

ACM-ICPC TEAM REFERENCE DOCUMENT

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1 Graphs

1.1 Max Cardinality Bipartite Matching Recursive

```
typedef vector<int> vi;
vector<vi> lst; // adj list: left-nodes links
vi rima, visited; // rima = right nodes' (left-)match
int n, m; // n = # of left nodes, m = # of right nodes

bool find_match(int where) {
    if (where == -1) return 1;
    for (int i = 0; i < (int)lst[where].size(); i++) {
        int match = lst[where][i];
        if (!visited[match]) {
            visited[match] = 1;
            if (find_match(rima[match])) {
                rima[match] = where;
                return 1;
            }
        }
    }
    return 0;
}

int maximum_matching() // O(V*E)
{
    int ans = 0;

    visited.resize(m), rima.assign(m, -1);
    for (int i = 0; i < n; ++i) {
        fill(visited.begin(), visited.end(), 0);
        ans += find_match(i);
    }

    return ans;
}
```

1.2 Max Flow

```
struct MfEdge {
    int v, cap;
    int backid; // id to the back edge
};

struct MaxFlow {
    vector<vector<int>> g; // integers represent edges' ids
    vector<MfEdge> edges; // edges.size() should always be even
```

```
int n, s, t; // n = # vertices, s = src vertex, t = sink vertex

int find_path() {
    const int inf = int(1e9 + 7);
    vector<int> from(n, -1), used_edge(n, -1);

    vector<int> visited(n, -1); queue<int> q;
    q.push(s); visited[s] = true;
    while (!visited[t] && !q.empty()) {
        int u = q.front();
        q.pop();
        for (int eid : g[u]) {
            int v = edges[eid].v;
            if (edges[eid].cap > 0 && !visited[v]) {
                from[v] = u, used_edge[v] = eid;
                q.push(v); visited[v] = true;
                if (v == t) break;
            }
        }
    }

    int f = inf;
    if (from[t] != -1) {
        for (int v = t; from[v] > -1; v = from[v]) {
            f = min(edges[used_edge[v]].cap, f);
        }
        for (int v = t; from[v] > -1; v = from[v]) {
            int backid = edges[used_edge[v]].backid;
            edges[used_edge[v]].cap -= f;
            edges[backid].cap += f;
        }
        return (f == inf ? 0 : f);
    }

    int get() {
        int mf = 0, d;
        while ((d = find_path())) mf += d;
        return mf;
    }
};
```

1.3 Disjoint Sets

```
struct UnionFind {
    vector<int> pset, set_size;
    int disjointSetsSize;

    void initSet(int N) {
        pset.assign(N, 0);
```

```

    set_size.assign(N, 1);
    disjointSetsSize = N;
    for (int i = 0; i < N; i++) pset[i] = i;
}

int findSet(int i) { return (pset[i] == i) ? i : (pset[i] = findSet(pset[i])); }

bool isSameSet(int i, int j) { return findSet(i) == findSet(j); }

void unionSet(int i, int j) {
    if (!isSameSet(i, j)) {
        set_size[findSet(j)] += set_size[findSet(i)];
        pset[findSet(i)] = findSet(j);
        disjointSetsSize--;
    }
}

int numDisjointsSets() { return disjointSetsSize; }

int sizeOfSet(int i) { return set_size[findSet(i)]; }
};

```

1.4 Tree Center

```

#define MAX_SIZE 50000

vector<int> L[MAX_SIZE];

bool visited[MAX_SIZE];
int V, prev[MAX_SIZE], Q[MAX_SIZE], tail;

int most_distant(int s) {
    fill(visited, visited + V, false);
    visited[s] = true;
    Q[0] = s;
    tail = 1;
    prev[s] = -1;

    int ans = s;

    for (int k = 0; k < V; ++k) {
        int aux = Q[k];
        ans = aux;

        for (int i = L[aux].size() - 1; i >= 0; --i) {
            int v = L[aux][i];
            if (visited[v]) continue;
            visited[v] = true;
            Q[tail] = v;

