Homework 2

7 Convelutional Neural Networks

7.1 From Fully Connected Layers to Convolution

Lets say we have a fully labeled collection of one-megapixel photographs of cats and dogs to distinguish. This is $10^6 \times 10^3 = 10^9$ parameters. This is an unfeasable amount of parameters to learn. As such we employ convolutional neural networks as a way to exploit the known structure in natural images

Take Where's Waldo, what Waldo looks like does not depend on Waldo's location. We could break the image into patches and assign a score to each patch, and CNNs systematize this idea of spacial invariance.

We can now make intuitions: In earlier layers, our network should respond similarly to the same patch, regardless of where it is in the images, focusing on local reigions. Deeper layer should aim to capture longer rage features of the image.

We start by representing the image X and intermediate hidden representation H as matrices, both with the same shape. X[i,j] and H[i,j] denotes pixel location.

 $H[i,j] = U[i,j] + sum_a(sum_b(V[i,j,a,b] X[i+a, j+b]))$ Where U contains biases and V is weights. becase we have i+a and j+b we can run over positive and negative offsets centered around i,j.

For this single layer we now need 10^12 parameters.

First Principle: Translation invariance means that a shift in X should result in a shift in H, which is only possible if V and U do not depend on [i,j]. We simplyify U to constant u and remove i and j from V:

 $H[i,j] = u + sum_a(sum_b(V[a,b] X[i+a, j+b]))$ This is a convolution, as we are weight pixels at i+a and j+b to obtain H[i,j] using V[a,b]. As we remove V depending on the location and simplifying U, we reduce the number of paramters from 10^12 to 4×10^6

Second Principle: Locality, we should not have to look far from [i,j] to glean relegant information, as such outputide some range $|a| > \Delta$ or $|b| > \Delta V[a,b] = 0$.

H[i,j] = u + sum[a = - Δ to Δ](sum[b = - Δ to Δ](V[a,b] X[i+a, j+b])) This reduces parameters from 4 x 10^6 to 4 Δ^2 , where Δ is typically smaller than 10.

With this we have reduced an image from billions of paramaeters to just several hundred, without altering dimensionality. However now this exclusivly works on local areas, we must

interleave nonlinearities and convolutional layers repeatedly to account for deeper layers needing to generalise the entire image.

However this is entirely based on non-colour images, if we include 3 channel colours instead of V[a,b] we now have V[a,b,c]. Additionally we want an entire vector of hidden representations to correspond to each spatial location. So we now have

```
H[i,j] = u + sum[a = -\Delta to \Delta](sum[b = -\Delta to \Delta](sum[c](V[a,b,c,d] X[i+a, j+b, c])))
```

