

# A Theoretical and Quantitative Geography Insight into Interactions between Networks and Territories

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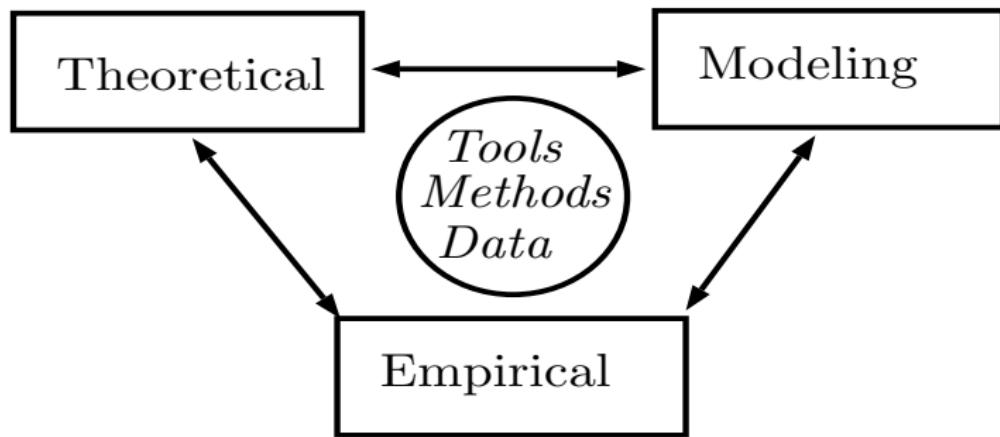
# Complex Urban Systems



Source : Wikipedia

# Theoretical and Quantitative Geography

An extended framework for TQG [Livet et al., 2010]



*To go further : speculative embedding of this scheme into a meta-modeling framework [Raimbault, 2016b]*

# Complex Urban Systems

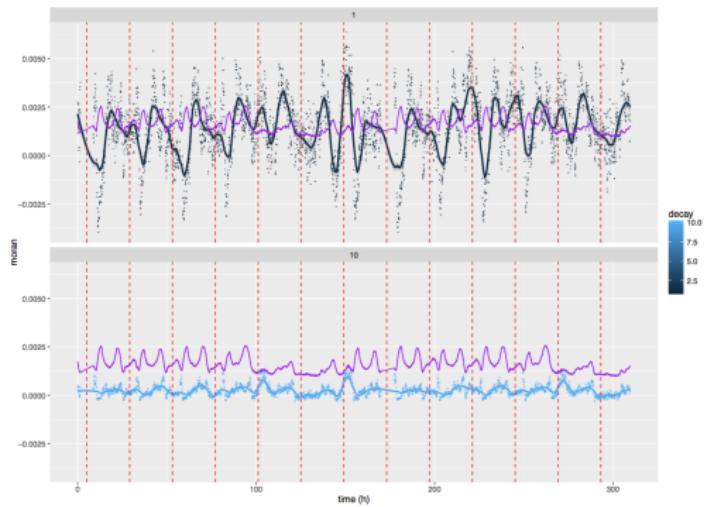
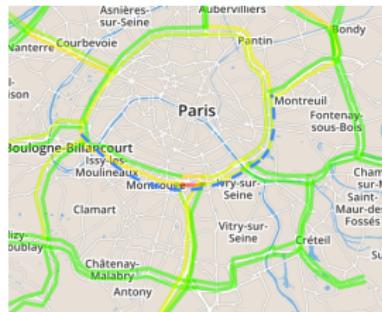
**Research Context :** *Investigate relations between Networks and Territories, in particular through the construction of models of co-evolution between land-use and transportation network, strangely absent in the literature [Raimbault, 2015b].*

- Collection of evidences from previous research ; proposition of a geographical theory
- Application to Transportation Governance Modeling ; potential insights from application to Pearl River Delta

# Non-equilibrium dynamics in Transportation Systems

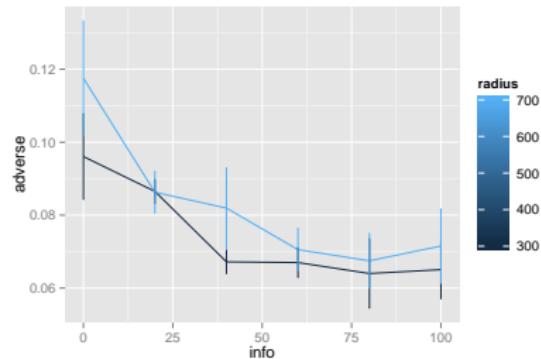
Investigation of empirical existence of Static User Equilibrium

[Raimbault, 2016] : data collection and empirical analysis for Parisian highway system



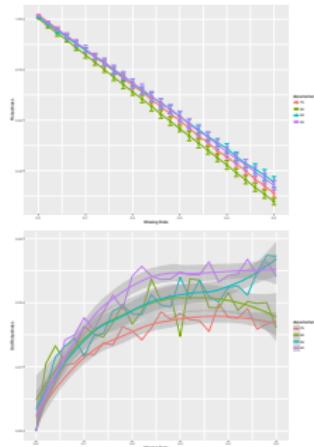
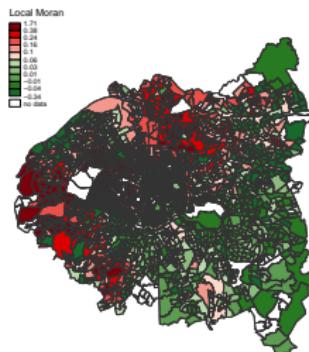
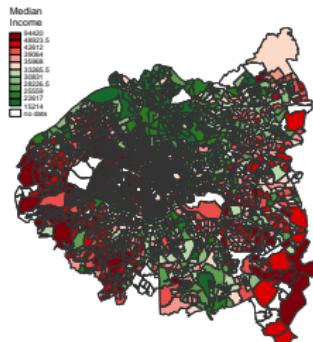
# Agent-based Modeling of Transportation Systems