```

```

            ++tail;
            prev[v] = aux;
        }
    }

    return ans;
}

void get_center() {
    int s = most_distant(0);
    int e = most_distant(s);
    int v = e, L = 0;

    while (v != -1) {
        Q[L] = v;
        v = prev[v];
        ++L;
    }

    if (L & 1)
        printf("%d\n", 1 + Q[L / 2]);
    else
        printf("%d %d\n", 1 + min(Q[L / 2 - 1], Q[L / 2]),
            1 + max(Q[L / 2 - 1], Q[L / 2]));
}

```

1.5 Bridges

```

#define SZ 100
bool M[SZ][SZ];
int N, colour[SZ], dfsNum[SZ], num, pos[SZ], leastAncestor[SZ], parent[SZ];

void dfs(int u) {
    int v;
    stack<int> S;
    S.push(u);

    while (!S.empty()) {
        v = S.top();
        if (colour[v] == 0) {
            colour[v] = 1;
            dfsNum[v] = num++;
            leastAncestor[v] = num;
        }

        for (; pos[v] < N; ++pos[v]) {
            if (M[v][pos[v]] && pos[v] != parent[v]) {
                if (colour[pos[v]] == 0) {
                    parent[pos[v]] = v;

```

```

        S.push(pos[v]);
        break;
    } else
        leastAncestor[v] < ? = dfsNum[pos[v]];
    }
}

if (pos[v] == N) {
    colour[v] = 2;
    S.pop();

    if (v != u) leastAncestor[parent[v]] < ? = leastAncestor[v];
}
}

void Bridge_detection() {
    memset(colour, 0, sizeof(colour));
    memset(pos, 0, sizeof(pos));
    memset(parent, -1, sizeof(parent));
    num = 0;

    int ans = 0;

    for (int i = 0; i < N; i++)
        if (colour[i] == 0) dfs(i);

    for (int i = 0; i < N; i++)
        for (int j = 0; j < N; j++)
            if (parent[j] == i && leastAncestor[j] > dfsNum[i]) {
                printf("%d - %d\n", i, j);
                ++ans;
            }

    printf("%d bridges\n", ans);
}

```

1.6 Heavy Light Decomposition

```

#include <bits/stdc++.h>
#define pb push_back
#define sz size
#define all(X) (X).begin(), (X).end()
#define for_each(it, X) \
    for (__typeof((X).begin()) it = (X).begin(); it != (X).end(); it++)

using namespace std;

typedef long long int lld;

```

```

typedef pair<int, int> pii;

const int MaxN = 1 << 20;

int N, M, Level[MaxN], Parent[MaxN], Size[MaxN], Chain[MaxN];
vector<int> E[MaxN];

void DFS(int Curr, int Prev) {
    Parent[Curr] = Prev;
    Size[Curr] = 1;

    for_each(it, E[Curr]) if (*it != Prev) Level[*it] = Level[Curr] + 1,
        DFS(*it, Curr),
        Size[Curr] += Size[*it];
}

void HLD(int Curr, int Prev, int Color) {
    Chain[Curr] = Color;

    int idx = -1;
    for_each(it, E[Curr]) if (*it != Prev && (idx == -1 || Size[*it] > Size[idx]))
        idx = *it;

    if (idx != -1) HLD(idx, Curr, Color);
    for_each(it, E[Curr]) if (*it != Prev && *it != idx) HLD(*it, Curr, *it);
}

inline int LCA(int idx, int idy) {
    while (Chain[idx] != Chain[idy])
        if (Level[Chain[idx]] < Level[Chain[idy]])
            idy = Parent[Chain[idy]];
        else
            idx = Parent[Chain[idx]];
    return Level[idx] < Level[idy] ? idx : idy;
}

int main(void) {
    cin.sync_with_stdio(0);
    cout.sync_with_stdio(0);

    cin >> N >> M;
    for (int i = 0; i < N - 1; i++) {
        int idx, idy;
        cin >> idx >> idy;
        idx--;
        idy--;

        E[idx].pb(idy);
        E[idy].pb(idx);
    }

    DFS(0, -1);
    HLD(0, -1, 0);
}

