

# Multi-modeling urban systems dynamics to explore sustainability trade-offs

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**SDG 11:** “Make cities and human settlements inclusive, safe, resilient, and sustainable” [Nations, 2015]

→ Cities as a transition state? [Batty, 2018] Incubators of social change and innovation, both the source and solution to sustainability issues? [Pumain, 2010]

→ Environmental Kuznet Curve hypothesis [Dinda, 2004, Stern, 2004]: inverted U-shaped relationship between environmental impact and income per-capita; not validated empirically [Harbaugh et al., 2002]

→ Trade-offs between SDGs in urban systems [Viguié and Hallegatte, 2012]



Research Article

# Trade-offs between sustainable development goals in systems of cities

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- More dimensions and SDGs with trade-offs?
- Several models introduced with the evolutionary urban theory [Pumain, 2018] tackle complementary dimensions (see [Raimbault et al., 2020a] for a benchmark)

## Research objective:

*Couple several models for complementary dimensions of urban dynamics (innovation, economic exchanges, infrastructure) into a multi-model for the dynamics of urban systems at the macroscopic scale, to explore trade-offs between SDGs in synthetic systems of cities.*

## Exploration of trade-offs with two dimensions: urban evolution model [Raimbault and Pumain, 2022]

→ **Innovation diffusion** is a crucial process in artificial life evolutionary systems and open-ended evolution [Bedau et al., 2000]

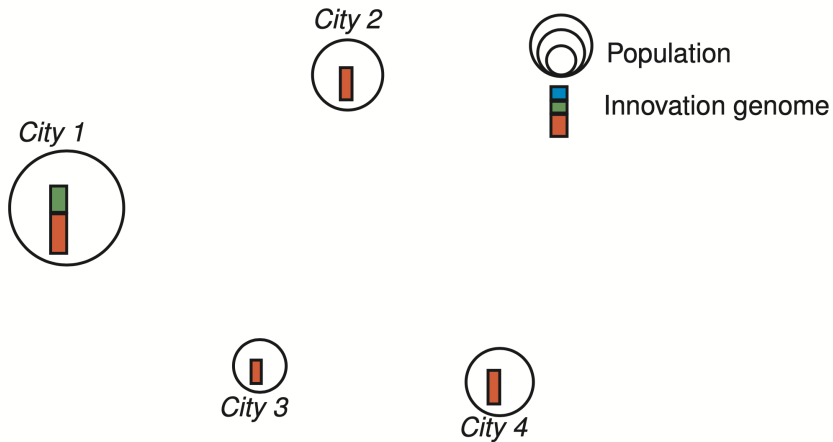
→ Artificial societies used to study the dynamics of innovation [Zenobia et al., 2009]

→ Innovations diffuse hierarchically in systems of cities [Hagerstrand, 1968], potential explanation of urban scaling laws [Pumain et al., 2006]

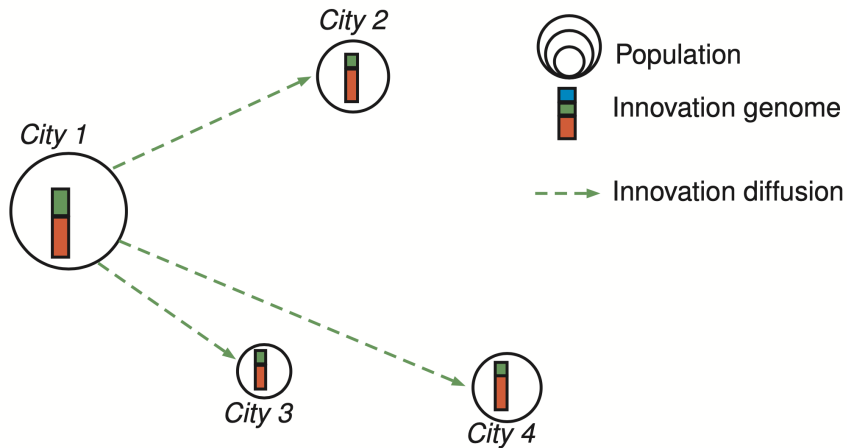
*Innovation diffusion as a privileged entry to understand urban evolution*

