# FEP Course Project: GeoMod

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#### Abstract

The use of non-manifold models can allow for better approximations of physical problems. This has been shown in previous research of matrix-fiber composites as well as on going work in coupled finite element-dislocation dynamics. The code created in this project allows users to make modifications to a preexisting model and define meshing attributes. The modifications include placement of model vertices, edges, and surfaces. When the user places these entities in the model, they also specify the local mesh refinement. Model entities are always created such that the topology of the model remains valid. Mesh refinement information is only updated if the new refinement level is finer than the current. Thirteen tests were created to confirm that expected behavior of the code was achieved. Of these tests, three focus on vertex placement, four on edge placement, and three on surface placement. The results of each test are presented as evidence of passing the test. Possible future work include parallelization, handling of assembly models, and inclusion of features that can delete or modify existing model entities.

## 1 Introduction

Non-manifold models can allow for better approximations of physical scenarios. In the scope of this report, a non-manifold model is taken to mean a model in which every point on a surface need not be two dimensional [1]. This allows for the creation of models where, for example, two or more three dimensional regions need only share a vertex or an edge. This also supports geometric entities containing lower entities. E.g., a vertex can be placed in a region, surface, or edge; an edge may be placed in a region or surface; a surface can be placed with in a region.

An example of how non-manifold models are used is in the modeling of the micro structure of cross-linked fiber networks embedded in a continuous matrix [2]. In this dissertation, a three dimensional region was used to represent a continuous matrix; one dimensional edges were used to represent collagen network fibers. The fibers were able to begin and terminate on either a model face or in the model region. The resulting model was then discretized such that volumetric elements represented the matrix and beam elements represented the collagen fibers.

Another example of how a non-manifold model can be used is in the modeling of coupled finite element analysis with dislocation dynamics. In this scenario, a crystalline solid is represented as a three dimensional region. Within this region, edge and screw dislocations are represented as two dimensional edges. These dislocation both create and are acted on by the stress field around them [3]. Similar to the collagen fibers, the edges that represent the dislocations may begin and end in any model surface or region. The discretized model is comprised of volumetric finite elements. The edges of the elements near the dislocation are collinear with the dislocation; the vertices of the element are also coincident with the nodes of the dislocation. Additionally, the mesh near the dislocation needs to be finer to better approximate stress at the dislocation.

The goal of this project is to create an interface to the Simmetrix modeling and meshing Application Program Interfaces (APIs). This interface will allow the user to add non-manifold geometric features to a base geometric model. Additionally, the user needs to be able to define local mesh characteristics for the created geometry. The created geometry can include model vertices, edges, and faces. The edges and faces cannot be limited to straight lines and flat planes, respectively. During model modification, the validity of the topology must be maintained. This will allow for correct discretization of the model and interrogation of both the model and mesh. During mesh case specification, updated refinement criteria must be merged with the existing information. For these cases, finer level of refinement must always be used.

The remainder of this report is organized in the following manner. The general design of the code is presented in section 2; the specifics of the implementation for vertex, edge, and face placement is discussed in the subsections 2.1, 2.2, and 2.3,

respectively. Testing is presented in 3 with test cases and their results for vertex, edge, and face placement discussed in subsections 3.1, 3.2, and 3.3, respectively. Conclusions are drawn and possible future work is presented in section 4. Finally, the source code for the project is appended in Appendix A.

# 2 Code Design

The user interacts with the code by constructing a gmd object based on an existing in-memory Simmetrix geometric model that they wish to modify. The header and source files for the gmd class are shown in Appendices A.4 and A.5, respectively. The user can then modify the model by creating model vertices, edges, and faces by calling gmd member functions. Mesh case information for these modifications is also specified by the user at this time. The gmd class is primarily a wrapper around two other classes. It also has member functions that check the validity of user input for creating edges and faces. The two classes that it wraps in turn wrap around Simmetrix APIs.

The first class is the *model\_helper* class which handles all model interactions. This includes making modifications to the model, checking its validity, and writing it to disk. Its member variables include a pointer to the Simmetrix model. The header and source file of the model\_helper class are shown in Appendices A.6 and A.7, respectively. The APIs used are from Simmetrix's GeoSim Core and Advanced libraries [4].

The second class wrapped within the gmd class is the *mesh\_helper* class which handles all mesh interactions. This includes defining global and local mesh parameters, checking for validity, and writing the mesh. Its member variables include a pointer to a Simmetrix mesh object and mesh case object. The header and source file for the mesh\_helper class are shown in Appendices A.8 and A.9, respectively. The APIs used are from Simmetrix's MeshSim Core and Advanced libraries [4].

Model entities are always created on the geometric entity with the lowest possible dimension when applicable. This ensures correct classification when model or mesh entities are later interrogated. For example, say the user wants to create a vertex whose coordinates lie upon an edge which bounds a face of a region. The vertex will be created and classified as a entity on the edge as opposed to only the face or region. This is detailed in subsection 2.1 and demonstrated in subsection 3.1.

Mesh case information, such as local refinement level, are specified during model modification by the user; the finer specification is always used. For example, if the user creates an edge with a relative local refinement of 0.1 and creates a vertex on that edge with a refinement of 0.5, then only a refinement level of 0.1 will be used throughout the whole edge. Alternatively, if a refinement level

of 0.5 is specified for the edge and 0.1 specified for a vertex on that edge, then a refinement level of 0.5 will be used throughout the edge except for space near the vertex. The rate at which the refinement level decreases from 0.5 to 0.1 for this case is controlled by the gradation rate. A rate of 2/3 is used by default but can be changed by the user.

Details regarding model vertex, edge, and face placement are discussed in subsections 2.1, 2.2, and 2.3, respectively. Testing and results of tests are presented in section 3.

#### 2.1 Vertex Placement

The gmd member function  $place\_point()$  is used to create model vertices as well as define the local mesh refinement level for the created vertex. The user specifies the coordinates of the vertex they want to create, the relative mesh refinement level, the radius of refinement, and a Simmetrix model vertex pointer that is overwritten to point to the created vertex.

The Simmetrix APIs  $GE\_closestPoint()$ ,  $GF\_closestPoint()$ , and  $GR\_containsPoint()$  are used to determine whether a 3D coordinate is in a model edge, face, or region, respectively. The function  $GR\_containsPoint()$  returns an integer denoting if the point is inside or outside of the model region. The functions  $GE\_closestPoint()$  and  $GF\_closestPoint()$  both return pointers to the real and parametric coordinates closest to a given test coordinate. The real coordinates of the closest point are then compared to the test point. If the magnitude of the distance between the two points is less then the tolerance of the model, then a model vertex is created. The value returned from the API  $GM\_tolerance()$  is used as the tolerance for all geometric comparisons.

If the user specifies coordinates which are outside any model region, the vertex is created but either a warning or error message is printed. By default, an error message is printed but this can be changed by the user. If the user specifies coordinates which are found to lie on a preexisting edge, then the point is created by splitting the edge into two. In this case, the model vertex pointer returned to the user is for the vertex at the split. Examples of vertex placement are shown in subsection 3.1.

### 2.2 Edge Placement

The gmd member function  $place\_edge()$  is used to create model edges and define the local mesh refinement for the created edge. The underlying API used is the  $SCurve\_createBSpline()$  function which creates rational and non-rational basis splines. The user specifies the order of the curve, control points, knots, weights,

mesh refinement level, and a Simmetrix model edge pointer which is overwritten with the created edge.

The place\_edge() function first checks the validity of the user's input. The checks ensure that the user defined input meets the following conditions:

- 1. The order is not less than one or greater than the number of control points.
- 2. The sum of the number of control points and order is equal to the number of knots.
- 3. The first order number of knots are equal to zero and the last order number of knots are equal to one. E.g., if order is two, then the first two knots must equal zero and the last two knots must equal one.
- 4. The knots are specified in a monotonically increasing order.
- 5. The number of weights satisfies one of two conditions:
  - (a) The number of weights is equal to the number of control points.
  - (b) The number of weights is one and the weight is equal to zero. This condition dictates the construction of a non-rational curve instead of a rational one.

If the user defined inputs do not meet the above conditions, then an error message is printed and the program aborts.

First, the end points of edge are created as vertices using the method described in subsection 2.2. Next, a curve is created using the  $SCurve\_createBSpline()$  API. The end points of the edge, the first and last control points, are created as model vertices using the method described subsection 2.1. This curve and two vertices are then used to create a geometric edge using the  $GIP\_insertEdgeInRegion()$  API. If all of the control points are coincident with a preexisting face, then the edge is inserted onto the corresponding face using the  $GM\_insertEdgeOnFace()$  API. Examples of edge placement are shown in subsection 3.2.

#### 2.3 Face Placement

The gmd member function  $place\_face()$  is used to create model faces and define the local mesh refinement for the created face. The underlying API is the  $SSurface\_createBSpline()$  function which creates rational and non-rational basis surfaces based on a local u and v coordinate system. The user specifies the following to create a surface:

1. The order of the surface in both the u and v directions.

- 2. The number of control points in the u and v directions.
- 3. The periodicity of the surface. In essence, whether the surface is periodic in either, neither, or both the u and v directions.
- 4. The coordinates of the control points. This is specified as shown in Table 1.
- 5. The weights for each control point. The order of the weights must also follow the pattern shown in Table 1.
- 6. The local mesh refinement on the face.
- 7. The geometric face pointer to be overwritten with the newly created face.

Table 1: Ordering for control points and weights for surface creation. N is the number of control points in the u direction. M is the number of control points in the v direction.

The *place\_face()* function first checks the user defined inputs for validity. The checks ensure that the user's input meets the following conditions:

- 1. The order in both the u and v directions is not less than one or greater than the number of control points in the u and v directions respectively.
- 2. The total number of control points equals to the product of declared control points in the u and v directions.
- 3. The weights meet one of the two conditions:
  - (a) The number of weights control points equals to the product of declared control points in the u and v directions.
  - (b) The number of weights in one and that one weight equals to zero. This condition dictates that a non-rational surface be created instead of a rational one.

- 4. The number of knots is equal to the sum of the number of control points and order in both the u and v directions.
- 5. The knots are specified in a monotonically increasing order.
- 6. The first order number of knots are equal to zero and the last order number of knots are equal to one for each direction. E.g., if order is three, then the first three knots must equal zero and the last three knots must equal one.

If the user's input does not meet all of the above conditions, then an error message is printed and the program aborts. Otherwise, the program next creates a surface using the  $SSurface\_createBSpline()$  API. The bounding edges of the face are created next. Each edge is created using the method described in subsection 2.2. Next, the edges and surfaces are used to create a model face using the  $GIP\_insertFaceInRegion()$  function. The normal direction of the face is taken as the crossproduct of the u and v directions (i.e.,  $n = u \times v$ ) for any given position.

# 3 Testing

Each of the features described in section 2 were tested. In total, 13 tests were created; the header and source files for these tests are shown in Appendix A.2 and A.3. The first three tests (tests 0, 1, and 2) check for basic functionality such as proper linking between classes and functions as well as creation and deletion of classes without memory leaks. Theses tests are described in Appendix A.3 and their results are shown in Appendix B.1 and B.2. The next three tests (tests 3, 4, and 5) exercise vertex placement. They and their results are discussed in detail in subsection 3.1. The next four tests (tests 6, 7, 8, and 9) exercise edge placement in different cases. These tests and their results are shown in 3.2. The last three tests (tests 10, 11, and 12) check face placement functionality. They and their results are described in subsection 3.3.

#### 3.1 Vertex Placement

Vertex placement was tested in three cases. For each test case, both the modified model and mesh were created and written to disk. Both the model and mesh were then viewed in the Simmodeler GUI to visually confirm that the expected behavior was achieved. Classification was also confirmed through use of Simmetrix APIs and through the GUI part tree.

The first case placed a vertex in the center of a three dimensional model region. The global mesh refinement level was set to 0.9 and the refinement level for the inserted vertex was 0.1. The resulting model is shown in Figure 1. The resulting mesh is shown in Figure 2.

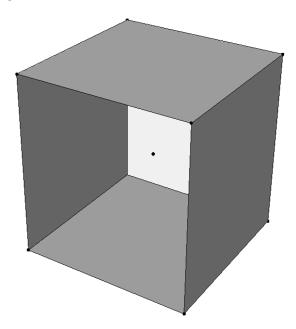


Figure 1: Cube with vertex placed at center. Front face hidden to to show interior.

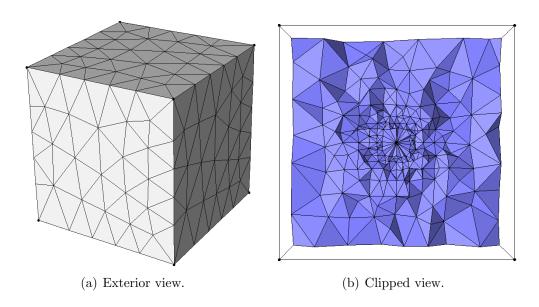


Figure 2: Mesh of cube with vertex placed at center.

The second case placed a vertex in the center of a face of a three dimensional

model. The global mesh refinement level was set to 0.9 and the refinement level of the vertex was set to 0.1. The resulting model is shown in Figure 3. The resulting mesh is shown in Figure 4.

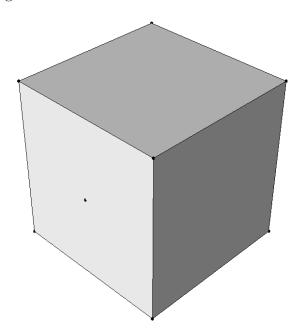


Figure 3: Cube with vertex placed at center of front face.