```

```

for (int i = 0; i < M; i++) {
    int idx, idy;
    cin >> idx >> idy;
    idx--;
    idy--;

    cout << LCA(idx, idy) + 1 << endl;
}

return 0;
}

```

1.7 Strongly Connected Components

```

vector<vector<int>> > g, gt;
stack<int> S;
int n;
vi scc;

void scc_dfs(const vector<vector<int>> > &g, int u, bool addToStack = false) {
    for (int i = 0; i < (int)g[u].size(); ++i) {
        int v = g[u][i];
        if (scc[v] == inf) {
            scc[v] = scc[u];
            scc_dfs(g, v, addToStack);
        }
    }
    if (addToStack) S.push(u);
}

int kosaraju() {
    const int inf = int(1e9 + 7);
    int ans = 0;

    scc.assign(n, inf);
    for (int u = 0; u < n; ++u) {
        if (scc[u] != inf) continue;
        scc[u] = true;
        scc_dfs(g, u, true);
    }
    scc.assign(n, inf);
    while (!S.empty()) {
        int u = S.top();
        S.pop();
        if (scc[u] != inf) continue;
        scc[u] = ans++;
        scc_dfs(gt, u);
    }
}

```

```

return ans;
}

```

1.8 Erdos Gallai

```

// Receives a sorted degree sequence (non ascending)
bool isGraphicSequence(const vector<int> &seq) // O(n lg n)
{
    vector<int> sum;
    int n = seq.size();

    if (n == 1 && seq[0] != 0) return false;

    sum.reserve(n + 1);
    sum.push_back(0);
    for (int i = 0; i < n; ++i) sum.push_back(sum[i] + seq[i]);
    if ((sum[n] & 1) == 1) return false;

    for (long long k = 1; k <= n - 1 && seq[k - 1] >= k; ++k) {
        int j = distance(seq.begin(), upper_bound(seq.begin() + k, seq.end(), k,
                                                    greater<int>())) +
            1;
        long long left = sum[k];
        long long right = k * (k - 1) + (j - k - 1) * k + (sum[n] - sum[j - 1]);

        if (left > right) return false;
    }

    return true;
}

```

1.9 Max Cardinality Bipartite Matching Iterative

```

struct MCBM {
    // n = # of left elements, m = # of right elements
    int n, m;
    // adj list for left elements
    // left elements are [0..n-1], right elements are [0..m-1]
    vector<vector<int>> > lst;

    bool find_match(int s, vector<int> &lema, vector<int> &rma) {
        vector<int> from(n, -1);
        queue<int> q;
        int where, match, next;
    }
}

```

```

bool found = false;

q.push(s), from[s] = s;
while (!found && !q.empty()) {
    where = q.front();
    q.pop();
    for (int i = 0; i < (int)lst[where].size(); ++i) {
        match = lst[where][i];
        next = rima[match];
        if (where != next) {
            if (next == -1) {
                found = true;
                break;
            }
            if (from[next] == -1) q.push(next), from[next] = where;
        }
    }
}

if (found) {
    while (from[where] != where) {
        next = lema[where];
        lema[where] = match, rima[match] = where;
        where = from[where], match = next;
    }
    lema[where] = match, rima[match] = where;
}

return found;
}

int maximum_matching() // O(V*E)
{
    int ans = 0;
    vector<int> lema(n, -1), rima(m, -1);
    for (int i = 0; i < n; ++i) {
        ans += find_match(i, lema, rima);
    }
    return ans;
}
};

```

1.10 Max Flow With Min Cost

```

struct McMaxFlow {
    struct MfEdge { int v, cap, cpu, backid; };
    struct FlowResult { int flow, cost; };
    vector<vector<int>> g; // integers represent edges' ids
    vector<MfEdge> edges; // edges.size() should always be even

