# Case Study 3

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# Setup

Setting up the dataset and the actual data realization information into accessible variables for analysis.

```
# Assuming the data is from the same working directory as this file
gene <- read.table("hcmv.txt", header=TRUE)
data <- gene[,1]
# Actual data
N <- 229354  # Population size
n <- 296  # Sample number of palindromes
editGene <- gene
site.random <- editGene[["location"]]
# Display the data
site.random</pre>
```

```
177
                   1321
                          1433
                                 1477
                                         3248
                                                3255
                                                        3286
                                                               7263
                                                                      9023
                                                                              9084
##
     Г17
##
    [11]
           9333
                  10884
                         11754
                                12863
                                        14263
                                               14719
                                                      16013
                                                              16425
                                                                     16752
                                                                             16812
##
    [21]
          18009
                  19176
                         19325
                                19415
                                        20030
                                               20832
                                                      22027
                                                              22739
                                                                     22910
                                                                             23241
##
    [31]
          25949
                  28665
                         30378
                                30990
                                        31503
                                               32923
                                                      34103
                                                              34398
                                                                     34403
                                                                             34723
                                40554
##
    [41]
          36596
                  36707
                         38626
                                        41100
                                               41222
                                                      42376
                                                              43475
                                                                     43696
                                                                             45188
##
    [51]
          47905
                  48279
                         48370
                                48699
                                        51170
                                               51461
                                                      52243
                                                              52629
                                                                     53439
                                                                             53678
##
    [61]
          54012
                  54037
                         54142
                                55075
                                        56695
                                               57123
                                                      60068
                                                              60374
                                                                     60552
                                                                             61441
##
    [71]
          62946
                  63003
                         63023
                                63549
                                        63769
                                               64502
                                                      65555
                                                              65789
                                                                     65802
                                                                             66015
##
    [81]
          67605
                  68221
                         69733
                                70800
                                        71257
                                               72220
                                                      72553
                                                              74053
                                                                     74059
                                                                             74541
    [91]
          75622
                  75775
                         75812
                                75878
                                        76043
                                               76124
                                                      77642
                                                              79724
                                                                     83033
##
                                                                             85130
   [101]
          85513
                  85529
                         85640
                                86131
                                        86137
                                               87717
                                                      88803
                                                              89586
                                                                     90251
                                                                             90763
   [111]
          91490
                  91637
                         91953
                                92526
                                        92570
                                               92643
                                                      92701
                                                              92709
                                                                     92747
                                                                             92783
   [121]
          92859
                  93110
                         93250
                                93511
                                        93601
                                               94174
                                                      95975
                                                              97488
                                                                     98493
  [131]
          99709 100864 102139 102268 102711 104363 104502 105534 107414 108123
   [141] 109185 110224 113378 114141 115627 115794 115818 117097 118555 119665
## [151] 119757 119977 120411 120432 121370 124714 125546 126815 127024 127046
## [161] 127587 128801 129057 129537 131200 131734 133040 134221 135361 136051
## [171] 136405 136578 136870 137380 137593 137695 138111 139080 140579 141201
## [181] 141994 142416 142991 143252 143549 143555 143738 146667 147612 147767
## [191] 147878 148533 148821 150056 151314 151806 152045 152222 152331 154471
## [201] 155073 155918 157617 161041 161316 162682 162703 162715 163745 163995
## [211] 164072 165071 165883 165891 165931 166372 168261 168710 168815 170345
## [221] 170988 170989 171607 173863 174049 174132 174185 174260 177727 177956
## [231] 178574 180125 180374 180435 182195 186172 186203 186210 187981 188025
## [241] 188137 189281 189810 190918 190985 190996 191298 192527 193447 193902
## [251] 194111 195032 195112 195117 195151 195221 195262 195835 196992 197022
## [261] 197191 198195 198709 201023 201056 202198 204548 205503 206000 207527
## [271] 207788 207898 208572 209876 210469 215802 216190 216292 216539 217076
## [281] 220549 221527 221949 222159 222573 222819 223001 223544 224994 225812
```

## The Data

Here a strip plot is shown to visualize where palindromes are distributed, by laying out all possible palindrome location sites and displaying binary values representative of palindrome occurances.