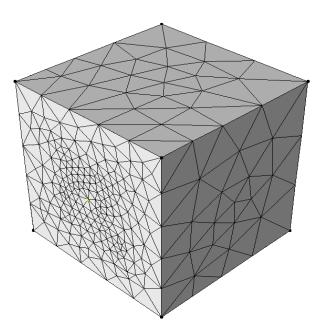


Figure 4: Mesh of cube with vertex on center of front face.

The third case placed a vertex on a preexisting model edge. The global mesh refinement level was 0.9 and the local refinement level for the vertex was 0.1. The resulting model is shown in Figure 5. The resulting mesh is shown in Figure 6.

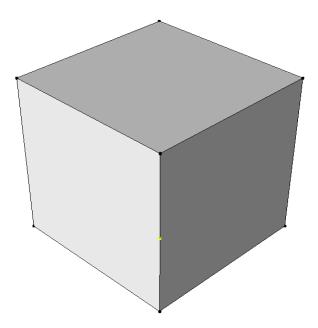


Figure 5: Cube with vertex placed at center of edge.

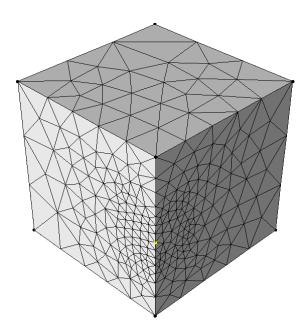


Figure 6: Mesh of cube with vertex on center of edge.

As shown in Figures 1 through 6, the gmd method  $place\_point()$  is able to correctly determine the model classification given a user defined location. It is also able to change the local mesh refinement level to a user's specification.

### 3.2 Edge Placement

Edge placement was tested in four cases. Similar to the vertex tests presented in subsection 3.1, models and meshes were created and written to disk; expected behavior and classification was confirmed through both the Simmetrix APIs and the GUI.

The first test placed a fully interior edge inside a model region. The edge was created as a rational basis spline with five control points; each control point was inside the model region. The global mesh refinement was set to 0.9 and the local set to 0.1. A wire frame view of the created model is shown in Figure 7. A clipped view of the mesh is shown in Figure 8.

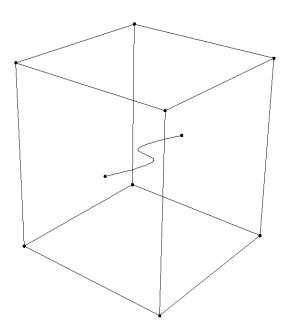


Figure 7: Cube with edge placed near center of region.

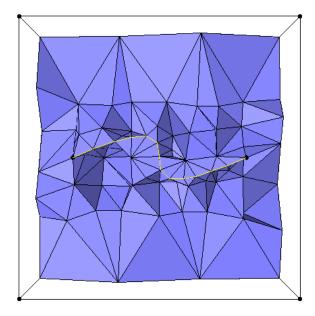


Figure 8: Clipped view of mesh for cube with edge near center of region. The edge is highlighted in yellow.

The second test placed an edge whose control points all laid on the same model face. The edge was created as a rational basis spline with five control points. The global mesh refinement was set to 0.9 and the local set to 0.1. The created model is shown in Figure 9. A view of the mesh is shown in Figure 10.

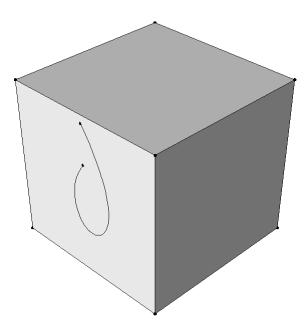


Figure 9: Cube with edge placed on model front face.

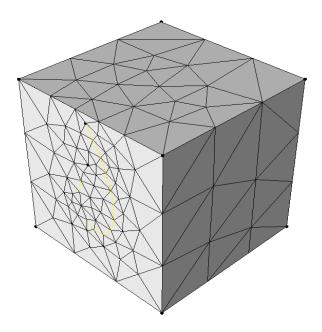


Figure 10: Clipped view of mesh for cube with edge on face. The edge is highlighted in yellow.

The third test placed an edge that started on a model face and terminated in the interior of the model region. The edge was created as a rational basis spline with five control points. The global mesh refinement was set to 0.9 and the local set to 0.1. Two images of the created model are shown in Figure 11. A external and clipped view of the mesh are shown in Figure 12.

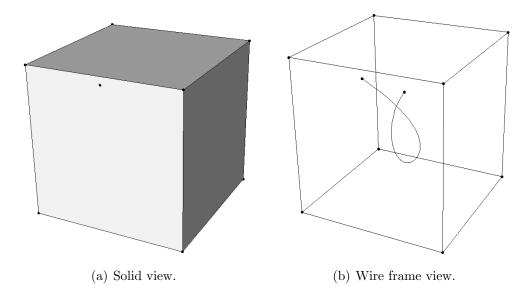


Figure 11: Model with edge inserted. Edge begins on front face and terminates with in the model region.

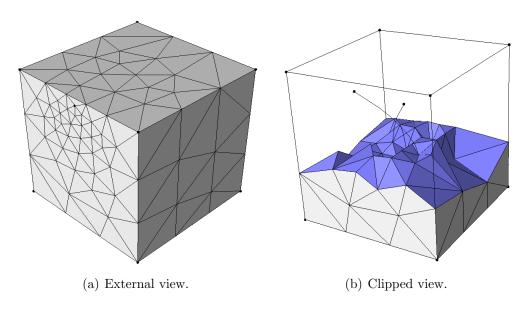


Figure 12: Mesh of model with edge from face to region inserted.

The fourth test placed an edge that started on a model edge and terminated

with in the model region. The edge was created as a rational basis spline with five control points. The global mesh refinement was set to 0.9 and the local set to 0.1. Two images of the created model are shown in Figure 13. A external and clipped view of the mesh are shown in Figure 14.

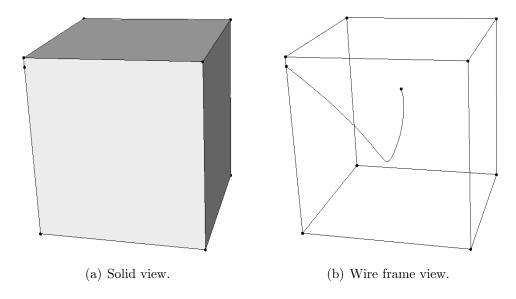


Figure 13: Model with edge inserted. Edge begins on left-most vertical model edge and terminates within the model region.

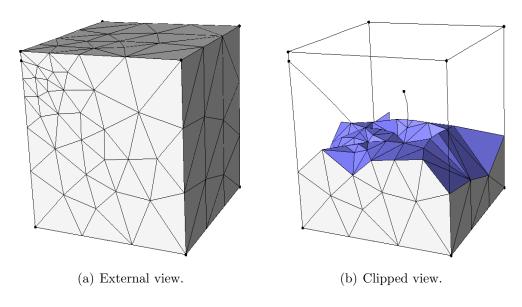


Figure 14: Mesh of model with edge from edge to region inserted.

As shown in Figures 7 through 14, the gmd method place\_edge() is able to correctly determine the model classification given user defined spline parameters. It is also able to change the local mesh refinement level to a user's specification.

### 3.3 Face Placement

Face placement was tested similarly to both the vertex and edge tests described in subsections 3.1 and 3.2. In total, three tests were performed. For each test, the created models and meshes were written to disk and viewed in the Simmetrix GUI. Classifications of model entities were confirmed through both the GUI and APIs where applicable.

The first face placement test created a model face that was completely interior to a model region. The face, and its bounding edges, were created as as a rational basis surface and splines. In total, 12 control points were defined; each control point was inside the model region and created a  $4 \times 3$  grid. The global mesh refinement was set to 0.9 and the local set to 0.1. A face view of the created model is shown in Figure 15. The face and clipped view of the mesh are shown in Figure 16.

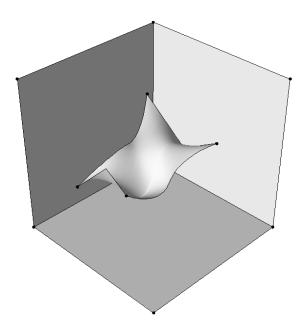


Figure 15: Cube with face created within the model region. Forward three faces were made transparent to show in the internal face.

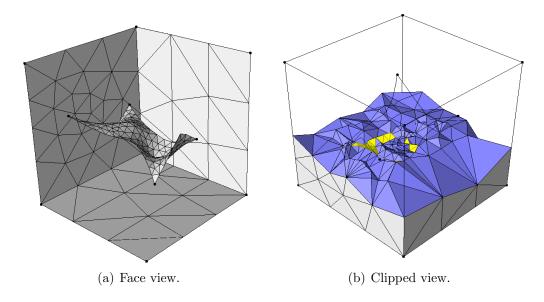


Figure 16: Mesh of model with interior face. Yellow mesh element faces indicate the mesh face is coplanar with the model face. Note the view is rotated right by 90° with respect to Figure 15.

The second face placement test created a model face that was completely interior to a model region except for one corner vertex. The face, and its bounding edges, were created as as a rational basis surface and splines. In total, 12 control points were defined; all but one control point was inside the model region and created a  $4 \times 3$  grid. The global mesh refinement was set to 0.9 and the local set to 0.1. A front and face view of the created model are shown in Figure 17. The face and clipped view of the mesh are shown in Figure 18. An external view of the mesh is shown in Appendix B.3.

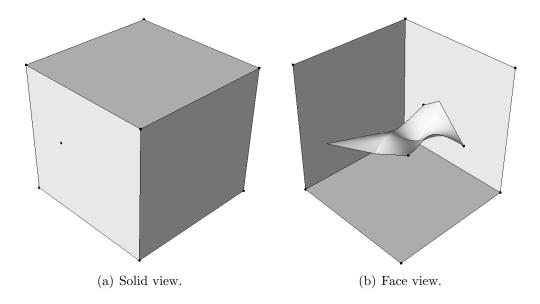


Figure 17: Model with face inserted. Face is fully interior except for one point.

The point is shown on the leftmost face in (a).

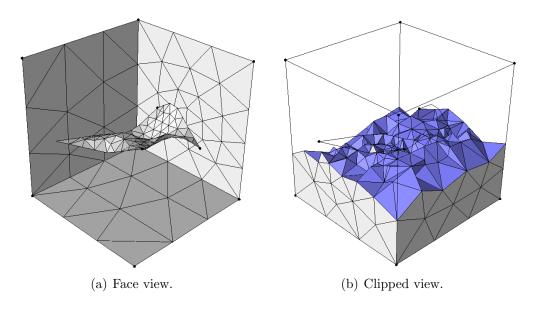


Figure 18: Mesh of model with interior face except for one point.

The third face placement test created a model face that was completely interior to a model region except for one edge. The face, and its bounding edges, were created as as a rational basis surface and splines. In total, 12 control points were defined; the control points created a  $4 \times 3$  grid. The global mesh refinement was

set to 0.9 and the local set to 0.1. A front and face view of the created model are shown in Figure 19. The face and clipped view of the mesh are shown in Figure 20. An external view of the mesh is shown in Appendix B.4.

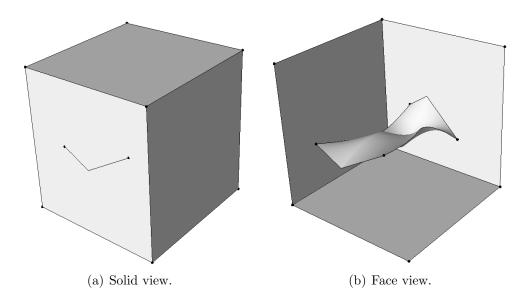


Figure 19: Model with face inserted. Face is fully interior except for one edge.

The edge is shown on the leftmost face in (a).

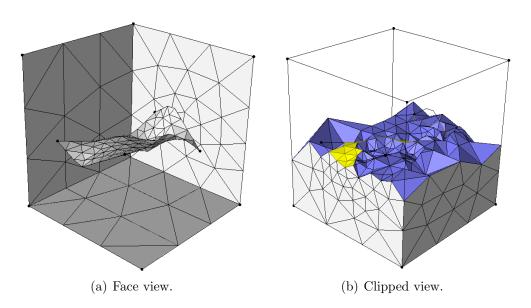


Figure 20: Mesh of model with interior face except for one edge. Yellow mesh element faces indicate the mesh face is coplanar with the model face.

As shown in Figures 15 through 20, the gmd method place\_face() is able to correctly determine the model classification given user defined surface parameters. It is also able to change the local mesh refinement level to a user's specification.

# 4 Conclusion

The purpose of this project was to create an interface to the Simmetrix APIs that allows for model and mesh modification. This was to include placement of vertices, edges, and surfaces. The interface was to be general enough to allow for the edges not be limited to straight lines and the surfaces not to be limited to flat planes. Additionally, the modified model was to remain topologically valid to allow for proper discretization and interrogation.

These features were completed in the project. Vertex placement is described in subsection 2.1 and is demonstrated in three examples in subsection 3.1. Edge placement is described in subsection 2.2 and is demonstrated in four examples in subsection 3.2. Face placement is described in subsection 2.3 and is demonstrated in three examples in subsection 3.3. The topology of the lower order entities is also valid since higher order geometric features make use of lower order ones. For example, if the method which placed vertices did not reliably create topologically valid vertices, then neither the place\_edge() or place\_face() methods would work properly.

#### 4.1 Future Work

A possible improvement to the created code is to allow for parallel model modification or model discretization. Currently, only one data structure that represents the model exists at any given time. This then leads to one data structure that represents the mesh. A parallel representation could use one common base model with different modification happening on different processors. Another possibility is to have a parallel mesh generated instead of a serial one.

The code currently can only handle native and non-manifold models, not assembly models. Additional work could be done to allow for modification of theses types of models. This would mostly include changes to region and part based functions. These changes include accounting for multiple parts and regions along with their interactions.