- Agents are cities, macroscopic scale (regional, country, continental) and long time scales (century)
- Cities characterised by their size in terms of population; genome as adoption proportions of innovations (social or technological) for each city (one single dimension to simplify)
- Following [Favaro and Pumain, 2011], attractiveness of cities due to level of innovation drive their population growth through spatial interactions; innovation diffuse through an other spatial interaction model [Fotheringham and O'Kelly, 1989]
- Mutations occur in cities as new innovations appear

# Model description

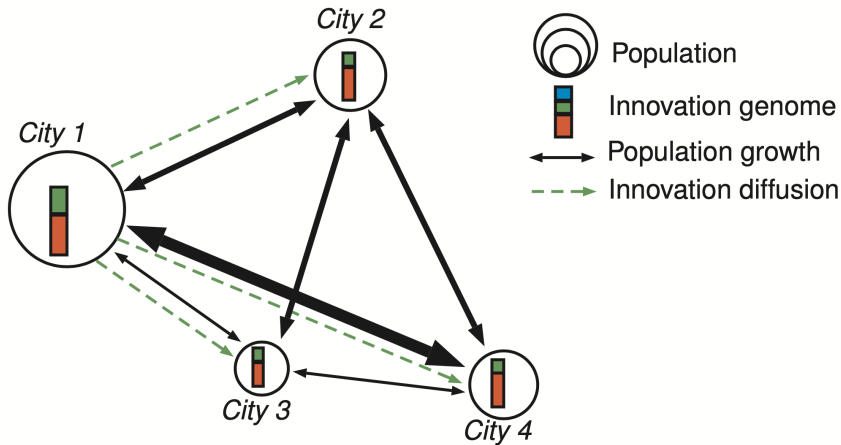


# Model description

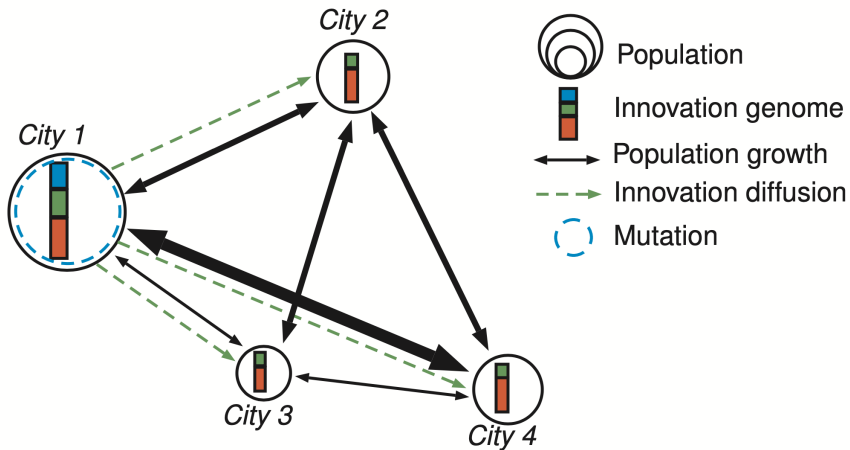




# Model description



# Model description



# Model formalisation

At each time step, with  $P_i(t)$  population,  $\delta_{c,i}(t)$  genome,  $u_c$  utility of innovation,  $p_{c,i,t}$  share of total population adopting innovation  $c$  in city  $i$

- 1 Crossover through the diffusion of innovations

$$\delta_{c,i,t} = \frac{\sum_j p_{c,j,t-1}^{\frac{1}{u_c}} \cdot \exp\left(-\frac{d_{ij}}{d_i}\right)}{\sum_c \sum_j p_{c,j,t-1}^{\frac{1}{u_c}} \cdot \exp\left(-\frac{d_{ij}}{d_i}\right)}$$