Agent-based model to investigate user-based policies for a bike-sharing transportation system [Raimbault, 2015c] ; hybrid modeling with statistics and discrete-choice models [Raimbault, 2015a]



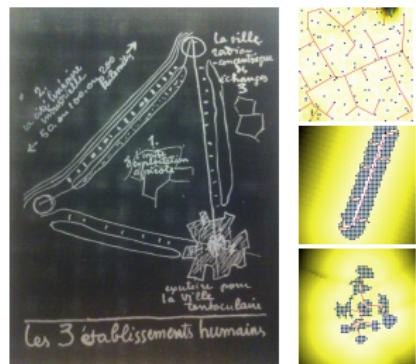
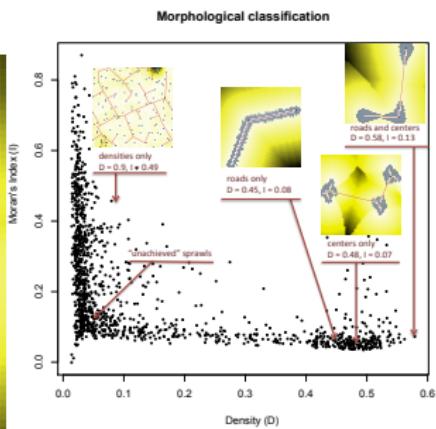
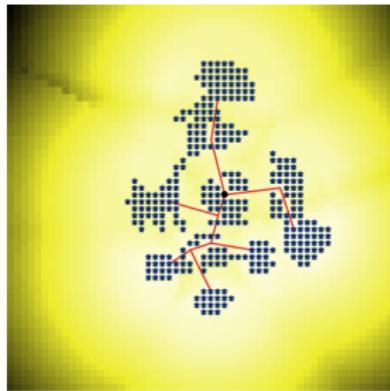
# Robustness of Multi-attribute Evaluations

Data-driven and Model-independant framework to compare robustnesses of multi-attributes evaluations [Raimbault, 2016a]



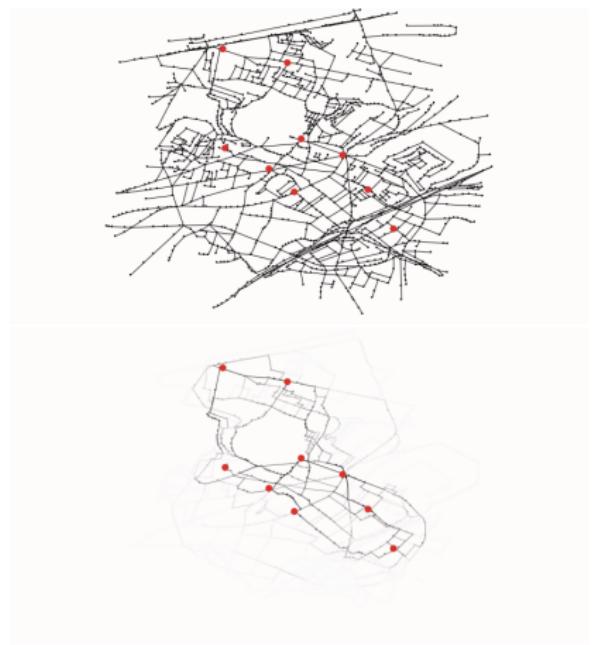
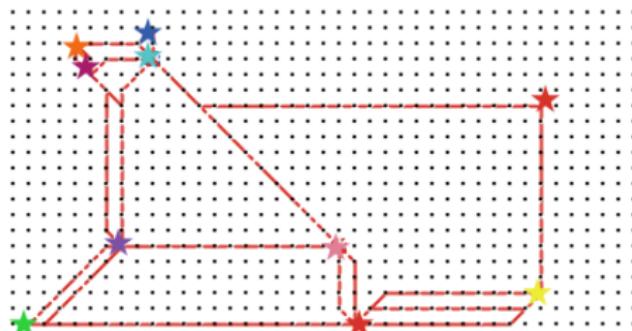
# Meso-scale Coupled Growth

Simple co-evolutionary dynamics produce stylized urban forms at a mesoscopic scale [Raimbault et al., 2014]