where d index the output channels in hidden representations H

7.2 Convolutions for Images

```
In [1]:
        import torch
        from torch import nn
        from d2l import torch as d2l
In [2]: \# take a matrix and multiply by kernal gives new matrix size n[h] \times n[w] minus conv
        \# (n[h] - k[h] + 1) \times (n[w] - k[w] + 1)
        def corr2d(X, K):
            h, w = K.shape
            Y = torch.zeros((X.shape[0] - h + 1, X.shape[1] - w + 1))
            for i in range(Y.shape[0]):
                for j in range(Y.shape[1]):
                    Y[i, j] = (X[i:i + h, j:j + w] * K).sum()
            return Y
        X = torch.tensor([[0.0, 1.0, 2.0], [3.0, 4.0, 5.0], [6.0, 7.0, 8.0]])
        K = torch.tensor([[0.0, 1.0], [2.0, 3.0]])
        corr2d(X, K)
Out[3]: tensor([[19., 25.],
                 [37., 43.]])
In [4]: # Convolutional layer cross-correlates the input and kernel and adds a scalar bias
        class Conv2D(nn.Module):
            def __init__(self, kernel_size):
                super().__init__()
                self.weight = nn.Parameter(torch.rand(kernel size))
                self.bias = nn.Parameter(torch.zeros(1))
            def forward(self, x):
                return corr2d(x, self.weight) + self.bias
In [5]: # here is a simple application, detecting the edge of an object by finding the firs
        X = torch.ones((6, 8))
        X[:, 2:6] = 0
        Χ
```

```
Out[5]: tensor([[1., 1., 0., 0., 0., 0., 1., 1.],
                [1., 1., 0., 0., 0., 0., 1., 1.],
                [1., 1., 0., 0., 0., 0., 1., 1.],
                [1., 1., 0., 0., 0., 0., 1., 1.],
                [1., 1., 0., 0., 0., 0., 1., 1.],
                [1., 1., 0., 0., 0., 0., 1., 1.]
In [6]: # kernel with height 1 and width 2, if horizontally adjacent elements are the same,
        K = torch.tensor([[1.0, -1.0]])
In [7]: # 1 from white to black, -1 from black to white
        Y = corr2d(X, K)
        Υ
Out[7]: tensor([[ 0., 1., 0., 0., 0., -1., 0.],
                [0., 1., 0., 0., 0., -1., 0.],
                [0., 1., 0., 0., 0., -1., 0.],
                [0., 1., 0., 0., 0., -1., 0.],
                [0., 1., 0., 0., 0., -1., 0.],
                [0., 1., 0., 0., 0., -1., 0.]
In [8]: # if we apply the kernel to transposed image we get nothing as it cannot detect ver
        corr2d(X.t(), K)
Out[8]: tensor([[0., 0., 0., 0., 0.],
                [0., 0., 0., 0., 0.]
                [0., 0., 0., 0., 0.]
                [0., 0., 0., 0., 0.]
                [0., 0., 0., 0., 0.]
                [0., 0., 0., 0., 0.]
                [0., 0., 0., 0., 0.]
                [0., 0., 0., 0., 0.]
In [9]: # this system is greate if we know what we are looking for, however at larger kerne
        # attemping to learn the kernel
        # two dimensional convolutional layer, kernel shape 1x2
        conv2d = nn.LazyConv2d(1, kernel_size=(1, 2), bias=False)
        # four dimensional input, 1 dimensional output
        # (batch size, channel, height, width), batch size and channels are 1
        X = X.reshape((1, 1, 6, 8))
        Y = Y.reshape((1, 1, 6, 7))
        # Learning rate
        lr = 3e-2
        for i in range(10):
            Y hat = conv2d(X)
            1 = (Y_hat - Y) ** 2
            conv2d.zero_grad()
            1.sum().backward()
            # update kernel
            conv2d.weight.data[:] -= lr * conv2d.weight.grad
```

```
if (i + 1) \% 2 == 0:
                 print(f'epoch {i + 1}, loss {l.sum():.3f}')
        epoch 2, loss 17.597
        epoch 4, loss 5.814
        epoch 6, loss 2.148
        epoch 8, loss 0.841
        epoch 10, loss 0.338
In [10]: conv2d.weight.data.reshape((1, 2))
Out[10]: tensor([[ 1.0471, -0.9279]])
         7.3 Padding and Stride
         # if we start off with a 240x240 image, 10 layers of 5x5 convolutions, we reduce th
In [11]:
         import torch
         from torch import nn
In [12]: # we can pad a 3x3 input to 5x5, and output a 4x4 matrix if we use a 2x2 kernel. As
         # here is a convolutional layer with height and width of 3, apply 1 pixel padding.
         def comp_conv2d(conv2d, X):
             X = X.reshape((1, 1) + X.shape)
             Y = conv2d(X)
             # strip batch size and channels
             return Y.reshape(Y.shape[2:])
         # padding 1 row/column each side
         conv2d = nn.LazyConv2d(1, kernel_size=3, padding=1)
         X = torch.rand(size=(8, 8))
         comp_conv2d(conv2d, X).shape
Out[12]: torch.Size([8, 8])
In [13]: # kernel height 5, width 3
         conv2d = nn.LazyConv2d(1, kernel_size=(5, 3), padding=(2, 1))
         comp_conv2d(conv2d, X).shape
Out[13]: torch.Size([8, 8])
In [14]: # instead of moving 1 by 1 by 1 pixel each time, we could skip a pixel or two, this
         conv2d = nn.LazyConv2d(1, kernel_size=3, padding=1, stride=2)
         comp_conv2d(conv2d, X).shape
         # in this case input height and width is halved as a result
Out[14]: torch.Size([4, 4])
In [15]: conv2d = nn.LazyConv2d(1, kernel_size=(3, 5), padding=(0, 1), stride=(3, 4))
         comp_conv2d(conv2d, X).shape
Out[15]: torch.Size([2, 2])
```

