

Exploration methods for Luti models

1 Introduction

- Luti model are a very diffuse class of models, dealing mainly with interactions between a land-use system and a transport system, at mesoscopic spatial scales (metropolitan areas) and medium time scales (decades) [Raimbault, 2018]. They are developed and used by various scientific fields, from urban economics, network economics to planning and transportation [Raimbault, 2017].
- Despite this sparsity, properties such as the spatial structure of population or the transportation network, or output indicators, can be put in correspondence between most Luti models.
- We aim here to illustrate generic methods that could be applied to the exploration of Luti models.

2 Model

We use a toy model to illustrate the application of exploration methods. The model Lutecia [Le Néchet and Raimbault, 2018] is an extended LUTI with an evolving network following endogenous rules for transportation governance. Blocking the network evolution yields a simplified LUTI (Lowry-type).

2.1 Model description

We describe the main features of the simplified LUTI. The metropolitan region is divided into cells, which are characterized by their number of actives A_i and number of employments E_i . The total number of actives and employments are fixed during the time period (no growth). At each time step, a proportion α of both relocate following a discrete choice model with parameter β , following a utility expressed as $X_i^{\gamma_A} \cdot \left(\frac{1}{A_i E_i}\right)^{1-\gamma_A}$ for actives and $X_i^{\gamma_E}$ for employments, where γ_A, γ_E are Cobb-Douglas parameters and X_i is the generalized accessibility, computed with an exponential decay of parameter λ and with the network distance within a network of uniform speed v_0 . The evolution is stopped at a fixed final time t_f . See [Raimbault, 2018] for a more thorough description of the full model.

The model is implemented in NetLogo (git repository) and explored with OpenMOLE.

2.2 Model evaluation

2.2.1 Parameters

The free Luti parameters are :

- α relocation rate
- λ cost of energy
- β discrete choice parameter
- γ_A Cobb-Douglas exponent actives

- γ_E Cobb-Douglas exponent employments
- v_0 network speed

2.2.2 Indicators

We use the following output indicators :

- Network indicators (fixed by the scenario and the replication), both contradictory objective for which the network generation heuristic finds a compromise :
 - network relative cost : length of the network relative to the length of the full euclidian network between all centers
 - network performance : [Banos and Genre-Grandpierre, 2012]
- Sustainability indicators (should be the objective of PSE / OSE / calibrations). Can be contradictory but not clear :
 - Evolution of the average accessibility between initial and final state
 - Average congestion, approximated by the average weighted betweenness centrality (using stationary commuting flows between actives and employments)
- Urban form indicators : four dimensions (morán, average distance, entropy, hierarchy) [Raimbault, 2017] for population and employments

2.2.3 Setup scenarios

To be relevant with classical application of LUTI models, we generate typical scenarios for the initial configuration of the model. The initial setup for actives and employments is done in a synthetic way to mimic a polycentric metropolitan area, i.e. with exponential mixtures spatial distributions with common centers, and a slightly higher concentration for employments. We play on the number of centers N_c .

Furthermore, a network must be generated, which will be interpreted as the application of the Luti to the design of a new infrastructure. We use the following options to generate a network:

1. Random tree-like network: each center connects with an other random center which has no links if there are some. This yield a costly and inefficient network.
2. Full network: all centers are directly connected. Extreme on the Pareto front: most efficient network, but costly.
3. Slime-mould biological network generator : applying the results of [Raimbault and Gonzalez, 2015], a network reinforcement model mimicking an organism self-organizes into Pareto-efficient networks (in the sense of cost/efficiency and cost/robustness). A single parameter γ allows to switch between redundant but costly networks to cheaper but less robust networks.

We do not add bord nodes and consider the transportation network within the metropolitan area only.

We currently implement 8 scenarios : (3/5 centers) x (tree/full/cheap slime-mould/robust slime-mould).

Table 1: ANOVA of the direct sampling experiment

Parameter	β	γ_A	γ_E	λ	α	v_0	scenario	residuals
% variance	0.11	0.68	0.46	45.71	2.22	23.12	7.27	20.43

2.2.4 Stylized facts

Question to answer through the study of sustainability indicators :

- compromise between congestion and accessibility across scenarios/parameters ? (attraction-repulsion urban narrative)
- Parameters/scenarios to maximize accessibility ?
- *less interesting regarding luti : classification of output urban forms ?*

Luti stylized facts to be targeted by the model : from [Wegener and Fürst, 2004], some qualitative empirical behavior can be studied in the model.

- “more accessible areas are developed faster”: $\rho[X_i, \Delta P_i] > 0$
- “employments locate in highly accessible areas”: $\rho[X_i, E_i] > 0$
- “good access \implies suburban dispersal \implies longer trips”: $\rho[X_i, t_i] > 0$ at the scale of a run, $\rho[\tilde{X}, \alpha_A] > 0$ on repetitions

3 Results

3.1 Sensitivity to indicators and convergence

3.1.1 Sensitivity experiment

First direct sampling to check the relative sensitivity to parameters, to see if we should fix spatial configurations

Basic experience plan (commit 8f848a) : LHS for parameters (400) x 6 scenarios x Random spatial configurations (100 repetitions)

Results: anova We fit indicators using linear models as a function of parameters and scenario number. An Analysis of Variance shows a comparable sensitivity to scenarios, parameters, and repetitions. Network indicators are as expected mostly sensitive to scenarios.

Since the most influent parameters for relative accessibility are the cost of energy λ and the network speed v_0 , and since these are relatively exogenous factors (compared to the governable parameters within the region e.g.), we fix them in following experiments to standard values of $\lambda = 0.005$ and $v_0 = 5$.