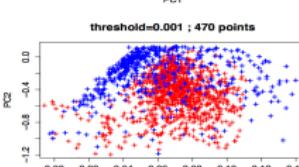
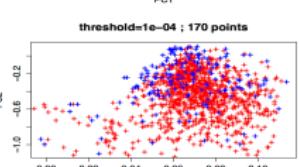
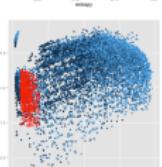
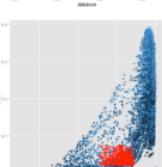
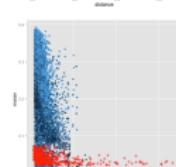
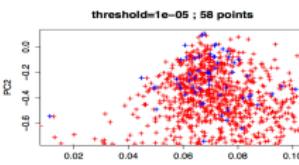
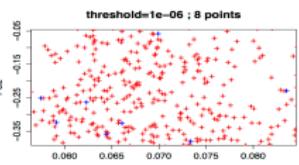
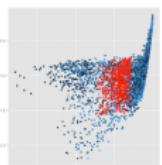
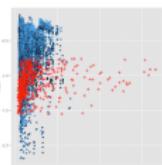
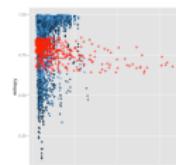
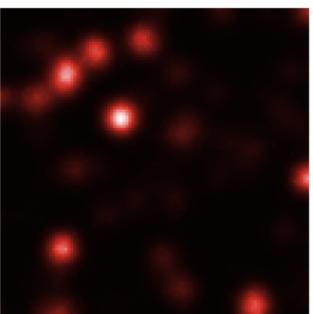
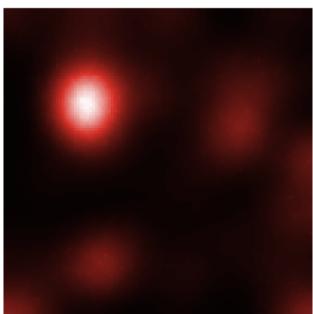
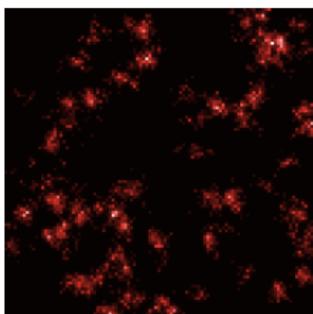
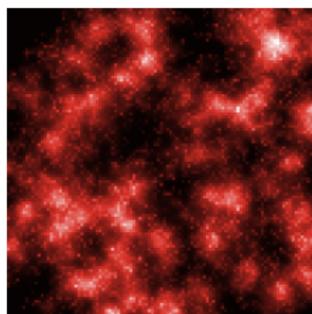
# Transportation Network Morphogenesis

Transportation network morphogenesis and optimal design using biologically inspired model (slime mold) [Raimbault and Gonzalez, 2015]



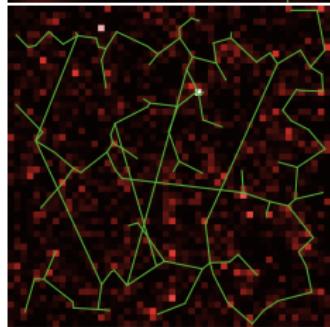
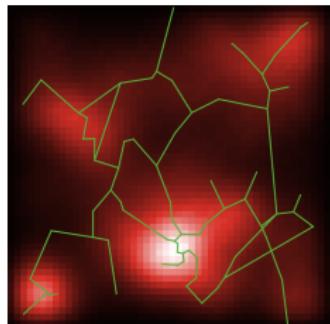
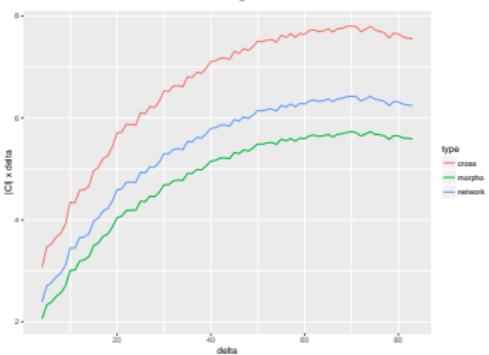
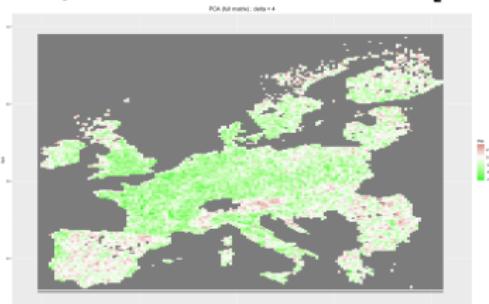
# Aggregation-diffusion Urban Growth

Evidence of autonomous Morphogenetic processes : morphological calibration of an Aggregation-diffusion growth model



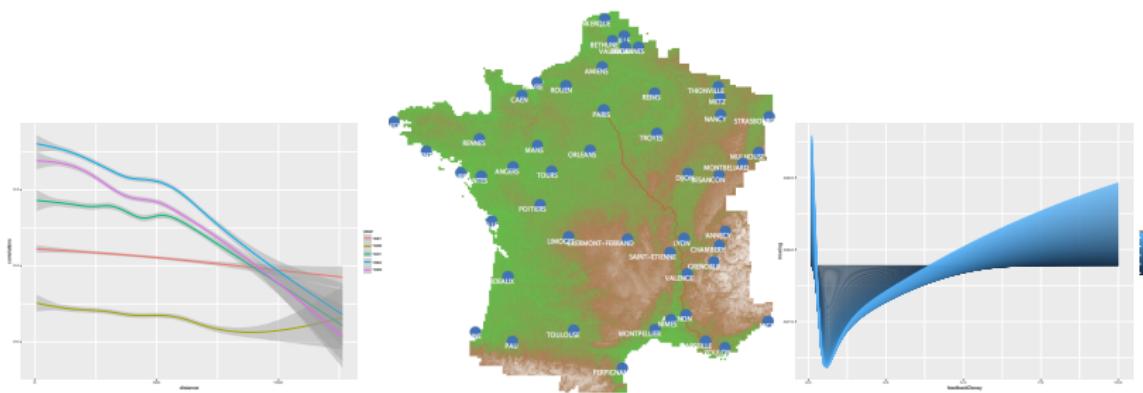
# Coupled Growth and Correlations

Spatial non-stationarity of correlation matrix between urban morphology and network topology [Raimbault, 2016b] ; coupled growth model yield a large range of potential correlations [Raimbault, 2016c]