Work can be done that would allow for geometric entity deletion that preserves topological validity. For example, a user can currently delete any edge. This will yield a topologically invalid model if the edge was one of the bounding edges of a model face. This addition of features could also include methods to trim or extend model entities as well.

# References

- [1] Weiler, Kevin J. (1986). Topological Structures for Geometric Modeling. (Doctoral dissertation).
- [2] Zhang, Lijuan. (2013). Microstructural modeling of cross-linked fiber network embedded in continuous matrix. (Doctoral dissertation).
- [3] Askeland, Donald R., Fulay, Pradeep P., Wright, Wendelin J. (2011). The Science and Engineering of Materials. Sixth ed. Stamford, CT: Cengage Learning. Print.
- [4] Simmetrix Inc., "The simulation modeling suite." [Online]. Available: http://www.simmetrix.com/.

# A Code

## A.1 main.cpp

```
// GeoMod Header
   #include "GeoMod.hpp"
 3
   #include "GeoMod_Tests.hpp"
 4
 5
   int main( int argc, char** argv)
 6
 7
8
      char sim_log[] = "Sim_log.log";
      \operatorname{std}::\operatorname{cout}<<\operatorname{"START"}<<\operatorname{std}::\operatorname{endl};
9
      GMD::sim_start(sim_log, argc, argv);
10
11
      test0();
12
13
      test1();
14
      test2();
15
      test3();
16
      test4();
17
      test5();
18
      test6();
      test7();
19
20
      test8();
21
      test9();
22
      test10();
23
      test11();
24
      test12();
25
26
      GMD:: sim_end();
      std::cout << "END" << std::endl;
27
28
      return 0;
29
```

## A.2 GeoMod\_Tests.hpp

```
#ifndef GEOMOD_TESTS_HPP
#define GEOMOD_TESTS_HPP
#include "GeoMod.hpp"
```

```
5
6
7
   void test0();
8
   void test1();
9
   void test2();
   void test3();
10
   void test4();
11
  void test5();
   void test6();
13
14
  void test7();
   void test8();
15
16
  void test9();
   void test10();
17
   void test11();
18
19
   void test12();
20
21
  #endif
```

## A.3 GeoMod\_Tests.cpp

```
#include "GeoMod_Tests.hpp"
 2 #include <string>
3
4
   using std::cout;
5
6
   /* test0():
7
           - Create a 3D model
           - Create a gmd object
8
9
           - \ Test \ printing \ features
10
           - Implicitly destory the gmd object
11
    */
   void test0()
12
13
     pGModel cube = GMD::create_cube( 10.0);
14
     GMD::gmd_t gmd( cube);
15
     gmd.test_printers();
16
17
     cout \ll " \n\parbox{nPassed\_test} 0 \n\n" ;
18
19
     return;
20 | }
```

```
21
   /*
22
      test1():
23
          - Create 2D model
          - Create gmd_{-}t instance with model
24
25
          - Write model
          - Create mesh from model
26
27
          - Write mesh
28
    */
29
   void test1()
30
     pGModel rectangle = GMD::create_2D_rectangle(5.0, 7.0) \leftarrow
31
     GMD::gmd_t gmd( rectangle);
32
33
34
     std::string name = "test1_rectangle";
35
     gmd.set_name( name);
36
     gmd.write_model();
37
     gmd.set_global_mesh_params(1, 0.9, 0.0);
38
     gmd.create_mesh();
39
     gmd.write_mesh();
40
41
     cout \ll " \n\parbox{nPassed\_test1} \n\n";
42
     return;
43
   }
44
   /* test2():
45
          - Create a 3D model
46
47
          - Create gmd_{-}t instance with model
48
          - Write model
49
          - Create mesh from model
          - Write mesh
50
51
    */
   void test2()
52
53
   {
     pGModel cube = GMD::create_cube( 10.0);
54
55
     GMD:: gmd_t gmd( cube);
     std::string name = "test2_cube";
56
     gmd.set_name( name);
57
     gmd.write_model();
58
     gmd.set_global_mesh_params(1, 0.9, 0.0);
59
```

```
60
     gmd.create_mesh();
61
     gmd.write_mesh();
62
     cout \ll " \n\parbox{nPassed\_test2} \n\n";
63
64
     return;
65
   }
66
67
   /* test3():
68
           - Create a 3D model
69
           - Place a point with defined mesh refinement in \leftarrow
       center
70
           - Write model
           - Create a mesh from model
71
72
           - Write mesh
73
    */
74
   void test3()
75
76
     pGModel cube = GMD::create_cube(5.0);
77
     GMD::gmd_t gmd( cube);
     std::string name = "test3_cube";
78
79
     gmd.set_name( name);
80
81
     gmd.set\_global\_mesh\_params(1, 0.5, 0.3);
82
     double coords [3] = \{0.0, 0.0, 0.0\};
     double refine = 0.01;
83
     double radius = 0.01;
84
85
     pGVertex vert;
86
     gmd.place_point( coords, refine, radius, vert);
87
88
     gmd.write_model();
89
     gmd.create_mesh();
90
     gmd.write_mesh();
91
92
     cout \ll " \n\passed test 3 \n\n";
93
     return;
94
  }
95
   /* test4():
96
97 | *
          - Create a 3D model
```

```
98
            - Place a point with defined mesh refinement on \leftarrow
        surface
            - Write model
99
            - Create mesh from model
100
101
            - Write mesh
102
     */
    void test4()
103
104
      pGModel cube = GMD::create_cube( 2.0);
105
106
      GMD::gmd_t gmd( cube);
      std::string name = "test4_cube";
107
108
      gmd.set_name( name);
109
110
      double coords [3] = \{1.0, 0.0, 0.0\};
111
      double refine = 0.1;
      double radius = 0.5;
112
113
      pGVertex vert;
114
      gmd.place_point( coords, refine, radius, vert);
115
116
      gmd.write_model();
      gmd.set_global_mesh_params(1, 0.9, 0.0);
117
118
      gmd.create_mesh();
119
      gmd.write_mesh();
120
      cout \ll " \n\propto nPassed test 4 \n\n";
121
122
      return;
123
    }
124
125
    /*
       test5():
126
            - Create a 3D model
            - Place a point with defined mesh refinement on an\leftarrow
127
     *
          edge
128
            - Write model
            - Create mesh from model
129
            - Write mesh
130
131
     */
    void test5()
132
133
      pGModel cube = GMD::create_cube(2.0);
134
      GMD::gmd_t gmd( cube);
135
```

```
136
      std::string name = "test5_cube";
137
      gmd.set_name( name);
138
      double coords [3] = \{1.0, 1.0, 0.0\};
139
      double refine = 0.1;
140
      double radius = 0.5;
141
142
      pGVertex vert;
143
      gmd.place_point( coords, refine, radius, vert);
144
145
      gmd.write_model();
      gmd.set_global_mesh_params(1, 0.9, 0.0);
146
147
      gmd.create_mesh();
      gmd.write_mesh();
148
149
150
      cout \ll " \n\parbox{ nPassed\_test5} \n\n";
151
      return:
152
    }
153
    /* test6():
154
155
            - Create a 3D model
            - Place a fully interior edge define by three \hookleftarrow
156
        points
            - Write model
157
            - Do not assign name so auto-nameing feature is \leftarrow
158
        checked
            - Create mesh
159
            - Write mesh
160
161
     */
162
    void test6()
163
      pGModel cube = GMD::create_cube(2.0);
164
      GMD::gmd_t gmd( cube);
165
      std::string name = "test6_cube";
166
      gmd.set_name( name);
167
168
      int order = 4;
169
170
      double p1[3] = \{0.7, 0.0, 0.0\};
171
172
      double p2[3] = \{0.0, 0.3, 0.0\};
      double p3[3] = \{0.0, 0.0, 0.0\};
173
```

```
174
      double p4[3] = \{0.0, -0.3, 0.0\};
      double p5[3] = \{-0.7, 0.0, 0.0\};
175
      std::vector<double*> points;
176
      points.push_back(p1);
177
178
      points.push_back(p2);
      points.push_back(p3);
179
180
      points.push_back(p4);
      points.push_back(p5);
181
182
183
      std::vector<double> knots;
      knots.push_back(0.0);
184
185
      knots.push_back(0.0);
      knots.push_back(0.0);
186
187
      knots.push_back(0.0);
188
      knots.push_back(0.5);
      knots.push_back(1.0);
189
190
      knots.push_back(1.0);
191
      knots.push_back(1.0);
192
      knots.push_back(1.0);
193
      std::vector<double> weights;
194
      weights.push_back(0.0);
195
196
197
      pGEdge edge;
      double refine = 0.1;
198
      gmd.place_edge( order, points, knots, weights, refine, ←
199
         edge);
200
201
      gmd.write_model();
      gmd.set_global_mesh_params(1, 0.9, 0.0);
202
203
      gmd.create_mesh();
204
      gmd.write_mesh();
205
206
      cout \ll " \n\propto nPassed test 6 \n\n";
207
      return;
208
    }
209
210
    /* test7():
           - Create a 3D model
211
```

```
212
           - Create one spline based on-face edge defined by \leftarrow
        five points
           - Write model
213
           - Create mesh
214
     *
215
           - Write mesh
216
     */
217
218
    void test7()
219
      pGModel cube = GMD::create_cube( 2.0);
220
      GMD::gmd_t gmd( cube);
221
222
      std::string name = "test7_cube";
223
      gmd.set_name( name);
224
225
      int order = 4;
226
227
      double p1[3] = \{1.0, 0.0, 0.9\};
228
      double p2[3] = \{1.0, 0.6, 0.0\};
      double p3[3] = \{1.0, 0.0, -0.9\};
229
      double p4[3] = \{1.0, -0.3, 0.0\};
230
231
      double p5[3] = \{1.0, 0.0, 0.4\};
232
      std::vector<double*> points;
233
      points.push_back(p1);
234
      points.push_back(p2);
235
      points.push_back(p3);
236
      points.push_back(p4);
      points.push_back(p5);
237
238
239
      std::vector<double> knots;
240
      knots.push_back(0.0);
      knots.push_back(0.0);
241
242
      knots.push_back(0.0);
243
      knots.push_back(0.0);
      knots.push_back(0.5);
244
245
      knots.push_back(1.0);
246
      knots.push_back(1.0);
247
      knots.push_back(1.0);
      knots.push_back(1.0);
248
249
250
      std::vector<double> weights;
```

```
251
                     weights.push_back(0.0);
252
253
                    pGEdge edge;
254
                    double refine = 0.1;
                    gmd.place_edge (order, points, knots, weights, refine, ←
255
                               edge);
256
257
                    gmd.write_model();
                    gmd.set_global_mesh_params(1, 0.9, 0.0);
258
259
                    gmd.create_mesh();
260
                    gmd.write_mesh();
261
262
                    cout \ll " \n\parbox{ } n \parbox{ } n \parb
263
                    return;
264
             }
265
266
                            test8():
              /*
267
                                     - Create a 3D model
                 *
268
                                     - Create an edge from a surface point to an \leftarrow
                            interior point
269
                                     - Write model
270
                                     - Create mesh
                                     - Write mesh
271
272
                 */
273
              void test8()
274
                    pGModel cube = GMD::create_cube( 2.0);
275
276
                    GMD::gmd_t gmd( cube);
277
                    std::string name = "test8_cube";
278
                    gmd.set_name( name);
279
280
                    int order = 4;
281
282
                    double p1[3] = \{1.0, 0.0, 0.9\};
283
                    double p2[3] = \{0.1, 0.6, 0.0\};
                    double p3[3] = \{0.3, 0.0, -0.9\};
284
                    double p4[3] = \{0.0, -0.3, 0.0\};
285
286
                    double p5[3] = \{0.0, 0.0, 0.4\};
287
                    std::vector<double*> points;
288
                     points.push_back(p1);
```

```
289
      points.push_back(p2);
290
      points.push_back(p3);
      points.push_back(p4);
291
292
      points.push_back(p5);
293
294
      std::vector<double> knots;
295
      knots.push_back(0.0);
296
      knots.push_back(0.0);
297
      knots.push_back(0.0);
298
      knots.push_back(0.0);
      knots.push_back(0.5);
299
300
      knots.push_back(1.0);
      knots.push_back(1.0);
301
302
      knots.push_back(1.0);
      knots.push_back(1.0);
303
304
305
      std::vector<double> weights;
306
      weights.push_back(0.0);
307
308
      pGEdge edge;
      double refine = 0.1;
309
310
      gmd.place_edge (order, points, knots, weights, refine, ←
         edge);
311
      gmd.write_model();
312
      gmd.set_global_mesh_params(1, 0.9, 0.0);
313
314
      gmd.create_mesh();
315
      gmd.write_mesh();
316
      cout \ll " \n\parbox{nPassed\_test8} \n\n";
317
318
      return;
319
    }
320
321
       test9();
322
           - Create a 3D model
323
           - Create an edge that starts at a pre existing \leftarrow
        edge and then terminates
324
               in the region
           - Write Model
325
           - Create Mesh
326
```

```
327
           - Write Mesh
328
     */
    void test9()
329
330
      pGModel cube = GMD::create_cube( 2.0);
331
      GMD::gmd_t gmd( cube);
332
333
      std::string name = "test9_cube";
334
      gmd.set_name( name);
335
336
      int order = 4;
337
338
      double p1[3] = \{1.0, 1.0, 0.9\};
      double p2[3] = \{0.1, 0.6, 0.0\};
339
340
      double p3[3] = \{0.3, 0.0, -0.9\};
341
      double p4[3] = \{0.0, -0.3, 0.0\};
      double p5[3] = \{0.0, 0.0, 0.4\};
342
343
      std::vector<double*> points;
344
      points.push_back(p1);
345
      points.push_back(p2);
      points.push_back(p3);
346
347
      points.push_back(p4);
348
      points.push_back(p5);
349
350
      std::vector<double> knots;
351
      knots.push_back(0.0);
      knots.push_back(0.0);
352
      knots.push_back(0.0);
353
354
      knots.push_back(0.0);
355
      knots.push_back(0.5);
356
      knots.push_back(1.0);
      knots.push_back(1.0);
357
358
      knots.push_back(1.0);
359
      knots.push_back(1.0);
360
361
      std::vector<double> weights;
362
      weights.push_back(0.0);
363
      pGEdge edge;
364
      double refine = 0.1;
365
```

```
gmd.place_edge (order, points, knots, weights, refine, ←
366
         edge);
367
      gmd.write_model();
368
369
      gmd.set_global_mesh_params(1, 0.9, 0.0);
      gmd.create_mesh();
370
371
      gmd.write_mesh();
372
      cout << "\n\parbox{nPassed\_test9}\n\n";
373
374
      return;
375
    }
376
377
       test10();
           - Create a 3D model
378
           - Create a face completely internal to the region
379
           - Write Model
380
381
           - Create Mesh
382
           - Write Mesh
383
     */
384
    void test10()
385
386
      pGModel cube = GMD::create_cube( 20.0);
      GMD::gmd_t gmd( cube);
387
      std::string name = "test10_cube";
388
389
      gmd.set_name( name);
390
391
      int u_order = 3;
392
      int v_{order} = 2;
393
      int u_num = 4;
394
      int v_num = 3;
      int periodicity = 0;
395
396
      // first 'row'
397
      double p1[3] = \{-6.0, -7.0, 3.0\};
398
399
      double p2 [3]
                    = \{-2.0, -4.0, 0.0\};
                    = \{ 3.0, -3.0, 1.0 \};
400
      double p3[3]
                     = \{ 7.0, -5.0, -3.0 \};
401
      double p4[3]
      // second 'row'
402
403
      double p5[3] = \{-5.0, 0.0, -1.0\};
      double p6[3] = \{-2.0, 0.0, 3.0\};
404
```

```
405
      double p7 [3]
                   = \{ 3.0, 1.0, -7.0 \};
      double p8 [3]
                     = \{ 7.0, 0.0, 2.0 \};
406
      // third 'row'
407
      double p9[3] = \{-6.0, 4.0, 1.0\};
408
      double p10[3] = \{-2.0, 2.0, 0.0\};
409
      double p11[3] = { 3.0, 4.0, -3.0};
410
      double p12[3] = \{ 7.0, 3.0, 0.0 \};
411
412
413
      std::vector<double*> points;
414
      points.push_back(p1);
415
      points.push_back(p2);
416
      points.push_back(p3);
      points.push_back(p4);
417
      points.push_back(p5);
418
419
      points.push_back(p6);
      points.push_back(p7);
420
421
      points.push_back(p8);
422
      points.push_back(p9);
423
      points.push_back(p10);
      points.push_back(p11);
424
      points.push_back(p12);
425
426
427
      std::vector<double> u_knots;
428
      u_knots.push_back(0.0);
      u_knots.push_back(0.0);
429
430
      u_knots.push_back(0.0);
      u_knots.push_back(0.5);
431
432
      u_knots.push_back(1.0);
433
      u_knots.push_back(1.0);
434
      u_knots.push_back(1.0);
435
      std::vector<double> v_knots;
436
      v_knots.push_back(0.0);
437
438
      v_knots.push_back(0.0);
439
      v_knots.push_back(0.5);
440
      v_knots.push_back(1.0);
441
      v_knots.push_back(1.0);
442
443
      std::vector<double> weights;
      weights.push_back(0.0);
444
```

```
445
446
      pGFace face;
      double refine = 0.1;
447
      gmd.place_surface_by_spline(
448
449
           u_order, v_order, u_num, v_num, periodicity,
450
           points, u_knots, v_knots, weights,
451
           refine, face);
452
      gmd.write_model();
453
454
      gmd.set_global_mesh_params(1, 0.9, 0.0);
      gmd.create_mesh();
455
456
      gmd.write_mesh();
457
458
      cout \ll " \n\parbox{nPassed\_test10} \n\n";
459
      return;
    }
460
461
462
    /* test11();
463
            - Create a 3D model
464
            - Create a face completely internal to the region \leftarrow
         expect for one point
465
               which is on a pre-existing surface
            - Write Model
466
            - Create Mesh
467
            - Write Mesh
468
     */
469
470
    void test11()
471
      pGModel cube = GMD::create_cube( 20.0);
472
473
      GMD::gmd_t gmd( cube);
474
      std::string name = "test11_cube";
475
      gmd.set_name( name);
476
477
      int u_order = 3:
478
      int v_{order} = 2;
479
      int u_num = 4;
480
      int v_num = 3;
      int periodicity = 0;
481
482
      // first 'row'
483
                                  y
```

```
484
      double p1[3]
                     = \{-6.0, -7.0, 3.0\};
                     = \{-2.0, -4.0, 0.0\};
      double p2[3]
485
                     = \{ 3.0, -3.0, 1.0 \};
486
      double p3[3]
                     = \{ 7.0, -5.0, -3.0 \};
      double p4[3]
487
488
      // second 'row'
      double p5[3]
                     = \{-5.0, 0.0, -1.0\};
489
                     = \{-2.0, 0.0, 3.0\};
      double p6[3]
490
                     = \{ 3.0, 1.0, -7.0 \};
      double p7[3]
491
      double p8[3]
                     = \{ 7.0, 0.0, 2.0 \};
492
493
      // third 'row'
      double p9[3]
494
                     = \{-10.0, 4.0, 1.0\};
495
      double p10[3] = \{-2.0, 2.0, 0.0\};
      double p11[3] = { 3.0, 4.0, -3.0};
496
497
      double p12[3] = \{ 7.0, 3.0, 0.0 \};
498
499
      std::vector<double*> points;
500
      points.push_back(p1);
501
      points.push_back(p2);
502
      points.push_back(p3);
      points.push_back(p4);
503
      points.push_back(p5);
504
505
      points.push_back(p6);
506
      points.push_back(p7);
      points.push_back(p8);
507
508
      points.push_back(p9);
      points.push_back(p10);
509
510
      points.push_back(p11);
511
      points.push_back(p12);
512
513
      std::vector<double> u_knots;
      u_knots.push_back(0.0);
514
515
      u_knots.push_back(0.0);
      u_knots.push_back(0.0);
516
      u_knots.push_back(0.5);
517
518
      u_knots.push_back(1.0);
519
      u_knots.push_back(1.0);
520
      u_knots.push_back(1.0);
521
522
      std::vector<double> v_knots;
523
      v_{knots.push_back(0.0)};
```

```
524
      v_{knots.push_back(0.0)};
      v_knots.push_back(0.5);
525
      v_knots.push_back(1.0);
526
      v_knots.push_back(1.0);
527
528
529
      std::vector<double> weights;
530
      weights.push_back(0.0);
531
532
      pGFace face;
533
      double refine = 0.1;
      gmd.place_surface_by_spline(
534
535
          u_order, v_order, u_num, v_num, periodicity,
          points, u_knots, v_knots, weights,
536
537
          refine, face);
538
539
      gmd.write_model();
540
      gmd.set_global_mesh_params(1, 0.9, 0.0);
541
      gmd.create_mesh();
542
      gmd.write_mesh();
543
544
      cout \ll "\n\nPassed\_test11\n\n";
545
      return:
    }
546
547
       test12();
548
           - Create a 3D model
549
           - Create a face completely internal to the region \leftarrow
550
        expect for one edge
551
               which is on a pre-existing surface
           - Write Model
552
           - Create Mesh
553
           - Write Mesh
554
     *
555
     */
    void test12()
556
557
558
      pGModel cube = GMD::create_cube( 20.0);
      GMD::gmd_t gmd( cube);
559
      std::string name = "test12_cube";
560
      gmd.set_name( name);
561
562
```

```
563
      int u_order = 3;
      int v_order = 2;
564
565
      int u_num = 4;
      int v_num = 3;
566
567
      int periodicity = 0;
568
      // first 'row'
569
                                 y
                     = \{-10.0, -7.0, 3.0\};
570
      double p1[3]
      double p2[3]
                     = \{-2.0, -4.0, 0.0\};
571
                     = \{ 3.0, -3.0, 1.0 \};
572
      double p3[3]
                     = \{ 7.0, -5.0, -3.0 \};
573
      double p4[3]
574
      // second 'row'
575
      double p5[3]
                     = \{-10.0, 0.0, -1.0\};
      double p6 [3]
                     = \{-2.0, 0.0, 3.0\};
576
577
      double p7[3]
                     = \{ 3.0, 1.0, -7.0 \};
                     = \{ 7.0, 0.0, 2.0 \};
578
      double p8[3]
      // third 'row'
579
580
      double p9[3] = \{-10.0, 4.0, 1.0\};
581
      double p10[3] = \{-5.0, 2.0, 0.0\};
582
      double p11[3] = { 3.0, 4.0, -3.0};
      double p12[3] = \{ 7.0, 3.0, 0.0 \};
583
584
585
      std::vector<double*> points;
      points.push_back(p1);
586
587
      points.push_back(p2);
      points.push_back(p3);
588
589
      points.push_back(p4);
590
      points.push_back(p5);
591
      points.push_back(p6);
592
      points.push_back(p7);
      points.push_back(p8);
593
594
      points.push_back(p9);
      points.push_back(p10);
595
      points.push_back(p11);
596
597
      points.push_back(p12);
598
599
      std::vector<double> u_knots;
      u_knots.push_back(0.0);
600
601
      u_knots.push_back(0.0);
      u_knots.push_back(0.0);
602
```

```
603
      u_knots.push_back(0.5);
      u_knots.push_back(1.0);
604
      u_knots.push_back(1.0);
605
606
      u_knots.push_back(1.0);
607
      std::vector<double> v_knots;
608
      v_knots.push_back(0.0);
609
      v_knots.push_back(0.0);
610
      v_knots.push_back(0.5);
611
      v_knots.push_back(1.0);
612
      v_knots.push_back(1.0);
613
614
      std::vector<double> weights;
615
616
      weights.push_back(0.0);
617
      pGFace face;
618
      double refine = 0.1;
619
620
      gmd.place_surface_by_spline(
          u_order, v_order, u_num, v_num, periodicity,
621
          points, u_knots, v_knots, weights,
622
          refine, face);
623
624
      gmd.write_model();
625
626
      gmd.set_global_mesh_params(1, 0.9, 0.0);
      gmd.create_mesh();
627
628
      gmd.write_mesh();
629
630
      cout \ll " \n\parbox{nPassed\_test12} \n\n";
631
      return;
632
```