# Testing

### Uniform Random Distribution by Simple Random Sampling

```
# Pseudo data for simulation
                    # Setting seed for the date at which this analysis was performed
set.seed(22217)
gene <- seq(1, N)
# Produce simple random sample
site.random <- sample.int(N, size=n)</pre>
site.random
##
     [1] 174949 85198 54658
                               83367
                                     72973 91865 106758 15113 19546 119591
##
    [11] 96009 164114 157638
                               70997 220364 144722 131728 181859
                                                                  53671
    [21] 130697 124433
                        72012 190519 183051
                                             95948 123480 224920 204215 225734
##
    [31]
                26994 215341 172002 131893 142875
                                                    15731 186370 206710
    [41] 89768 133009 196581 215916 97206 135873 57820
```

```
[51] 175670 100715 91087 148991 129680 189277 47631 157104 70484 63601
    [61] 105306
                 41189
                        63919 124143
                                      67861 225315 204752
                                                              2902 208373 225741
##
                                                                    23050 154151
    [71] 208412
                 82017
                        18803
                               90473
                                       86555 166688 194563
    [81] 199346 151015 112659
                               67559 221899 188870
                                                     91449 136312 118009 112991
    [91] 177821
                 22628
                        40832 174562 133071 174368 190177 107483
                                                                   98033
  [101] 156135 146687
                        43177
                               56412
                                       54455
                                              46738
                                                     29438 190864 207306 166013
                        83949 161648 199413
          24206
                 23508
                                              15621
                                                     60911 225348 101947 153596
  [121]
          38596
                 40275 165459
                               80415 133956
                                              78921 190555 211874 108806 183468
   [131] 166963 138078 194812 111652
                                       41423
                                              81951 103166
                                                            62846 173352
                                                                           47548
                                       38986
                                              92882 147599
  [141] 185794 217170
                        56090
                               34055
                                                            51325
                                                                   32614
  [151]
          76009 107916 146298 101794
                                       19782
                                               5773
                                                     93454 119658 170997 179921
                         5355 205314 164279 199427
  [161] 152061 102443
                                                     81979 119920 169866
         50119 127009
  [171]
                        30217 128574 125884 184474
                                                     11390 113468 131415 145078
                                                                   29061 227086
  [181]
          57659 129479 152350 104617 138299 178905 166946 105186
  [191]
                        18149
                               31320 166789
                                              75231 218477 100994 183115
          39966
                 66443
## [201] 214790 148054
                        17754
                               27584 205823
                                              36830 215960 152500 153030 159426
  [211] 173815 112666
                        46851
                               49676 161107
                                              69637
                                                     11329 221523 228302
  [221] 180094 124225 220926
                               31336
                                       41832
                                              34085
                                                      8653 101249
                                                                   72057 159021
                                                            47843 211100
         33585 160137 190886 147808
                                       45605 162896
                                                     50239
  Г231]
## [241] 192546
                 83934
                        13614
                               81505 151623 182934 215324 211606 228835 168165
## [251] 115714
                 45974
                        75841
                                 9223
                                       40997 155648 203873 186298
                                                                   99977 109712
         94906
                 97925 103631 161921
                                       65500 199918 129636
                                                              3849 101848
                 22927
                          163
                               51070
                                       95523
## [271] 175712
                                              69072 164911 173253
                                                                    68029 218164
## [281] 189971 107415 21279 185108 178498 155443 137114 14635
                                                                   56735 200160
## [291]
                 66517 122735
                               83140 155824 108215
          21943
```