# Macro-scale Growth and Network Necessity

Macro-scale population growth model reveals physical network effects in French System of Cities [Raimbault, 2016a]



## Theory : Pillars

- ① *Networked Human Territories* → Raffestin approach to territory combined with Dupuy theory of networks.
- ② *Evolutive Urban Theory* → City Systems as complex Adaptive systems, applied to human settlements in general and thus territorial systems.
- ③ *Urban Morphogenesis* → Morphogenesis as autonomous rules to explain growth of urban form. Used as the provider of modular decompositions.
- ④ *Boundaries and Co-evolution* → Co-evolution as the existence of *niche*, consequence of boundary patterns.

# Theory : Specification

**Definition :** Territorial systems are networked Human Territories. They are multi-level complex adaptive systems following Evolutive Urban Theory.

**Hypothesis :** The existence of Morphogenetic processes in which networks are essential drivers is equivalent to the existence of co-evolutive niches in territorial systems. We call thus these *Co-evolutive Networked Territorial Systems*.

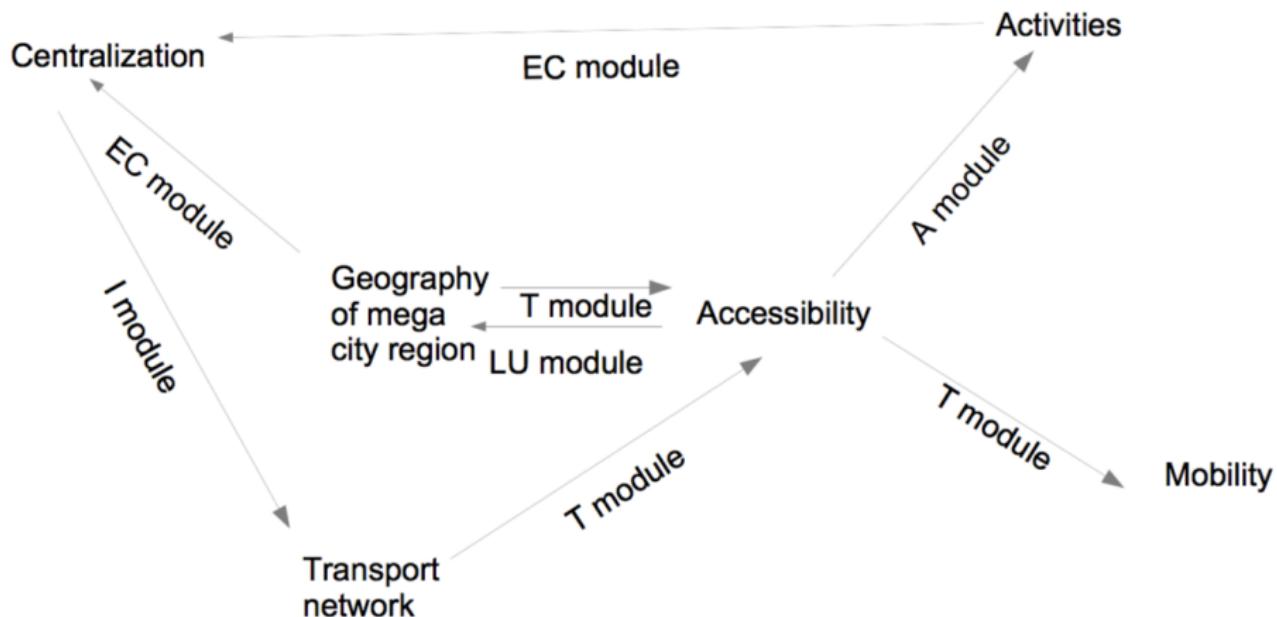
# The LUTECIA Model : Rationale

*Mega-city Regions [Hall and Pain, 2006] exhibit new qualitative regimes of urban systems ?*

- A LUTI + infrastructure provision model (LUTECIA)
- Coevolution transport / urbanism (LUTI model with endogeneous transport infrastructure provision)
- Game theory framework to predict emergence of centralized decision within a polycentric region
- Importance of accessibility at MCR scale

# The LUTECIA Model : Structure

LU : Land Use module ; T : Transport module ; EC : Evaluation of Centralized decision module ; I : Infrastructure provision module ; A : Agglomeration economies module