# A.4 GeoMod\_gmd.hpp

```
#ifndef GEOMOD_GMD_T_HPP
#define GEOMOD_GMD_T_HPP
#include <string>
#include <vector>
#include "GeoMod_printer.hpp"
#include "GeoMod_model_helper.hpp"
```

```
#include "GeoMod_mesh_helper.hpp"
9
10
   namespace GMD
   {
11
12
13
     class gmd_t
14
        public:
15
16
          // Util methods
17
          gmd_t( pGModel in_model);
18
           \operatorname{gmd}_{-t}();
19
          void set_abort_on_fail( bool abort_on_fail);
20
          void test_printers();
21
          void verify_mesh();
22
23
          // Writing methods
24
          void set_name( std::string file_name);
25
          void write_model();
26
          void write_mesh();
27
28
          // Methods to modify the geometry
29
          void place_point(
30
              double coords [3],
              double refine,
31
32
              double radius,
              pGVertex& vert);
33
34
          void place_edge(
35
              int order,
36
              std::vector<double*> points,
37
              std::vector<double> knots,
              std::vector<double> weights,
38
39
              double refine,
              pGEdge& edge);
40
          void place_surface_by_spline(
41
              int u_order,
42
43
              int v_order,
44
              int u_num,
45
              int v_num,
46
              int periodicity,
```

```
47
                // 0=none, 1=u periodic, 2=v periodic, 3=u
                    periodic
48
              std::vector<double*> points,
              std::vector < double > u_knots,
49
              std::vector<double> v_knots,
50
              std::vector<double> weights,
51
              double refine,
52
              pGFace& face);
53
54
          // Methods for only meshing
55
          void set_global_mesh_params (
56
57
              int order_in,
              double refine in,
58
              double grad_rate_in);
59
60
          void create_mesh();
61
62
       private:
63
          bool panicStatus;
          std::string name;
64
          model_helper_t* modeler;
65
          mesh_helper_t* mesher;
66
67
          void check_spline_params (
              int order,
68
              std::vector<double*> points,
69
              std::vector<double> knots,
70
              std::vector<double> weights);
71
          void check_surface_params(
72
73
              int u_order,
74
              int v_order,
75
              int u_num,
76
              int v_num,
77
              int periodicity,
              std::vector<double*> points,
78
              std::vector<double> u_knots,
79
80
              std::vector<double> v_knots,
81
              std::vector<double> weights);
82
     };
83
84
   }
85
```

