

Department of Data Science and Knowledge Engineering

Data Analysis 2017/2018

Final Exam

- Do not turn this page before the official start of the exam! -

First name, Surname: KEY	
Student ID:	
Expected Exam Grade (out of 50): (optional)	
Program: Bachelor Data Science and Knowledge Engineering	Course code: KEN3450
Examiner: Dr. Gerasimos (Jerry) Spanakis	Exam version: S
Date/time: Thursday, 5 th April 2017, 14.00-17.00h	Format: Open book exam
Allowed aides: Pens, simple (non-programmable) calculator from the I	OKE-list of allowed calculators.
Instructions to students:	

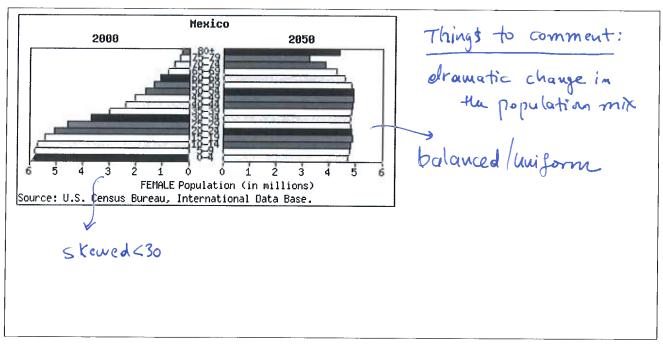
- The exam consists of 7 questions (plus one bonus question) on 15 pages.
- Fill in your name and student ID number on each page, including the cover page.
- Answer every question at the reserved space below the questions (keep your answers short and to the point). If
 you run out of space, continue on the back side, and if needed, use the extra blank page.
- Ensure that you properly motivate your answers.
- This exam sums to 50 points (plus 1 bonus point) and counts for 50% of your final grade. The rest 50% comes from data clinics (30%), data madness (10%) and Kaggle competition (10%)
- While you shouldn't spend too much time on calligraphy, please make sure that I have at least a chance at deciphering your exam.
- You are not allowed to have a communication device within your reach, nor to wear or use a watch.
- You have to return all pages of the exam. You are not allowed to take any sheets, even blank, home.
- If you think a question is ambiguous, or even erroneous, and you cannot ask during the exam to clarify this, explain this in detail in the space reserved for the answer to the question.
- If you have not registered for the exam, your answers will not be graded, and thus handled as invalid.
- Success!

The following table will be filled by the examiner:

Question:	1	2	3	4	5	6	7	В	Total
Maximum points:	7	8	7	8	6	7	7	1	51
Achieved points:									

Question 1: EDA warmup (7 Points)

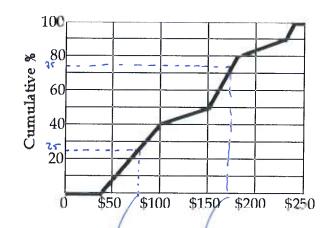
A.(1) At <u>www.census.gov</u> you can create a population pyramid for any country. These pyramids are back-to-back histograms. This pyramid shows Mexico's 2000 female population and the projection for 2050. Write *a few sentences* in order to summarize to your boss the changes that are forecast. Feel free to use (or not) any of the storytelling examples we discussed in class.



B. (1)

The weekly expenses for alcohol for a random person are summarized in the graph on the right. Estimate the IQR of these expenses.

- i) \$50
- ii) \$75
- (iii) \$100
- iv) \$150
- v) \$200



~75

Explanation (not needed, only if you are not sure):

Iar=43-41=175-75=100

-175

C. (1) Last weekend Maastricht police department ticketed 18 women whose mean speed was 72 km/h, and 30 men going an average of 64 km/h. Overall, what was the mean speed of all the people ticketed?

- i) 67 km/h
- ii) 68 km/h
- iii) 69 km/h
- iv) none of those
- v) it cannot be determined

Explanation (not needed, only if you are not sure):

- **D.** (4) A publishing company pays its sales staff \in 600 a week plus a commission of \in 0.50 per book sold. For example, a salesman who sold 440 books earned $600 + 0.50(440) = \in 820$.
- i.(2) The table on the right shows summary statistics for the number of books the sales staff sold last week. Fill in the table to show the statistics for the pay these people earned. Show your calculations below.

