

# A multi-dimensional percolation approach to characterize sustainable mega-city regions

J. Raimbault<sup>1,2,\*</sup>

[juste.raimbault@polytechnique.edu](mailto:juste.raimbault@polytechnique.edu)

<sup>1</sup>UPS CNRS 3611 ISC-PIF

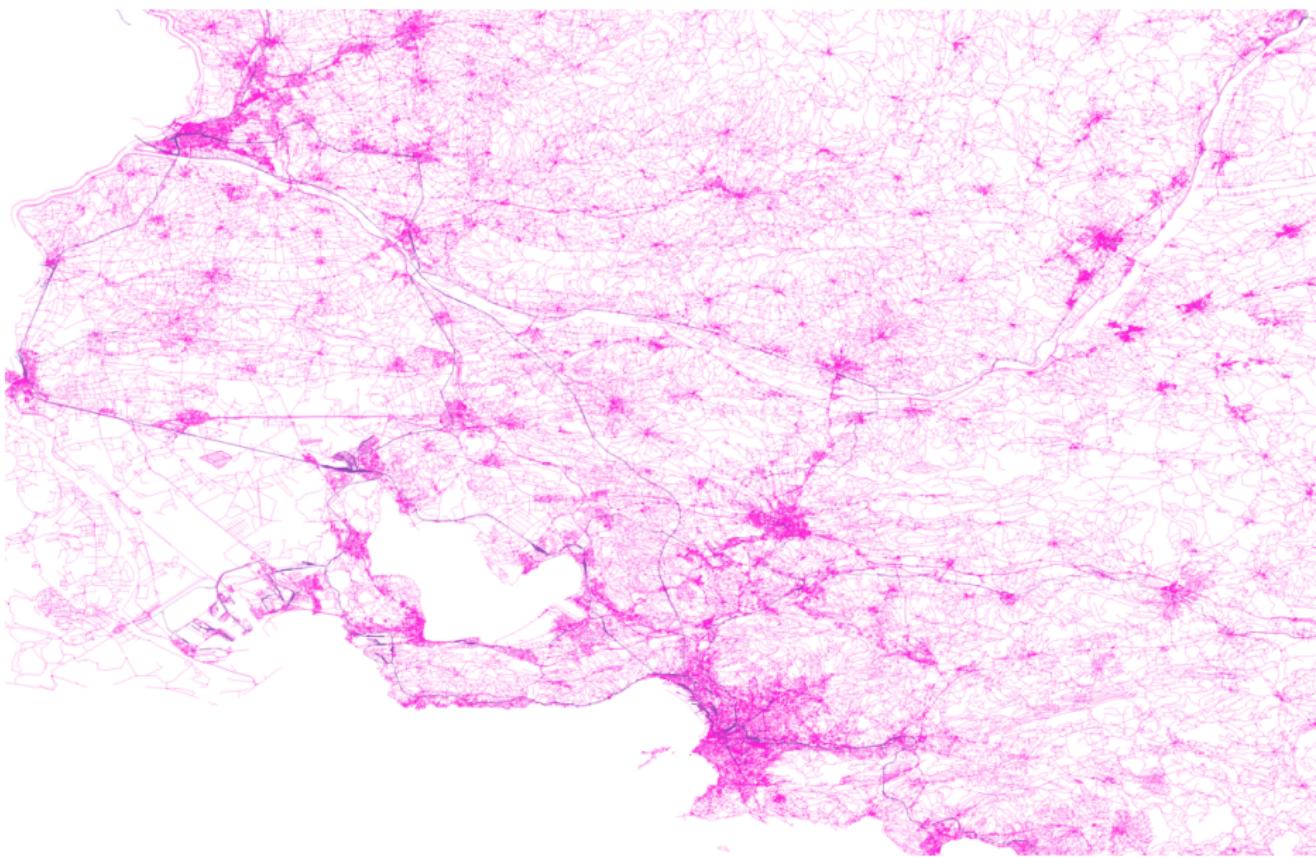
<sup>2</sup>UMR CNRS 8504 Géographie-cités

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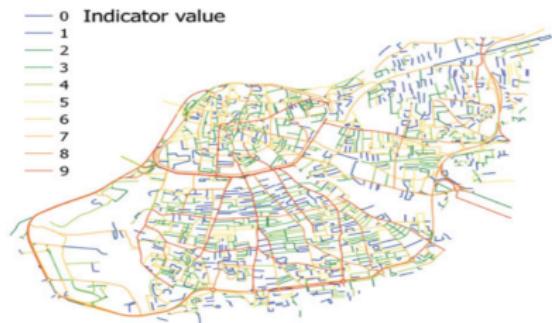
# Morphologies of networks and territories



Source: *OpenStreetMap*

# Characterizing Road networks

*Multiple dimensions to characterize road networks*



© data from BD TOPO 2014

Lagesse, C., Bordin, P., & Douady, S. (2015). A spatial multi-scale object to analyze road networks. *Network Science*, 3(1), 156-181. [Lagesse et al., 2015]