#### $GeoMod\_gmd.cpp$ **A.5**

```
#include "GeoMod_gmd_t.hpp"
 2
3
  namespace GMD
4
     gmd_t::gmd_t( pGModel in_model)
5
6
 7
       panicStatus = true;
8
       modeler = new model_helper_t ( in_model);
       mesher = new mesh_helper_t (in_model);
9
10
       return;
11
     }
12
13
     gmd_t := gmd_t ()
14
       delete modeler;
15
16
       delete mesher;
       return;
17
18
     }
19
20
     void gmd_t::set_abort_on_fail( bool abort_on_fail)
21
22
       panicStatus = abort_on_fail;
23
       return;
24
     }
25
26
     void gmd_t::test_printers()
27
28
       modeler->model_print();
       mesher—>mesh_print();
29
30
       return;
31
     }
32
     void gmd_t::place_point( double coords[3], double \leftarrow
33
         refine, double radius, pGVertex& vert)
34
     {
```

```
35
       bool updateMesh = modeler→place_point( coords, vert, ←
           panicStatus);
36
       if ( updateMesh )
37
         mesher->place-point (coords, refine, radius, ←
38
             panicStatus);
39
40
41
       return;
42
43
     void gmd_t::set_name( std::string file_name)
44
45
46
       name = file_name;
47
       return;
48
     }
49
     void gmd_t::check_spline_params(
50
         int order,
51
         std::vector<double*> points,
52
         std::vector<double> knots,
53
54
         std::vector<double> weights)
55
     {
       if(order <=1)
56
       { print_error("Spline_order_too_low._Must_be_←
57
          polnomial_order_+_1.");}
       if ( (int) points.size() < order)
58
       { print_error("Spline_order_too_high_for_number_of_←
59
          given_control_points.");}
60
       if(((int)points.size()+order) != (int)knots.size())
       { print_error("Mismatch_between_knot_vector_size_and _←
61
          sum_of_order_with_control_point_size.");}
62
       for ( int i=0; i<(int) knots. size (); i++)
63
64
65
         double tmp1 = knots[i];
          if(i < ((int) knots. size() -1))
66
67
           double tmp2 = knots [i+1];
68
            if (tmp2 < tmp1)
69
```

```
70
            { print_error("Knots_must_be_in_accending_order") ←
               ;}
71
          if ( i < order && tmp1 != 0.0)
72
73
          { print_error("First_order_number_of_knots_must_be_←
             zero.");}
          if(i>((int)knots.size()-order) \&\& tmp1 != 1.0)
74
          { print_error("Last_order_number_of_knots_must_be_←
75
             one.");}
76
          if (tmp1 > 1.0 | tmp1 < 0.0)
77
78
            print_error ("Knots_must_satisfy_0.0<=k[i]<=1.0_."←
79
               );
80
81
82
83
        if ( (int) weights.size() != 1 && (int) weights.size() ←
            != (int) points.size())
        { print_error("Mismatch_between_weight_vector_size →
84
           and_number_of_points.");}
85
        return;
      }
86
87
      void gmd_t::place_edge(
88
          int order,
89
90
          std::vector<double*> points,
91
          std::vector<double> knots,
92
          std::vector<double> weights,
93
          double refine,
          pGEdge& edge)
94
95
        check_spline_params( order, points, knots, weights);
96
        modeler->place_edge( order, points, knots, weights, ←
97
           edge);
98
        if(refine > 0.0)
        { mesher->refine_edge( refine, edge);}
99
100
        return;
      }
101
102
```

```
103
      void gmd_t::write_model()
104
         modeler->write ( name);
105
         return;
106
107
      }
108
      void gmd_t::create_mesh()
109
110
         if ( modeler -> is V alid ( ) )
111
112
           mesher->create();
113
114
         else if ( (modeler->isValid ()) && !panicStatus)
115
116
117
           print_warning("Attempting_to_mesh_invalid_model.");
118
         else
119
120
           print_error("Invalid_model._No_mesh_created");
121
122
123
         return;
124
      }
125
      void gmd_t::verify_mesh()
126
127
         if (!mesher->isValid())
128
129
130
           if (panicStatus)
           { print_error("Mesh_Not_Valid.");}
131
           else if( !panicStatus)
132
           { print_warning("Mesh_Not_Valid.");}
133
134
135
         return;
      }
136
137
138
      void gmd_t::write_mesh()
139
         if (modeler->isWritten())
140
         { mesher->write( name); }
141
         else
142
```

```
{ print_error("Model_must_be_written_before_mesh."); ←
143
        return;
144
145
146
      void gmd_t::set_global_mesh_params( int order_in, ←
147
         double refine_in, double grad_rate_in)
148
      {
        mesher->set_global(order_in, refine_in, grad_rate_in←
149
150
        return;
      }
151
152
      void gmd_t::place_surface_by_spline(
153
154
          int u_order,
          int v_order,
155
          int u_num,
156
          int v_num,
157
          int periodicity,
158
          std::vector<double*> points,
159
          std::vector<double> u_knots,
160
161
          std::vector<double> v_knots,
          std::vector<double> weights,
162
          double refine,
163
          pGFace& face)
164
165
        check_surface_params(
166
             u_order, v_order, u_num, v_num, periodicity, ←
167
                points, u_knots, v_knots, weights);
168
        modeler->place_surface_by_spline(
169
170
             u\_order, v\_order, u\_num, v\_num, periodicity, \leftarrow
                points, u_knots, v_knots, weights, face);
171
172
        mesher->refine_face ( refine, face);
173
174
        return;
175
176
177
      void gmd_t::check_surface_params(
```

```
178
          int u_order,
179
          int v_order,
180
          int u_num,
181
          int v_num,
182
          int periodicity,
          std::vector<double*> points ,
183
          std::vector<double> u_knots,
184
          std::vector<double> v_knots,
185
186
          std::vector<double> weights)
187
        if ( periodicity < 0 \mid | periodicity > 4)
188
        { print_error("Bad_periodicity.");}
189
190
191
        if(u_order \ll 1)
192
        { print_error("u_order_too_low.");}
193
        if(v_order \ll 1)
        { print_error("v_order_too_low.");}
194
195
        if( (int)points.size() != (u_num*v_num))
196
        { print_error("Mismatched_number_of_declared_and _←
197
           given control points.");}
198
199
        if((int)) weights.size() != 1 && (int) weights.size() \leftarrow
           != (u_num*v_num)
        { print_error("Mismatched_number_of_weights_and _←
200
           declared_control_points.");}
201
        if((int)) weights.size() = 1 \&\& weights[0] != 0.0)
202
        { print_error("Bad_weights_vector.");}
203
204
        if((int)u_knots.size() != (u_num+u_order))
        { print_error("Mismatch_between_number_of_u_knots_and←
205
           _uorder+unum.");}
206
        for ( int i=0; i<(int)u_knots.size(); i++)
207
208
209
          double tmp1 = u_knots[i];
           if(i < ((int)u_knots.size() -1))
210
211
            double tmp2 = u_knots[i+1];
212
             if (tmp2 < tmp1)
213
```

```
{ print_error("Knots_must_be_in_accending_u_order←
214
                ");}
215
           if ( i < u_order && tmp1 != 0.0)
216
217
           { print_error("First_u_order_number_of_u_knots_must←
              _be_zero.");}
           if(i>((int)u_knots.size()-u_order) \&\& tmp1 != 1.0)
218
           { print_error("Last_u_order_number_of_u_knots_must_←
219
              be_one.");}
220
           if (tmp1 > 1.0 | tmp1 < 0.0)
221
222
             print_error ("Knots_must_satisfy_0.0<=k[i]<=1.0_."←
223
                );
224
        }
225
226
227
        if((int)v_knots.size() != (v_num+v_order))
        \{ print\_error ("Mismatch\_between\_number\_of\_v\_knots\_and \leftarrow \} \}
228
           _{\rm v_order+v_num."});}
229
230
        for(int i=0; i<(int)v_knots.size(); i++)
231
232
           double tmp1 = v_k nots[i];
233
           if (i < ((int) v_knots.size() -1))
234
             double tmp2 = v_k nots[i+1];
235
236
             if (tmp2 < tmp1)
237
             { print_error("Knots_must_be_in_accending_v_order←
                ");}
238
239
           if ( i < v_{order} \&\& tmp1 != 0.0)
240
           { print_error("First_v_order_number_of_v_knots_must←
              _be_zero.");}
241
           if(i>((int)v_knots.size()-v_order) \&\& tmp1 != 1.0)
242
           { print_error("Last_v_order_number_of_v_knots_must_←
              be_one.");}
243
           if ( tmp1 > 1.0 \mid | tmp1 < 0.0)
244
245
```

```
246 | print_error("Knots_must_satisfy_0.0<=k[i]<=1.0_.." \( ) \);
247 | }
248 | }
249 |
250 | return;
251 | }
252 | }
```

## A.6 GeoMod\_model\_helper.hpp

```
#ifndef GEOMOD_MODEL_HELPER_HPP
2 #define GEOMOD_MODEL_HELPER_HPP
3
  #include <string>
  #include <vector>
6 #include "GeoMod_SIM.hpp"
  #include "GeoMod_printer.hpp"
  #include "GeoMod_coords.hpp"
8
9
  pGVertex GIP_insertVertexInFace(pGIPart part, double* xyz←
10
      , pGFace face);
11
12
   namespace GMD
13
14
     class model_helper_t
15
       friend class gmd_t;
16
       private:
17
         // Util methods
18
         model_helper_t (pGModel& in_model);
19
20
         ~model_helper_t();
         void model_print();
21
22
         void write( std::string name);
         bool isValid();
23
24
         bool is Written ();
25
         void unpack_vector_spline_points(
             std::vector<double*> vec,
26
             double* x);
27
```

```
28
         void unpack_vector ( std::vector < double > vec, double ←
             * x);
29
         void unpack_surface_vector(
              std::vector<double*> points,
30
              double * all_points);
31
         void create_bounding_edges(
32
              int u_order,
33
              int v_order,
34
35
              int u_num,
36
              int v_num,
37
              std::vector<double*> points,
              std::vector<double> u_knots,
38
39
              std::vector<double> v_knots,
              std::vector<double> weights,
40
41
              std::vector<pGEdge>& edges);
42
         void unpack_bounding_edges (
              std::vector<pGEdge>& edges,
43
44
              pGEdge* bounding_edges);
45
         // Members
46
         pGModel model;
47
48
         pGIPart part;
49
         bool Written;
50
51
         // Methods to place a point
         bool place_point (
52
              double coords [3],
53
              pGVertex& vert,
54
55
              bool abort_on_fail);
         bool point_on_dim ( int dim, double coords [3]);
56
         int point_location( double coords[3]);
57
         bool PointOnFace( double coords[3], pGFace face);
58
         bool PointOnEdge( double coords[3], pGEdge edge);
59
         void put_point_outside ( double coords [3], pGVertex&←
60
              vert);
61
         void put_point_in_line ( double coords [3], pGVertex&←
              vert);
         void put_point_in_face ( double coords [3], pGVertex&←
62
              vert);
```

```
63
          void put_point_in_region ( double coords [3], \leftarrow
              pGVertex& vert);
64
          // Methods to place an edge
65
          void place_edge(
66
               int order,
67
               std::vector<double*> points,
68
               std::vector<double> knots,
69
               std::vector<double> weights,
70
               pGEdge& edge);
71
          void create_curve (
72
73
               int order,
74
               std::vector<double*> points,
               std::vector<double> knots,
75
76
               std::vector<double> weights,
77
               pCurve& curve);
          void create_edge(
78
79
               int order,
               std::vector<double*> points,
80
               pCurve& curve,
81
82
               pGEdge& edge);
83
          bool PointsOnSameFace( std::vector<double*> points)←
84
          // Methods to place a surface
85
          void place_surface_by_spline(
86
87
               int u_order,
               int v_order,
88
89
               int u_num,
90
               int v_num,
               int periodicity,
91
92
               std::vector<double*> points,
               std::vector<double> u_knots,
93
               std::vector<double> v_knots,
94
               std::vector<double> weights,
95
96
               pGFace& face);
97
          void create_surface (
               int u_order,
98
99
               int v_order,
100
               int u_num,
```

```
101
               int v_num,
               int periodicity,
102
               std::vector<double*> points,
103
               std::vector<double> u_knots,
104
               std::vector<double> v_knots,
105
               std::vector<double> weights,
106
               pSurface& surface,
107
108
               std::vector<pGEdge>& edges);
           void create_face(
109
               pSurface& surface,
110
               std::vector<pGEdge>& edges,
111
112
               pGFace& face);
113
114
      };
115
116
    }
117
118
   #endif
```

