

STNUM - TP1

LOGICIEL R ET RAPPEL DES PROBABILITÉS

MAÏLIS BOUDIER
JUSTE RAIMBAULT

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Question 1

The command `rnorm` generates random numbers following a centered gaussian law, for which the density is, if σ is the standard deviation, $f(x) = \frac{1}{\sqrt{2\pi\sigma^2}} \cdot e^{-\frac{1}{2} \cdot \frac{x^2}{\sigma^2}}$. The maximal value taken is then $\frac{1}{\sigma\sqrt{2\pi}}$, and therefore we fix the upper bound for y just a little above this value (1.2 times, taking the maximum with the frequencies of the histogram, since the bars can go above the theoretical curve), after having calculated σ by $\sigma = \text{sd}(\mathbf{x})$.

Question 2

See code for loading of data of geyser eruptions.

Command `summary(geyser)` gives basic informations about waiting times between eruptions and duration of each eruption. Result are presented in figure 1. Figure 2 presents the empirical distributions and figure 3 histogram for both series.

waiting		duration	
Min.	: 43.00	Min.	:0.8333
1st Qu.	: 59.00	1st Qu.	:2.0000
Median	: 76.00	Median	:4.0000
Mean	: 72.31	Mean	:3.4608
3rd Qu.	: 83.00	3rd Qu.	:4.3833
Max.	:108.00	Max.	:5.4500