# Network percolation

**Network percolation:** *progressive occupation/connection of nodes of a network* [Callaway et al., 2000]

Application to the study of cities:

- modeling urban growth [Makse et al., 1998]
- endogenous determination of regions [Arcaute et al., 2016]
- characterization of spatial point patterns [Huynh et al., 2018]

*Towards complementary dimensions to condition road network percolation*  
→ similar to [Cottineau et al., 2018] to define urban areas

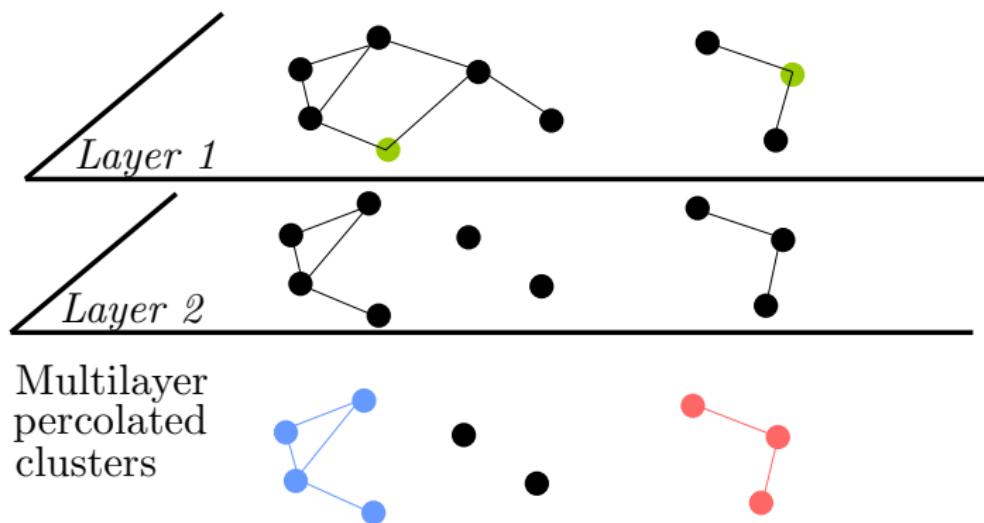
# Multidimensional percolation

- Need to combine morphological and functional dimensions of cities [Burger and Meijers, 2012]
- Interactions between networks and territories to capture the link between form and function [Rambault, 2018a]; potential application to sustainability of urban systems

**Research objective :** *Investigate a multi-dimensional percolation of territorial networks taking into account urban morphology and road network topology; endogenous characterization of urban regions.*

# Multilayer percolation

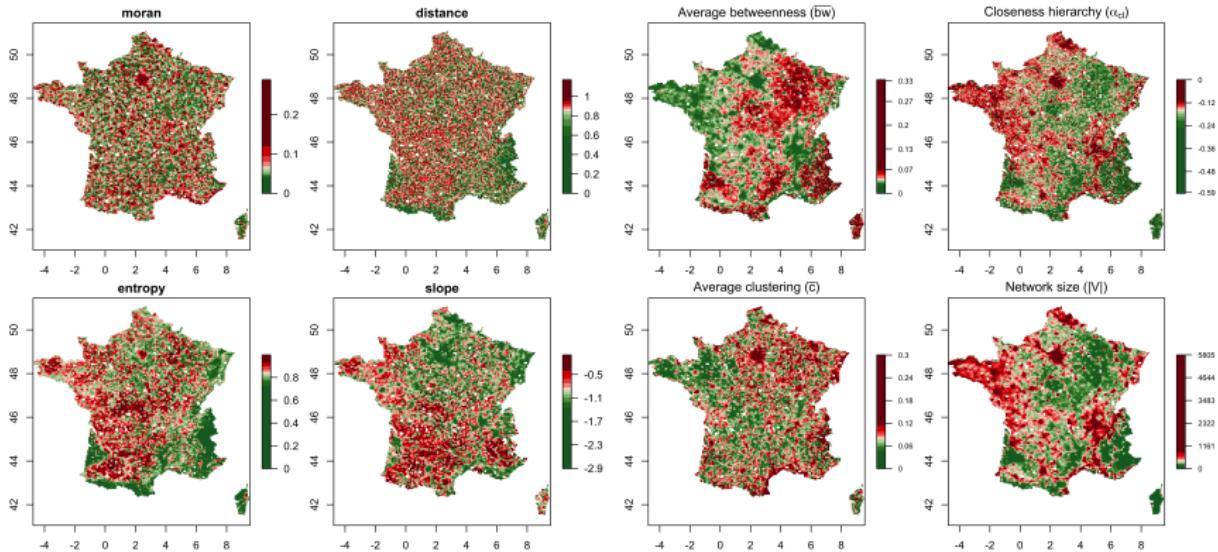
*Multi-dimensional network percolation heuristic, similar to multilayer percolation [Boccaletti et al., 2014]*