### A.7 GeoMod\_model\_helper.cpp

```
#include "GeoMod_model_helper.hpp"
3
   namespace GMD
4
5
     model_helper_t :: model_helper_t ( pGModel& in_model)
6
     {
 7
       model = in\_model;
       Written = false;
8
       if (!isValid())
9
10
          print_warning ("Created_gmd_object_on_invalid_model. ←
11
             ");
12
       part = GM_part( model);
13
       if( part == NULL)
14
15
          print_error ("GeoMod_does_not_support_assembly _←
16
             models.");
17
       }
```

```
18
       return;
19
20
     model_helper_t: ~ model_helper_t()
21
22
23
        GM_release ( model);
24
       return;
25
     }
26
27
     void model_helper_t :: model_print()
28
        std::cout << "Modeler_says_hello!" << std::endl;
29
30
       return;
     }
31
32
     bool model_helper_t :: isValid()
33
34
35
        if(GM_isValid(model, 1, NULL) = 1)
        { return true; }
36
37
        else
        { return false; }
38
39
40
     void model_helper_t :: write( std :: string name)
41
42
       name = name + ".smd";
43
       const char* name_c = name.c_str();
44
        if( !isValid())
45
        { print_warning ("Attempting_to_write_invalid_model.") ←
46
           ; }
47
        std::cout << "MODEL_INFORMATION:_"
48
         << "\nVertices:"<< GM_numVertices(model)</pre>
49
         << "\nEdges: _"<< GM_numEdges(model)</pre>
50
         << "\nFaces: _"<< GM_numFaces(model)</pre>
51
         << "\nRegions: _"<< GM_numRegions(model) << std::←</pre>
52
             endl;
53
       int writestat = GM_write(model, name_c, 0,0);
54
        if(writestat == 0)
55
```

```
56
          std::cout << "Model_" << name << "_written." << std←
57
             :: endl;
          Written = true;
58
       }
59
60
       else
61
          std::cout << "Model_" << name
62
            << "_failed_to_be_written." << std::endl;</pre>
63
64
65
66
       return;
67
68
69
     bool model_helper_t::point_on_dim( int dim, double ←
        coords [3])
70
       double tol = GM_tolerance( model);
71
72
       bool answer = false;
73
       bool areSame = false;
       double closest [] = \{0.0, 0.0, 0.0\};
74
75
        if (dim == 1)
76
          GEIter e_it = GM_edgeIter( model);
77
78
          pGEdge e;
79
          while ((e = GEIter_next(e_it)))
80
81
            GE_closestPoint(e, coords, closest, NULL);
82
            compare_coords(coords, closest, areSame, tol);
83
            if (areSame)
84
85
              answer = true;
86
87
          GEIter_delete( e_it);
88
89
90
       else if (\dim = 2)
91
92
          GFIter f_it = GM_faceIter(model);
          pGFace f;
93
```

```
while ((f = GFIter_next(f_it)))
94
 95
             GF_closestPoint(f, coords, closest, NULL);
 96
             compare_coords (coords, closest, areSame, tol);
97
             if (areSame)
98
99
100
               answer = true;
101
102
           GFIter_delete( f_it);
103
104
105
         else if (\dim = 3)
106
           print\_warning ("point\_on\_dim\_does\_not\_support\_this\_ \leftarrow
107
              dimension");
108
109
         return answer;
110
111
      int model_helper_t::point_location(double coords[3])
112
113
114
         int answer = 0;
115
         // Want to find classification on lowest gEnt dim
         // start from top work down, overwrite old answer
116
         for (int i=3; i>0; i--)
117
118
           if (i < 3)
119
120
121
             if (point_on_dim(i, coords))
122
123
               answer = i;
124
125
           else
126
127
             GRIter r_it = GM_regionIter(model);
128
             pGRegion region;
129
             while(( region= GRIter_next(r_it)))
130
131
             {
               if (GR_containsPoint (region, coords) == 0)
132
```

```
133
               { // Point is in the void region (spooky!)
134
                 return 0;
135
               else if (GR_containsPoint( region, coords) ==1)
136
137
138
                 answer = 3;
139
               else
140
141
               { print_error("Point_placement_not_possible.") ←
                  ; }
142
143
             GRIter_delete( r_it);
           }
144
145
146
        return answer;
147
148
149
      bool model_helper_t :: PointOnFace( double coords [3], ←
         pGFace face)
150
        double tol = GM_tolerance( model);
151
152
        bool ans = false;
        double cp [] = \{0.0, 0.0, 0.0\};
153
        GF_closestPoint( face, coords, cp, NULL);
154
155
        compare_coords (coords, cp, ans, tol);
156
        return ans;
      }
157
158
159
      bool model_helper_t :: PointOnEdge( double coords [3], ←
         pGEdge edge)
160
        double tol = GM_tolerance( model);
161
        bool ans = false;
162
        double cp [] = \{0.0, 0.0, 0.0\};
163
        double para [] = \{0.0, 0.0, 0.0\};
164
165
        GE_closestPoint( edge, coords, cp, para);
166
        compare_coords (coords, cp, ans, tol);
167
168
        return ans;
169
```

```
170
171
      void model_helper_t::put_point_outside( double coords←
         [3], pGVertex& vert)
172
        pGRegion out_region = GIP_outerRegion( part);
173
        vert = GIP_insertVertexInRegion( part, coords, ←
174
           out_region);
175
        return;
      }
176
177
      void model_helper_t::put_point_in_line( double coords←
178
         [3], pGVertex& vert)
179
        bool placed = false;
180
181
        GEIter e_it = GM_edgeIter( model);
        pGEdge edge;
182
        while (!placed && (edge = GEIter_next(e_it)))
183
184
           if (PointOnEdge(coords, edge))
185
186
187
             double param = 0.0;
188
             GE_closestPoint( edge, coords, NULL, &param);
189
             vert = GM_splitEdge( edge, param);
             if(vert == NULL)
190
191
             {
192
               pPList vert_list = PList_new();
               vert_list = GE_vertices( edge);
193
               pGVertex tmp_vert;
194
195
               \mathbf{void} * iter = 0;
               bool found = false;
196
               while ((!found) && ( tmp_vert = (pGVertex) ←
197
                  PList_next( vert_list, &iter)))
               {
198
                 bool areSame = false;
199
                 double tol = GM_tolerance( model);
200
201
                 double conf_coords[3] = \{0.0\};
202
                 GV_point( tmp_vert, conf_coords);
                 compare_coords ( coords , conf_coords , areSame , ←
203
                     tol);
                 if( areSame)
204
```

```
205
                 {
206
                    found = true;
207
                    vert = tmp_vert;
208
209
               PList_delete ( vert_list);
210
211
212
             placed = true;
           }
213
214
        GEIter_delete( e_it);
215
216
217
        if (!placed)
218
219
           print_warning("Failed_to_place_point_on_edge_at");
220
           print_coords ( coords);
221
        }
222
        return;
      }
223
224
225
      void model_helper_t::put_point_in_face( double coords←
          [3], pGVertex& vert)
226
227
        bool placed = false;
        GFIter f_it = GM_faceIter( model);
228
229
        pGFace face;
        while (!placed && (face = GFIter_next( f_it)))
230
231
           if (PointOnFace(coords, face))
232
233
234
             vert = GIP_insertVertexInFace( part, coords, face ←
235
             placed = true;
           }
236
237
238
        GFIter_delete(f_it);
239
        if( !placed)
240
241
           print_warning("Failed_to_place_point_in_face_at");
242
```

```
243
           print_coords( coords);
244
245
246
        return;
      }
247
248
249
      void model_helper_t :: put_point_in_region (
250
           double coords [3],
           pGVertex& vert)
251
252
        bool placed = false;
253
254
        GRIter r_it = GM_regionIter( model);
255
        pGRegion region;
256
        while (!placed && (region= GRIter_next(r_it)))
257
           if (GR_containsPoint( region, coords) ==1)
258
259
260
             vert = GIP_insertVertexInRegion( part, coords, ←
                region);
261
             placed = true;
262
263
         GRIter_delete( r_it);
264
265
        return;
266
      }
267
268
      bool model_helper_t :: place_point (
269
           double coords[3],
270
           pGVertex& vert,
           bool abort_on_fail)
271
272
273
        bool updateMesh = true;
        int location = point_location(coords);
274
        if(location = 0)
275
276
           print_warning("Point_outside_of_known_regions.");
277
278
           updateMesh = false;
           put_point_outside( coords, vert);
279
280
        else if (location = 1)
281
```

```
282
283
           put_point_in_line( coords, vert);
284
         else if (location = 2)
285
286
287
           put_point_in_face( coords, vert);
288
         else if (location == 3)
289
290
           put_point_in_region( coords, vert);
291
292
293
         (void) abort_on_fail;
294
        return updateMesh;
295
      }
296
297
      void model_helper_t :: unpack_vector_spline_points(
298
           std::vector<double*> vec,
299
           double* x)
300
        int pos = 0;
301
        double* tmp = vec[0];
302
303
        for (int i=0; i<(int) vec. size(); i++)
304
           tmp = vec[i];
305
306
           for ( int j=0; j < 3; j++)
307
308
             pos = j+3*i;
309
             x[pos] = tmp[j];
310
311
312
        return;
313
314
315
      void model_helper_t::unpack_vector( std::vector < double> ←
          vec, double* x)
316
        for (int i=0; i<(int) vec. size(); i++)
317
318
           x[i] = vec[i];
319
320
```

```
321
        return;
322
323
      void model_helper_t :: create_curve(
324
325
          int order,
          std::vector<double*> points,
326
          std::vector<double> knots,
327
          std::vector<double> weights,
328
          pCurve& curve)
329
330
        int num_points = (int) points.size();
331
332
        bool weightLess = false;
        if((int) weights.size() = 1 \&\& weights[0] = 0.0)
333
        { weightLess = true;}
334
335
        double u_points[num_points*3] = \{0.0\};
336
337
        double u_k nots[(int)knots.size()] = \{0.0\};
        double un_weights [(int) weights.size()] = \{0.0\};
338
        unpack_vector_spline_points( points, u_points);
339
        unpack_vector(knots, u_knots);
340
341
342
        if (weightLess)
343
          curve = SCurve_createBSpline(
344
345
             order, num_points, u_points, u_knots, NULL);
346
        else
347
348
349
          unpack_vector( weights, un_weights);
350
          curve = SCurve_createBSpline(
             order, num_points, u_points, u_knots, un_weights) ←
351
        }
352
353
        return;
354
      }
355
      bool model_helper_t :: PointsOnSameFace( std :: vector <←
356
         double*> points)
357
        bool on Face = true;
358
```

```
359
         for ( int i=0; i<(int) points. size (); i++)
360
         { // Check if all points are on any face
361
           if (!point_on_dim(2, points[i]))
362
363
             onFace = false;
364
365
366
         if( onFace)
367
368
           bool answer = false;
369
370
           pGFace face;
           pGFace conFace;
371
           GFIter f_it = GM_faceIter( model);
372
373
           while (( face = GFIter_next(f_it)))
374
375
             for(int i=0; i<(int) points.size(); i++)
376
                if( (i==0) && PointOnFace( points[i], face))
377
378
379
                  conFace = face;
380
                else if( PointOnFace( points[i], face))
381
382
                  if( face == conFace)
383
                  \{ answer = true; \}
384
385
                  else
386
                  \{ answer = false; \}
387
             }
388
389
390
           GFIter_delete(f_it);
391
           return answer;
         }
392
393
         else
394
395
           return false;
396
397
      }
398
```

```
399
      void model_helper_t :: create_edge (
400
          int order,
401
          std::vector<double*> points,
          pCurve& curve,
402
          pGEdge& edge)
403
404
        double* start_point = points[0];
405
        pGVertex start_vert = NULL;
406
        if( start_point == NULL)
407
        { print_error("_start_point_is_NULL_");}
408
        place_point( start_point, start_vert, false);
409
410
        double* end_point = points[(int)points.size()-1];
411
        pGVertex end_vert = NULL;
412
413
        place_point( end_point, end_vert, false);
414
        // Assumes a one region, one part model
415
        pGIPart part = GM_part( model);
416
        GRIter r_it = GM_regionIter(model);
417
        pGRegion region = GRIter_next( r_it);
418
419
420
        if( part == NULL)
        { print_error("Part_is_NULL");}
421
422
        if( start_vert == NULL)
        { print_error("start_vert_is_NULL");}
423
        if( end_vert == NULL)
424
        { print_error("end_vert_is_NULL");}
425
426
        if( curve == NULL)
        { print_error("curve_is_NULL");}
427
428
        if( region == NULL)
        { print_error("region_is_NULL");}
429
430
431
        edge = GIP_insertEdgeInRegion(
             part, start_vert, end_vert, curve, 1, region);
432
        GRIter_delete( r_it);
433
434
435
        bool onSameFace = PointsOnSameFace( points);
436
        if (onSameFace)
437
438
          pGFace face;
```

```
439
           GFIter f_it = GM_faceIter( model);
           bool found = false;
440
           while (!found && (face = GFIter_next(f_it)))
441
442
             if(PointOnFace(points[0], face))
443
             \{ \text{ found } = \text{true}; \}
444
445
446
           GFIter_delete(f_it);
           pGFace new_faces[2] = {NULL, NULL};
447
           GM_insertEdgeOnFace( face, edge, new_faces);
448
         }
449
450
451
         (void) order;
        return;
452
453
      }
454
      void model_helper_t :: place_edge(
455
456
           int order,
           std::vector<double*> points,
457
           std::vector<double> knots,
458
           std::vector<double> weights,
459
460
           pGEdge& edge)
461
        pCurve curve;
462
         create_curve( order, points, knots, weights, curve);
463
         create_edge( order, points, curve, edge);
464
        return;
465
466
      }
467
      void model_helper_t :: place_surface_by_spline(
468
469
           int u_order,
470
           int v_order,
471
           int u_num,
472
           int v_num,
           int periodicity,
473
474
           std::vector<double*> points,
475
           std::vector<double> u_knots,
           std::vector<double> v_knots,
476
477
           std::vector<double> weights,
           pGFace& face)
478
```

```
479
480
        pSurface surf;
        std::vector<pGEdge> edges;
481
482
483
        create_surface (
484
             u_order, v_order, u_num, v_num, periodicity,
485
             points, u_knots, v_knots, weights, surf, edges);
486
         create_face( surf, edges, face);
        return:
487
      }
488
489
490
      void model_helper_t::unpack_bounding_edges(
           std::vector<pGEdge>& edges,
491
492
          pGEdge* bounding_edges)
493
        for ( int i=0; i<(int) edges.size(); i++)
494
495
496
           bounding_edges[i] = edges[i];
497
498
        return;
499
500
      void model_helper_t :: create_face(
501
502
           pSurface& surface,
           std::vector<pGEdge>& edges,
503
           pGFace& face)
504
      {
505
506
507
        pGIPart part = GM_part( model);
        int numEdges = (int)edges.size();
508
        pGEdge bounding_edges[numEdges] = {NULL};
509
        unpack_bounding_edges ( edges, bounding_edges);
510
        int dirs[numEdges] = \{0\};
511
        for ( int i = 0; i < numEdges; i++)
512
513
514
           dirs[i] = 1;
515
        int numLoops = 1;
516
        int indLoop[numLoops] = \{0\};
517
        for ( int i = 0; i < numLoops; i++)
518
```

```
519
          indLoop[i] = 0;
520
521
        int normal = 1;
522
523
        GRIter r_it = GM_regionIter(model);
524
525
        pGRegion region = GRIter_next( r_it);
526
527
        face = GIP_insertFaceInRegion(
528
             part, numEdges, bounding_edges, dirs,
529
             numLoops, indLoop, surface, normal, region);
530
531
        GRIter_delete( r_it);
532
        return;
533
      }
534
535
      void model_helper_t::create_bounding_edges(
           int u_order,
536
           int v_order,
537
           int u_num,
538
539
           int v_num,
540
           std::vector<double*> points,
541
           std::vector<double> u_knots,
           std::vector<double> v_knots,
542
543
           std::vector<double> weights,
           std::vector<pGEdge>& edges)
544
545
        // Since GeomSim needs splines surface to be four \leftarrow
546
547
        // and have a regular control point spacing (X \ by \ Y),
        // the edges need can be infered from the surface \leftarrow
548
            points
549
550
        int N = u_num:
        int M = v_num;
551
552
        pGEdge tmp_edge0;
        bool weightLess = false;
553
        if((int)) weights. size() = 1 && weights[0] = 0.0)
554
        { weightLess = true;}
555
556
```

```
557
        std::vector<double*> edge_points;
558
        std::vector<double> edge_weights;
559
        for(int n = 0; n < N; n++)
560
           edge_points.push_back( points[n] );
561
           if (!weightLess)
562
563
564
             edge_weights.push_back( weights[n]);
           }
565
        }
566
567
568
        if (weightLess)
569
570
           edge_weights.push_back(0.0);
571
        place_edge( u_order, edge_points, u_knots, ←
572
            edge_weights, tmp_edge0);
573
        edges.push_back(tmp_edge0);
574
        edge_points.clear();
575
576
        pGEdge tmp_edge1;
577
        for ( int m=0; m<M; m++)
578
           int ind = (N-1)+m*N;
579
           edge_points.push_back( points[ind] );
580
           if (!weightLess)
581
582
583
             edge_weights.push_back( weights[ind]);
584
           }
        }
585
586
587
        place_edge (v_order, edge_points, v_knots, ←
            edge_weights, tmp_edge1);
588
        edges.push_back(tmp_edge1);
589
        edge_points.clear();
590
591
592
        pGEdge tmp_edge2;
593
        for ( int n=(N-1); n>(-1); n--)
594
```

```
595
           int ind = n+(M-1)*N;
596
           edge_points.push_back( points[ind]);
           if (!weightLess)
597
598
599
             edge_weights.push_back( weights[ind]);
           }
600
601
        }
602
        place_edge( u_order, edge_points, u_knots, ←
603
           edge_weights, tmp_edge2);
604
        edges.push_back(tmp_edge2);
605
        edge_points.clear();
606
607
        pGEdge tmp_edge3;
608
        for ( int m=(M-1); m>(-1); m=-)
609
610
           int ind = N*m;
           edge_points.push_back( points[ind]);
611
612
           if (!weightLess)
613
             edge_weights.push_back( weights[ind]);
614
615
        }
616
617
        place_edge ( v_order, edge_points, v_knots, ←
618
            edge_weights, tmp_edge3);
        edges.push_back(tmp_edge3);
619
620
621
        edge_points.clear();
        edge_weights.clear();
622
623
624
        return;
      }
625
626
627
      void model_helper_t :: create_surface(
628
           int u_order,
629
           int v_order,
630
           int u_num,
631
           int v_num,
632
           int periodicity,
```

```
633
          std::vector<double*> points,
634
          std::vector<double> u_knots,
          std::vector<double> v_knots,
635
          std::vector<double> weights,
636
          pSurface& surface,
637
          std::vector<pGEdge>& edges)
638
639
        int u_per = 0;
640
        int v_per = 0;
641
642
        if (periodicity == 0)
        { // No chages from default
643
644
        else if (periodicity = 1)
645
646
647
          u_per = 1;
648
        else if (periodicity = 2)
649
650
651
           v_{per} = 1;
652
        else if (periodicity = 3)
653
654
655
           u_per = 1;
656
           v_per = 1;
        }
657
658
        bool weightLess = false;
659
660
        if((int) weights.size() = 1 \&\& weights[0] = 0.0)
661
        { weightLess = true;}
662
        int num_points = (int) points.size();
663
664
        double unp_u_knots [(int)u_knots.size()] = \{0.0\};
665
        unpack_vector( u_knots, unp_u_knots);
666
667
668
        double unp_v_knots [(int)v_knots.size()] = \{0.0\};
669
        unpack_vector(v_knots, unp_v_knots);
670
        double all_points [3*num_points] = \{0.0\};
671
        unpack_vector_spline_points ( points , all_points);
672
```

```
673
674
        create_bounding_edges(
675
             u_order, v_order, u_num, v_num,
             points, u_knots, v_knots, weights, edges);
676
677
        if (weightLess)
678
679
680
           surface = SSurface_createBSpline(
               u_order, v_order,
681
682
               u_num, v_num,
683
               u_per, v_per,
684
               all_points, NULL,
               unp_u_knots, unp_v_knots);
685
686
687
        else
688
689
           double unp_weights [num_points] = \{0.0\};
690
           unpack_vector( weights, unp_weights);
691
           surface = SSurface_createBSpline(
692
               u_order, v_order,
693
               u_num,
                         v_num,
694
               u_per,
                         v_per,
695
               all_points, unp_weights,
696
               unp_u_knots, unp_v_knots);
697
698
        return;
699
700
701
      bool model_helper_t :: isWritten()
      { return Written;}
702
    }
703
```