Figure 1: Basic statistical data for both series

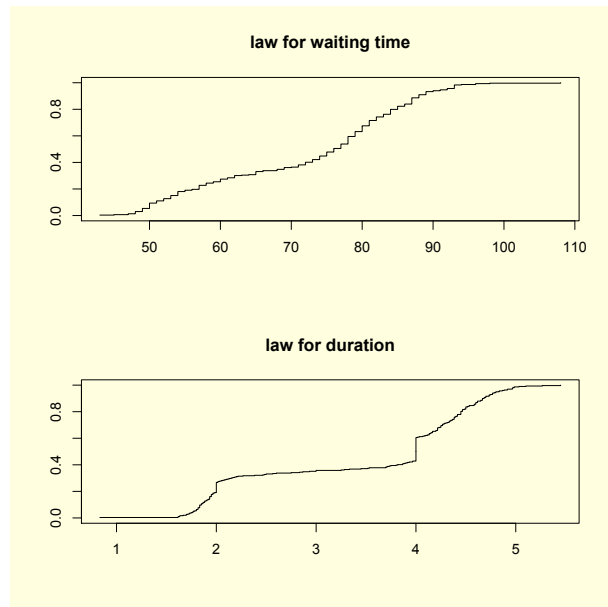


Figure 2: Empirical distributions

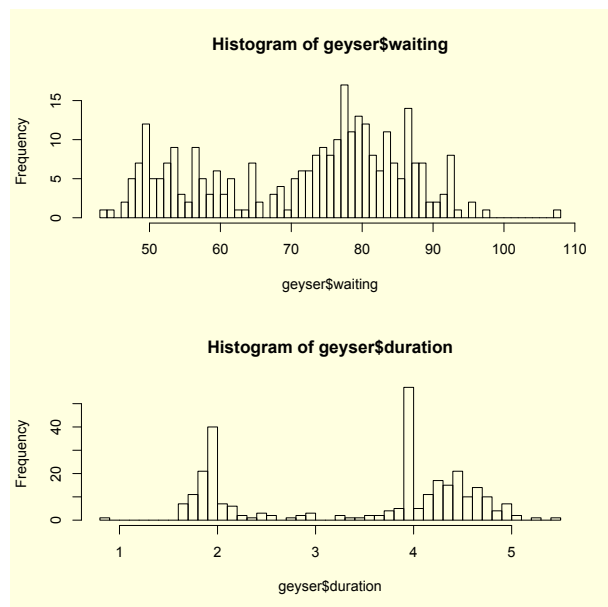


Figure 3: Histograms for geyser waiting time and duration

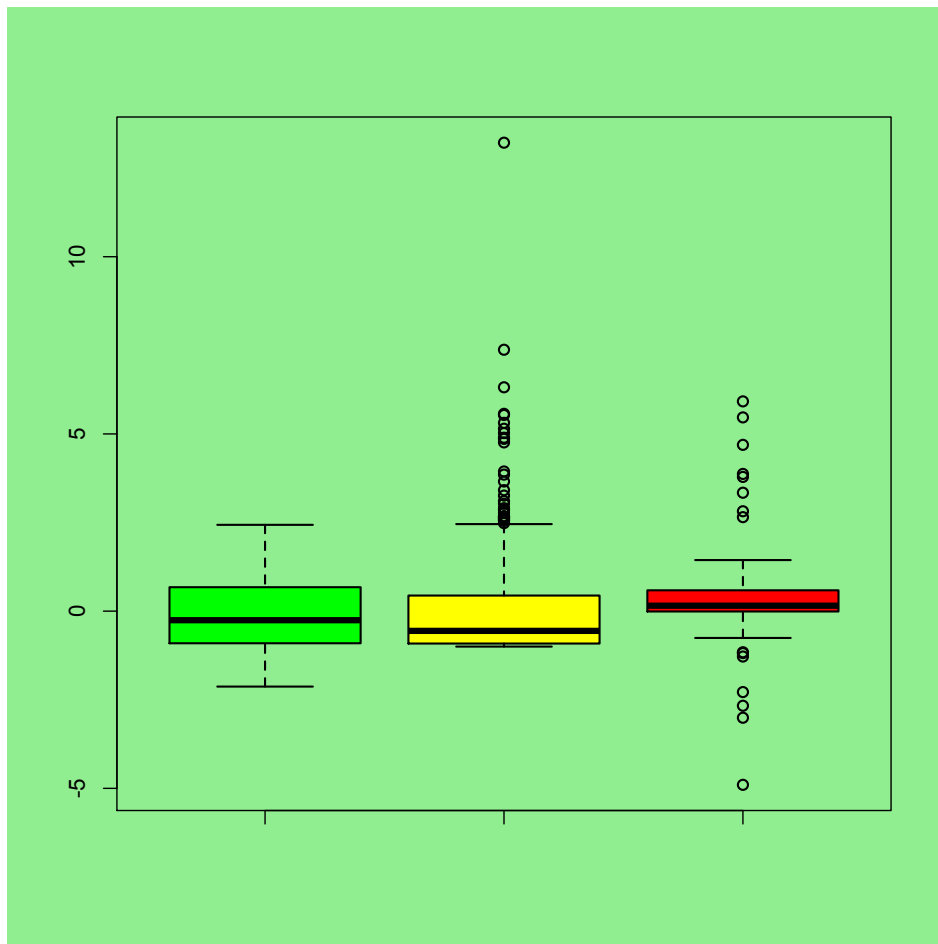


Figure 4: Boxplots of 3.5

Question 3

The parallel boxplots of 3.5 are presented in figure 4.

- (a) The most dispersed distribution is the first one since dispersion corresponds to the size of the box with tails (from A to B).
- (b) The second distributions seems to have more outliers points than the two others.

Question 4

(a) The weight that such a proportion of cable can carry corresponds to the 3rd quartile, i. e. 12,25 T.

(b) The boxplot can be seen in figure 5. There is one outlier (point at 7), because it appears to be outside the standard values (and is therefore represented that way). The value of the third quartile is the coordinate of the upper bound of the box.

(c) The parts of the box around the median are not of same size and the tails are also of different sizes, so the distribution is not symmetric.

Question 5

See code for graphic representation of empirical laws.

(i) Figure 5 shows superposition of empirical curve of the law of T_i and the curve $1 - \exp(-x/2)$. The distribution function of T_i should be that one since their shapes are very close. One can find the result by calculations: $F_T(x) = \mathbb{P}(T < x) = \mathbb{P}(-2\ln(U) < x) = \mathbb{P}(U > \exp(-x/2)) = 1 - \mathbb{P}(U \leq \exp(-x/2)) = 1 - \exp(-x/2)$, because U is uniformly distributed.

(ii) See figure 6. The law of X_i seems to be not so far from the function $\frac{1}{0.82*\pi} \arctan(\pi * x/2.3) + 0,5$. The exact law can be calculated by conditioning on \sqrt{T} and is given by an integral.

