3.12 Using Eq. (3.22) and
$$N_A = N_D$$

$$= 5 \times 10^{16} \text{ cm}^{-3} \text{ and } n_i = 1.5 \times 10^{10} \text{ cm}^{-3},$$

we have $V_0 = 778 \text{ mV}$.

Using Eq. (3.26) and $\epsilon_s = 11.7 \times 8.854 \times 10^{-14}$ F/cm, we have

$$W = 2 \times 10^{-5}$$
 cm = 0.2 μ m. The extension of

the depletion width into the n and p regions is given in Eqs. (3.27) and (3.28), respectively:

$$x_n = W \cdot \frac{N_A}{N_A + N_D} = 0.1 \,\mu\text{m}$$

$$x_p = W \cdot \frac{N_D}{N_A + N_D} = 0.1 \,\mu\text{m}$$

Since both regions are doped equally, the depletion region is symmetric.

Using Eq. (3.29) and

$$A = 20 \,\mu\text{m}^2 = 20 \times 10^{-8} \,\text{cm}^2$$
, the charge magnitude on each side of the junction is

$$Q_J = 1.6 \times 10^{-14} \text{ C}.$$

3.15 Equation (3.26):

$$W = \sqrt{\frac{2\epsilon_s}{q} \left(\frac{1}{N_A} + \frac{1}{N_D}\right) V_0},$$

Since $N_A \gg N_D$, we have

$$W \simeq \sqrt{\frac{2\epsilon_s}{q} \frac{1}{N_D} V_0}$$

$$V_0 = \frac{qN_D}{2\epsilon_s} \cdot W^2$$

Here $W = 0.2 \,\mu\text{m} = 0.2 \times 10^{-4} \,\text{cm}$

So
$$V_0 = \frac{1.6 \times 10^{-19} \times 10^{16} \times (0.2 \times 10^{-4})^2}{2 \times 1.04 \times 10^{-12}}$$

= 0.31 V

$$Q_J = Aq \left(\frac{N_A N_D}{N_A + N_D}\right) W \cong Aq N_D W$$

since $N_A \gg N_D$, we have $Q_J = 3.2$ fC.

3.19 Equation (3.39):

$$I = Aqn_i^2 \left(\frac{D_p}{L_p N_D} + \frac{D_n}{L_n N_A}\right) \left(e^{V/V_T} - 1\right)$$

Here
$$I_p = Aqn_i^2 \frac{D_p}{L_p N_D} \left(e^{V/V_T} - 1 \right)$$

$$I_n = Aqn_i^2 \frac{D_n}{L_n N_A} \left(e^{V/V_T} - 1 \right)$$

$$\frac{I_p}{I_n} = \frac{D_p}{D_n} \cdot \frac{L_n}{L_p} \cdot \frac{N_A}{N_D}$$

$$=\frac{10}{20}\times\frac{10}{5}\times\frac{10^{18}}{10^{16}}$$

$$\frac{I_p}{I_n} = 100$$

Now
$$I = I_p + I_n = 100 I_n + I_n \equiv 1 \text{ mA}$$

$$I_n = \frac{1}{101} \text{ mA} = 0.0099 \text{ mA}$$

$$I_p = 1 - I_n = 0.9901 \text{ mA}$$

3.21
$$n_i = BT^{3/2}e^{-E_g/2kT}$$

At 300 K,

$$n_i = 7.3 \times 10^{15} \times (300)^{3/2} \times e^{-1.12/(2 \times 8.62 \times 10^{-5} \times 300)}$$

$$= 1.4939 \times 10^{10} / \text{cm}^2$$

$$n_i^2$$
 (at 300 K) = 2.232 × 10²⁰

At 305 K,

$$n_i = 7.3 \times 10^{15} \times (305)^{3/2} \times e^{-1.12/(2 \times 8.62 \times 10^{-5} \times 305)}$$

$$= 2.152 \times 10^{10}$$

$$n_i^2$$
 (at 305 K) = 4.631 × 10²⁰

so
$$\frac{n_i^2 \text{ (at 305 K)}}{n_i^2 \text{ (at 300 K)}} = 2.152$$

Thus I_S approximately doubles for every 5°C rise in temperature.

3.25 Equation (3.49),
$$C_j = \frac{C_{j0}}{\left(1 + \frac{V_R}{V_0}\right)^m}$$

For
$$V_R = 1 \text{ V}$$
, $C_j = \frac{0.4 \text{ pF}}{\left(1 + \frac{1}{0.75}\right)^{1/3}}$

$$= 0.3 \, pF$$

For
$$V_R = 10 \text{ V}$$
, $C_j = \frac{0.4 \text{ pF}}{\left(1 + \frac{10}{0.75}\right)^{1/3}}$

$$= 0.16 \, pF$$