Statistic	Books	€
	sold	Earned
Mean	640	920
Standard Deviation	360	180
IQR	450	552
Maximum	1420	1310

	640 = 5 600 to . 50 × 640 = 12 to
wax:	1420 -> 600 + 0.50x 1420 = 1310
!! The	sder & IUR are not affected by the mean

640 - 600 +0 50x 640 -92 0

ii.(2) The newest employee had a pretty crazy selling week. Among all the salespeople, her pay corresponded to a *z-score* of +1.80. What was the *z-score* of the number of books she sold? Are you surprised by the result? Explain shortly.

Question 2: Traffic Delays (8 Points)

The US administration is trying to fight fake news about traffic jams in USA. A prominent data scientist used data that include information on the *Total Delay per Person* (hours per year spent delayed by traffic), the *Average Arterial Road Speed* (mph), the *Average Highway Road Speed* (mph), and the *Size* of the city (small, medium, large, very large). The regression model based on these variables is presented below. The variables *Small, Large* and *Very Large* are indicators which are 1 for cities of the named size and 0 otherwise.

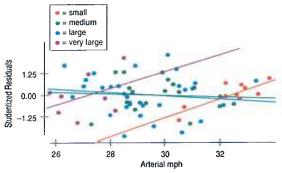
Dependent variable is: Total Delay per Person R-squared = 79.1% R-squared (adjusted) = 77.4%

Variable	Coefficient	SE (Coeff)	t-ratio	P-value
Intercept	139.104	16.69	8.33	< 0.0001
Arterial mph	-2.04836	0.6672	-3.07	0.0032
Hiway mph	-1.07347	0.2474	-4.34	< 0.0001
Small	-3.5897	2.953	-1.22	0.2287
Large	5.00967	2.104	2.38	0.0203
Very Large	3.41058	3.323	1.06	0.2951

- **A.(2)** Predict the Total Delay for a person with average arterial speed 30 mph, average highway speed 45 mph living in a large city.
- **B.(1)** Explain shortly how we interpret the R-squared in this case.
- C.(2) Explain how the coefficients *Small*, *Large* and *Very Large* account for the size of the city in the model. Why there is no coefficient for Medium? What is the interpretation of the value of coefficient *Large* in this particular regression model?

- A) total delay = 139.104 2,04836 x 30 1.07347 x45 + 5.00967 = 34,35672 hours/year
- 7) 79.1%. If the variance in the delay due to traffic can be explained by the variables sted in this undel
- C). medium is used as a baseline model
- add to the total delay (or reduce it) based on the
- darge: In a large city the effect on total delay is ~5 hours, given fixed values for all other variables

D.(3) Here is a plot of the residuals against the Arterial mph for the model fit above. The plot is colored according to City Size and regression lines are fit for each size.



Considering this display, would you conclude that including the indicator variables for the size of the city accomplished what is needed for the regression model? Explain shortly. Hint: Think about how we interpret categorical predictors

In the case of categorial variables what we expect to change the interrept (but the slope to remain the same) see slide 74 of Statistical larush

Since we don't see this figure, we assume that is was not that successful

Question 3: Cats & Dogs (7 points)

Consider the following two documents:

- D1: Dog eat dog. Eat cat too!
- D2: Eat home, it's raining cats and dogs.
- **A.(1)** What would be some standard pre-processing steps applied on these documents and what kind of problems are they expected to solve?
- **B.(2)** Given the pre-processing you did at **A.** what would be the cosine similarity of these documents in a typical information retrieval setup where we only care about raw term frequencies?
- C.(2) In a standard cosine-based tf-idf information retrieval system, can a query retrieve a document that does not contain any of the query words? Justify your answer properly.

A) - make everything (over case (Pog = dog) - remove punithation (, !) = lemmatitation (cats = cat, dogs = dog) - stop-word removal (too, it's,)									
B)	D1	2	eat 2	Cat	hone 0	rain			

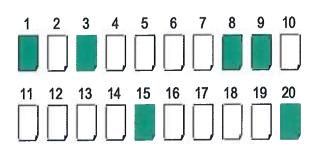
$$(2)(D1_1D2) = \frac{2\times 1 + 2\times 1 + 1\times 1 + 0\times 1 + 0\times 1}{\sqrt{2^2 + 2^2 + 1^2} \cdot \sqrt{1^2 + 1^2 + 1^2 + 1^2 + 1^2}}$$

$$= \frac{\sqrt{5}}{3}$$

(Note that if the retriever needs! to return somethy might bring roudon documents back)

Student ID:

D.(2) An information retrieval system returns the following ranked list for a particular query:



Colored blocks represent relevant documents; white blocks represent irrelevant documents. From the known relevance judgments, you know that there are eight relevant documents in total.