**Parameters:** percolation radius  $r_0$ , percolation thresholds  $\theta_i$  for each layer

# Empirical data and variables

*Territorial indicators computed for Europe by [Raimbault, 2018b]*



**Population distribution morphology and Network topology** (betweenness, closeness, clustering, efficiency, ...) computed on 50km spatial windows (Eurostat density grid and OpenStreetMap)

# Network construction

**Two layers:** population density (threshold  $\theta_P$ ) and network characteristics (threshold  $\theta_N$ ) taken among {Number of edges, Number of vertices, Cyclomatic number  $\mu$ , Euclidian efficiency  $v$ }; percolated with a radius  $r_0$

**Rationale:** *two locations will be in relation if they are close, have a high population density and given network characteristics.*

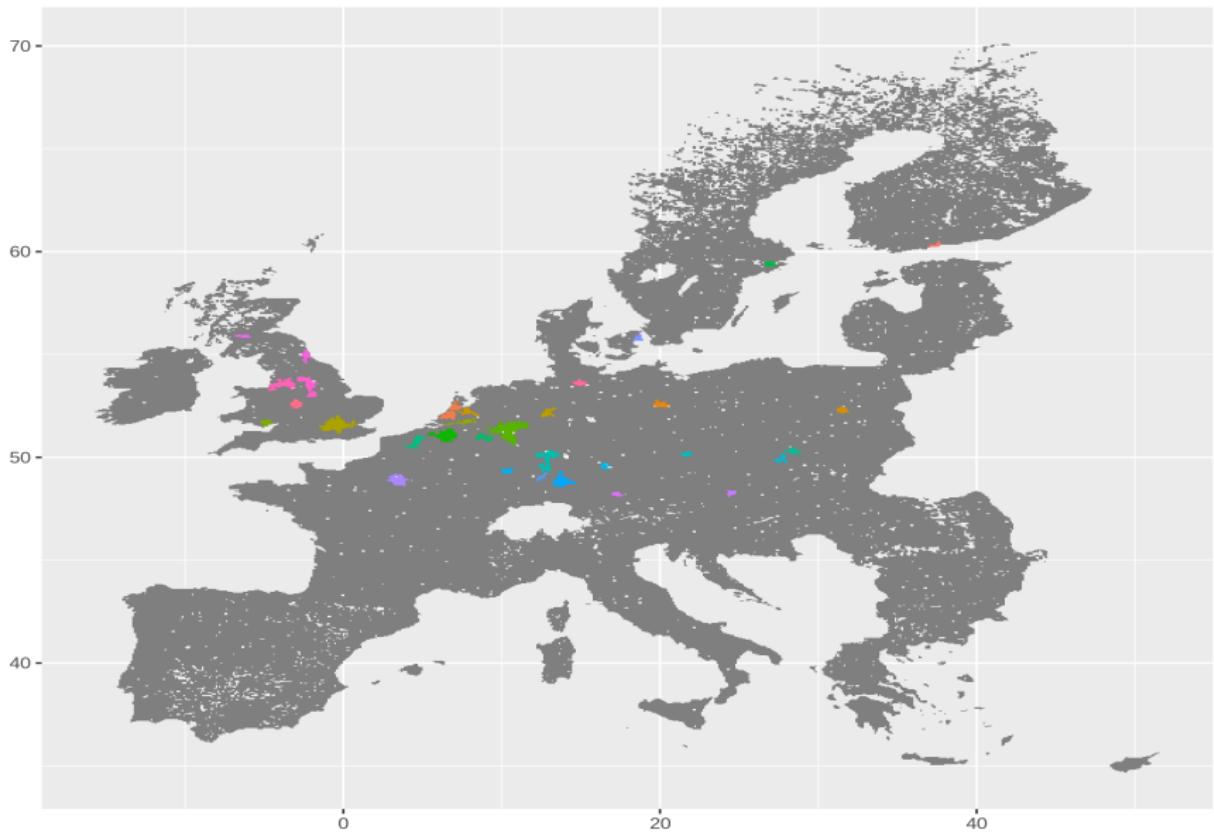
**Implementation:** construction of a single layer spatial network given the condition on the two layers and distances, from the 5km resolution indicators spatial field; extraction of connected components.