```

```

    int n, s, t; // n = # vertices, s = src vertex, t = sink vertex

    // Directed Edge u -> v with capacity 'cap' and cost per unit 'cpu'
    void add_edge(int u, int v, int cap, int cpu) {
        int eid = edges.size();
        g[u].push_back(eid);
        g[v].push_back(eid + 1);
        edges.push_back(MfEdge{v, cap, cpu, eid + 1});
        edges.push_back(MfEdge{u, 0, -cpu, eid});
    }

    FlowResult find_path() {
        const int inf = int(1e9 + 7);
        vector<int> from(n, -1), used_edge(n, -1);

        vector<int> dist(n, inf);
        queue<int> q; vector<bool> queued(n, false);
        dist[s] = 0; q.push(s); queued[s] = true;

        while (!q.empty()) {
            const int u = q.front(); q.pop();
            queued[u] = false;

            for (int eid : g[u]) {
                int v = edges[eid].v;
                int cand_dist = dist[u] + edges[eid].cpu;
                if (edges[eid].cap > 0 && cand_dist < dist[v]) {
                    dist[v] = cand_dist;
                    from[v] = u; used_edge[v] = eid;
                    if (!queued[v]) { q.push(v); queued[v] = true; }
                }
            }
        }

        int f = 0, fcost = 0;
        if (from[t] != -1) {
            f = inf;
            for (int v = t; from[v] > -1; v = from[v]) {
                f = min(edges[used_edge[v]].cap, f);
                fcost += edges[used_edge[v]].cpu;
            }
            for (int v = t; from[v] > -1; v = from[v]) {
                int backid = edges[used_edge[v]].backid;
                edges[used_edge[v]].cap -= f;
                edges[backid].cap += f;
            }
            fcost *= f;
        }

        return (FlowResult){f, fcost};
    }

    FlowResult get() {

```

```

FlowResult res = {0, 0};
while (true) {
    FlowResult fr = find_path();
    if (fr.flow == 0) break;
    res.flow += fr.flow;
    res.cost += fr.cost;
}
return res;
}
};

```

1.11 Articulation Points

```

#define SZ 100
bool M[SZ][SZ];
int N, colour[SZ], dfsNum[SZ], num, pos[SZ], leastAncestor[SZ], parent[SZ];

int dfs(int u) {
    int ans = 0, cont = 0, v;

    stack<int> S;
    S.push(u);

    while (!S.empty()) {
        v = S.top();
        if (colour[v] == 0) {
            colour[v] = 1;
            dfsNum[v] = num++;
            leastAncestor[v] = num;
        }

        for (; pos[v] < N; ++pos[v]) {
            if (M[v][pos[v]] && pos[v] != parent[v]) {
                if (colour[pos[v]] == 0) {
                    parent[pos[v]] = v;
                    S.push(pos[v]);
                    if (v == u) ++cont;
                    break;
                } else
                    leastAncestor[v] < ? = dfsNum[pos[v]];
            }
        }

        if (pos[v] == N) {
            colour[v] = 2;
            S.pop();

            if (v != u) leastAncestor[parent[v]] < ? = leastAncestor[v];
        }
    }
}

```

```

}

if (cont > 1) {
    ++ans;
    printf("%d\n", u);
}

for (int i = 0; i < N; ++i) {
    if (i == u) continue;
    for (int j = 0; j < N; ++j)
        if (M[i][j] && parent[j] == i && leastAncestor[j] >= dfsNum[i]) {
            printf("%d\n", i);
            ++ans;
            break;
        }
}

return ans;
}

void Articulation_points() {
    memset(colour, 0, sizeof(colour));
    memset(pos, 0, sizeof(pos));
    memset(parent, -1, sizeof(parent));
    num = 0;

    int total = 0;
    for (int i = 0; i < N; ++i)
        if (colour[i] == 0) total += dfs(i);

    printf("# Articulation Points : %d\n", total);
}

