

ComplexSpace.jl

"""

```
struct ComplexSpace <: EuclideanSpace{C}
```

A standard complex vector space \mathbb{C}^d with Euclidean inner product and no additional structure. It is completely characterised by its dimension and whether its the normal space or its dual (which is canonically isomorphic to the conjugate space).

"""

```
struct ComplexSpace <: EuclideanSpace{C}
```

```
    d::Int
```

```
    dual::Bool
```

```
end
```

```
ComplexSpace(d::Integer = 0; dual = false) = ComplexSpace{Int}(d, dual)
```

```
function ComplexSpace(dim::Pair; dual = false)
```

```
    if dim.first === Trivial()
```

```
        return ComplexSpace(dim.second; dual = dual)
```

```
    else
```

```
        msg = "$(dim) is not a valid dimension for ComplexSpace"
```

```
        throw(SectorMismatch(msg))
```

```
    end
```

```
end
```

```
ComplexSpace(dims::AbstractDict; dual = false) = ComplexSpace{Int}(dims..., dual = dual)
```

```
# convenience constructor
```

```
Base.^(::ComplexNumbers, d::Int) = ComplexSpace(d)
```

```
Base.getindex(::ComplexNumbers) = ComplexSpace
```

```
Base.getindex(::ComplexNumbers, d::Int) = ComplexSpace(d)
```

```
# Corresponding methods:
```

```
#-----
```

```
dim(V::ComplexSpace) = V.d
```

```
isdual(V::ComplexSpace) = V.dual
```

```
Base.axes(V::ComplexSpace) = Base.OneTo(dim(V))
```

```
Base.conj(V::ComplexSpace) = ComplexSpace(dim(V), !isdual(V))
```

```
Base.oneunit(::Type{ComplexSpace}) = ComplexSpace{Int}(1)
```

```
⊕(V1::ComplexSpace, V2::ComplexSpace) = isdual(V1) == isdual(V2) ?
```

```
    ComplexSpace(dim(V1)+dim(V2), isdual(V1)) :
```

```
    throw(SpaceMismatch("Direct sum of a vector space and its dual does not exist"))
```

```
fuse(V1::ComplexSpace, V2::ComplexSpace) = ComplexSpace(V1.d*V2.d)
```

```
flip(V::ComplexSpace) = dual(V)
```

```
infinum(V1::ComplexSpace, V2::ComplexSpace) = isdual(V1) == isdual(V2) ?
```

```
    ComplexSpace(min(dim(V1), dim(V2)), isdual(V1)) :
```

```
    throw(SpaceMismatch("Infinum of space and dual space does not exist"))
```

```
supremum(V1::ComplexSpace, V2::ComplexSpace) = isdual(V1) == isdual(V2) ?
```

```
    ComplexSpace(max(dim(V1), dim(V2)), isdual(V1)) :
```

```
    throw(SpaceMismatch("Supremum of space and dual space does not exist"))
```

```
Base.show(io::IO, V::ComplexSpace) = print(io, isdual(V) ? "($(\mathbb{C}^$(V.d)))" : "($(\mathbb{C}^$(V.d)))")
```

```
Base.show(io::IO, ::Type{ComplexSpace}) = print(io, "ComplexSpace")
```

