

option

command

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command

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option

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control

$$51 - \underline{110011} = 110011 \times 2^{-7}$$

module 2]

$$\begin{array}{ccccccccc} & 14 & 13 & 4 & -0 & \rightarrow & 10 & 4 = 5 & 7 \\ 3.1] & E & D & 0100 & 0000 & 0111 & 1010 & 0100 = 0101 & 0111 \\ 0101 & 1110 & 1101 & 0100 & & & 0011 & 0011 & 0000 \end{array}$$

$$\begin{array}{r} 5 \text{ E } \text{D} 4 \\ - 07 \text{ A } 4 \end{array}$$

$$\begin{array}{r} 0101 \quad 1110 \quad 1101 \quad 0100 \\ + 1411 \\ \hline 0000 \quad 0111 \quad 1010 \quad 0100 \end{array}$$

$$\begin{array}{r} 4 \cancel{+} 0100 \rightarrow 0111 + 1 = 1000 \\ \cancel{A} \cancel{+} 1010 \rightarrow 0101 \end{array}$$

sign bit not set so calculation same as above

$$3.3] \quad 5 \text{ E } \text{D} 4 \quad 0101 \quad 1110 \quad 1101 \quad 0100$$

Each hexadecimal number = 4 bits, saves time and space. 1 byte = 2 hexa-digits

$$\begin{array}{r} 4365 \\ - 3412 \\ \hline 2293 \end{array}$$

$4365 \rightarrow 4 \cdot 8^3 + 3 \cdot 8^2 + 6 \cdot 8^1 + 5 \cdot 8^0 = 0753_8$

$$\begin{array}{r} 4365 \\ - 3412 \\ \hline 2293 \end{array}$$

$4365 \rightarrow 0100 \ 0011 \ 0110 \ 0101 \rightarrow 2293$   
 $3412 \rightarrow 0011 \ 0100 \ 0001 \ 0010 \rightarrow 1802$   
 $2293 + 1802 = 491 \quad [0753_8]$   
 $3 + 40 + 60.7 = 491$

Encoded oct	4365
Bin	100 011 110 101
Sign	1
Magnitude Bin	00 011 110 101
Oct	365

$$3.6] \quad 185 = 128 + 32 + 16 + 8 + 1 = 10111001$$

$$122 = 64 + 32 + 16 + 8 + 2 = 122 = 01111010$$

00111111 header

$$\begin{array}{r} 10111001 \\ - 01111010 \\ \hline 111011 \end{array}$$

$\begin{array}{r} 1 \\ 1 \\ 1 \\ 1 \\ 0 \\ 0 \\ 1 \\ 0 \\ 1 \\ 0 \\ 1 \\ 0 \end{array}$

$$\begin{array}{r} 122 \\ 64 \\ 58 \\ 26 \\ 16 \\ 10 \\ 2 \end{array}$$

$$3.7] \quad 185 \quad | \quad 0111001$$

$$\begin{array}{r} 122 \\ 64 \\ 58 \\ 26 \\ 16 \\ 10 \\ 2 \end{array}$$

$01111010$   
 $10011001$  overflow

$$3.5] \quad \begin{array}{r} 4365 \\ 3412 \end{array} \quad \begin{array}{r} \text{binary} \\ 011 \end{array} \quad \begin{array}{r} \text{decimal} \\ 110 \end{array} \quad \begin{array}{r} \text{decimal} \\ 101 \end{array} \quad \begin{array}{r} 0 \\ -245 \end{array}$$

$$3412 \quad 011 \quad \begin{array}{r} \text{binary} \\ 100 \end{array} \quad \begin{array}{r} \text{decimal} \\ 001 \end{array} \quad \begin{array}{r} \text{decimal} \\ 010 \end{array} \quad \begin{array}{r} 0 \\ 1802 \end{array}$$

$$4365 \quad 100 \quad 011 \quad 110 \quad 101$$

$$3412 \quad 011 \quad 100 \quad 001 \quad 010 \quad \rightarrow 1802$$

$$\begin{array}{r} 0 \\ 4365 \\ -245 \\ \hline 1557 \end{array}$$

$$\begin{array}{r} 0 \\ \text{dec} \\ \text{sum} \end{array}$$

begin next  
dec 1557  
→ 1001

How do I convert to  
Octal?