Results: repetitions To have a rough ideas of the number of repetitions needed to reach a given confidence interval on averages, we consider the relative accessibility \tilde{X} . Distributions can roughly be approximated as Gaussians (see Fig. 1), and we can use the formula giving the size of the confidence interval around the mean as $2\sigma z_{level}/\sqrt{n}$.

Looking at the distribution of $\frac{c_i + c_j}{|m_i - m_j|}$ for all (i, j) , where c_i and c_j are half-width of confidence intervals and m_i, m_j the average estimated values, we find that the 97.5% centile corresponds to a value of 0.96, what means that a large majority of estimated values can be differentiated at a 95% confidence level with this number of repetitions.

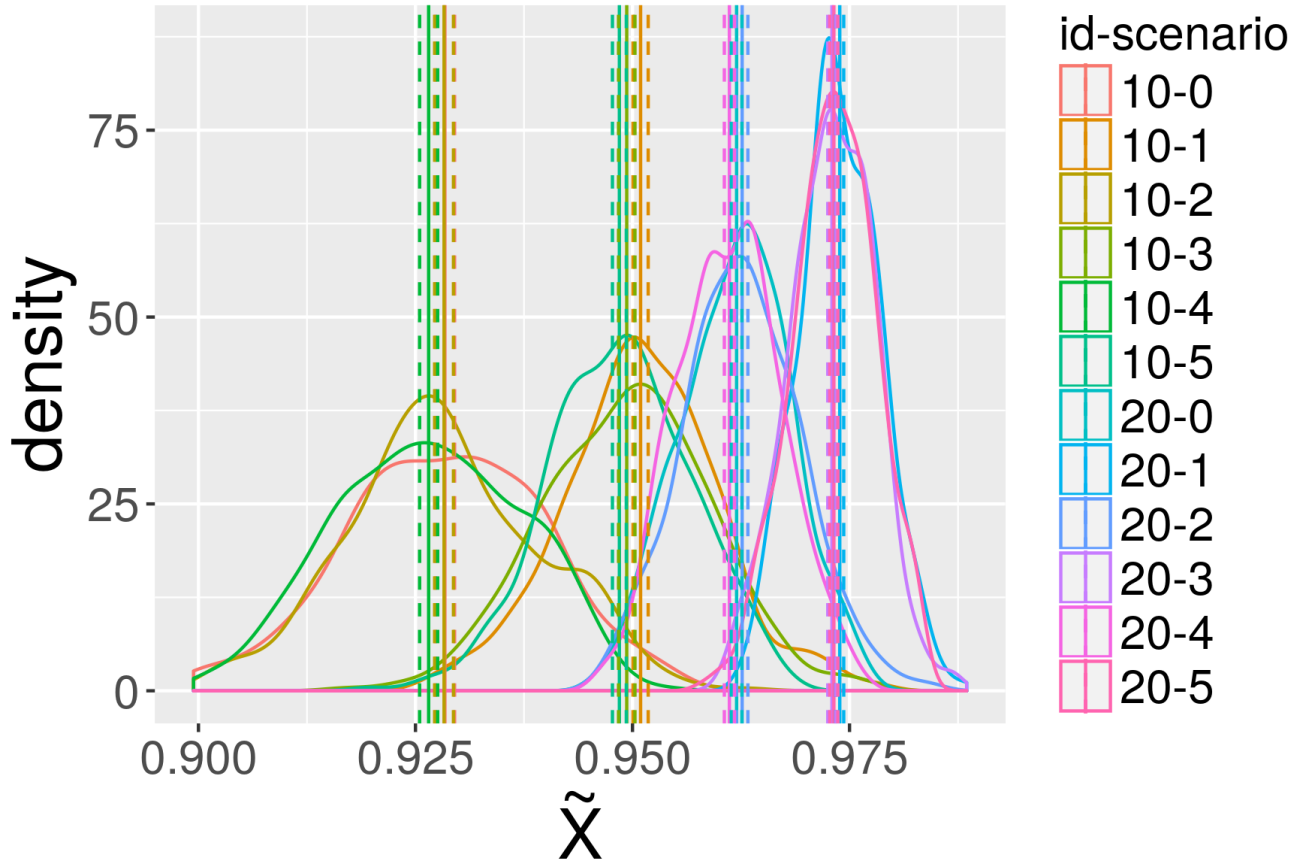


Figure 1: Distribution of relative accessibility \tilde{X} for two example parameter values and the 6 scenarios (parameter point 10 corresponds to $\beta = 1.71, \gamma_A = 0.787, \gamma_E = 0.798, \lambda = 0.00572, v_0 = 4.15, \alpha = 0.96$, parameter point 20 to $\beta = 0.74, \gamma_A = 0.92, \gamma_E = 0.70, \lambda = 0.0045, v_0 = 2.72, \alpha = 0.74$).

3.1.2 Refined experiment

Similar experience plan, with fixed λ and v_0 , additional scenarios (complete network), a weighted congestion indicator, and indicators for correlations (test for stylized facts). (commit 8f7725b) :

→ 200 replications x 500 parameter points (LHS) x 8 scenarios

For this experiment, we find that with the Anova that the average accessibility is mainly explained by the scenario (39.9%) and residuals (51.8%), the relocation rate α plays a significant role, and other parameters have a marginal role (β 0.25%, γ_A 0.22%, γ_E 0.75%).

With 200 replications, we obtain a third quartile of 1.07 for the relative confidence interval between all possible couples.

Behavior in comparison to reference *TODO : compare tree and full network scenarios to the slime mould*

3.2 PSE

PSE to launch separately on sustainability/urban form - decide if across scenarios or if scenario as discrete genome

3.3 OSE

experiment Romain

3.4 Space matters

Experiments testing various urban structure - similar to scenarios in the first sensitivity experiment but broader.

References

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