**Experience plan:** grid sampling for  $r_0, \theta_P, \theta_N$  and network variables; additional gravity potential parameters  $\gamma, d_0$  (detailed after)  
→ 4800 parameter points

# Results: endogenous mega-regions

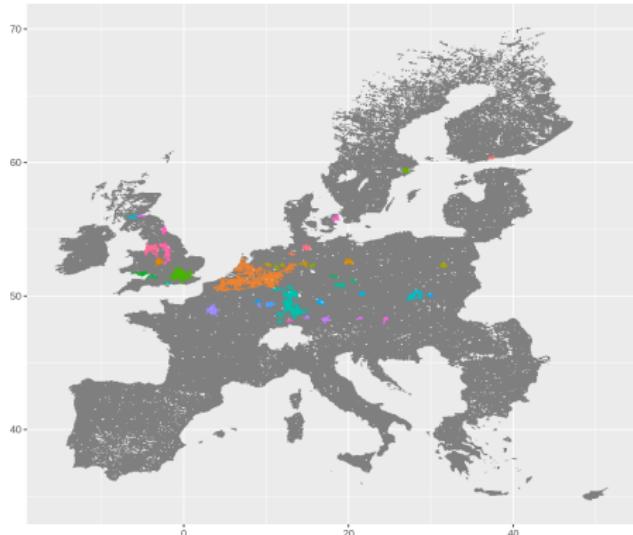
*Extraction of endogenous polycentric mega-city regions [Hall and Pain, 2006]*

$\theta_P=0.95$  ;  $\theta_N=0.9$  ; ecount ;  $r_0 = 8\text{km}$

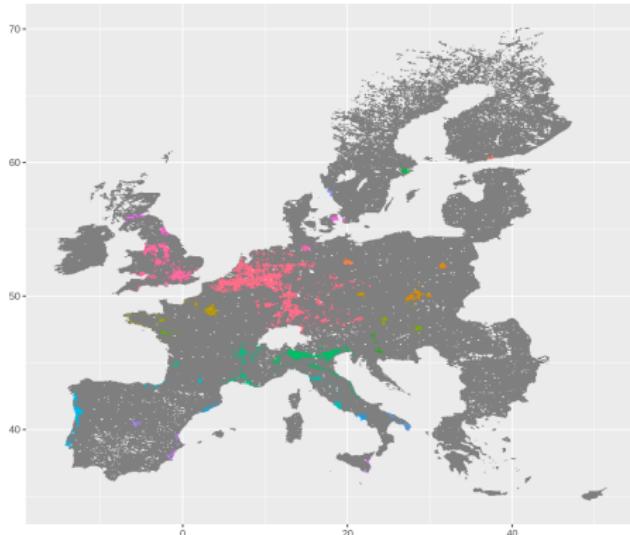


# Different endogenous morphologies

$\theta_P=0.9$  ;  $\theta_N=0.8$  ; vcount ;  $r_0 = 8\text{km}$



$\theta_P=0.85$  ;  $\theta_N=0.9$  ; vcount ;  $r_0 = 50\text{km}$



# Characterizing sustainability

**Application:** sustainability indicators for the endogenous urban regions; proxys for two conflicting dimensions: GHG emissions and economic integration [Viguié and Hallegatte, 2012].

**Data:** EDGAR database for GHG emissions (v4.3.2)  
[Janssens-Maenhout et al., 2017]

**Estimation:** Abstract flows approximated with a gravity model

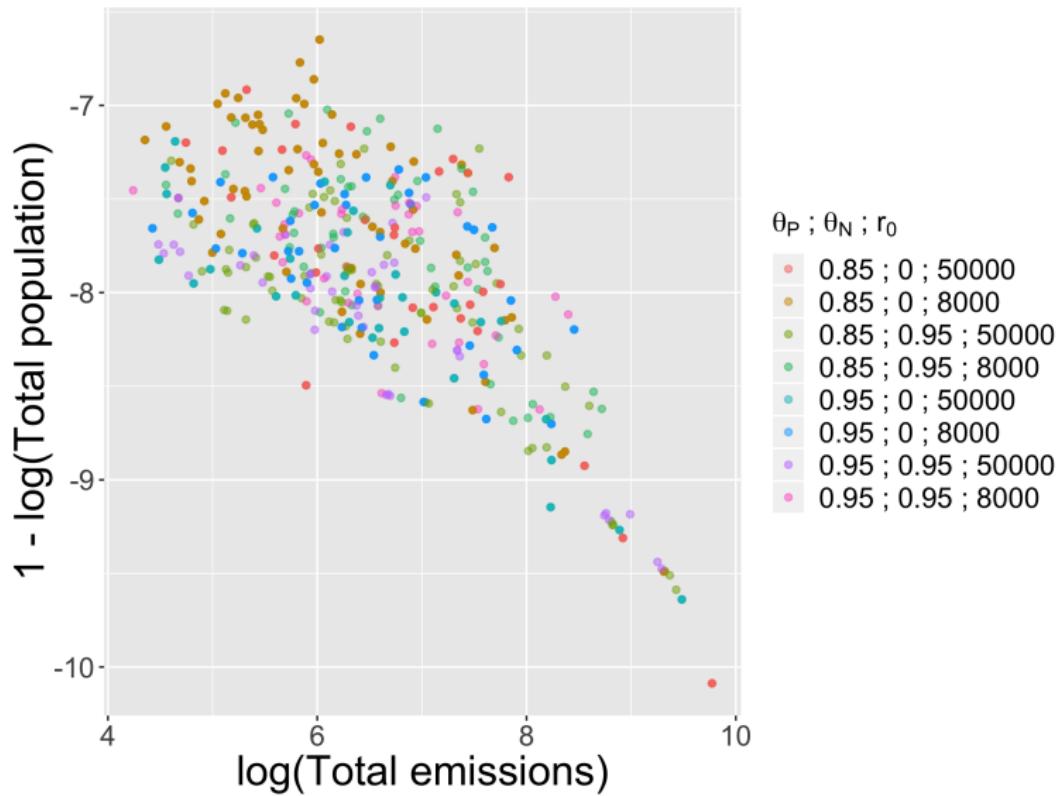
$$\phi_{ij} = \left( \frac{v_i v_j}{(\sum_k v_k)^2} \right)^\gamma \cdot \exp \left( \frac{-d_{ij}}{d_0} \right)$$