7.4 Multiple Input and Multiple Output Channcels

```
# previously we just considered multiple input and output as multiple single input
         # Adding additional channels transforms it into tree-dimensional tensor. We will lo
         import torch
         from d2l import torch as d2l
         # we need our kernal to have the same number of channels as input.
         # we use this to perform cross-correlation with input data
         def corr2d_multi_in(X, K): # perform cross correlation per channel and add them up
             return sum(d21.corr2d(x, k) for x, k in zip(X, K))
In [18]: X = \text{torch.tensor}([[[0.0, 1.0, 2.0], [3.0, 4.0, 5.0], [6.0, 7.0, 8.0]]),
                         [[1.0, 2.0, 3.0], [4.0, 5.0, 6.0], [7.0, 8.0, 9.0]]])
         K = torch.tensor([[[0.0, 1.0], [2.0, 3.0]], [[1.0, 2.0], [3.0, 4.0]]])
         corr2d_multi_in(X, K)
Out[18]: tensor([[ 56., 72.],
                  [104., 120.]])
In [19]: # it is essential to have multiple channels at each layer. In most popular models w
         # the shape of the kernel is co x ci x kh x kw. co and ci are input and output chan
         def corr2d multi in out(X, K):
             return torch.stack([corr2d_multi_in(X, k) for k in K], 0)
In [20]: # triviual kernel with three output channels
         K = torch.stack((K, K + 1, K + 2), 0)
         K.shape
Out[20]: torch.Size([3, 2, 2, 2])
In [21]: corr2d multi in out(X, K)
Out[21]: tensor([[[ 56., 72.],
                   [104., 120.]],
                  [[ 76., 100.],
                   [148., 172.]],
                  [[ 96., 128.],
                   [192., 224.]]])
In [22]: # 1 x 1 kernel
         def corr2d_multi_in_out_1x1(X, K):
             c_i, h, w = X.shape
             c_0 = K.shape[0]
             X = X.reshape((c_i, h * w))
             K = K.reshape((c_o, c_i))
             Y = torch.matmul(K, X) # matrix multiplication in fully connected layer
             return Y.reshape((c_o, h, w))
```

```
X = torch.normal(0, 1, (3, 3, 3))
K = torch.normal(0, 1, (2, 3, 1, 1))
Y1 = corr2d_multi_in_out_1x1(X, K)
Y2 = corr2d_multi_in_out(X, K)
assert float(torch.abs(Y1 - Y2).sum()) < 1e-6</pre>
```

7.5 Pooling

```
In [23]: # pooling layers serves the dual purpose of mitigating the sensetivity of convoluti
         import torch
         from torch import nn
         from d2l import torch as d2l
         # average pooling takes the average of the elements in the pooling window and reduc
In [24]:
         # max pooling takes the maximum of all the elements in the pooling window
         def pool2d(X, pool_size, mode='max'):
             p_h, p_w = pool_size
             Y = torch.zeros((X.shape[0] - p_h + 1, X.shape[1] - p_w + 1))
             for i in range(Y.shape[0]):
                 for j in range(Y.shape[1]):
                     if mode == 'max':
                         Y[i, j] = X[i: i + p_h, j: j + p_w].max()
                     elif mode == 'avg':
                         Y[i, j] = X[i: i + p_h, j: j + p_w].mean()
             return Y
In [25]: X = torch.tensor([[0.0, 1.0, 2.0], [3.0, 4.0, 5.0], [6.0, 7.0, 8.0]])
         pool2d(X, (2, 2))
Out[25]: tensor([[4., 5.],
                 [7., 8.]])
In [26]: pool2d(X, (2, 2), 'avg')
Out[26]: tensor([[2., 3.],
                 [5., 6.]])
In [27]: # as with convolutional layers, we can adjust the shape through padding and stride
         X = torch.arange(16, dtype=torch.float32).reshape((1, 1, 4, 4))
         Χ
Out[27]: tensor([[[[ 0., 1., 2., 3.],
                   [4., 5., 6., 7.],
                    [8., 9., 10., 11.],
                    [12., 13., 14., 15.]]])
```

```
In [28]: # with a pooling window of (3, 3), we get a stride shape of (3, 3)
         pool2d = nn.MaxPool2d(3, padding=1, stride=2)
         pool2d(X)
Out[28]: tensor([[[[ 5., 7.],
                   [13., 15.]]])
In [29]: # we can have arbitary rectangular pooling windows too
         pool2d = nn.MaxPool2d((2, 3), stride=(2, 3), padding=(0, 1))
         pool2d(X)
Out[29]: tensor([[[[ 5., 7.],
                   [13., 15.]]])
In [30]: # for multiple layers it processes each layer individually
         X = torch.cat((X, X + 1), 1)
Out[30]: tensor([[[[ 0., 1., 2., 3.],
                   [4., 5., 6., 7.],
                   [8., 9., 10., 11.],
                   [12., 13., 14., 15.]],
                  [[1., 2., 3., 4.],
                   [5., 6., 7., 8.],
                   [ 9., 10., 11., 12.],
                   [13., 14., 15., 16.]]])
In [31]: pool2d = nn.MaxPool2d(3, padding=1, stride=2)
         pool2d(X)
Out[31]: tensor([[[[ 5., 7.],
                   [13., 15.]],
                  [[ 6., 8.],
                   [14., 16.]]])
         7.6 Convolutional Neural Networks
In [32]:
         import torch
         from torch import nn
         from d2l import torch as d2l
In [33]: # initialize weights
         def init_cnn(module):
             if type(module) == nn.Linear or type(module) == nn.Conv2d:
                 nn.init.xavier_uniform_(module.weight)
         # LeNet 5 model
         class LeNet(d21.Classifier):
             def __init__(self, lr=0.1, num_classes=10):
                 super().__init__()
                 self.save_hyperparameters()
                 self.net = nn.Sequential(
                     nn.LazyConv2d(6, kernel_size=5, padding=2), nn.Sigmoid(),
```