- 2 Population growth through spatial interactions

$$P_i(t) - P_i(t-1) = w_I \cdot \sum_j \frac{V_{ij}}{\langle V_{ij} \rangle} \text{ with}$$

$$V_{ij} = \frac{P_i(t-1) \cdot P_j(t-1)}{(\sum_k P_k(t-1))^2} \cdot \exp\left(-\frac{d_{ij}}{d_G} \cdot \prod_c \delta_{c,i,t}^{\phi_{c,t}}\right)$$

$$\text{and } \phi_{c,t} = \sum_i \delta_{i,c,t} \cdot P_i(t-1) / \sum_{i,c} \delta_{i,c,t} \cdot P_i(t-1)$$

- 3 Mutations with innovations introduced with probability

$\beta \cdot (P_i(t) / \max_k P_k(t))^{\alpha_I}$  and an initial penetration rate  $r_0$ ; new utility  $u_c$  randomly distributed (normal or log-normal) with average current average utility and standard deviation a given parameter  $\sigma_U$

# Synthetic configurations

Model applied on synthetic systems of cities (so that conclusions are independent of geographical contingencies [Raimbault et al., 2019]):

- random positions and rank-size hierarchy  $P_i(0) = \frac{P_{max}}{i^{\alpha_0}}$  with  $\alpha_0 = 1.0$  and  $P_{max} = 100,000$
- regional urban system scale:  $N = 30$  cities
- simulated for  $t_f = 50$  macroscopic time steps (order of magnitude of a century)

# Model parameters for the innovation model

Parameter	Not.	Process	Range	Def.
Number of cities	$N$	Spatial scale	[10; 100]	30
Initial hierarchy	$\alpha_0$	System of cities	[0.5; 2.0]	1
Initial population	$P_{max}$	System of cities	$[10^4; 10^7]$	$10^5$
Simulation steps	$t_f$	Temporal scale	[10; 100]	50
Growth rate	$w_I$	Pop. growth	[0.001; 0.01]	0.005
Gravity range	$d_G$	Crossover	[0; 2]	1
Innovation range	$d_I$	Crossover	[0; 2]	1
Innovation rate	$\beta$	Mutation	[0; 1]	0.5
Innovation hierarchy	$\alpha_I$	Mutation	[0; 2]	1
Innov. utility std.	$\sigma_U$	Mutation	[0.7; 2]	1
Penetration rate	$r_0$	Mutation	[0.1; 0.9]	0.5
Utility type	-	Mutation	$\{n; \ln\}$	$\ln$

# Implementation

Model implemented in scala; relatively large parameter space; integration into the `spatialdata` scala library for spatial sensitivity analysis [Raimbault et al., 2020b]

→ integration into the OpenMOLE model exploration open source software [Reuillon et al., 2013]



*Enables seamlessly (i) model embedding; (ii) access to HPC resources; (iii) exploration and optimization algorithms*

<https://openmole.org/>

→ Which trade-offs between innovation (SDG 9: innovation) and emissions (SDG 14: climate) in systems of cities?

Application of the urban evolution model, optimising with NSGA2 for conflicting objectives in synthetic systems of cities:

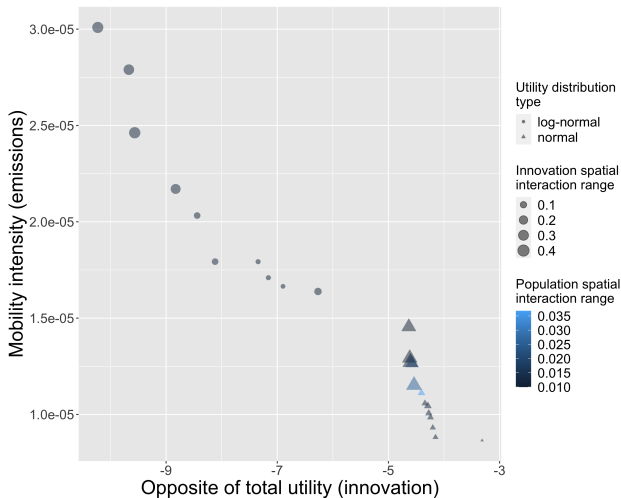
- 1 total utility of innovations

$$U = \sum_{t,i,c} \delta_{t,i,c} \cdot u_c$$

- 2 gravity mobility flows as proxy for emissions

$$E = \sum_{t,i,j} \frac{P_{t,i} P_{t,j}}{P_t^2} \cdot \exp(-d_{ij}/d_G)$$

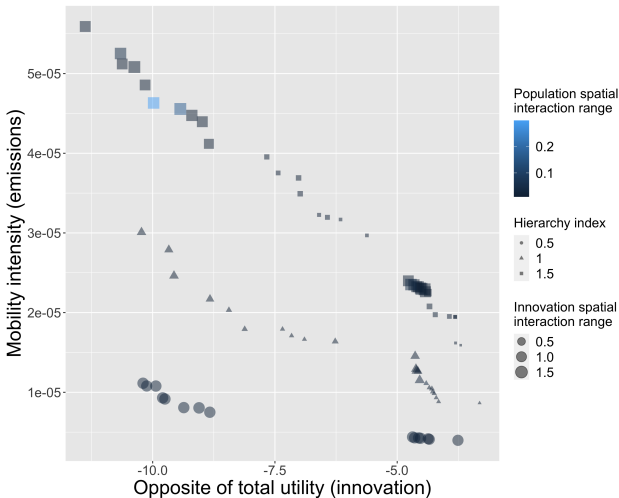
# Trade-offs between SDG9 and SDG14



*Pareto front confirms the existence of a trade-off*

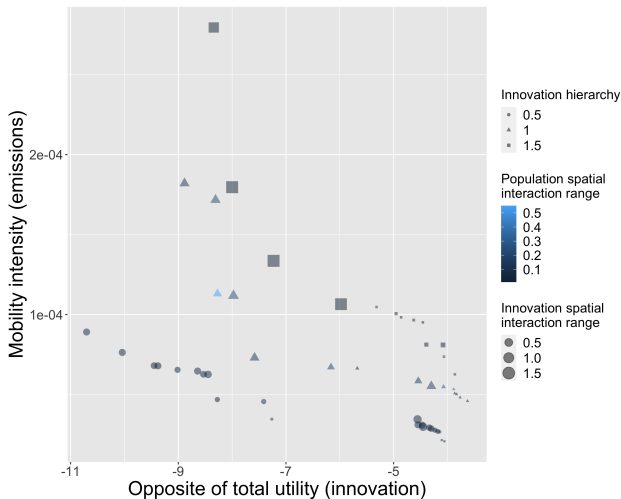


# Influence of urban hierarchy



*Higher inter-urban inequalities yield stronger trade-offs*

# Influence of innovation hierarchy



*More balanced innovation yield higher utilities and less emissions  
(dominating Pareto front)*

# Generic multi-model of urban dynamics

Other dimensions benchmarked by [Raimbault et al., 2020a] to fit population dynamics on several large urban systems

## Models integrated:

- Innovation diffusion urban evolution model [Raimbault and Pumain, 2022]
- Marius model for economic exchanges [Cottineau et al., 2015]
- Co-evolution model for cities and infrastructure networks [Raimbault, 2021]

## “Semi-weak” coupling of submodels:

$$\begin{aligned} S_0 \rightarrow \left[ S_1^{(0)} = M_0(S_0) \rightarrow \dots \rightarrow S_1^{(K-1)} = M_{K-1}(S_1^{(K-2)}) = S_1 \right] \longrightarrow \dots \\ \longrightarrow \left[ S_T^{(0)} = M_0(S_{T-1}) \rightarrow \dots \rightarrow S_T^{(K-1)} = M_{K-1}(S_T^{(K-2)}) = S_T \right] \quad (1) \end{aligned}$$