where  $v_k$  are either effective local GHG emissions or population (economic activity scaling law of population [Bettencourt et al., 2007])

→ sum of flows within the geographical span of the cluster (convex hull)  
approximate potential emissions and economic activity

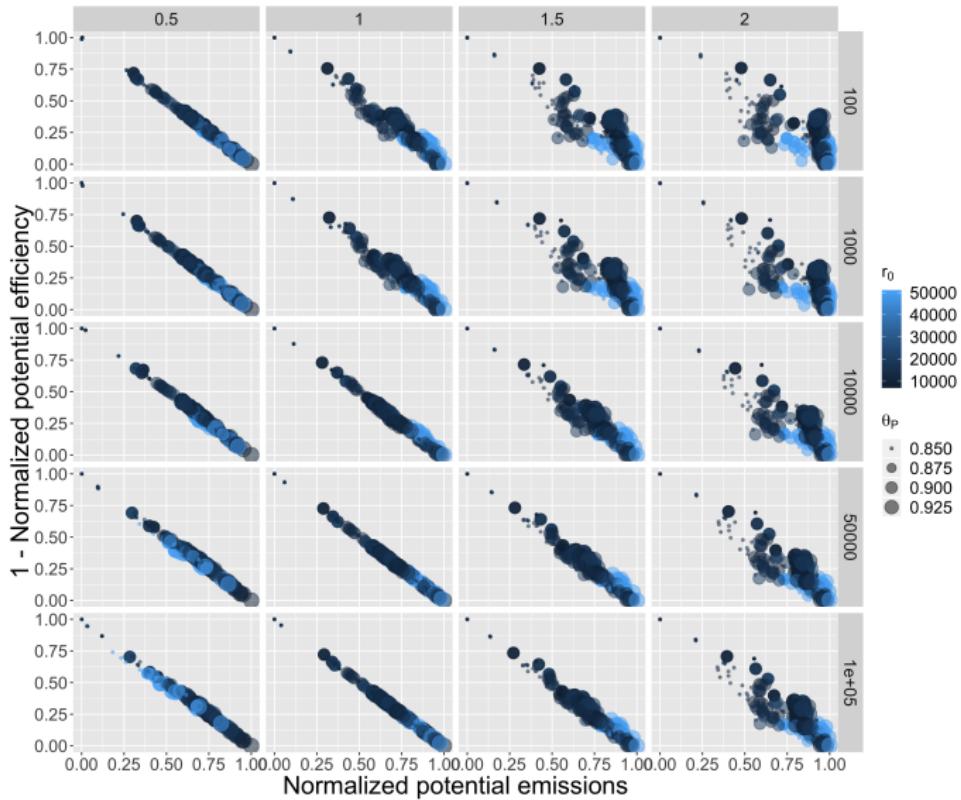
# Pareto fronts for sustainability

*Superposing Pareto front for observed population and emissions, on all clusters.*