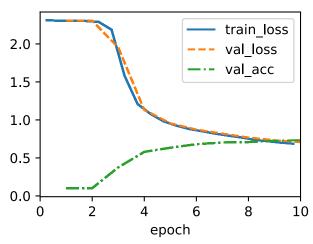
```
nn.AvgPool2d(kernel_size=2, stride=2),
nn.LazyConv2d(16, kernel_size=5), nn.Sigmoid(),
nn.AvgPool2d(kernel_size=2, stride=2),
nn.Flatten(),
nn.LazyLinear(120), nn.Sigmoid(),
nn.LazyLinear(84), nn.Sigmoid(),
nn.LazyLinear(num_classes))
```

```
In [34]: # summary of all the layer sizes
@d21.add_to_class(d21.Classifier)
def layer_summary(self, X_shape):
    X = torch.randn(*X_shape)
    for layer in self.net:
        X = layer(X)
        print(layer.__class__.__name__, 'output shape:\t', X.shape)

model = LeNet()
model.layer_summary((1, 1, 28, 28))
```

```
Conv2d output shape:
                         torch.Size([1, 6, 28, 28])
Sigmoid output shape:
                         torch.Size([1, 6, 28, 28])
AvgPool2d output shape: torch.Size([1, 6, 14, 14])
Conv2d output shape:
                         torch.Size([1, 16, 10, 10])
Sigmoid output shape:
                         torch.Size([1, 16, 10, 10])
AvgPool2d output shape: torch.Size([1, 16, 5, 5])
Flatten output shape:
                         torch.Size([1, 400])
Linear output shape:
                         torch.Size([1, 120])
Sigmoid output shape:
                         torch.Size([1, 120])
Linear output shape:
                         torch.Size([1, 84])
Sigmoid output shape:
                         torch.Size([1, 84])
Linear output shape:
                         torch.Size([1, 10])
```

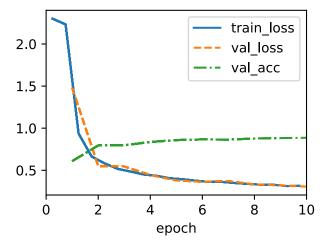
```
In [35]: # training LeNet
    trainer = d21.Trainer(max_epochs=10, num_gpus=1)
    data = d21.FashionMNIST(batch_size=128)
    model = LeNet(lr=0.1)
    model.apply_init([next(iter(data.get_dataloader(True)))[0]], init_cnn)
    trainer.fit(model, data)
```