# Governance Modeling

Matrix of actors utilities, depending on respective choices

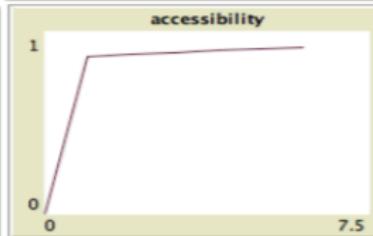
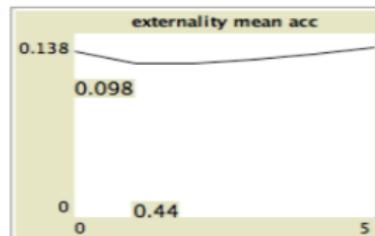
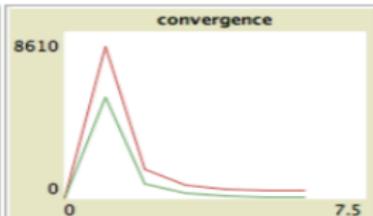
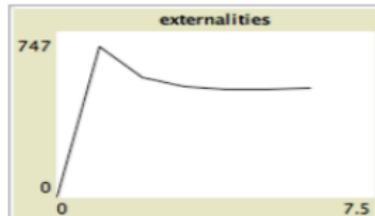
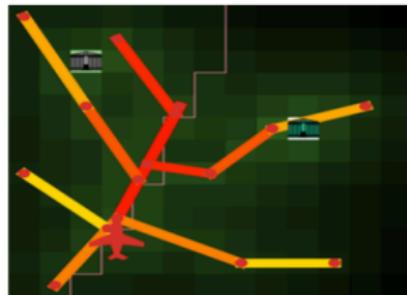
1   2	C	A
C	$U_i = \kappa \cdot \Delta X_i(Z_C^*) - I - \frac{\delta I}{2}$	$\begin{cases} U_1 = \kappa \cdot \Delta X_1(Z_1^*) - I \\ U_2 = \kappa \cdot \Delta X_2(Z_2^*) - I - \frac{\delta I}{2} \end{cases}$
A	$\begin{cases} U_1 = \kappa \cdot \Delta X_1(Z_1^*) - I - \frac{\delta I}{2} \\ U_2 = \kappa \cdot \Delta X_2(Z_2^*) - I \end{cases}$	$U_i = \kappa \cdot \Delta X_i(Z_i^*) - I$

Two types of games implemented :

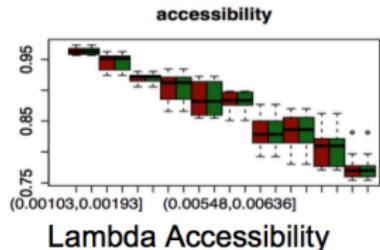
- Mixed Nash equilibrium, where actors compete
- One Rational Discrete Choice equilibrium

# Model Output : Examples

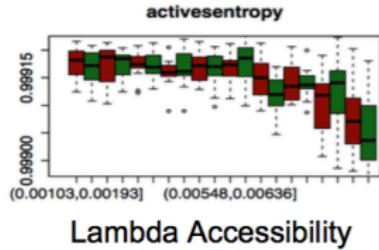
**Implementation :** NetLogo ; particular treatment for dynamical programming computation of network shortest distances. Exploration with High Performance Computing on grid with OpenMole [Reuillon et al., 2013]



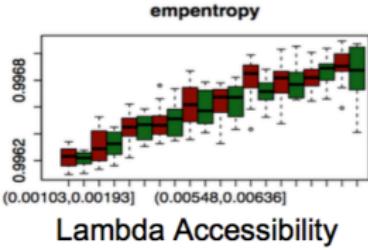
# Model Exploration : Examples



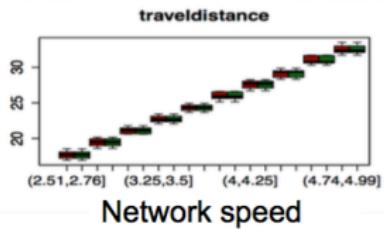
Lambda Accessibility



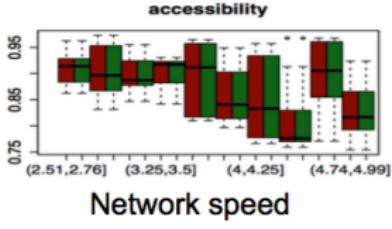
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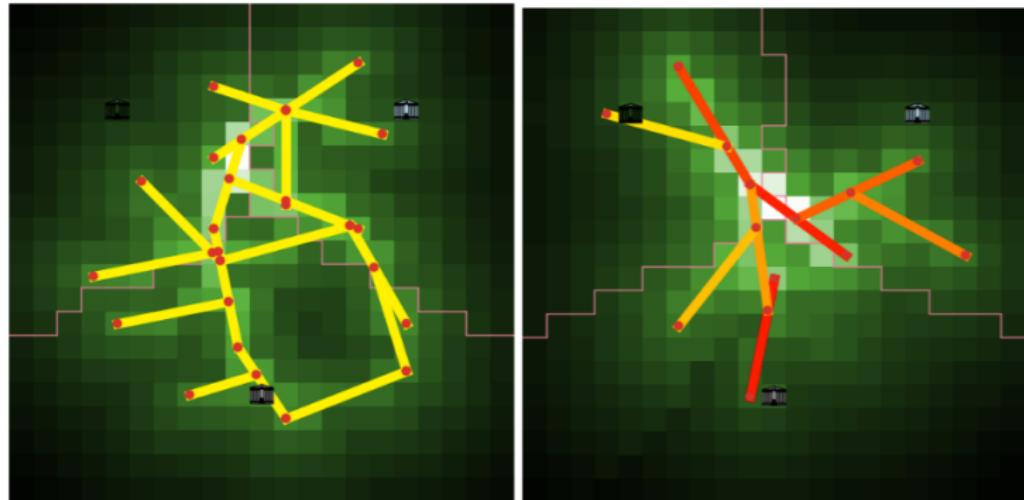


Network speed



Network speed

# Long Time Limits for Transportation Networks



# Application to Pearl River Delta Mega-city Region

Stylized characteristics of Pearl River Delta make a perfect candidate for model application



Source : Guangdong Province Government

# Application to Pearl River Delta

## Specific characteristics :

- Regional Governance new level of State action ; Mega-city region roughly at regional scale.
- Large development of infrastructures in a relatively short time
- Local and Regional Transportation masterplans at different dates
- Bridges across the delta : expensive infrastructure, require difficult collaboration
- High economic competition between cities ; particular role of Hong-Kong and Macao

# Application : Experience plan and Expected Results

## Requirements :

- Thematic model adaptation
- Technical model adjustments

## Experience plan :

- Conditions for emergence of the functional MCR
- Calibrate model retrospectively : unveil governance processes
- Calibrate model on planned infrastructure : collaboration patterns equivalent to a central planning
- Calibrate model on optimal infrastructure (multi-objectives to be determined) : what are corresponding "optimal" governance structures ?