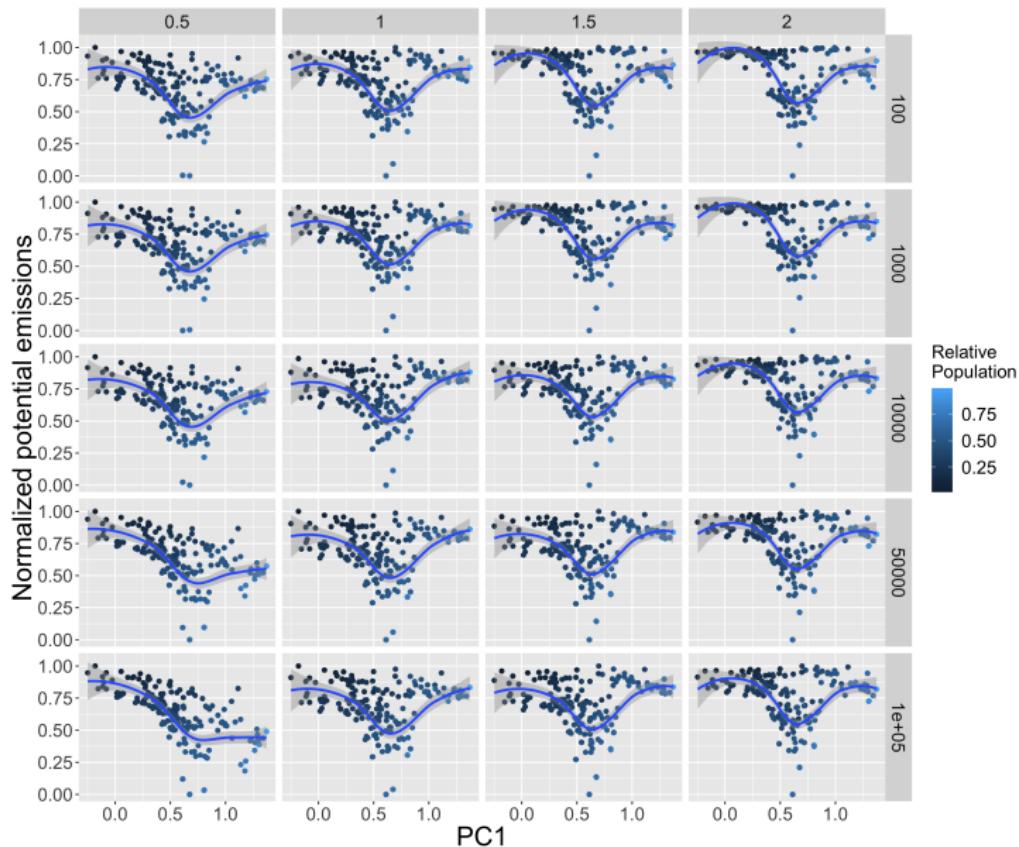
# Pareto fronts for aggregated indicators

Aggregated sustainability indicators suggest some configurations are more Pareto efficient (high  $\gamma$  regime, activities with high added value).



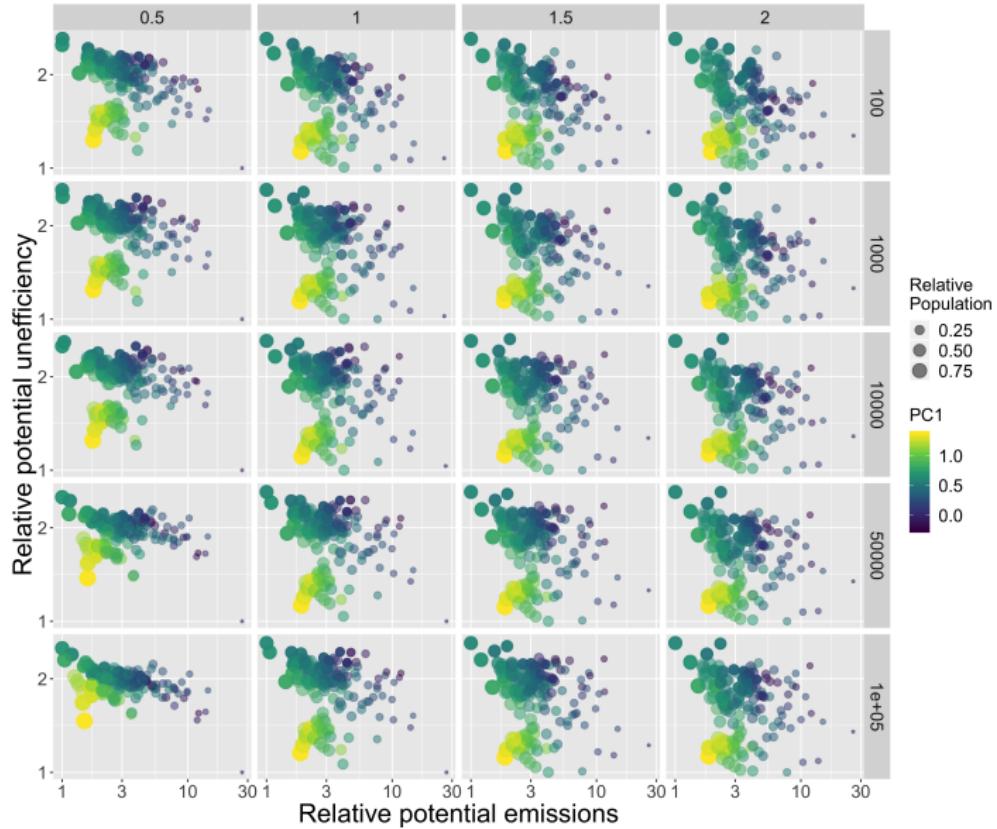
# An optimal morphology ?