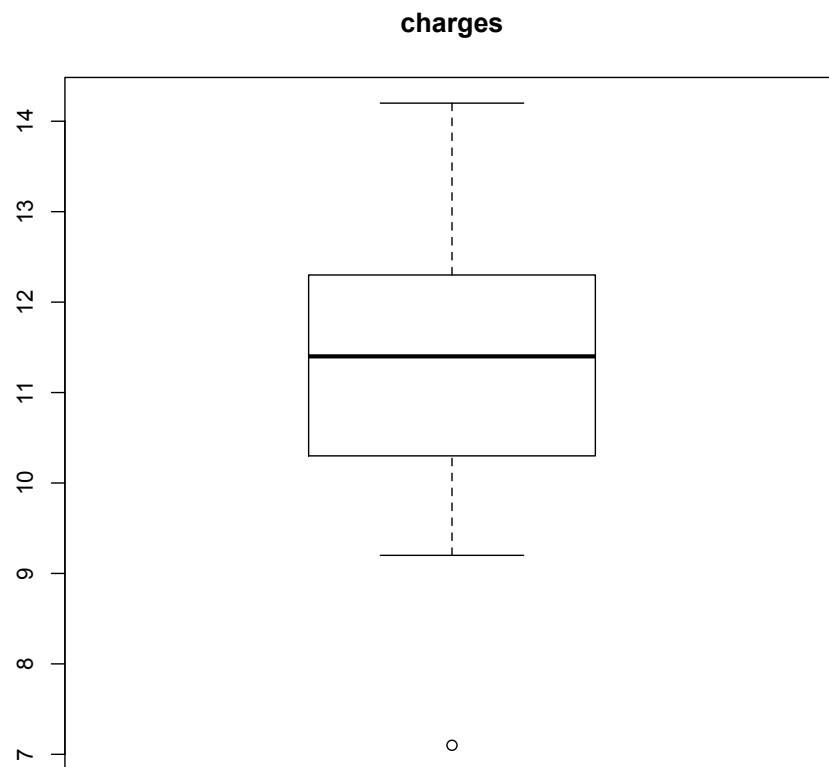


Figure 5: Boxplot for cables capacity data

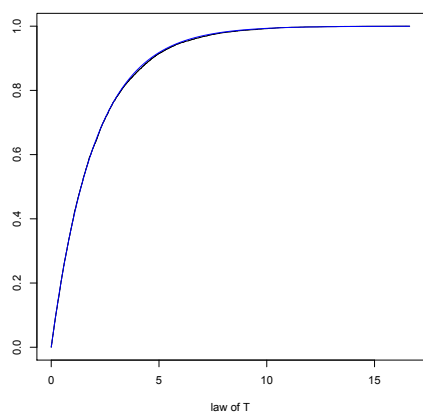


Figure 6: Law of T_i

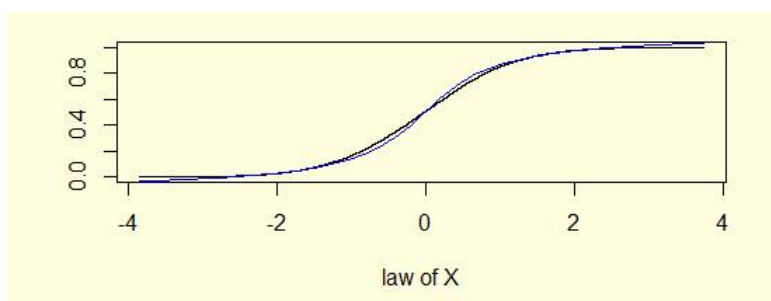


Figure 7: Law of X_i

Source code

```

1  ##SINUM – TP1

    ##Question 1
    ##see report

6  ##Question 2
    library(MASS)
    data(geyser)

    #Statistic description
11  summary(geyser)
    #Distribution function
    par(mfcol=c(2,1),bg="lightyellow")
    n=length(geyser$waiting)
    plot(sort(geyser$waiting), 1:n/n, type="s", ylim=c(0,1),
16      xlab="", ylab="",main="law for waiting time")
    n=length(geyser$duration)
    plot(sort(geyser$duration), 1:n/n, type="s", ylim=c(0,1),
      xlab="", ylab="",main="law for duration")
    #Boxplots
21  par(mfcol=c(2,1),bg="lightyellow")
    boxplot(geyser$waiting)
    boxplot(geyser$duration)
    #histograms
    par(mfcol=c(2,1),bg="lightyellow")
26  hist(geyser$waiting,breaks=50)
    hist(geyser$duration,breaks=50)

    ##Question 3
    ###see report

31  ##Question 4
    charges<-c(10.1,12.2,9.3,12.4,13.7,10.8,11.6,10.1,11.2,
      11.3,12.2,12.6,11.5,9.2,14.2,11.1,13.3,11.8,7.1,10.5)

36  ##a
    summary(charges)
    ##The value of the 3rd quartile is 12.25

    ##b
41  boxplot(charges,main="charges")

    ## Question 5
    U = runif(10000,0,1)
    V = runif(10000,0,1)
46  T = -2*log(U)
    X = sqrt(T)*cos(2*pi*V)

    #i : law of T ?
    n=length(T)
51  plot(sort(T), 1:n/n, type="s", ylim=c(0,1), xlab="law of T", ylab="")
    curve(1-exp(-x/2),add=TRUE,col="blue",ylab="")
    #ii : law of X
    f<-function(x){1-area(function(v){0.5-atan(pi*x/2.3)/(0.82*pi)},0,1)}
    n=length(X)

```

```
56 plot(sort(X), 1:n/n, type="s", ylim=c(0,1), xlab="law of X", ylab="")
   curve(from = -5,to = 5,0.5+atan(x)/pi,add=TRUE,col="blue",ylab="")
```