8.2 Networks Using Blocks

```
In [36]: import torch
         from torch import nn
         from d2l import torch as d2l
In [37]: # the design of nerual network architectures has grown more abstract, moving from i
         # a CNN is a sequence of convolutional layers, nonlinear activation functions, and
         # One key idea is to use multiple convolutions in between downsampling, i.e. two 3x
         # VGG consists of a sequence of convolutions with 3x3 layers with padding of 1 to k
         # this code is to implement one VGG block
         def vgg_block(num_convs, out_channels):
             layers = []
             for _ in range(num_convs):
                 layers.append(nn.LazyConv2d(out_channels, kernel_size=3, padding=1))
                 layers.append(nn.ReLU())
             layers.append(nn.MaxPool2d(kernel_size=2,stride=2))
             return nn.Sequential(*layers)
In [38]: | # one major advantage is that it is primarily composed of these blocks, compared to
         # VGG defines a family of networks rather than a specific manifestation, and we can
         class VGG(d21.Classifier):
             def __init__(self, arch, lr=0.1, num_classes=10):
                 super().__init__()
                 self.save_hyperparameters()
                 conv_blks = []
                 for (num_convs, out_channels) in arch:
                     conv_blks.append(vgg_block(num_convs, out_channels))
                 self.net = nn.Sequential(
                     *conv_blks, nn.Flatten(),
                     nn.LazyLinear(4096), nn.ReLU(), nn.Dropout(0.5),
                     nn.LazyLinear(4096), nn.ReLU(), nn.Dropout(0.5),
                     nn.LazyLinear(num_classes))
                 self.net.apply(d21.init_cnn)
         # the original VGG network had 5 convolutional blocks, the first two with one convo
         # the first block has 64 output channels and each subsequent block doubles the numb
         VGG(arch=((1, 64), (1, 128), (2, 256), (2, 512), (2, 512))).layer_summary(
             (1, 1, 224, 224))
        Sequential output shape:
                                         torch.Size([1, 64, 112, 112])
        Sequential output shape:
                                         torch.Size([1, 128, 56, 56])
                                         torch.Size([1, 256, 28, 28])
        Sequential output shape:
        Sequential output shape:
                                         torch.Size([1, 512, 14, 14])
                                         torch.Size([1, 512, 7, 7])
        Sequential output shape:
        Flatten output shape:
                                 torch.Size([1, 25088])
        Linear output shape:
                                 torch.Size([1, 4096])
        ReLU output shape:
                                 torch.Size([1, 4096])
        Dropout output shape:
                                 torch.Size([1, 4096])
        Linear output shape:
                                 torch.Size([1, 4096])
        ReLU output shape:
                                 torch.Size([1, 4096])
        Dropout output shape:
                                 torch.Size([1, 4096])
        Linear output shape:
                                 torch.Size([1, 10])
In [40]: # we are training here with a smaller number of channels to decrease computation til
```

```
model = VGG(arch=((1, 16), (1, 32), (2, 64), (2, 128), (2, 128)), lr=0.01)
trainer = d2l.Trainer(max_epochs=10, num_gpus=1)
data = d2l.FashionMNIST(batch_size=128, resize=(224, 224))
model.apply_init([next(iter(data.get_dataloader(True)))[0]], d2l.init_cnn)
trainer.fit(model, data)
```



8.6 Residual Networks

```
In [41]: import torch
    from torch import nn
    from torch.nn import functional as F
    from d2l import torch as d2l
```

It is important to know how adding layers can increase complexity and expressibeness of the network, and design networks where adding layers makes networks more expressive rather than just different.

If larger function classes contain smaller ones, we are guaranteed that increasing them strictly increases expressive power of a network. For deep neural networks, if we can train the newly added layer into an identity function, the new model will be just as effective as the original