*Optimal degree of monocentricity of the system for emissions.*



# Morphological trade-offs

No “optimal” cities, different forms yield different compromises in terms of relative indicators.



# Towards a systematic calibration

Grid sampling to explore regions rapidly limited

→ towards the use of genetic algorithms on grid, made smooth with the OpenMOLE software <https://next.openmole.org/>



*OpenMOLE: (i) embed any model as a black box; (ii) transparent access to main High Performance Computing environments; (iii) model exploration and calibration methods.*

**Apply to the summer school !** <https://exmodelo.org/>

# Discussion

## Implications

- Multi-dimensionality of urban systems and a link between form and function captured through multilayer percolation.
- Possible transfer to policy-making recommendations: Pareto-optimal configuration can be used for the planning of regional transportation networks, policies for subsidies, etc.

## Developments

- Systematic calibration of parameters to unveil more exhaustive Pareto fronts.
- Extrapolation of transportation flows to estimate potential emissions linked to transportation: calibration of gravity model on actual transportation emissions; use of the extrapolated parameters in potentials.
- More refined indicators for sustainability (socio-economic integration, accessibilities, different scaling exponents).

# Conclusion

- Empirical and theoretical research directed towards concrete policy-making applications. **Need for more data-driven approaches.**
- Towards multi-scalar approaches ? **Need for more integrated models.**
- Multidimensionality of urban systems ? **Need for more interdisciplinarity.**

## Related works

Raimbault, J. (2018). Calibration of a density-based model of urban morphogenesis. *PloS one*, 13(9), e0203516.

Raimbault, J. (2018). An Urban Morphogenesis Model Capturing Interactions between Networks and Territories. *Forthcoming in Mathematics or Urban Morphogenesis*. arXiv:1805.05195.

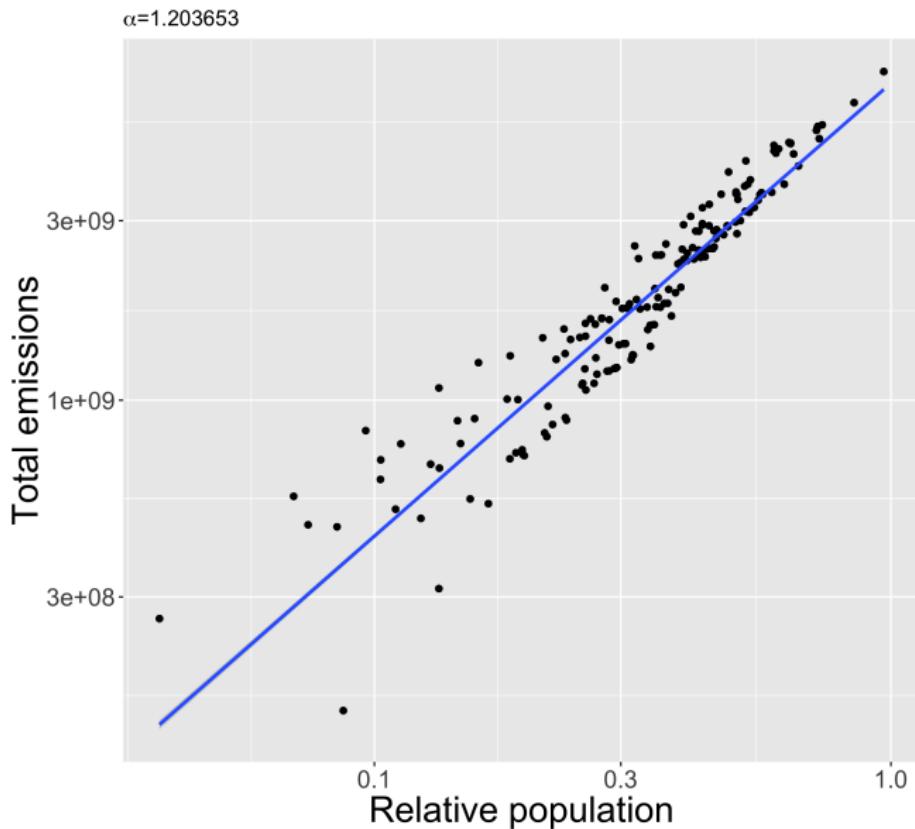
Raimbault, J. (2018). Caractérisation et modélisation de la co-évolution des réseaux de transport et des territoires (Doctoral dissertation, Université Paris 7 Denis Diderot). <https://halshs.archives-ouvertes.fr/tel-01857741>