**Remarks:** strictly weak coupling does not capture dynamics nor synergies; stronger coupling may exist to better capture interdependencies processes (here no specific coupling ontology, only population and distance matrix are shared between submodels)

MARIUS family of models [Cottineau et al., 2015]:

Initial wealth as a power law of population (exponent  $\alpha_W$ )

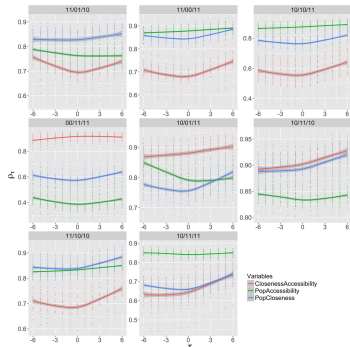
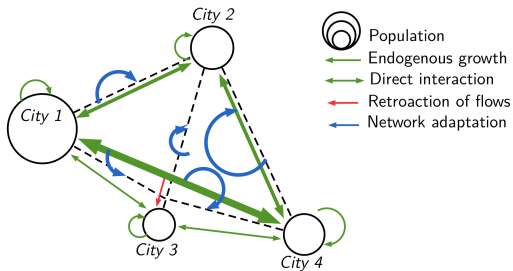
1) Update supply and demands as super-linear functions of population (exponents  $\alpha_S, \alpha_D$ )

2) Exchange goods according to a gravity potential of interaction (distance decay  $d_M$ ), supplies and demands; update wealth accordingly

3) Update population such that population difference is a power law of wealth difference (economic multiplier  $e_M$  and exponent  $\alpha_P$ )

# Infrastructure co-evolution model

## *System of cities interaction model including network evolution.*



Raimbault, J. (2020). Indirect evidence of network effects in a system of cities. *Environment and Planning B: Urban Analytics and City Science*, 47(1), 138-155.

Raimbault, J. (2021). Modeling the co-evolution of cities and networks. In *Handbook of Cities and Networks* (pp. 166-193). Edward Elgar Publishing.

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## Proxies for SDGs:

- Total utility of innovations (SDG 9 “Innovation”)
- Total spatial interaction flows across submodels (SDG 13 “Climate”)
- Average distance between cities (SDG 9 “Resilient infrastructure”)
- Economic inequalities (SDG 10 “Inequalities”)
- Total wealth of cities (SDG 8 “Economic Growth”)

**Optimisation parameters:** fixed synthetic urban system parameters but random configurations (10 repetitions); 8 parameters for innovation; 6 parameters for economic exchanges; 6 parameters for co-evolution

# Optimisation results



Scatterplots of the 5D Pareto front. Color level: Gini economic wealth.

## Parametrisation on case studies:

- Patent data as a proxy for innovation: geolocation of inventors not straightforward [Bergeaud and Verluise, 2021] [De Rassenfosse et al., 2019]; which technological (sub-)classes? Model with one dimension (extension with a matrix genome?); semantic content to better capture innovation diffusion? [Bergeaud et al., 2017]
- Emissions: inter-urban mobility emissions difficult to capture (need an additional transport model?)
- Historical infrastructure networks data?

## Work in progress

- Many-objective optimisation: NSGA3 algorithm
- Empirical stylised facts on possible trade-offs in systems of cities

## Future work

- Towards multi-scale models: quantifying goal 11 (sustainable cities and communities) implies in some cases intra-urban dynamics (mobility, segregation, e.g.)
- Transfer to policies and planning? Models with multiple functions? [Varenne, 2018] (towards companion modeling and stakeholder involvement)



- Towards an integrative urban and territorial science applied to sustainable planning at multiple scales
- Transfer to decision-making, policies and governance? *e-team* of the CSDC campus

**To use OpenMOLE (free and open software) and contribute:**  
<https://openmole.org>

**Model code and results open source at**  
<https://github.com/JusteRaimbault/SDGTradeoffs> and  
<https://github.com/openmole/spatialdata>



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