

C1- Tutorial-9

Exercise 5

1) we can fix the input alphabet $\Sigma = \{0, 1\}$.

so set $L = \{x_1, x_2, \dots, x_n \mid x_n \in \Sigma, n \in \mathbb{N}\}$.

$\Rightarrow \bar{1} = 0, \bar{0} = 1$

$$1 \vee 0 = 1, 1 \vee 1 = 1, 0 \vee 0 = 0, 1 \wedge 0 = 0, 1 \wedge 1 = 1, 0 \wedge 0 = 0.$$

so it could be a boolean algebra.

2). Definition of DFA:

① A finite set of states Q

② A finite set of input symbols Σ .

③ A transition function $\delta : Q \times \Sigma \rightarrow Q$

④ A start state $q_0 \in Q$

⑤ A set of accept states $F \subseteq Q$

we could fix the sets: $Q = \{0, 1\}$, $\Sigma = \{0, 1\}$,

so definition ①, ② hold

$Q \times \Sigma \rightarrow Q$: We could use boolean operators,

$$\bar{1} = 0, \bar{0} = 1, 1 \vee 0 = 1, 1 \wedge 0 = 0,$$

$$1 \vee 1 = 1, 1 \wedge 1 = 1$$

$$0 \vee 0 = 0, 0 \wedge 0 = 0.$$

So definition ③ holds.

We don't have start state and accept states, so definition ④, ⑤ don't hold.

3)

Add start and accept states.