final network after convergence given a threshold parameter for diameters
- Multi-scale model : diameters are constant during an iteration to obtain equilibrium flows

## Biological network: indicators

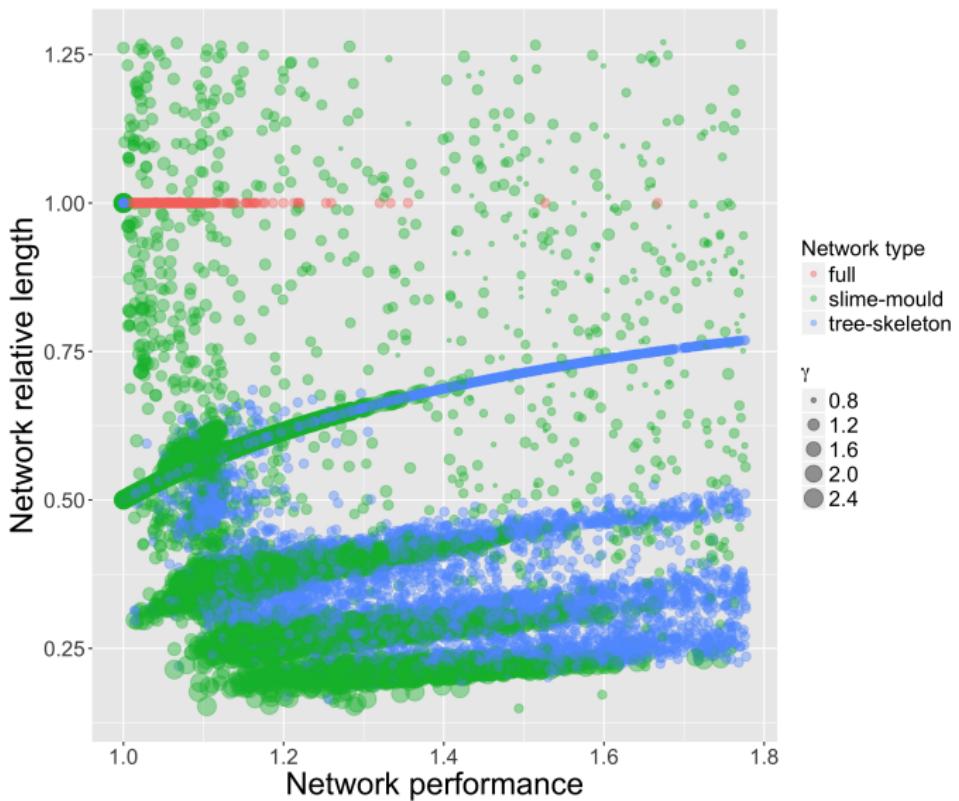
Behavior of the model evaluated with performance indicators for generated network  $(V_f, E_f)$ , that are contradictory objectives :

- Construction costs  $c = \sum_{ij \in E_f} D_{ij}(t_f)$
- Average performance [Banos and Genre-Grandpierre, 2012]

$$\nu = \frac{1}{|V_f|^2} \sum_{i,j \in V_f} \frac{d_{i \rightarrow j}}{||\vec{i} - \vec{j}||}$$

- Robustness (*Network Trip Robustness* index [Sullivan et al., 2010])

# Biological network: optimal networks



*Exploration of parameter space for synthetic network generation*

Network Topology measured by:

- Betweenness and Closeness centralities: average and hierarchy
- Accessibility (weighted closeness)
- Efficiency (network pace relative to euclidian distance)
- Mean path length, diameter

- ① Gravity potential given by

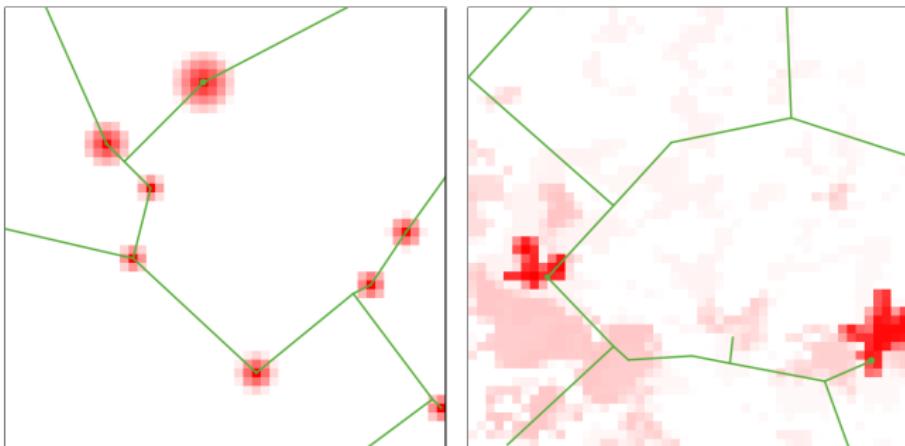
$$V_{ij}(d) = \left[ (1 - k_h) + k_h \cdot \left( \frac{P_i P_j}{P^2} \right)^{\gamma} \right] \cdot \exp \left( -\frac{d}{r_g(1 + d/d_0)} \right)$$