```

2 Java

2.1 Fast Input Output Template

```

import java.io.*;
import java.math.*;
import java.util.*;
import java.lang.*;

public class Main {
    public static void main(String[] args) {
        InputReader in = new InputReader(System.in);
        OutputWriter out = new OutputWriter(System.out);
        // Do your thing
    }
}

```

```

        out.close();
    }
}

class InputReader {
    private InputStream stream;
    private byte[] buf = new byte[1024];
    private int curChar;
    private int numChars;
    private SpaceCharFilter filter;

    public InputReader(InputStream stream) {
        this.stream = stream;
    }

    public int read() {
        if (numChars == -1) {
            throw new InputMismatchException();
        }

        if (curChar >= numChars) {
            curChar = 0;
            try {
                numChars = stream.read(buf);
            } catch (IOException e) {
                throw new InputMismatchException();
            }
            if (numChars <= 0) {
                return -1;
            }
        }

        return buf[curChar++];
    }

    public int readInt() {
        int c = read();
        while (isSpaceChar(c)) {
            c = read();
        }

        int sgn = 1;
        if (c == '-') {
            sgn = -1;
            c = read();
        }

        int res = 0;
        do {
            if (c < '0' || c > '9') {
                throw new InputMismatchException();
            }
            res *= 10;

```

```

            res += c - '0';
            c = read();
        } while (!isSpaceChar(c));

        return res * sgn;
    }

    public String readString() {
        int c = read();
        while (isSpaceChar(c)) {
            c = read();
        }

        StringBuilder res = new StringBuilder();
        do {
            res.appendCodePoint(c);
            c = read();
        } while (!isSpaceChar(c));
        return res.toString();
    }

    public boolean isSpaceChar(int c) {
        if (filter != null) {
            return filter.isSpaceChar(c);
        }
        return c == ' ' || c == '\n' || c == '\r' || c == '\t' || c == -1;
    }

    public String next() {
        return readString();
    }

    public interface SpaceCharFilter {
        public boolean isSpaceChar(int ch);
    }
}

class OutputWriter {
    private final PrintWriter writer;

    public OutputWriter(OutputStream outputStream) {
        writer = new PrintWriter(
            new BufferedWriter(new OutputStreamWriter(outputStream))
        );
    }

    public OutputWriter(Writer writer) {
        this.writer = new PrintWriter(writer);
    }

    public void print(Object... objects) {
        for (int i = 0; i < objects.length; i++) {
            if (i != 0) {

```



```

        writer.print(' ');
    }
    writer.print(objects[i]);
}

public void printLine(Object... objects) {
    print(objects);
    writer.println();
}

public void close() {
    writer.close();
}

public void flush() {
    writer.flush();
}
}

class IOUtils {
    public static int[] readIntArray(InputReader in, int size) {
        int[] array = new int[size];
        for (int i = 0; i < size; i++) {
            array[i] = in.readInt();
        }
        return array;
    }
}

```

3 Geometry

3.1 Geometry

```

#define EPS 1e-8
#define PI acos(-1)
#define Vector Point

struct Point {
    double x, y;
    Point() {}
    Point(double a, double b) {
        x = a;
        y = b;
    }
    double mod2() { return x * x + y * y; }
    double mod() { return sqrt(x * x + y * y); }
}