Plotting the uniform random distribution with a strip plot, we can compare it to the actualized data above.

```
library(lattice)
stripplot(site.random, pch=16, cex=0.25, xlab="Palindrome Location (Simple Random Simulation)")
```

0 50000 100000 150000 200000 Palindrome Location (Simple Random Simulation)

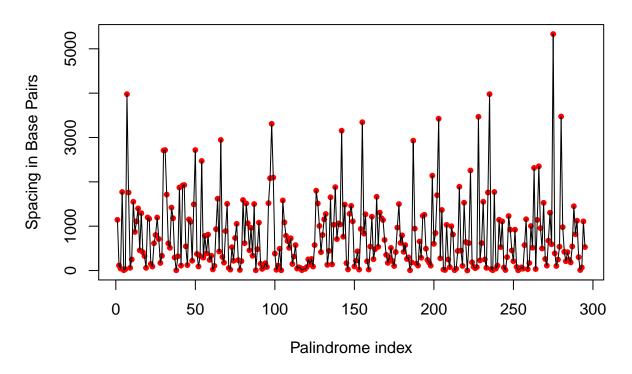
It's easy to notice that while although similar, the actualized data may appear to have a couple more dense clusters than what was generated via the simple sample. We will need to perform more testing to confirm whether these apparent clusters are statistically significant within the actualized data.

### Spacing

Here we create a graph to determine the usualness of spacing in the dataset.

```
spacing <- {0}
for (i in 1:length(data)){
    spacing[i] <- data[i+1] - data[i];
}
spacing <- spacing[!is.na(spacing)]
plot(spacing, pch=20,col='red', main="Spacing of Palindrome locations", xlab = "Palindrome index", ylab lines(spacing, y=NULL)</pre>
```

# **Spacing of Palindrome locations**



#### Monte Carlo Uniform Simulation

#### Generating the samples

Here we are generating one thousand instances of 296 simple randomly chosen uniformally distributed vriables, in order to acquire distributions of desired parameters for testing.

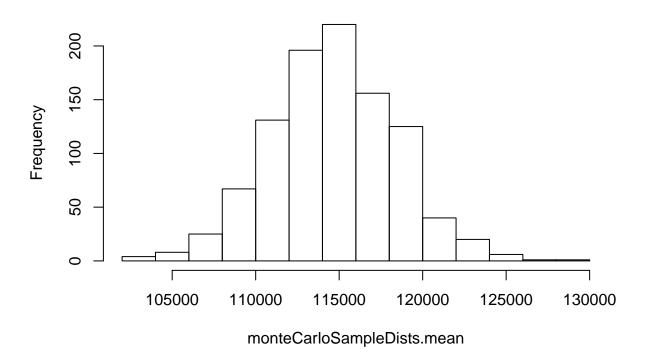
```
B <- 1000 # 1000 bootstrap uniform samples
monteCarloSampleDists <- matrix(data = NA, ncol = n, nrow = B)
monteCarloSampleDists.mean <- vector(mode="logical", length = B)
for (i in 1:B) {
    # Row is overall sample, column is data per sample</pre>
```

```
monteCarloSampleDists[i,] <- sample.int(N,n)
# Need to sort them in order to check consecutive palindromes
monteCarloSampleDists[i,] <- monteCarloSampleDists[i,order(monteCarloSampleDists[i,])]
monteCarloSampleDists.mean[i] <- mean(monteCarloSampleDists[i,])

#print(monteCarloSampleDists[1,])

hist(monteCarloSampleDists.mean)</pre>
```