- ②  $k \cdot N_L$  links are selected with lowest  $V_{ij}(d_N)/V_{ij}(d_{ij})$ , among which  $N_L$  links with highest (lest costly) are realized
- ③ Network is planarized

# Model setup

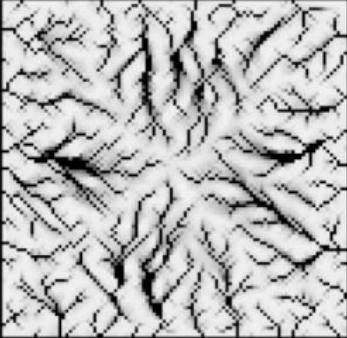
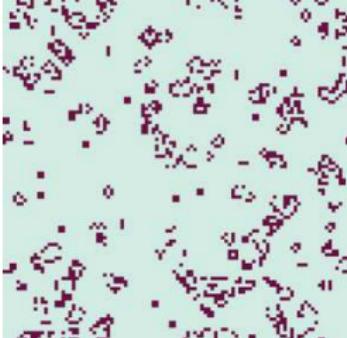
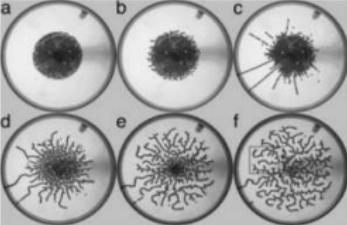
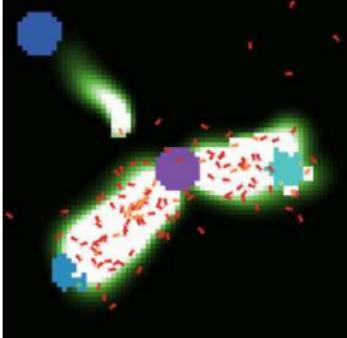
**Synthetic setup:** rank-sized monocentric cities, simple connection with bord nodes to avoid bord effects

**Real setup:** Population density raster at 500m resolution (European Union, from Eurostat)



**Stopping conditions:** fixed final time; fixed total population; fixed network size.

# What is Morphogenesis ? Examples

	Physical	Biological	Engineered
Non Functional			
Functional			

Sources (in order by column). Ants, Erosion, Game of Life: NetLogo Library ; Arbotron [Jun and Hübler, 2005]; Industrial design [Aage et al., 2017]; Swarm chemistry [Sayama, 2009]

# What is Morphogenesis ?

## Morphogenesis (*Oxford dictionary*)

- ① *Biology* : The origin and development of morphological characteristics
- ② *Geology* : The formation of landforms or other structures.

## History of the notion

- Started significantly with embryology around 1930 [Abercrombie, 1977]
- Turing's 1952 paper [Turing, 1952], linked to the development of Cybernetics
- first use in 1871, large peak in usage between 1907-1909, increase until 1990, decrease until today. *Scientific fashion* ?

# Interdisciplinary Definition of Morphogenesis

*Construction of an interdisciplinary definition in [Antelope et al., 2016]*

**Meta-epistemological framework of imbricated notions:**

Self-organization ⊂ Morphogenesis ⊂ Autopoiesis ⊂ Life

**Properties:**

- Architecture links form and function
- Emergence strength [Bedau, 2002] increases with notion depth, as bifurcations [Thom, 1972]