# Conclusion

- From this particular model and the case study, theory should be confirmed/informed/refined/etc. (ex. : network plays indeed a crucial role in governance bifurcations, territorial systems should include explicit agents, etc. )
  - Knowledge production process is itself a metaphor of studied geographical processes : co-evolutive and complex.
  - Vertical and Horizontal integration : Interdisciplinarity beyond qualitative/quantitative artificial distinctions
- All code and data available at  
<https://github.com/JusteRaimbault/CityNetwork/tree/master/Models>

Reserve slides

# Reserve Slides

# Governance Game Specification

Mixed Nash equilibrium probability :

$$p_i = \frac{J}{\Delta X_{\bar{i}} Z_C^* - \Delta X_i Z_{\bar{i}}^*}$$

Discrete Choice model :

$$U_i(C) - U_i(NC) = p_{\bar{i}}(\Delta X_i Z_C^* - \Delta X_i Z_{\bar{i}}^*) - J$$

then

$$p_i = \frac{1}{1 + \exp \left( -\beta_{DC} \cdot \left( \frac{\Delta X_i Z_C^* - \Delta X_i Z_{\bar{i}}^*}{1 + \exp(-\beta_{DC}(p_{\bar{i}} \cdot (\Delta X_{\bar{i}} Z_C^* - \Delta X_i Z_{\bar{i}}^*) - J))} - J \right) \right)}$$

## Lutetia : default parameter values

$A_{max} = E_{max} = 500; r_A = 1; r_E = 0.8; \gamma_E = 0.9; \gamma_A = 0.65; \beta_I = 1.8; \lambda = 0.005; r_0 = 2$

$N_{expl} = 25; I = 0.001; J = 0.0001; v = 5; E_{ext}(t_0) = 3E_{max}; t_f = 4$

# Lutetia : Land-use Initialization

Initial distribution of Actives and Employments around governance centers at positions  $\vec{x}_i$  by

$$A(\vec{x}) = A_{max} \cdot \exp\left(-\frac{\|\vec{x} - \vec{x}_i\|}{r_A}\right); E(\vec{x}) = E_{max} \cdot \exp\left(-\frac{\|\vec{x} - \vec{x}_i\|}{r_E}\right)$$

## Lutetia : Transportation

Transportation module : computation of flows  $\phi_{ij}$  by solving on  $p_i, q_j$  by a fixed point method (Furness algorithm), the system of gravitational flows

$$\begin{cases} \phi_{ij} = p_i q_j A_i E_j \exp(-\lambda_{tr} d_{ij}) \\ \sum_k \phi_{kj} = E_j; \sum_k \phi_{ik} = A_i \\ p_i = \frac{1}{\sum_k q_k E_k \exp(-\lambda_{tr} d_{ik})}; q_j = \frac{1}{\sum_k p_k A_k \exp(-\lambda_{tr} d_{kj})} \end{cases}$$

Trajectories then attributed by effective shortest path, and corresponding congestion  $c$  obtained (no Wardrop equilibrium).

Speed of network given by BPR function  $v(c) = v_0 (1 - \frac{c}{\kappa})^{\gamma_c}$ . Congestion not used in current studies (infinite capacity  $\kappa$ ).

## Lutetia : Land-use Evolution

Land-Use module : we assume that residential/employments relocations are at equilibrium at the time scale of a tick, that corresponds to transportation infrastructure evolution time scale which is much larger (Bretagnolle, 2009).

We take a Cobb-douglas function for utilities of actives/employments at a given cell

$$U_i(A) = X_i(A)^{\gamma_A} \cdot F_i(A)^{1-\gamma_A}; F_i(A) = \frac{1}{A_i E_i}$$

$$U_j(E) = X_j(E)^{\gamma_E} \cdot F_j(E)^{1-\gamma_E}; F_j(E) = 1$$

where  $X_i(A) = A_i \cdot \sum_j E_j \exp(-\lambda \cdot d_{ij})$  and  $X_j(E) = E_j \cdot \sum_i A_i \exp(-\lambda \cdot d_{ij})$ . Relocations are then done deterministically following a discrete choice model :

$$A_i(t+1) = \sum_i A_i(t) \cdot \frac{\exp(\beta U_i(A))}{\sum_i \exp(\beta U_i(A))}$$