```

```

double arg() { return atan2(y, x); }
Point ort() { return Point(-y, x); }
Point unit() {
    double k = mod();
    return Point(x / k, y / k);
}
};

Point operator+(const Point &a, const Point &b) {
    return Point(a.x + b.x, a.y + b.y);
}
Point operator-(const Point &a, const Point &b) {
    return Point(a.x - b.x, a.y - b.y);
}
Point operator/(const Point &a, double k) { return Point(a.x / k, a.y / k); }
Point operator*(const Point &a, double k) { return Point(a.x * k, a.y * k); }

bool operator==(const Point &a, const Point &b) {
    return abs(a.x - b.x) < EPS && abs(a.y - b.y) < EPS;
}
bool operator!=(const Point &a, const Point &b) { return !(a == b); }
bool operator<(const Point &a, const Point &b) {
    if (abs(a.x - b.x) > EPS) return a.x < b.x;
    return a.y < b.y;
}

//### FUNCIONES BASICAS
//#####

double dist(const Point &A, const Point &B) {
    return hypot(A.x - B.x, A.y - B.y);
}

double cross(const Vector &A, const Vector &B) { return A.x * B.y - A.y * B.x; }
double dot(const Vector &A, const Vector &B) { return A.x * B.x + A.y * B.y; }
double area(const Point &A, const Point &B, const Point &C) {
    return cross(B - A, C - A);
}

// Heron triangulo y cuadrilatero ciclico
// http://mathworld.wolfram.com/CyclicQuadrilateral.html
// http://www.spoj.pl/problems/QUADAREA/

double areaHeron(double a, double b, double c) {
    double s = (a + b + c) / 2;
    return sqrt(s * (s - a) * (s - b) * (s - c));
}

double circumradius(double a, double b, double c) {
    return a * b * c / (4 * areaHeron(a, b, c));
}

double areaHeron(double a, double b, double c, double d) {
    double s = (a + b + c + d) / 2;
}

```

```

    return sqrt((s - a) * (s - b) * (s - c) * (s - d));
}

double circumradius(double a, double b, double c, double d) {
    return sqrt((a * b + c * d) * (a * c + b * d) * (a * d + b * c)) /
        (4 * areaHeron(a, b, c, d));
}

#### DETERMINA SI P PERTENECE AL SEGMENTO AB
#####
bool between(const Point &A, const Point &B, const Point &P) {
    return P.x + EPS >= min(A.x, B.x) && P.x <= max(A.x, B.x) + EPS &&
        P.y + EPS >= min(A.y, B.y) && P.y <= max(A.y, B.y) + EPS;
}

bool onSegment(const Point &A, const Point &B, const Point &P) {
    return abs(area(A, B, P)) < EPS && between(A, B, P);
}

#### DETERMINA SI EL SEGMENTO P1Q1 SE INTERSECTA CON EL SEGMENTO P2Q2
#####
// funciona para cualquiera P1, P2, P3, P4
bool intersects(const Point &P1, const Point &P2, const Point &P3,
    const Point &P4) {
    double A1 = area(P3, P4, P1);
    double A2 = area(P3, P4, P2);
    double A3 = area(P1, P2, P3);
    double A4 = area(P1, P2, P4);

    if (((A1 > 0 && A2 < 0) || (A1 < 0 && A2 > 0)) &&
        ((A3 > 0 && A4 < 0) || (A3 < 0 && A4 > 0)))
        return true;

    else if (A1 == 0 && onSegment(P3, P4, P1))
        return true;
    else if (A2 == 0 && onSegment(P3, P4, P2))
        return true;
    else if (A3 == 0 && onSegment(P1, P2, P3))
        return true;
    else if (A4 == 0 && onSegment(P1, P2, P4))
        return true;
    else
        return false;
}

#### DETERMINA SI A, B, M, N PERTENECEN A LA MISMA RECTA
#####
bool sameLine(Point P1, Point P2, Point P3, Point P4) {
    return area(P1, P2, P3) == 0 && area(P1, P2, P4) == 0;
}

#### SI DOS SEGMENTOS O RECTAS SON PARALELOS
#####
bool isParallel(const Point &P1, const Point &P2, const Point &P3,

