

# A co-evolution agent-based model for systems of cities and transportation networks integrating top-down governance through game theory

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**Abstract.**

## 1. Introduction

Interactions between networks and territories

*Accessibility as part of complex processes of co-evolution between transportation networks and territories.*

Raimbault, J. (2019). Evolving accessibility landscapes: mutations of transportation networks in China. In Aveline-Dubach, N., ed. *Pathways of sustainable urban development across China - the cases of Hangzhou, Datong and Zhuhai*, pp 89-108. Imago. ISBN:978-88-94384-71-0

Urban evolutionary theory

Development of an evolutionary urban theory

→ Recurrent stylized facts on main systems of cities

→ Construction of simulation models (with an explicative purpose)

→ Tools and methods to explore simulation models

Pumain, D. (2018). An evolutionary theory of urban systems. In *International and Transnational Perspectives on Urban Systems* (pp. 3-18). Springer, Singapore.

Reuillon, R., Leclaire, M., and Rey-Coyrehourcq, S. (2013). OpenMOLE, a workflow engine specifically tailored for the distributed exploration of simulation models. *Future Generation Computer Systems*, 29(8), 1981-1990.

Co-evolution of cities and transportation networks

*System of cities interaction model including network evolution; exhibits multiple co-evolution regimes; calibrated for France 1830-2000.*

Raimbault, J. (2020). Indirect evidence of network effects in a system of cities. *Environment and Planning B: Urban Analytics and City Science*, 47(1), 138-155.

Raimbault, J. (2020). Modeling the co-evolution of cities and networks. In Niel, Z., Rozenblat, C., eds. *Handbook of Cities and Networks*, Edward Elgar Publishing, *in press*.

International transport infrastructure projects

[4]

[5]

[6]

[7]

Multinational transport investments

*At the macroscopic scale: governance of multinational transport investments*

- Positive effects of transport investments: [8] meta-analysis, [9] One-Belt-One-Road economic impact
- Difficult implementation of multinational investments [10]; many trans-European projects fail in cost-benefit analysis [11]
- Example of framework for prioritization based on multi-attribute theory [12]

Co-evolution and governance processes

**Modeling co-evolution with governance processes**

- Model of governance choice [13]
- Spatialized simulation model [14]
- LUTI model with evolving network and game theory [15]

**Game theory and transportation models**

- Competition HSR/airplane [16]
- Public-private partnerships [17]
- Public transport integration [18]

Proposed approach

*Interaction of bottom-up and top-down planning processes in network and territories co-evolution*

*Stylized yet applicable simple models accounting for governance processes may be useful tools towards sustainable small scale territorial planning*

**Research objective**

Explore a co-evolution model for cities and transportation networks at the macroscopic scale, focusing on network evolution rules including governance choices.

## 2. Model

Model rationale

→ *Extend the model of [19] and [3] with two governance levels (national and international) and the game theoretic cooperation module introduced by [15]*

- Cities described by their population  $P_i(t)$ , linked with a physical transportation network with links described by effective distance  $d_l(t)$
- Iterative macro-scale LUTI simulation model: at each time step
  - (i) Update spatial interaction flows
  - (ii) Evolve cities populations depending on flows
  - (iii) Evolve network speeds depending on link flows assigned in the network

Cities populations

Spatial interaction flows

$$\varphi_{ij} = (P_i P_j)^\gamma \cdot \exp\left(-\frac{d_{ij}}{d_0}\right)$$

Assume growth rate of cities are proportional to cumulated interaction flows as

$$\frac{P_i(t+\Delta t) - P_i(t)}{\Delta t} \propto c_{ij} \cdot P_i(t)^\gamma \cdot \sum_j P_j(t)^\gamma \cdot \exp\left(-\frac{d_{ij}}{d_0}\right)$$

with  $c_{ij}$  a multiplier parameter equal to 1 if cities are in the same country and  $c_0 \leq 1$  otherwise

Network

- (i) Baseline model: self-reinforcement of link speed according to

$$d_l(t+\Delta t) = d_l(t) \cdot \left[ 1 + \Delta t \cdot g_M \left( \frac{1 - \left(\frac{\varphi_l}{\varphi_0}\right)^{\gamma_N}}{1 + \left(\frac{\varphi_l}{\varphi_0}\right)^{\gamma_N}} \right) \right]$$

for links with  $\varphi_l > \varphi_0$ , where  $\varphi_0$  corresponds to the  $\varphi_0^{(q)}$  quantile of link flows

- (ii) Estimate for each country  $k$  accessibility gains  $\Delta Z_k^{(N)}$  and  $\Delta Z_k^{(I)}$  obtained respectively with national ( $N$ ) and international ( $I$ ) flows, and corresponding construction costs  $C_k^{(N)}$ ,  $C_k^{(I)}$