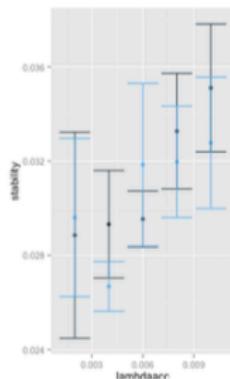
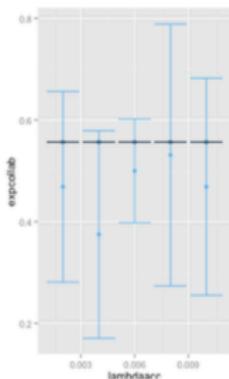
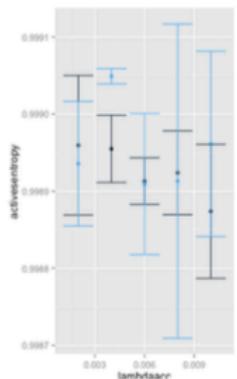
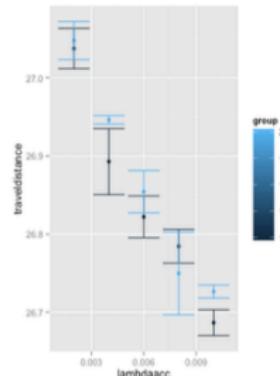
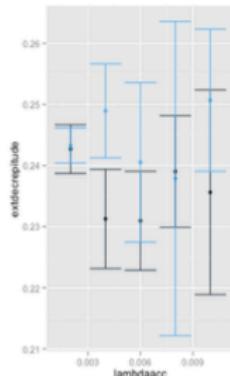
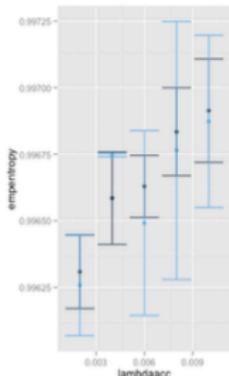
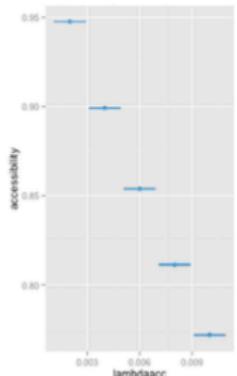
$$E_j(t+1) = \sum_j E_j(t) \cdot \frac{\exp(\beta U_j(E))}{\sum_j \exp(\beta U_j(E))}$$

# Lutetia : Network Distance Computation

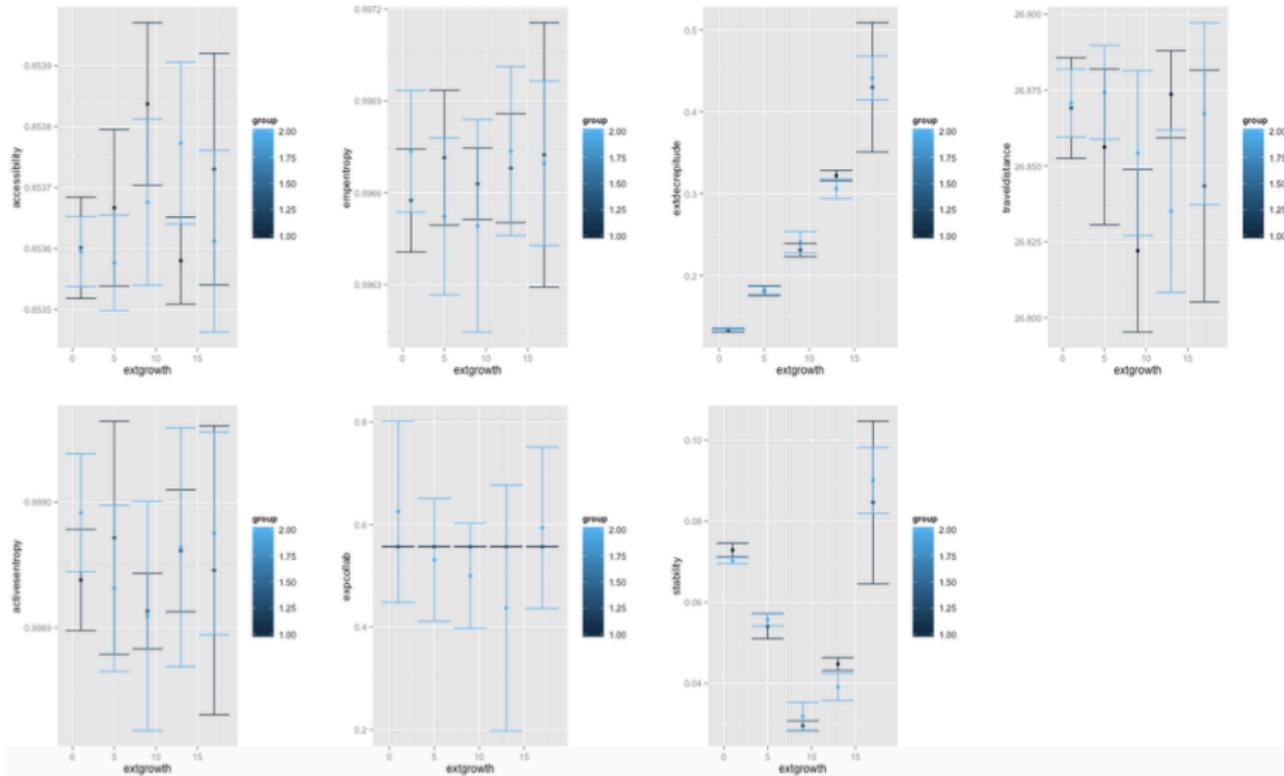
## Effective distances computation

- Euclidian distance matrix  $d(i,j)$  computed analytically
- Network shortest paths between network intersections (rasterized network) updated in a dynamic way (addition of new paths and update/change of old paths if needed when a link is added), correspondance between network patches and closest intersection also updated dynamically ;  $O(N_{inters}^3)$
- Weak component clusters and distance between clusters updated ;  $O(N_{nw}^2)$
- Network distances between network patches updated, through the heuristic of only minimal connexions between clusters ;  $O(N_{nw}^2)$
- Effective distances (taking paces/congestion into account) updated as minimum between euclidian time and  
 $\min_{C,C'} d(i, C) + d_{hw}(p_C(i), p'_C(j)) + d(C', j) ; O(N_{clusters}^2 \cdot N^2)$   
[Approximated with  $\min_C$  only in the implementation, consistent within the interaction ranges  $\sim 5$  patches taken in the model]