What is the overall precision and recall? What is the precision and recall at 10? Could you shortly explain why traditional recall measure might be unsatisfactory in question-answering systems?

$$P_{20} = \frac{6}{20} = 0.3$$

$$P_{10} = \frac{4}{10} = 0.4$$

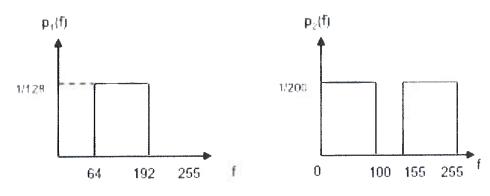
$$P_{20} = \frac{6}{8} = 0.75$$

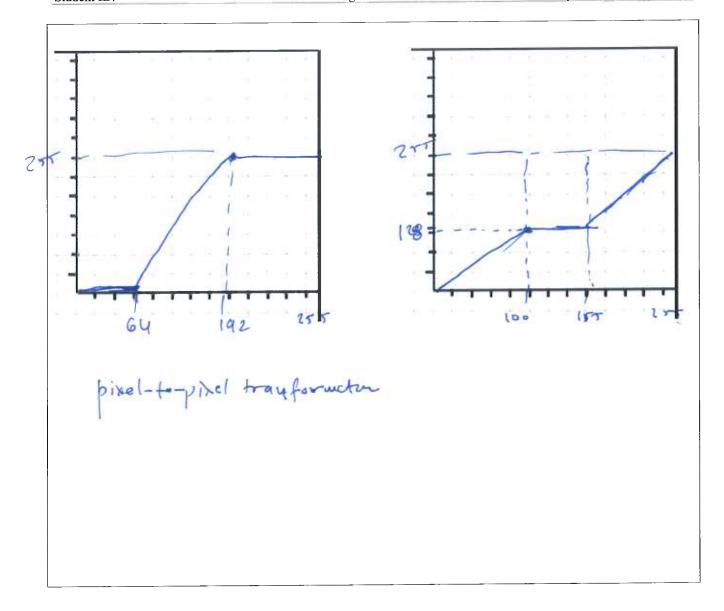
$$P_{10} = \frac{4}{10} = 0.4$$

$$P_{10} = \frac{4}{10$$

Question 4: An image is worth 1000 words (8 points)

A.(4) Given the following **normalized** histograms, sketch the appropriate pixel value transformations that will lead them to be enhanced (so have better contrast). You are given specific numbers (in the histograms below) so try to be as specific with the values for the x-axis (and as much as possible with y-axis). Justify your reasoning.





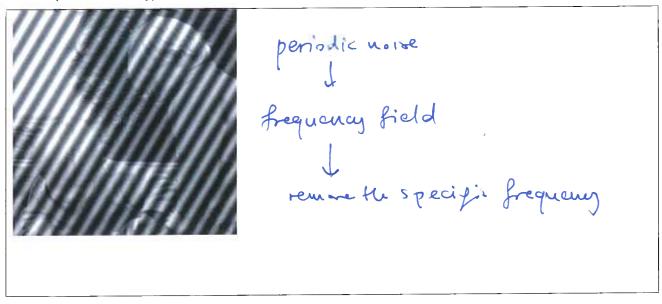
- B.(2) What you expect to happen to an image when we apply the following steps:
- i) smooth the original image (let's call it B) by an average filter, let's call the result image SB
- ii) subtract the smoothed image (SB) from the original one (B) let's call the result image DB
- iii) add DB (perhaps by a multiplying factor) to the original image (B)

Explain (shortly) your answer.