# Histogram of monteCarloSampleDists.mean



### **Expected Consecutive Palindrome Occurences**

Now, we want to build some statistics surrounding the randomly distributed monte carlo simulation. Here we will count the longest string of consecutive palindromes using the sorted data, and more.

```
counts <- matrix(data = NA, nrow = B, ncol = n)</pre>
for (i in 1:B) {
  indexHighestCount <- 0
  tempFirstIndex <- 0</pre>
  # 0 indicates false, 1 indicates true
  booleanIsConsecutiveNow <- 0
  # Counting the amount of consecutive palindromes
  count <- 1
                            # Initialized to one since we're counting backwards down below in loop
                           # Used to track the highest count overall
  highestCount <- 1
  # Inefficient, but stable
  # Starts from 2 to compare to last element
  for (j in 2:n) {
     #monteCarloSampleDists[i, j]
     \  \  \text{if } (\texttt{monteCarloSampleDists[i,j]} - 1)) \  \  \{ \  \  (\texttt{monteCarloSampleDists[i,j]}) - 1)) \  \  \{ \  \  (\texttt{monteCarloSampleDists[i,j]}) - 1) \}
```

```
if(booleanIsConsecutiveNow == 0) {
          tempFirstIndex <- (j - 1) # Index at first palindrome in at least 2 consecutive occurances
      count \leftarrow (count + 1)
      booleanIsConsecutiveNow <- 1
    }
    else {
      if (count > highestCount) {
        highestCount <- count
        indexHighestCount <- tempFirstIndex</pre>
      }
      count <- 1
      tempFirstIndex <- 0</pre>
      booleanIsConsecutiveNow <- 0
    }
  }
  # Store highest count into the counts array
  counts[i,1] <- highestCount</pre>
  # Store the index at which highestCount occured into the array also.
  counts[i,2] <- indexHighestCount</pre>
}
# Clearly, two consecutively is quite normal.
plot(counts[,1])
      3.0
                                                                     0
      2.5
counts[, 1]
      2.0
                                     3
      0.
             0
                          200
                                       400
                                                                   800
                                                     600
                                                                                1000
                                             Index
```

```
summary(counts[,1])
```

## Min. 1st Qu. Median Mean 3rd Qu. Max. ## 1.000 1.000 1.000 1.324 2.000 3.000

Now we have to run the same process on the actualized data, to determine if there's an unusually long string of palindromes to help us easily identify the replication site.

```
indexHighestCount <- 0</pre>
tempFirstIndex <- 0</pre>
# 0 indicates false, 1 indicates true
booleanIsConsecutiveNow <- 0
# Counting the amount of consecutive palindromes
count <- 1
                      # Initialized to one since we're counting backwards down below in loop
highestCount <- 1
                      # Used to track the highest count overall
# Inefficient, but stable
# Starts from 2 to compare to last element
for (i in 2:n) {
  if (data[ (i - 1) ] == ((data[i]) - 1)) {
    if(booleanIsConsecutiveNow == 0) {
        tempFirstIndex <- (i - 1) # Index at first palindrome in at least 2 consecutive occurances
    }
    count \leftarrow (count + 1)
    booleanIsConsecutiveNow <- 1
  }
  else {
    if (count > highestCount) {
      highestCount <- count
      indexHighestCount <- tempFirstIndex</pre>
    count <- 1
    tempFirstIndex <- 0</pre>
    booleanIsConsecutiveNow <- 0
  }
}
# Print out the highest count, and its index.
highestCount
```

## [1] 2

indexHighestCount

## [1] 221

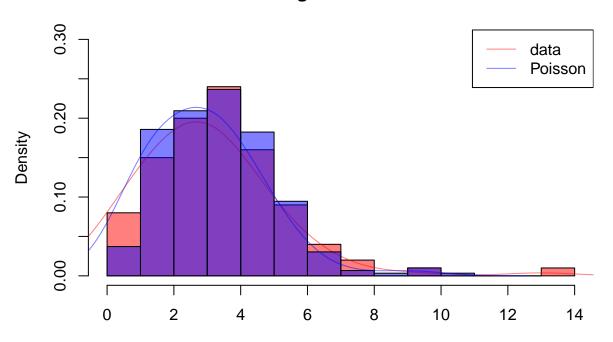
Unfortunately, our realized data matches the above statistics when it comes to consecutive occurrences of palindromes, since the max amount of consecutive occurrences matched that of the third quartile value above. This means there were no unusually long strings of consecutively occurring palindromes, therefore we'll have to resort to the poisson process in order to help us better determine unusual clusters for the replication site.

