## Warm up with EDA! (13 points)

(7) a. The Board of Examiners of "Super University" collects information about how much time students spend in toilet during exams. Here are the results of some statistics:

7,39 minutes

3,05 minutes

3

3

6

11

mean

st.dev.

median

min

Q1

Q3

(2) i. Notice that the 1<sup>st</sup> quartile and minimum number of minutes are the same. Explain how this can be.

(2) ii.	Were	there	any	outliers?	Explain	how	you
	made	your d	ecisio	on.			-

(3) iii. The rules and regulations of Super University max 16 declare that students that stay in toilet more than 15 minutes are "suspect for fraud". Would you consider 15 minutes too much? Explain.

	ns just put in a circle the correct answer. Only if choice in the space provided, otherwise it's
coffee in an office worker I. $r^2$ (R-squared) = -16% II. There is a linear relations	ionship between the time of day and amount of s's mug, which are true?" Ship between time and amount of coffee. Unit of coffee in the mug is correctly predicted by
A) I B) II C) III D) II and III only E) none of these	(very short) explanation:
barrier at speeds of 5 to 25 mph They found a correlation of r = the speed at which a car hit th	ustry crashed some test vehicles into a cement to investigate the amount of damage to the cars.  0.60 between speed (MPH) and damage (\$). If the barrier is 1.5 standard deviations above the tage to be? the mean damage."
A) equal to B) 0.36 SD above C) 0.60 SD above D) 0.90 SD above E) 1.5 SD above	(very short) explanation:
(2) iii) "The correlation betweer decrease each Y by 0.20, and int vice versa), the new correlation"	of X and Y is $r = 0.35$ . If we double each X value, we see the variables (put X on the Y-axis and
A) is 0.35 B) is 0.50 C) is 0.70 D) is 0.90 E) cannot be determined	(very short) explanation:

## 5 Modeling skiing (16 points)

I have never been skiing and I would love to try it but I am also not fond of crowded places, so I decided to build a model in order to estimate when a small ski resort near Maastricht is crowded. Since I am also very busy, I assigned this problem to some young hard-working students. They collected data from the past two ski seasons, measuring different variables and then they started fighting with each other because everyone claimed to have the best model.

Let's see the solution of a student that came to me having fit a model using the following variables:

Skiers	the	number	of skiers	who v	isit th	e resort	on that day.
Snow	the	number	of inch	ies c	of sno	w on	the ground.
Temp	the	high t	emperature	for	the	day in	degrees F.
Weekend	an	indicator	r variable	e, if	it's	weeken	d (YES/NO).

Variable	Coefficient	SE (Coeff.)	t-ratio	p-value
Intercept	559.869	76.78	7.29	< 0.0001
Snow	1.424	2.70	0.53	0.6019
Temp	-1.604	2.77	-0.58	0.5677
Weekend: YES	147.349	51.86	2.84	0.0086

**(2) a.** What is the predicted number of skiers for a Saturday with a temperature of 40 F and a snow cover of 25 inches? What would change if it was a Friday?

model is: 
$$\hat{y} = 559.869 + 1.424 \times 5000 - 1.604 \times 4000 + 147.349 \times weekend$$

$$\hat{y}_1 = 559.869 + 1.424 \times 25 - 1.604 \times 40 + 147.349 \leq 679 \text{ people}$$

$$\hat{y}_2 \leq 531 \text{ people} \quad \text{(only the 147.349 change)}$$

**(2) b.** Which of the explanatory variables appear to be associated with the number of skiers and which do not? Explain how you reached your conclusion.

-ouly the weekend seems to have & significant
effect

(2) c. Compute a 95% confidence interval (assume for simplicity that t=2, i.e. simply compute the intervals as for simple regression) for the slope of the variable **weekend** and explain the meaning of this interval *in the context of this specific problem*.

147.349 ± 2×51.86 -> [44, 251]

Civey Lixed values for snow/temperature

people on weekerds will vary from 44 to 251

**(3) d.** One of the students is claiming that, given the above results, if we run a single regression where **skiers** remains the dependent variable and **snow** is the only independent variable, we will get a similar result in terms of significance of the coefficient. Do you agree? Why yes/no?

It seems that such is not significant in the presence of weekend (perhaps it "sucks" the effect of snaw)

But if we take the effect of snaw by itself the result might be different

**(3) e.** If you think that the temperature might affect ski attendance differently on weekends than on weekdays, how would you change the regression to test this? Sketch how the regression equation would look like.