SB: a bit blurred DB: edges/details

BIDB: sharpenthe image & show the details

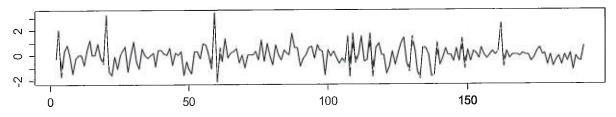
C.(2) You have the following image where we have added extra periodic noise. Explain shortly how you would (most effectively) remove this noise.



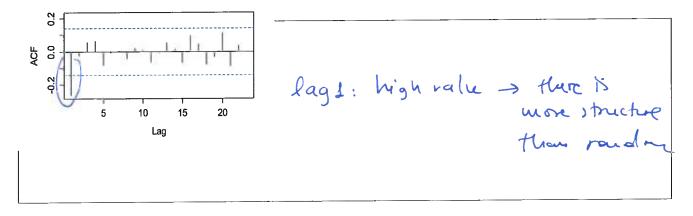
Question 5: Smart investments (6 points)

Jerry decided to start investing money in specific bonds. In the following plot you can see the daily changes in the return of a high-risk/high-reward bond for 200 consecutive days.

Daily Changes in the Return of an AT&T Bond



A.(2) Given the autocorrelation plot below, what can you say about the stationarity of the timeseries?



B.(2) Jerry fit an ARIMA(0,0,1) model and the results were the following:

Coefficients:

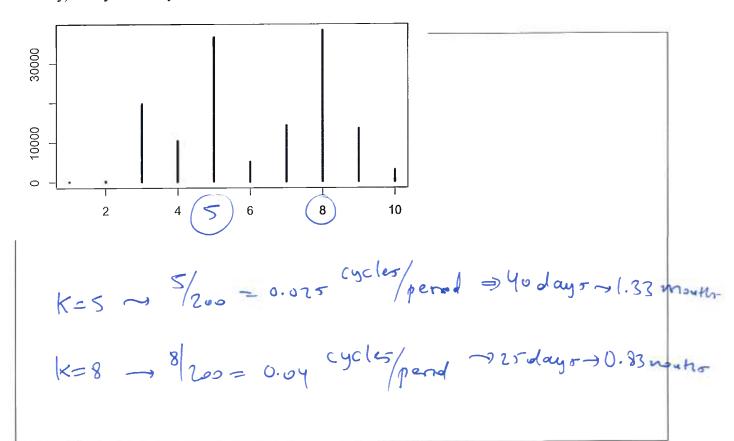
mal intercept -0.2865 -0.0247 s.e. 0.0671 0.0426

What information is this model using for future prediction? Write clearly the equation of the model and explain all variables involved.

$$\hat{X}_{t} = -0.0247 - 0.2967 \hat{e}_{t}$$

error term

C.(2) In order to find the most critical period of the timeseries (i.e. when important changes happen to the bond), Jerry got the following periodogram (x-axis shows the k-th Fourier frequencies and y-axis the spectral density). Can you identify which are the two most critical periods (in months) in this specific dataset?



Question 6: Dimensionality Reduction (7 points)

A.(5) A matrix (Q) contains ratings of 4 users (A,B,C,D) for 4 films (I,II,III,IV) and is decomposed using Singular Value Decomposition (SVD). The data scientist in charge decided to keep just 3 singular values (13.1, 3.9 and 1.6) and consequently (by dropping one dimension) the matrices U and V (of SVD) are:

$$U = \begin{bmatrix} -0.48 & -0.16 & -0.06 \\ -0.52 & -0.59 & -0.44 \\ -0.56 & 0.78 & 0.21 \\ -0.44 & -0.12 & 0.87 \end{bmatrix} \qquad V = \begin{bmatrix} -0.34 & -0.53 & -0.36 & -0.7 \\ 0.27 & -0.62 & 0.74 & -0.05 \\ 0.86 & -0.18 & -0.47 & -0.04 \end{bmatrix}$$

Form (just show, do not compute) how SVD (in the case of using 3 singular values) can reconstruct the original matrix Q. Can you predict the ratings f user A for films I and IV?