```

```

    const Point &P4) {
        return cross(P2 - P1, P4 - P3) == 0;
    }

#### PUNTO DE INTERSECCION DE DOS RECTAS NO PARALELAS
#####
Point lineIntersection(const Point &A, const Point &B, const Point &C,
    const Point &D) {
    return A + (B - A) * (cross(C - A, D - C) / cross(B - A, D - C));
}

Point circumcenter(const Point &A, const Point &B, const Point &C) {
    return (A + B + (A - B).ort() * dot(C - B, A - C) / cross(A - B, A - C)) / 2;
}

#### FUNCIONES BASICAS DE POLIGONOS
#####
bool isConvex(const vector<Point> &P) {
    int n = P.size(), pos = 0, neg = 0;
    for (int i = 0; i < n; i++) {
        double A = area(P[i], P[(i + 1) % n], P[(i + 2) % n]);
        if (A < 0)
            neg++;
        else if (A > 0)
            pos++;
    }
    return neg == 0 || pos == 0;
}

double area(const vector<Point> &P) {
    int n = P.size();
    double A = 0;
    for (int i = 1; i <= n - 2; i++) A += area(P[0], P[i], P[i + 1]);
    return abs(A / 2);
}

bool pointInPoly(const vector<Point> &P, const Point &A) {
    int n = P.size(), cnt = 0;
    for (int i = 0; i < n; i++) {
        int inf = i, sup = (i + 1) % n;
        if (P[inf].y > P[sup].y) swap(inf, sup);
        if (P[inf].y <= A.y && A.y < P[sup].y)
            if (area(A, P[inf], P[sup]) > 0) cnt++;
    }
    return (cnt % 2) == 1;
}

#### CONVEX HULL
#####
// O(nh)
vector<Point> ConvexHull(vector<Point> S) {
    sort(all(S));
}

```

```

int it = 0;
Point primero = S[it], ultimo = primero;

int n = S.size();

vector<Point> convex;
do {
    convex.push_back(S[it]);
    it = (it + 1) % n;

    for (int i = 0; i < S.size(); i++) {
        if (S[i] != ultimo && S[i] != S[it]) {
            if (area(ultimo, S[it], S[i]) < EPS) it = i;
        }
    }

    ultimo = S[it];
} while (ultimo != primero);

return convex;
}

// O(n log n)
vector<Point> ConvexHull(vector<Point> P) {
    sort(P.begin(), P.end());
    int n = P.size(), k = 0;
    Point H[2 * n];

    for (int i = 0; i < n; ++i) {
        while (k >= 2 && area(H[k - 2], H[k - 1], P[i]) <= 0) --k;
        H[k++] = P[i];
    }

    for (int i = n - 2, t = k; i >= 0; --i) {
        while (k > t && area(H[k - 2], H[k - 1], P[i]) <= 0) --k;
        H[k++] = P[i];
    }

    return vector<Point>(H, H + k - 1);
}

##### DETERMINA SI P ESTA EN EL INTERIOR DEL POLIGONO CONVEXO A #####

// O (log n)
bool isInConvex(vector<Point> &A, const Point &P) {
    int n = A.size(), lo = 1, hi = A.size() - 1;

    if (area(A[0], A[1], P) <= 0) return 0;
    if (area(A[n - 1], A[0], P) <= 0) return 0;

    while (hi - lo > 1) {
        int mid = (lo + hi) / 2;