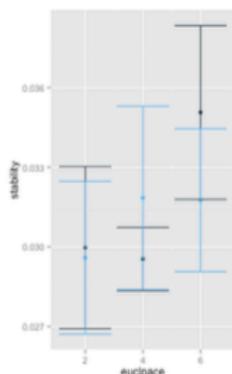
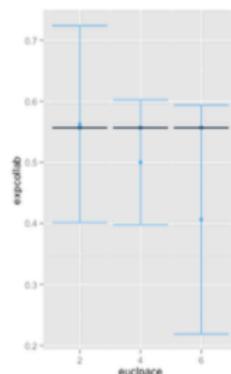
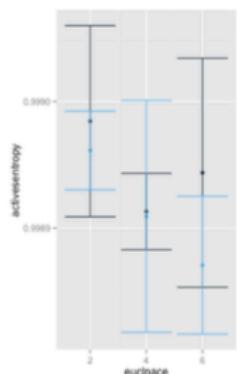
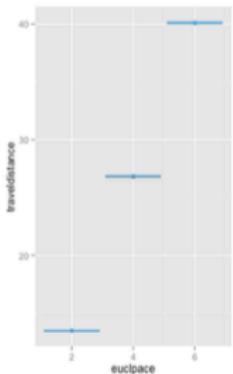
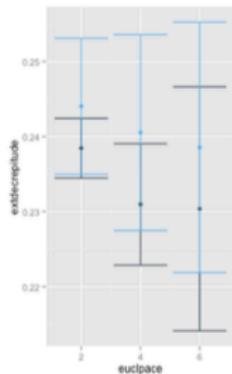
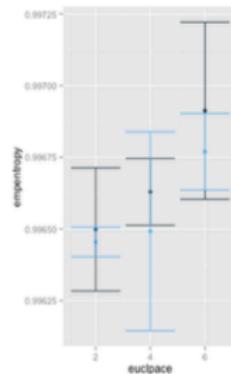
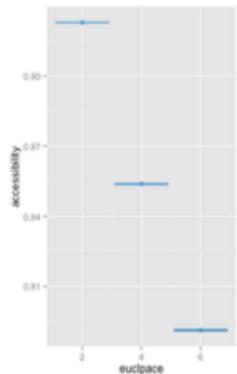
# Lutecia : Exploration



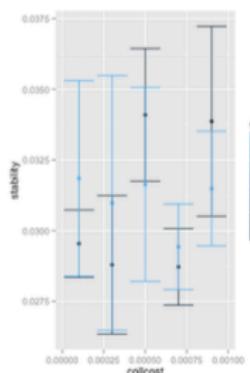
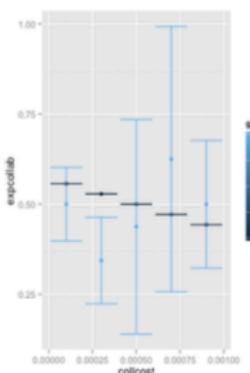
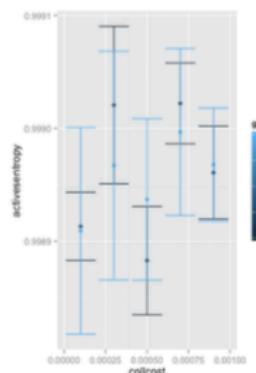
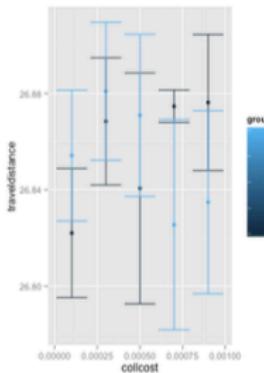
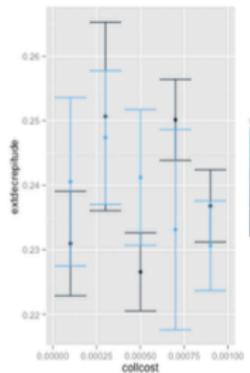
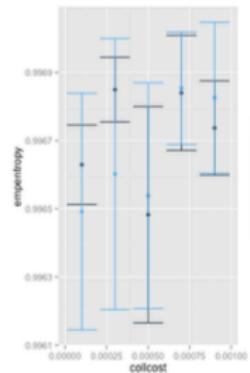
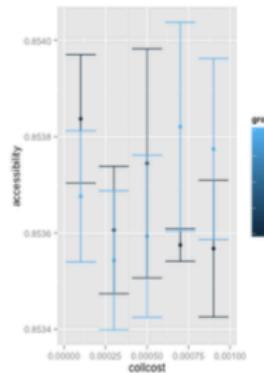
# Lutecia : Exploration



# Lutecia : Exploration



# Lutecia : Exploration



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