$$Q = U \cdot \Sigma \cdot V = \begin{bmatrix} U \\ V \\ 2/x? \\ 3/x3 \\ 3/x4 \end{bmatrix} \times \begin{bmatrix} 3.1 & 0 & 0 \\ 0 & 3.9 & 0 \\ 0 & 3.9 & 0 \\ 0 & 3.9 & 0 \\ 0 & 0.16 \end{bmatrix} \times \begin{bmatrix} -0.39 \\ 0.73 \\ 0.96 \end{bmatrix} = \begin{bmatrix} -6.288 & -0.629 & -0.096 \end{bmatrix} \times \begin{bmatrix} -0.79 \\ 0.27 \\ 0.86 \end{bmatrix} = 1.88$$
Similarly:
$$Q_{A-IV} = 4.36078$$

B.(2) Using the example above (and/or other intuitive examples), mention one reason to use SVD versus one reason to use Non-Negative Matrix Factorization (NMF) for the case of movie ratings.

e.g.

SVD: unique decomposition/solution

NMF: mon-negative value-

Question 7: Regularization magic (7 points)

One bright student tried to fit a Ridge regression model where many of the variables were correlated to each other. The student quickly noticed that Ridge tends to give similar coefficient values to the correlated variables. Let's prove this property with a simple intuitive example.

Suppose that n = 2 (i.e. 2 data points) and p = 2 (i.e. 2 coefficients). Furthermore, we assume that $x_{11} = x_{12}$, $x_{21} = x_{22}$ and that $y_1 + y_2 = 0$ and $x_{11} + x_{21} = 0$ and $x_{12} + x_{22} = 0$, so that the estimate for the intercept in (solving the simple linear regression using least squares), is zero: $\hat{\beta} = 0$.

A.(2) Write out the ridge regression optimization problem in this setting (in its simplest form, given the simplifications given above).

Coveral Ridge: min
$$\sum_{i=1}^{m} (y_i - b_0 - \sum_{j=1}^{n} x_{i\tau})^2 + \lambda. \sum_{j=1}^{n} y_{j}^2$$

In this setting: $b_0 = 0$, $x_{11} = x_{12} = x_1$, $x_{21} = x_{22} = x_2$
when $(y_1 - b_1 x_1 - b_2 x_1)^2 + (y_2 - b_1 x_2 - b_2 x_2)^2 + \lambda.(b_1 + b_2)^2$

B.(5) Argue that in this setting (and under the simplifications we did), the ridge coefficient estimates satisfy $\hat{\beta}_1 = \hat{\beta}_2$. Hint: Attempt solving the optimization problem of the previous question in order to find the $\beta 1$ and $\beta 2$. Given the simplifications we did, it should be easy to compute.

The derivative of a function $f(x)=g^2(x)$ is f'(x)=2 g(x) g'(x), where g' is the derivative of g.

one possible way:

$$\frac{\partial Q}{\partial b_{1}} = 2 \cdot (y_{1} - b_{1} \times 1 - b_{2} \times 1) (-x_{1}) + 2(y_{2} - b_{1} \times 2 - b_{1} \times 2) (-x_{1}) + 2ab_{1} = 0$$

$$-y_{1} \times 1 + b_{2} \times 1^{2} + x_{1}^{2} \cdot b_{1}^{2} - x_{2}y_{2} + b_{2} \times x_{2}^{2} + x_{2}^{2} \cdot b_{1}^{2} + 1ab_{1}^{2} = 0$$

$$(x_{1}^{2} + x_{2}^{2} + 1) \cdot b_{1} = x_{1} y_{1} + x_{2} y_{2} - b_{1}^{2} (x_{1}^{2} + x_{2}^{2})$$

$$\frac{\partial Q}{\partial b_{1}} = x_{1} y_{1} + x_{2} y_{2} + b_{1}^{2} (x_{1}^{2} + x_{2}^{2})$$

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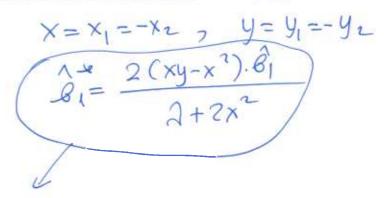
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If we take $\frac{\partial a}{\partial \hat{r}}$, due to symmetry we will have that $\hat{Q}_{2} = \frac{2(xy-x^{2})B_{2}}{2+2x^{2}}$

which we und that By = lo

Bonus Question (1 point)

Complete the next verse:

All the leaves are brown / And the sky is grey / I've been for a walk / On a winter's day...

Student name:

Student ID:

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Extra answer sheet.