Jutodice an interaction term
Weekend x temp  $\hat{y} = d_1 + d_1 + emp + d_2 snow + d_3 weekend + d_4 weekend x temp$ 

**(4) f.** Following my advice to fit simple models, two students selected only one variable (**snow**), however they had different opinions on how they should fit the model. Here are the two models they presented:

A: 
$$y = w_1^2 x + w_2 x$$

B: 
$$y = wx$$

Note that model A now uses two parameters (though both multiply with the same input value x). Which of the following is correct?

- I) A will perform better than B -most of the times-
- II) B will perform better than A -most of the times-
- III) They would perform equally well on all cases

Hint: Think of how regression coefficients are estimated.

Least squares estimation:  $u_1u_1u_1^2 = 2(\hat{y}-y)^2 \text{ or } 2(W_1^2, X_1+W_2X_1)-y_1$   $(W_1^2+W_2)^2 = y_1^2$ To the end  $(W_1^2+W_2)^2 = y_1^2$ So its the same model

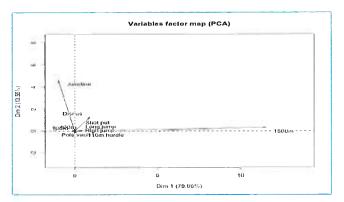
## 6 Is Decathlon really 10 events? (15 points)

(9) a) Decalthon (from the greek word " $\delta \acute{\epsilon} \kappa \alpha$ " which means "ten") consists of 10 events (namely: 100m, Long Jump, Shot Put, High Jump, 400m, 110m Hurdles, Discus Throw, Pole Vault, Javeline Throw, 1500m). A sports bet company is looking into some data from some athletes in order to reveal which events/sports are most significant.

The chief data scientist of the company (after some googling) decided to run a Principal Component Analysis (PCA), however has no idea on how to interpret the results. The dataset consists of 41 athletes and the performance in 10 sports (see a part of it below).

	100m	Long.jump	Shot.put	High.jump	400m	110m.hurdle	Discus	Pole.vault	Javeline	1500m
SEBRLE	11.04	7.58	14.83	2.07	49.81	14.69	43.75	5.02	63.19	291.7
CLAY	10.76	7.40	14.26	1.86	49.37	14.05	50.72	4.92	60.15	301.5
KARPOV	11.02	7.30	14.77	2.04	48.37	14.09	48.95	4.92	50.31	300.2
BERNARD	11.02	7.23	14.25	1.92	48.93	14.99	40.87	5.32	62.77	280.1
YURKOV	11.34	7.09	15.19	2.10	50.42	15.31	46.26	4.72	63.44	276.4
WARNERS	11.11	7.60	14.31	1.98	48.68	14.23	41.10	4.92	51.77	278.1

(3) i) The data scientist ran a PCA and by plotting the first 2 PCs got the result on the right. Can you explain the mistake here, why the figure has this form and how you would correct it? Use the data sample above to make assumptions for the data.

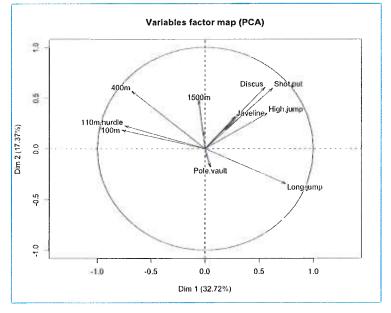


-No scaling of the variables

The 1st dimension is dominated by 1500m which was the largest variance scale

Rescaling/normality variables

- (7) ii) A more reasonable PCA plot using the two first components appears on the right. Answer the following questions.
  - Is in this case, is the use of two PCs enough to explain the data? Why yes/no?
  - Given the loadings of the figure, what is the 1<sup>st</sup> and 2<sup>nd</sup> PC are capturing/ explaining? Can we



somehow differentiate between characteristics of different sports? Provide an intuitive description of the above PCA plot.

- First 2 PCs explain around 50%, so its not enough

- Ist PC ~ jumps

2nd PC~ running (soom/som) - filed &

events

**(6) b,** We discussed in class that regularization can be applied to any "learning" algorithm in order to avoid overfitting and improve generalization over unseen data. Thinking about Non-Negative Matrix Factorization (NMF), how would you formulate the optimization problem in order to account for regularization? Provide the adjusted optimization equation and the interpretation of parameter shrinking in this case. If we prefer a non-sparse decomposition, would you prefer Ridge (L2) or Lasso (L1) regularization in this case?

normal NMF: while IA-W.H! parameters di the actual coefficients

50: winimite: IA-WHI + 7. || µ| dassi

or 7. || µ|| Lidge

where || µ|| is a ve (for with all parameters

af WH matrices

Bonus question (1 point)						
How old is Jerry?	9.53					
Answer:						