$$\begin{array}{r} \text{Octal} \\ 3777 \end{array}$$

return

Z X C V B N M < > ? / shift  
option command

⌘ command ⌘ option ⌘ control

3.8] A 185      10111001 → -57  
       -B 122      01111010 → 122  
             signed      too small → -179  
             (look at hints)      overflow  
             in module 2      Underflow

overflow

underflow

underflow

185 in binary  
 1 0 1 1 1 0 0 1  
 128 64 32 16 8 4 2 1  
 195 20  
 128 16  
 57 9  
 32 8  
 25 7

3.9] 214      11010110      binary  
       151      10010111      two's  
                     00101001 → 00101010  
                     01101000 → 01101001

decimal

-105

-42

decimal → binary conversion  
 214 → 1 0 1 0 1 0 1 0  
 128 64 32 16 8 4 2 1  
 214 128 64 32 16 8 4 2 1  
 80 64 32 16 8 4 2 1  
 20 16 8 4 2 1  
 0 0 0 0 0 0 0 1

A      00101010  
 01101001  
 10010011 ← -147 ?

Sum of two positive numbers = negative so overflow

3.10] A ⊕ B 151 - 214  
       151      10010111      binary  
       214      11010110      two's complement  
                     01101000 + 1 → 01101001  
                     00101001 + 1 → 00101010  
                     [00111111] → 63 → -63

3.11] 151      10010111      binary  
       214      11010110      add  
                     1) 01101101 ← 365      overflow  
                     2) check right

3.12] A.  $3.984375 \times 10^{-1} = 1.1001100000 \times 2^{-2}$  (see side note)  $A + B = 10.1111000000 \times 2^{-2}$   
 B.  $3.4375 \times 10^{-1} = 1.0110000000 \times 2^{-2}$   
 C.  $1.771 \times 10^3 = 1.1011.01011 \times 2^{10}$

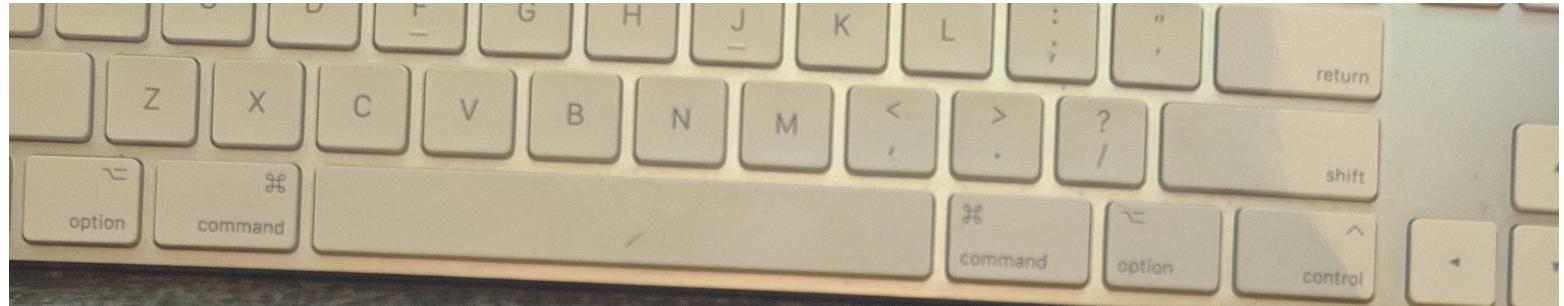
0.0000000000 | 0111100000  $\times 2^{10}$   
 + 1.1011101011  
 1.101110101101  
 guard

side note  
 $3.984375 \times 10^{-1}$

$= 0.3984375 \leftarrow$  convert to decimal

$= \frac{51}{128} = \frac{110011}{2^7} = 110011 \times 2^{-7}$   
 $= 1.10011 \times 2^{-2}$

round  
 $1.1011101100 \times 2^{10}$   
 $= 11011101100_2 = 1772$



$$3.33 \quad 3.984375 \times 10^{-1} = 0.3984375 \text{ is decimal } \rightarrow \frac{5}{128} = \frac{110011}{2^7} = 110011 \times 2^{-7} = 1.10011 \times 2^{-2}$$

$$1.1771 \times 10^3 = 1771 \text{ in decimal} \quad \begin{array}{r} 0 \\ 1 \\ 0 \\ 0 \\ 1 \\ 1 \\ 0 \\ 1 \\ 1 \\ 0 \\ 1 \\ 1 \end{array} = 1,101101011 \times 2^{10}$$

$$\begin{array}{r} 114 \\ 64 \\ 50 \\ \hline 72 \\ 12 \\ \hline 16 \end{array}$$

$$1.1010011 \times 2^{-8} + 0.000000000110011 \times 2^{10} = 1.10111010111 \times 2^{10}$$

3.34] It does not equal, Not associative