

$$1) A = \begin{bmatrix} 0 & -2 & 1 \\ 1 & -1 & 0 \\ 0 & 0 & 2 \end{bmatrix} \text{ so } |A| = 2 \cdot 1 \cdot 2 = 4$$

$$|AB| = |A||B| = \boxed{24}$$

$$B = \begin{bmatrix} 3 & 0 & 0 \\ -2 & 1 & 0 \\ 4 & -4 & 2 \end{bmatrix} \text{ so } |B| = 3 \cdot 1 \cdot 2 = 6$$

$$2) A = \begin{bmatrix} 2 & -1 & 1 \\ 0 & 2 & 6 \\ 0 & 0 & 3 \end{bmatrix} \text{ so } |A| = 3 \cdot 1 \cdot 4 = 12 \text{ so } |A^{-1}| = \boxed{\frac{1}{12}}$$

$$3) A = \begin{bmatrix} -1 & 2 \\ 2 & 3 \end{bmatrix} \text{ so } |A| = -3 - 4 = -7 \text{ so } |3AA^T| = 3^2 \cdot (-7) = \boxed{441}$$

$$= |A^T|$$

$$\text{check: } 3AA^T = 3 \begin{bmatrix} -1 & 2 \\ 2 & 3 \end{bmatrix} \begin{bmatrix} -1 & 2 \\ 2 & 3 \end{bmatrix} = \begin{bmatrix} -3 & 6 \\ 6 & 9 \end{bmatrix} \begin{bmatrix} -1 & 2 \\ 2 & 3 \end{bmatrix} = \begin{bmatrix} 15 & 12 \\ 12 & 39 \end{bmatrix} = \boxed{441}$$

$$4) A = \begin{bmatrix} 2 & 0 \\ 3 & 1 \end{bmatrix} \text{ so } |A| = 2 \text{ so } |A^{-1}| = \boxed{\frac{1}{2}}$$

$$b) \text{ find } A^{-1} = \begin{bmatrix} 2 & 0 & 1 & 0 \\ 3 & 1 & 0 & 1 \end{bmatrix} \rightarrow \begin{bmatrix} 3 & 1 & 0 & 1 \\ 2 & 0 & 1 & 0 \end{bmatrix} \rightarrow \begin{bmatrix} 1 & 1 & -1 & 1 \\ 2 & 0 & 1 & 0 \end{bmatrix} \rightarrow \begin{bmatrix} 1 & 1 & -1 & 1 \\ 0 & -2 & 3 & -2 \end{bmatrix} \rightarrow \begin{bmatrix} 1 & 0 & \frac{1}{2} & 0 \\ 0 & 1 & \frac{3}{2} & 1 \end{bmatrix}$$

$$\text{so } A^{-1} = \begin{bmatrix} \frac{1}{2} & 0 \\ -\frac{3}{2} & 1 \end{bmatrix} \text{ and } |A^{-1}| = \boxed{\frac{1}{2}}$$

$$5) A = \begin{bmatrix} 1 & 2 \\ 2 & 4 \end{bmatrix} \quad B = \begin{bmatrix} 1 & 0 \\ 0 & 2 \end{bmatrix} \text{ so } A+B = \begin{bmatrix} 2 & 2 \\ 2 & 6 \end{bmatrix} \text{ and } |A+B| = 12 - 4 = 8$$

$$|A| = 4 - 4 = 0 \quad |B| = 2 \quad |A| + |B| = 2 \quad |A| + |B| \neq |A+B|$$

$$6) \text{ Singular when } |A| = 0 \quad (-5 - t)(7 - t) = 32$$

$$\begin{aligned} -35 + 4t - 12t &= 32 \\ +2 - 12t + 6 &= 32 \\ -35 + 5t - 7t + 2 &= -32 \\ +2 - 2t - 3 &= 0 \end{aligned}$$

$$(t + 1)(t - 3) = 0$$

$$t = \boxed{\{3, -1\}}$$