#### Poisson Process

First, we'll generate a histogram forming the basis of the poisson distribution of clusters given fixed intervals of one hundred.

```
hist(counts, breaks=seq(0,14,by=1), col = rgb(1,0,0,0.5),
    probability = TRUE,
    xlab = "number of palindromes inside an interval (~ 2300 bases)",
    ylim = c(0,0.3), include.lowest = TRUE, right = FALSE);
lines(density(counts, adjust = 2), col = rgb(1,0,0,0.5))
Pois <- rpois(296, lambda = mean(counts))
hist(Pois, breaks=seq(0,13,by=1), col = rgb(0,0,1,0.5), probability = TRUE, add = TRUE,
    include.lowest = TRUE, right = FALSE);
lines(density(Pois, adjust = 2), col = rgb(0,0,1,0.5))
legend("topright", legend = c("data", "Poisson"), lty = c(1,1), col = c(rgb(1,0,0,0.5), rgb(0,0,1,0.5))</pre>
```

# **Histogram of counts**



number of palindromes inside an interval (~ 2300 bases)

### Finding the Cluster

Then, we'll calculate the highest likely amount of clusters within any one given interval, and compare it to the highest amount of palindromes we have in any one cluster in the actualized data.

```
# Here, the 99.95th percentile is calculated to help determine upper outlier.
highestLikelyCluster <- qpois(.9995, mean(tab))  # Using sample statistic of lambda hat = x bar
print('The highest likely amount in a cluster is:')

## [1] "The highest likely amount in a cluster is:"
highestLikelyCluster

## [1] 10
print('and the highest amount of any cluster in our actualized data is:')</pre>
```

## [1] "and the highest amount of any cluster in our actualized data is:"

```
max(tab)
```

## [1] 13

It's clear that with 99.95% probability, a maximum of ten palindromes will be in any one cluster. Due to our outlier of 13, and given it's the only above 10, it seems like a likely candidate for our replication site.