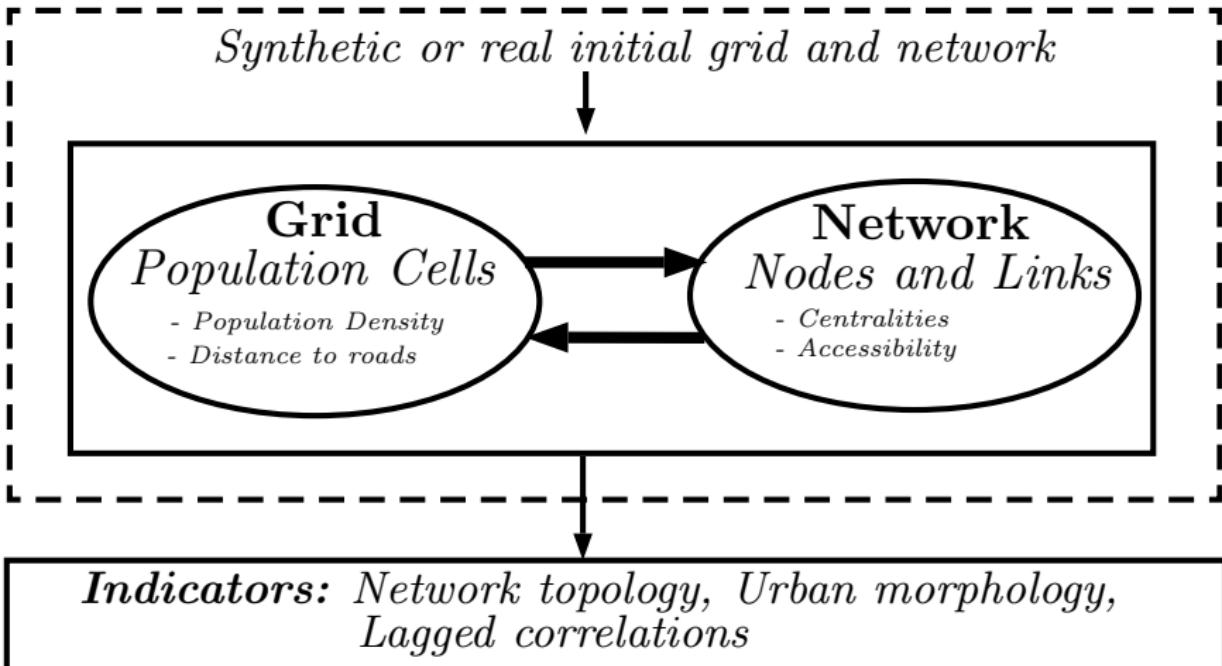
**Definition of Morphogenesis :** *Emergence of the form and the function in a strongly coupled manner, producing an emergent architecture [Doursat et al., 2012]*

# Modeling Urban Morphogenesis

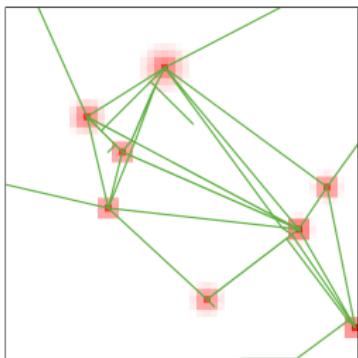
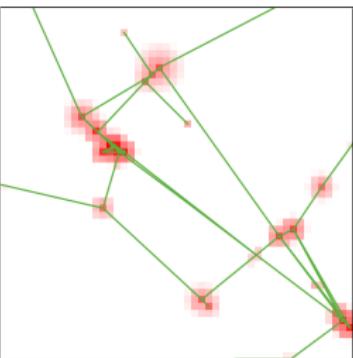
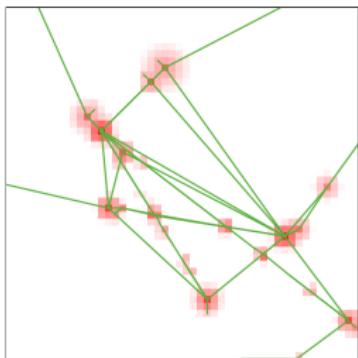
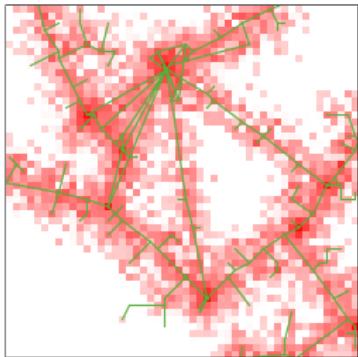
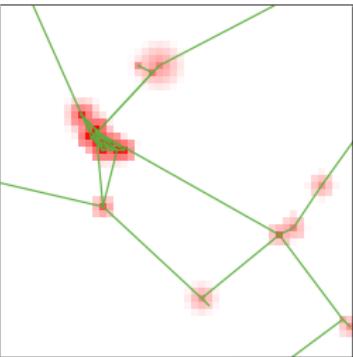
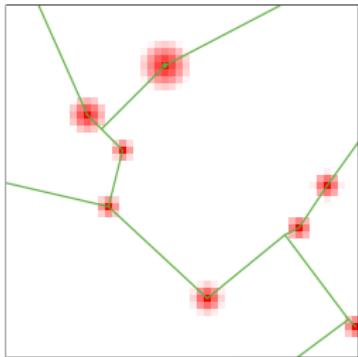
*More or less explicit use of the concept of Morphogenesis in Urban Simulation, depending on the scale and the approach.*

- [Makse et al., 1998] correlated growth
- [Murcio et al., 2015] multi-scale migration and percolation
- [Bonin et al., 2012] qualitative differentiation of urban function
- [Achibet et al., 2014] procedural model at the micro-scale
- [Caruso et al., 2011] micro-economic model of sprawl
- [Bonin and Hubert, 2014] urban economics morphogenesis, only work to explicitly mention the morphogen

## Extension into a co-evolution model



# Generated Urban Shapes: urban form



*In order: setup; accessibility driven; road distance driven; betweenness driven; closeness driven; population driven.*

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