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300. Longest Increasing Subsequence
 Given an array A of size N
 i ∈ [0; N-1]
 LIS(i) = length of LIS ending strictly at position i
1, if $ j \in [0; i-1]: A[j] < A[i]

LIS(i) =

[1 + max(LIS(j) for j \in [0; i-1] if A[j] < A[i]), else
LIS(A) = max (LIS(i) for i ∈ [0; N-1])
Naive aproach: Recursion (Slow)
 A=[]
 lenght Of LIS (nums):
   n = len (nums)
   A = nums
   max Len = 0
   for i in range (n):
     maxlen = max (max Len, aux(i))
   return maxlen
aux (i):
 maxlen = 0
 for jin range (i):
 [1] A > [ [] A 7,
     maxlen = max(maxlen, aux(j))
 return 1+ maxlen
Exponential time complexity => TLE
Space: O(n) (stack recursiveness)
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Recursion + Memorization (Faster) (Top-down)
mem = list
[] = A
len LIS (nums):
  n= len(nums)
  A= nums
  mem = list (n,-1)
  result = 0
  for i in range (n):
     result = max (result, aux (i))
  return result
aux (i):
 if mem[i] $1:
    return mem[i]
  maxlen= 0
  for j in range (i):
     :[i]A >[i]A fi
       maxlen = max(maxlen, aux(j))
  return 1+ maxlen
Time: O(n2)
Space: O(n)
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Dynamic Programming (Bottom-up)
len LIS (nums):
  n = len(nums)
  dp = list (n, 1)
  for in range (n):
    for j in range (i):
      if (nums[j] < nums[i]):
        dp[i]= max (dp[i], 1+dp[j])
  return max (dp)
Time: 0(n2)
Space: O(n)
```