# A.8 GeoMod\_mesh\_helper.hpp

```
#ifndef GEOMOD_MESH_HELPER_HPP
#define GEOMOD_MESH_HELPER_HPP

#include <string>
#include <vector>
#include "GeoMod_SIM.hpp"
```

```
7 |#include "GeoMod_printer.hpp"
8
9
   namespace GMD
10
11
     class mesh_helper_t
12
13
       friend class gmd_t;
       private:
14
15
          // Util methods
16
          mesh_helper_t ( pGModel in_model);
17
          ~mesh_helper_t();
18
          void mesh_print();
          void write( std::string name);
19
20
          bool is Valid();
21
          void create();
22
         // Members
23
24
          pMesh mesh;
25
          pACase m_case;
26
          bool globalSet;
27
          double order;
28
          double refine;
29
          double grad_rate;
30
31
          // Mesh preping methods
32
          void place_point(
33
              double coords [3],
34
              double refine,
35
              double radius,
36
              bool abort_on_fail);
          void set_global (int order_in, double refine_in, ←
37
             double grad_rate_in);
          void refine_vertex( double refine, pGVertex vert);
38
          void refine_edge( double refine, pGEdge edge);
39
         void refine_face( double refine, pGFace face);
40
41
42
     };
43
44
   }
45
```

### $GeoMod\_mesh\_helper.cpp$ A.9

```
#include "GeoMod_mesh_helper.hpp"
3
   namespace GMD
4
     mesh_helper_t::mesh_helper_t(pGModelin_model)
5
6
7
       mesh = M_new(0, in_model);
       m_case = MS_newMeshCase( in_model);
8
9
       globalSet = false;
10
11
       return;
12
     }
13
     mesh_helper_t::~mesh_helper_t()
14
15
16
       MS_deleteMeshCase (m_case);
       M_release ( mesh);
17
18
       return;
19
20
21
     void mesh_helper_t :: mesh_print()
22
       std::cout << "Mesher_says_hello!" << std::endl;
23
24
       return;
25
     }
26
     bool mesh_helper_t :: isValid()
27
28
     { // Only validates serial meshes for now
29
       bool ans = false;
       pGModel model = M_model(mesh);
30
       pPList mesh_list = PList_new();
31
       PList_append( mesh_list, mesh);
32
33
       pParMesh par_mesh = PM_createFromMesh(
           model,
34
35
            M_representation (mesh),
36
            mesh_list, NULL, NULL, NULL);
```

```
37
38
       int status = PM_verify(par_mesh, 0, NULL);
39
       if (status == 1)
       \{ ans = true; \}
40
41
42
       M_release (par_mesh);
       PList_delete ( mesh_list);
43
       return ans;
44
45
     }
46
47
     void mesh_helper_t :: create()
48
49
       if (!globalSet)
       { print_error("Global_Mesh_Parameters_not_set.");}
50
51
       pModelItem domain = GM_domain( M_model(mesh));
       MS_setMeshSize(m_case, domain, 2, refine, NULL);
52
53
54
       if(grad_rate > 0.0)
       { MS_setGlobalSizeGradationRate(m_case, grad_rate); }
55
56
       if(order = 2)
57
58
       { MS_setMeshOrder(m_case, order);}
59
       pSurfaceMesher surf = SurfaceMesher_new(m_case, mesh) ←
60
       SurfaceMesher_execute( surf, NULL);
61
62
       SurfaceMesher_delete(surf);
63
64
       pVolumeMesher_vol = VolumeMesher_new( m_case, mesh);
65
       VolumeMesher_execute( vol, NULL);
       VolumeMesher_delete(vol);
66
67
68
       return;
     }
69
70
71
     void mesh_helper_t :: write( std :: string name)
72
       std::string tmp_name = name + ".sms";
73
74
       const char* name_c = tmp_name.c_str();
       if( !isValid())
75
```

```
76
        { print_warning ("Attempting_to_write_invalid_mesh.") ←
           ;}
77
        std::cout << "MESH_INFORMATION:_"
78
          << "\nVertices:"<< M_numVertices(mesh)</pre>
79
          << "\nEdges: _"<< M_numEdges(mesh)</pre>
80
          << "\nFaces: _"<< M_numFaces(mesh)</pre>
81
          << "\nRegions: \_"<< M_numRegions(mesh) << std::endl;</pre>
82
83
84
        int writestat = M_write(mesh, name_c, 0,0);
85
         if(writestat == 0)
86
           std::cout << "Mesh_" << name << "_written." << std←
87
              :: endl;
88
        }
89
        else
         { std::cout << "Mesh_" << name << "_failed_to_be_←
90
            written." << std::endl; }</pre>
91
        return;
      }
92
93
94
      void mesh_helper_t::refine_vertex( double refine, ←
         pGVertex vert)
95
        MS_setMeshSize(m_case, vert, 2, refine, NULL);
96
97
        return;
98
      }
99
100
      void mesh_helper_t :: place_point(
101
           double coords [3],
           double refine,
102
           double radius,
103
           bool abort_on_fail)
104
105
        if (refine > 0.0)
106
107
           if (radius = 0.0)
108
109
             MS_addPointRefinement ( m_case, refine, coords);
110
111
```

```
112
           else if (radius > 0.0)
113
             MS_addSphereRefinement( m_case, refine, radius, ←
114
                coords);
115
          else if(abort_on_fail)
116
117
             print_error ( "Refinement_radius_must_be_zero_or _ ←
118
                greater");
119
          else
120
121
             print_warning ( "Refinement_radius_must_be_zero_or ←
122
                _greater");
123
124
125
        return;
126
127
128
      void mesh_helper_t::set_global(int order_in, double ←
         refine_in, double grad_rate_in)
129
        globalSet = true;
130
        order = order_in;
131
132
        refine = refine_in;
        grad_rate = grad_rate_in;
133
        return;
134
135
      }
136
      void mesh_helper_t::refine_edge( double refine, pGEdge ←
137
         edge)
138
        MS_setMeshSize(m_case, edge, 2, refine, NULL);
139
140
        return;
141
      }
142
143
      void mesh_helper_t::refine_face( double refine, pGFace ←
         face)
144
      {
        MS_setMeshSize(m_case, face, 2, refine, NULL);
145
```

```
146 | return;
147 | }
148 |}
```

## A.10 GeoMod\_printer.hpp

```
#ifndef GEOMOD_PRINTER_HPP
  #define GEOMOD_PRINTER_HPP
3
  #include <cstdlib>
4
  #include <iostream>
  #include <string.h>
8
   namespace GMD
9
10
     void print_error ( std::string message, bool ←
        abort_on_fail=true);
11
     void print_warning( std::string message);
12
13
     void print_coords( double x[3]);
14
15
16 #endif
```

### A.11 GeoMod\_printer.cpp

```
#include "GeoMod_printer.hpp"
3 #include <cstdlib>
  #include <iostream>
  #include < string.h>
6
7
   namespace GMD
8
9
     void print_error ( std::string message, bool ←
        abort_on_fail)
10
       std::cout << "Error:" << message << std::endl;
11
12
       if( abort_on_fail)
```

```
13
14
          std::abort();
15
16
       return;
17
     }
18
     void print_warning( std::string message)
19
20
       std::cout << "Warning:" << message << std::endl;
21
22
       return;
     }
23
24
25
     void print_coords ( double x[3])
26
27
       std::cout << "(";
       for (int i=0; i < 3; i++)
28
29
          std::cout << x[i] << ", ";
30
31
        std::cout << "b)\n";
32
33
       return;
34
35
```

#### A.12 GeoMod\_coords.hpp

```
#ifndef GEOMOD_COORDS_HPP
  #define GEOMOD_COORDS_HPP
3
4
   namespace GMD
5
     void sum_coords(double x[3], double y[3], double ans\leftarrow
6
         [3]);
     void subtract_coords ( double fin [3], double intil [3], \leftarrow
        double ans [3]);
9
     void divide ( double vec [3], double denom, double ans←
10
         [3]);
11
```

```
12
     void get_mag(double vec[3], double& mag);
13
     void get_unit_vector( double vec[3], double unit[3]);
14
15
     void cross_product ( double x[3], double y[3], double \leftarrow
16
         ans [3]);
17
18
     void dot_product( double x[3], double y[3], double& ans\leftarrow
         );
19
     void compare_coords ( double x[3], double y[3], bool& \leftarrow
20
         areSame, double tol = 0.0);
21
22
23
  #endif
```