### Chi-Squared Test

```
First we perfom chi-squared test on the simulated data.
regionsplit <- function(n.region, gene, site){</pre>
  count.int <- table(cut(site, breaks = seq(1, length(gene), length.out=n.region+1), include.lowest=TRU</pre>
  count.vector <- as.vector(count.int)</pre>
  count.tab <- table(count.vector)</pre>
 return (count.tab)
}
n.region <- 50
regionsplit(n.region, gene, site.random)
## count.vector
## 2 3 4 5 6 7 8 9 10 11
## 2 2 5 18 6 6 5 3 2 1
chisqtable <- function(n.region, site, N){</pre>
 n <- length(site)</pre>
  # lambda estimate
 lambda.est <- n/n.region
  # cut into n.region number of non-overlapping intervals
  count.int <- table(cut(site, breaks = seq(1, length(gene), length.out=n.region+1), include.lowest=TRU</pre>
  # get the count levels range
  count.vector <- as.vector(count.int)</pre>
  count.range <- max(count.vector) - min(count.vector) + 1</pre>
  # create contingency table
  table <- matrix(rep(NA, count.range*3), count.range, 3)
  for (i in 1:count.range){
    offset <- min(count.vector) - 1
    # first column = count level
    table[i, 1] <- i + offset
    # second column = observed count
    table[i, 2] <- sum(count.vector == i + offset)</pre>
    # third column = expected count
    if ((i + offset == min(count.vector)) && (min(count.vector) != 0))
      table[i, 3] <- ppois(i+offset, lambda.est)*n.region
    else if (i + offset == max(count.vector))
      table[i, 3] <- 1 - ppois(i + offset - 1, lambda.est)
    else
      table[i, 3] <- (ppois(i+offset, lambda.est) - ppois(i + offset - 1, lambda.est))*n.region
  }
  return (table)
site.random.tabtemp <- chisqtable(n.region, site.random, N)</pre>
```

```
site.random.tab <- matrix(rep(NA, 7*2), 7, 2)</pre>
site.random.tab[1,] <- colSums(site.random.tabtemp[1:2, 2:3])</pre>
site.random.tab[2:6,] <- site.random.tabtemp[3:7, 2:3]</pre>
site.random.tab[7,] <- colSums(site.random.tabtemp[7:9, 2:3])</pre>
site.random.stats <- sum((site.random.tab[,2] - site.random.tab[,1])^2/site.random.tab[,2])</pre>
pchisq(site.random.stats, 7 - 2, lower.tail=FALSE) #if lower.tail=TRUE then you're testing something el
## [1] 0.01025207
Here we get a result of about .01.
We then again perform the chi-squared test on the real data.
#actual data
N <- 229354
n <- 296
site.random <- editGene[["location"]]</pre>
library(lattice)
stripplot(site.random, pch=16, cex=0.25)
                                    100000
     0
                   50000
                                                     150000
                                                                      200000
                                      site.random
n.region <- 50
regionsplit <- function(n.region, gene, site){</pre>
  count.int <- table(cut(site, breaks = unique(seq(1, N, length.out=n.region+1)), include.lowest=TRUE))</pre>
  count.vector <- as.vector(count.int)</pre>
  count.tab <- table(count.vector)</pre>
  return (count.tab)
}
```

```
regionsplit(n.region, gene, site.random)
## count.vector
## 0 1 2 3 4 5 6 7 8 9 10 13 15
## 1 2 1 4 8 8 5 9 4 5 1 1 1
chisqtable <- function(n.region, site, N){</pre>
 n <- length(site)</pre>
  # lambda estimate
  lambda.est <- n/n.region
  # cut into n.region number of non-overlapping intervals
  count.int <- table(cut(site, breaks = unique(seq(1, N, length.out=n.region+1)), include.lowest=TRUE))</pre>
  # get the count levels range
  count.vector <- as.vector(count.int)</pre>
  count.range <- max(count.vector) - min(count.vector) + 1</pre>
  # create contingency table
  table <- matrix(rep(NA, count.range*3), count.range, 3)
  for (i in 1:count.range){
    offset <- min(count.vector) - 1
    # first column = count level
    table[i, 1] <- i + offset
    # second column = observed count
    table[i, 2] <- sum(count.vector == i + offset)</pre>
    # third column = expected count
    if ((i + offset == min(count.vector)) && (min(count.vector) != 0))
      table[i, 3] <- ppois(i+offset, lambda.est)*n.region
    else if (i + offset == max(count.vector))
      table[i, 3] <- 1 - ppois(i + offset - 1, lambda.est)
      table[i, 3] <- (ppois(i+offset, lambda.est) - ppois(i + offset - 1, lambda.est))*n.region</pre>
  }
 return (table)
}
site.random.tabtemp <- chisqtable(n.region, site.random, N)</pre>
site.random.tab \leftarrow matrix(rep(NA, 7*2), 7, 2)
site.random.tab[1,] <- colSums(site.random.tabtemp[1:2, 2:3])</pre>
site.random.tab[2:6,] <- site.random.tabtemp[3:7, 2:3]</pre>
site.random.tab[7,] <- colSums(site.random.tabtemp[7:9, 2:3])</pre>
site.random.stats <- sum((site.random.tab[,2] - site.random.tab[,1])^2/site.random.tab[,2])</pre>
pchisq(site.random.stats, 7 - 2, lower.tail=FALSE) #if lower.tail=TRUE then you're testing something el
## [1] 0.2219605
```

We here get a result of about .22.