**Open repository** at <https://github.com/JusteRaimbault/UrbanMorphology> (code, data and results)

# Reserve Slides

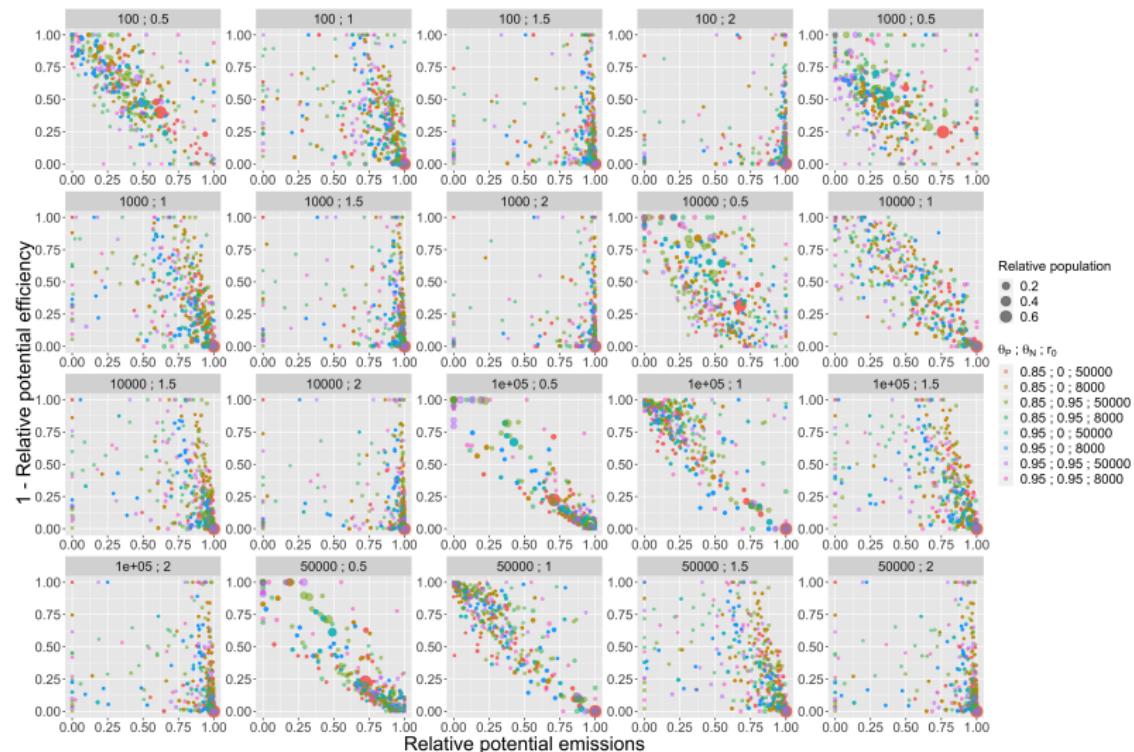
# Results: effective emissions

*Effective emissions exhibit a supralinear scaling of population*



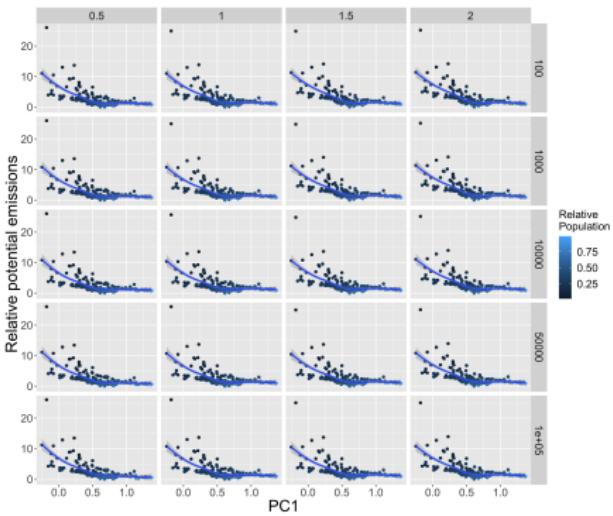
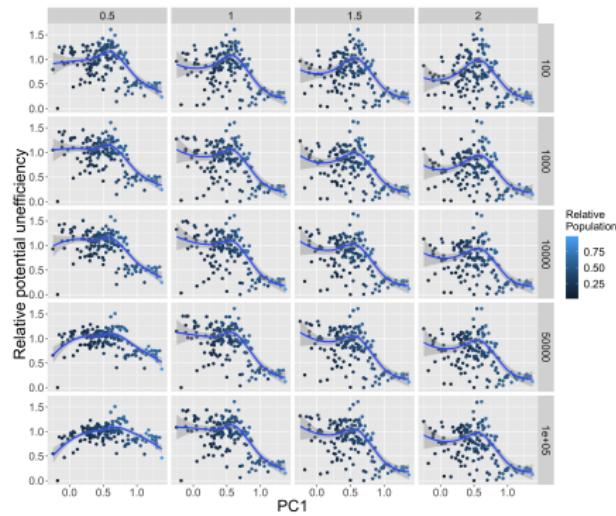
# Results: all clusters Pareto fronts

Variation of Pareto front patterns when potential parameter  $\gamma, d_0$  vary.



# Results: an optimal morphology

*More monocentric areas are more optimal in terms of relative emissions and efficiency ?*



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