This leads to the discovery of a residual block. If we have f(x) where x is the input, the activation function must directly learn from x, however if we take the residual mapping g(x) = f(x) - x we may be able to learn better, with the ideal of f(x) = x or g(x) = 0. As such we only need to push weights and biases of the upper weight layer to zero.

```
if use_1x1conv:
                      self.conv3 = nn.LazyConv2d(num_channels, kernel_size=1,
                                                 stride=strides)
                 else:
                      self.conv3 = None
                 self.bn1 = nn.LazyBatchNorm2d()
                 self.bn2 = nn.LazyBatchNorm2d()
             def forward(self, X):
                 Y = F.relu(self.bn1(self.conv1(X)))
                 Y = self.bn2(self.conv2(Y))
                 if self.conv3:
                     X = self.conv3(X)
                 Y += X
                 return F.relu(Y)
In [43]: | # where 1x1 convolution is not needed
         blk = Residual(3)
         X = torch.randn(4, 3, 6, 6)
         blk(X).shape
Out[43]: torch.Size([4, 3, 6, 6])
In [44]: # where 1x1 convolution is needed, halve output height and width while increasing of
         blk = Residual(6, use_1x1conv=True, strides=2)
         blk(X).shape
Out[44]: torch.Size([4, 6, 3, 3])
In [45]: # 7x7 convolutional layer with 64 output channels and stride of 2, followed by a 3x
         class ResNet(d21.Classifier):
             def b1(self):
                 return nn.Sequential(
                      nn.LazyConv2d(64, kernel_size=7, stride=2, padding=3),
                      nn.LazyBatchNorm2d(), nn.ReLU(),
                      nn.MaxPool2d(kernel_size=3, stride=2, padding=1))
In [46]: # four modules made up of residual blocks
         # retains the same height and width, but doubles the number of channels
         @d21.add_to_class(ResNet)
         def block(self, num_residuals, num_channels, first_block=False):
             blk = []
             for i in range(num_residuals):
                 if i == 0 and not first_block:
                      blk.append(Residual(num_channels, use_1x1conv=True, strides=2))
                      blk.append(Residual(num_channels))
             return nn.Sequential(*blk)
In [47]: # average pooling layer followed by fully connected layer output
         @d21.add_to_class(ResNet)
         def __init__(self, arch, lr=0.1, num_classes=10):
             super(ResNet, self).__init__()
             self.save_hyperparameters()
             self.net = nn.Sequential(self.b1())
```

```
for i, b in enumerate(arch):
                 self.net.add_module(f'b{i+2}', self.block(*b, first_block=(i==0)))
             self.net.add_module('last', nn.Sequential(
                 nn.AdaptiveAvgPool2d((1, 1)), nn.Flatten(),
                 nn.LazyLinear(num_classes)))
             self.net.apply(d21.init_cnn)
         # there are four convelutional layers in each module, with the first 7x7 convolution
In [48]:
         # shape changes
         class ResNet18(ResNet):
             def __init__(self, lr=0.1, num_classes=10):
                 super().__init__(((2, 64), (2, 128), (2, 256), (2, 512)),
                                 lr, num_classes)
         ResNet18().layer_summary((1, 1, 96, 96))
        Sequential output shape:
                                          torch.Size([1, 64, 24, 24])
                                          torch.Size([1, 64, 24, 24])
        Sequential output shape:
        Sequential output shape:
                                         torch.Size([1, 128, 12, 12])
        Sequential output shape:
                                         torch.Size([1, 256, 6, 6])
        Sequential output shape:
                                         torch.Size([1, 512, 3, 3])
        Sequential output shape:
                                         torch.Size([1, 10])
In [49]: # training
         model = ResNet18(lr=0.01)
         trainer = d21.Trainer(max epochs=10, num gpus=1)
         data = d21.FashionMNIST(batch_size=128, resize=(96, 96))
         model.apply_init([next(iter(data.get_dataloader(True)))[0]], d21.init_cnn)
         trainer.fit(model, data)
        0.8
        0.6
                                       train_loss
                                       val loss
        0.4
                                       val acc
        0.2
        0.0
            0
                    2
                                  6
                                          8
                                                 10
                            epoch
In [50]: # ResNeXt splits the input into multiple paths/groups. In Resnet, no information is
         # this implementation takes argument groups q, with bot channels b
         class ResNeXtBlock(nn.Module):
             def __init__(self, num_channels, groups, bot_mul, use_1x1conv=False,
                          strides=1):
                 super().__init__()
                 bot_channels = int(round(num_channels * bot_mul))
                 self.conv1 = nn.LazyConv2d(bot_channels, kernel_size=1, stride=1)
                 self.conv2 = nn.LazyConv2d(bot_channels, kernel_size=3,
                                             stride=strides, padding=1,
```

```
groups=bot_channels//groups)
   self.conv3 = nn.LazyConv2d(num_channels, kernel_size=1, stride=1)
   self.bn1 = nn.LazyBatchNorm2d()
   self.bn2 = nn.LazyBatchNorm2d()
   self.bn3 = nn.LazyBatchNorm2d()
   if use_1x1conv:
        self.conv4 = nn.LazyConv2d(num_channels, kernel_size=1,
                                   stride=strides)
        self.bn4 = nn.LazyBatchNorm2d()
   else:
        self.conv4 = None
def forward(self, X):
   Y = F.relu(self.bn1(self.conv1(X)))
   Y = F.relu(self.bn2(self.conv2(Y)))
   Y = self.bn3(self.conv3(Y))
   if self.conv4:
       X = self.bn4(self.conv4(X))
   return F.relu(Y + X)
```

```
In [51]: blk = ResNeXtBlock(32, 16, 1)
X = torch.randn(4, 32, 96, 96)
blk(X).shape
```

Out[51]: torch.Size([4, 32, 96, 96])