#### A.13 GeoMod\_coords.cpp

```
1 #include "GeoMod_coords.hpp"
  #include "GeoMod_printer.hpp"
3 #include <cstdlib>
  #include <math.h>
   namespace GMD
6
7
     void sum_coords(double x[3], double y[3], double ans\leftarrow
8
         [3])
9
       for (int i=0; i < 3; i++)
10
11
          ans[i] = x[i]+y[i];
12
13
14
       return;
15
16
     void subtract_coords ( double fin [3], double intil [3], ←
17
        double ans [3])
18
19
       for (int i=0; i < 3; i++)
20
```

```
ans[i] = fin[i] - intil[i];
21
22
23
       return;
24
25
     void get_mag(double vec[3], double& mag)
26
27
28
        double tmp = 0.0;
29
        for (int i=0; i < 3; i++)
30
          tmp += (vec[i]*vec[i]);
31
32
33
       mag = sqrt(tmp);
34
35
     void compare_coords( double x[3], double y[3], bool& \leftarrow
36
        areSame, double tol)
37
38
        areSame = false;
39
        double mag;
        double ans [] = \{0.0, 0.0, 0.0\};
40
41
        subtract_coords( x, y, ans);
42
        get_mag(ans, mag);
43
        if (mag<=tol)
44
45
          areSame = true;
46
47
       return;
48
     }
49
     void divide ( double vec [3], double denom, double ans←
50
         [3])
     {
51
        if(denom = 0.0)
52
53
54
          print_error ("Denominator_is_zero._Division_not_←
             defined.");
55
56
        else
        {
57
```

```
58
          for (int i=0; i < 3; i++)
59
             ans[i] = vec[i]/denom;
60
61
62
63
        return;
64
65
      void get_unit_vector( double vec[3], double unit[3])
66
67
        double mag = 0.0;
68
69
        get_mag( vec, mag);
70
        divide (vec, mag, unit);
71
        return;
72
      }
73
      void cross_product( double x[3], double y[3], double \leftarrow
74
         ans [3])
75
        ans [0] = x[1] * y[2] - x[2] * y[1];
76
        ans [1] = x[2]*y[0]-x[0]*y[2];
77
78
        ans [2] = x[0] * y[1] - x[1] * y[0];
79
        return;
80
      }
81
      void dot_product( double x[3], double y[3], double& ans\leftarrow
82
83
      {
84
        for (int i=0; i < 3; i++)
85
          ans = x[i]*y[i];
86
87
88
        return;
89
90
91
```

## A.14 GeoMod\_util.hpp

```
1 #ifndef GEOMOD_UTIL_HPP
```

```
2 |#define GEOMOD_UTIL_HPP
3
  // Simmetrix Headers
4
5 #include "SimUtil.h"
6 |#include "SimModel.h"
7 #include "SimAdvModel.h"
  #include "MeshSim.h"
9 #include "SimPartitionedMesh.h"
10
   // Standard C++ Headers
11
  #include <cstdlib>
12
  #include <iostream>
13
14
   pGVertex GIP_insertVertexInFace(pGIPart_part, double* xyz←
15
      , pGFace face);
16
   namespace GMD
17
18
19
     void sim_start ( char* Sim_log_file_name, int argc, char←
        ** argv);
20
21
     void sim_end();
     pGModel create_cube (double length);
22
     pGModel create_2D_rectangle ( double y_length , double ←
23
        x_width);
24
25 #endif
```

## A.15 GeoMod\_util.cpp

```
10
        SimPartitionedMesh_start(&argc, &argv);
11
        Sim_logOn(Sim_log_file_name);
12
        SimUtil_start();
        Sim_readLicenseFile(0);
13
        SimModel_start();
14
15
        MS_init();
16
     }
17
18
     void sim_end()
19
        std::cout << "Stopping_Simmetrix" << std::endl;
20
21
        MS_exit();
22
        SimModel_stop();
23
        Sim_unregisterAllKeys();
24
        SimUtil_stop();
        Sim_logOff();
25
26
        SimPartitionedMesh_stop();
27
28
     pGModel create_cube (double length)
29
30
        pGModel model;
31
        pGIPart part;
32
        pGRegion outerRegion;
        pGVertex vertices [8]; // array to store the returned \leftarrow
33
           model\ vertices
        pGEdge edges [12]; // array to store the returned \leftarrow
34
           model edges
35
        double hl = length/2;
36
        model = GM_new();
37
        part = GM_part(model);
38
        outerRegion = GIP_outerRegion(part);
39
        double vert_xyz[8][3] =
40
41
        \{-hl, -hl, -hl\},\
          \{ hl, -hl, -hl \},
42
43
          \{ hl, hl, -hl \},
          \{-hl, hl, -hl\},\
44
          \{-hl, -hl, hl\},\
45
          \{ hl, -hl, hl \},
46
          { hl, hl, hl},
47
```

```
48
         \{-hl, hl, hl\};
49
50
       int i;
       for (i=0; i<8; i++)
51
          vertices [i] = GIP_insertVertexInRegion (part, ←
52
             vert_xyz[i],outerRegion);
53
54
       pGVertex startVert, endVert;
55
       double point 0[3], point 1[3]; // xyz locations of the \leftarrow
          two vertices
56
       pCurve linearCurve;
57
58
       // First, the bottom edges
       for (i = 0; i < 4; i++)
59
60
         startVert = vertices[i];
61
         endVert = vertices[(i+1)\%4];
62
         GV_point(startVert, point0);
63
         GV_point(endVert, point1);
         linearCurve = SCurve_createLine(point0, point1);
64
65
         edges[i] =
            GIP_insertEdgeInRegion(part, startVert, endVert, ←
66
               linearCurve, 1, outerRegion);
       }
67
68
69
       // Now the side edges of the box
70
       for (i = 0; i < 4; i++)
          startVert = vertices[i];
71
72
         endVert = vertices[i+4];
73
         GV_point(startVert, point0);
74
         GV_point (endVert, point1);
75
         linearCurve = SCurve_createLine(point0, point1);
76
         edges[i+4] =
77
            GIP_insertEdgeInRegion(part, startVert, endVert, ←
               linearCurve, 1, outerRegion);
       }
78
79
80
       // Finally the top edges
81
       for (i=0; i<4; i++)
82
          startVert = vertices[i+4];
         endVert = vertices [(i+1)\%4+4];
83
```

```
GV_point(startVert, point0);
84
85
           GV_point(endVert, point1);
86
           linearCurve = SCurve_createLine(point0, point1);
87
           edges[i+8] =
             GIP_insertEdgeInRegion(part, startVert, endVert, ←
88
                linearCurve, 1, outerRegion);
89
         }
90
91
        double corner[3], xPt[3], yPt[3];
                                                // the points \leftarrow
            defining the surface of the face
92
        pGEdge faceEdges [4];
                                                // the array of \hookleftarrow
            edges connected to the face
93
                                                // the direction \Leftrightarrow
        int faceDirs [4];
            of the edge with respect to the face
94
         int loopDef[1] = \{0\};
95
         pSurface planarSurface;
96
97
         // First the bottom face
         // Define the surface – we want the normal to point \leftarrow
98
            out of the box
99
         for (i = 0; i < 3; i++)
100
101
           corner[i] = vert_xyz[1][i];
102
           xPt[i] = vert_xyz[0][i];
           yPt[i] = vert_xyz[2][i];
103
104
         planarSurface = SSurface_createPlane(corner,xPt,yPt);
105
         // Define and insert the face into the outer "void" \leftarrow
106
            region
107
         for (i=0; i<4; i++)
108
           faceDirs[i] = 0;
           faceEdges[i] = edges[3-i]; // edge order 3->2->1->0
109
110
111
         GIP_insertFaceInRegion (part, 4, faceEdges, faceDirs, 1, ←
            loopDef, planarSurface, 1, outerRegion);
112
113
         // Now the side faces of the box - each side face has \leftarrow
             the edges defined in the same way
         // for the first side face, the edge order is \leftarrow
114
            0 -> 5 -> 8 -> 4
```

```
115
         for (i=0; i<4; i++)
           //Define surface such that normals all point out of
116
               the box
117
           for (int j=0; j < 3; j++) {
             corner[j] = vert_xyz[i][j];
118
                                                  // the corner is\Leftrightarrow
                  the lower left vertex location
             xPt[j] = vert_xyz[(i+1)\%4][j];
                                                  // the xPt the \Leftrightarrow
119
                lower right vertex location
120
             yPt[j] = vert_xyz[i+4][j];
                                                  // the yPt is \Leftrightarrow
                the upper left vertex location
121
           planarSurface = SSurface_createPlane(corner,xPt,yPt↔
122
              );
123
124
           faceEdges [0] = edges [i];
125
           faceDirs[0] = 1;
           faceEdges[1] = edges[(i+1)\%4+4];
126
           faceDirs[1] = 1;
127
           faceEdges[2] = edges[i+8];
128
           faceDirs[2] = 0;
129
           faceEdges[3] = edges[i+4];
130
131
           faceDirs[3] = 0;
132
           GIP_insertFaceInRegion (part, 4, faceEdges, faceDirs, 1, ←
133
              loopDef, planarSurface, 1, outerRegion);
        }
134
135
         // Finally the top face of the box
136
137
         // Define the surface – we want the normal to point \leftrightarrow
            out of the box
138
         for (i=0; i<3; i++)
139
           corner[i] = vert_xyz[4][i];
           xPt[i] = vert_xyz[5][i];
140
141
           yPt[i] = vert_xyz[7][i];
142
143
         planarSurface = SSurface_createPlane(corner, xPt, yPt);
         // Define and insert the face
144
145
        for (i=0; i<4; i++)
           faceDirs[i] = 1;
146
```

```
147
           faceEdges[i] = edges[i+8]; // edge order \leftrightarrow
              8->9->10->11
148
         // when this face is inserted, a new model region \leftarrow
149
            will automatically be created
         GIP\_insertFaceInRegion(part, 4, faceEdges, faceDirs, 1, \leftarrow)
150
            loopDef , planarSurface ,1 , outerRegion );
151
152
         return model;
153
154
      pGModel create_2D_rectangle ( double y_length, double ←
155
          x_width)
156
      {
157
         // Create an empty modeling space to work with
158
         pGModel model = GM_new();
         pGIPart part = GM_part(model);
159
         pGRegion outRegion = GIP_outerRegion(part);
160
161
         // Create model vertices
162
         pGVertex verts [4];
163
164
         double vert_xyz[4][3] = \{\{0.0, 0.0, 0.0\},
165
           \{ y_{length}, 0.0, 0.0 \},
           \{ y_{length}, x_{width}, 0.0 \},
166
           \{0.0, x_{width}, 0.0\}\};
167
         for (int i=0; i<4; i++)
168
169
170
           verts[i] = GIP_insertVertexInRegion( part, vert_xyz←
              [i], outRegion);
171
172
173
         // Create model edges
         pCurve line;
174
         pGEdge edges [4];
175
         for (int i = 0; i < 4; i + +)
176
177
           pGVertex start = verts[i];
178
           pGVertex end = verts [(i+1)\%4];
179
           line = SCurve_createLine(vert_xyz[i], vert_xyz[(i↔
180
              +1)\%4]);
```

```
181
          edges[i] = GIP_insertEdgeInRegion( part, start, end ←
              , line , 1, outRegion);
182
        }
183
        // Create Face
184
185
        pSurface plane;
        int face_dirs[4] = {1,1,1,1};
186
187
        int loopDef[1] = \{0\};
        plane = SSurface_createPlane(vert_xyz[0], vert_xyz←
188
            [1], vert_xyz[2]);
        GIP_insertFaceInRegion(part, 4, edges, face_dirs, 1, ←
189
           loopDef , plane , 1 , outRegion );
190
191
        return model;
192
      }
    }
193
```

#### A.16 GeoMod\_SIM.hpp

```
#ifndef GEOMOD.SIM.HPP

#define GEOMOD.SIM.HPP

// Simmetrix Headers

#include "SimUtil.h"

#include "SimModel.h"

#include "SimAdvModel.h"

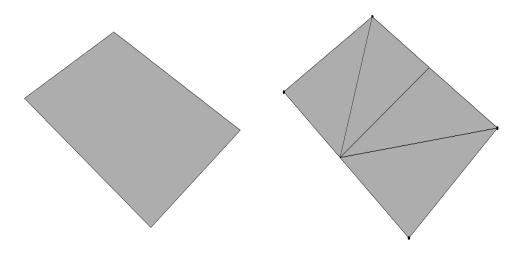
#include "MeshSim.h"

#include "SimPartitionedMesh.h"

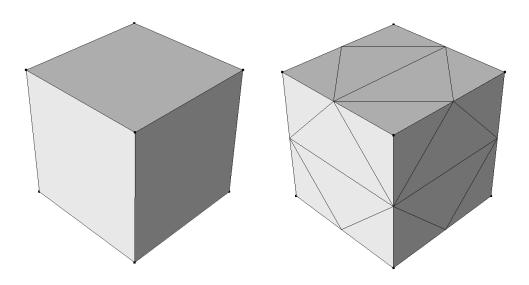
#include "SimPartitionedMesh.h"
```

# B Supplementary Images

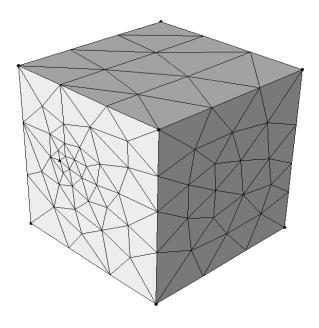
# B.1 Model and Mesh of Test 1



# B.2 Model and Mesh of Test 2



# B.3 Mesh of Test 11



# B.4 Mesh of Test 12