Payoff matrix

Utility matrix for the two actor game is

$$U_0 = \Delta Z_0^{(N)} - \kappa \cdot C_0^{(N)} - \frac{J}{2}$$

$$U_1 = \Delta Z_1^{(N)} - \kappa \cdot C_1^{(N)} \quad U_i = \Delta Z_i^{(N)} - \kappa \cdot C_i^{(N)}$$

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Mixed Nash equilibrium probabilities

The general mixed Nash equilibrium probabilities are

$$p_{1-i} = -\frac{U_i(C, NC) - U_i(NC, NC)}{(U_i(C, C) - U_i(NC, C)) - (U_i(C, NC) - U_i(NC, NC))}$$

what gives with the payoff matrix

$$p_i = \frac{J}{(Z_{1-i}^{(I)} - Z_{1-i}^{(N)}) - \kappa \cdot (C_{1-i}^{(I)} - C_{1-i}^{(N)})}$$

Parameters  $\kappa, J$  are in practiced rescaled such that: (i) given a baseline model run, average cost absolute difference times  $\kappa$  is a fixed proportion  $k_0$  of average absolute accessibility difference; and (ii) collaboration cost  $J$  yields a fixed probability  $p_0$  computed on absolute average of the baseline run.

### 3. Results

#### Implementation and experiments

##### Implementation

- Model implemented in NetLogo (good compromise interactivity / ergonomics), with fast data structures (matrix/table extensions)
- Applied on synthetic systems of cities [20]
- Integrated seamlessly into OpenMOLE [2] for model exploration <https://openmole.org/>

##### Experiments

- Saltelli Global Sensitivity Analysis [21]
- Role of stochasticity
- Grid experiment with role of spatial configuration

#### Example of simulated systems

*Global sensitivity analysis* **Indicators:**  $\Delta P$  average population growth;  $\Delta Z$  average accessibility growth;  $\Delta \alpha_P$  population hierarchy change;  $r_P$  population rank correlation;  $g$  average governance level;  $C$  total cost

*effect of spatial configuration (seed and hierarchy) [22]; crossed effects between network, cities and governance*

*Role of stochasticity* On 100 parameters sampled (LHS) with 100 replications:

- All indicators have a high Sharpe ratio (1st quartile with a minimum of 7.7 expect governance level  $g$  with a median at 1.02)
- Distance between average relative to standard deviations are also high (1st quartile higher than 2.3, except for  $g$  with a median at 1.2 and  $r_P$  with a median of 1.26)

	$\alpha_0$		$\gamma_G$		$d_G$		$c_0$		$g_{max}$		$\gamma_N$	
	F	T	F	T	F	T	F	T	F	T	F	T
$\Delta P$	0.094	0.22	0.17	0.37	0.07	0.15	0.3	0.59	$7 \cdot 10^{-5}$	0.003	-0.002	$6.9 \cdot 10^{-5}$
$\Delta Z$	0.05	0.1	0.02	0.16	0.52	0.8	0.02	0.03	-0.006	0.18	-0.006	0.008
$\Delta \alpha_P$	0.2	0.3	0.3	0.5	0.06	0.12	0.17	0.26	-0.002	0.002	0.0001	0.0003
$r_P$	-0.7	0.1	-0.1	0.2	-0.4	0.3	0.26	0.002	-0.09	0.01	0.5	0.01
$g$	-0.01	0.26	-0.004	0.3	-0.01	0.44	0.03	0.6	-0.03	0.25	-0.02	0.2
$C$	-0.002	0.002	-0.007	0.01	-0.001	0.002	0.002	0.002	0.06	0.09	0.002	0.01

*Grid exploration* Rows: hierarchy; columns:  $\gamma_G$

*Larger span in spatial interaction decrease relative accessibility gain, as do less hierarchical flows; effect of interaction decay on governance level qualitatively changed by  $p_0$*

*Optimizing accessibility and cost* Intermediate values of governance levels on the optimal Pareto front when international exchanges are intense (right column)

## 4. Discussion

### Developments

Towards a macroscopic Land-use Transport model (including other network assignment procedures and congestion)

More elaborated representation of decision-making and governance processes

Integration into a multi-scale model [23]

### Applications

Evaluate transportation scenarios/projects in a multinational stakeholders context

Planning for sustainable territories on long time scales

## 5. Conclusion

A co-evolution model at the macroscopic scale complexified by including transportation governance

Well understood stylized models as a first step towards policy applications

### Open repositories

<https://github.com/JusteRaimbault/CoevolGov> for the model

<https://github.com/JusteRaimbault/Governance> for results

**Simulation data at <https://doi.org/10.7910/DVN/WP4V7S>**

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