```

[illegible]

```

        O = circumcenter(P[i], P[j], P[k]), R2 = (P[k] - O).mod2();
    }
}
}
return make_pair(O, sqrt(R2));
}

//##### CLOSEST PAIR OF POINTS
//#####
bool XYorder(Point P1, Point P2) {
    if (P1.x != P2.x) return P1.x < P2.x;
    return P1.y < P2.y;
}
bool YXorder(Point P1, Point P2) {
    if (P1.y != P2.y) return P1.y < P2.y;
    return P1.x < P2.x;
}
double closest_recursive(vector<Point> vx, vector<Point> vy) {
    if (vx.size() == 1) return 1e20;
    if (vx.size() == 2) return dist(vx[0], vx[1]);

    Point cut = vx[vx.size() / 2];

    vector<Point> vxL, vxR;
    for (int i = 0; i < vx.size(); i++)
        if (vx[i].x < cut.x || (vx[i].x == cut.x && vx[i].y <= cut.y))
            vxL.push_back(vx[i]);
        else
            vxR.push_back(vx[i]);

    vector<Point> vyL, vyR;
    for (int i = 0; i < vy.size(); i++)
        if (vy[i].x < cut.x || (vy[i].x == cut.x && vy[i].y <= cut.y))
            vyL.push_back(vy[i]);
        else
            vyR.push_back(vy[i]);

    double dL = closest_recursive(vxL, vyL);
    double dR = closest_recursive(vxR, vyR);
    double d = min(dL, dR);

    vector<Point> b;
    for (int i = 0; i < vy.size(); i++)
        if (abs(vy[i].x - cut.x) <= d) b.push_back(vy[i]);

    for (int i = 0; i < b.size(); i++)
        for (int j = i + 1; j < b.size() && (b[j].y - b[i].y) <= d; j++)
            d = min(d, dist(b[i], b[j]));

    return d;
}
double closest(vector<Point> points) {

```

```

    vector<Point> vx = points, vy = points;
    sort(vx.begin(), vx.end(), XYorder);
    sort(vy.begin(), vy.end(), YXorder);

    for (int i = 0; i + 1 < vx.size(); i++)
        if (vx[i] == vx[i + 1]) return 0.0;

    return closest_recursive(vx, vy);
}

// INTERSECCION DE CIRCULOS
vector<Point> circleCircleIntersection(Point O1, double r1, Point O2,
                                       double r2) {
    vector<Point> X;

    double d = dist(O1, O2);

    if (d > r1 + r2 || d < max(r2, r1) - min(r2, r1))
        return X;
    else {
        double a = (r1 * r1 - r2 * r2 + d * d) / (2.0 * d);
        double b = d - a;
        double c = sqrt(abs(r1 * r1 - a * a));

        Vector V = (O2 - O1).unit();
        Point H = O1 + V * a;

        X.push_back(H + V.ort() * c);

        if (c > EPS) X.push_back(H - V.ort() * c);
    }

    return X;
}

// LINEA AB vs CIRCULO (O, r)
// 1. Mucha perdida de precision, reemplazar por resultados de formula.
// 2. Considerar line o segment

vector<Point> lineCircleIntersection(Point A, Point B, Point O, long double r) {
    vector<Point> X;

    Point H1 = O + (B - A).ort() * cross(O - A, B - A) / (B - A).mod2();
    long double d2 = cross(O - A, B - A) * cross(O - A, B - A) / (B - A).mod2();

    if (d2 <= r * r + EPS) {
        long double k = sqrt(abs(r * r - d2));

        Point P1 = H1 + (B - A) * k / (B - A).mod();
        Point P2 = H1 - (B - A) * k / (B - A).mod();

        if (between(A, B, P1)) X.push_back(P1);

```

```

    if (k > EPS && between(A, B, P2)) X.push_back(P2);
}

return X;
}

##### PROBLEMAS BASICOS
#####
void CircumscribedCircle() {
    int x1, y1, x2, y2, x3, y3;
    scanf("%d %d %d %d %d %d", &x1, &y1, &x2, &y2, &x3, &y3);

    Point A(x1, y1), B(x2, y2), C(x3, y3);

    Point P1 = (A + B) / 2.0;
    Point P2 = P1 + (B - A).ort();
    Point P3 = (A + C) / 2.0;
    Point P4 = P3 + (C - A).ort();

    Point CC = lineIntersection(P1, P2, P3, P4);
    double r = dist(A, CC);

    printf("%.6lf,%.6lf,%.6lf\n", CC.x, CC.y, r);
}

void InscribedCircle() {
    int x1, y1, x2, y2, x3, y3;
    scanf("%d %d %d %d %d %d", &x1, &y1, &x2, &y2, &x3, &y3);

    Point A(x1, y1), B(x2, y2), C(x3, y3);

    Point AX = A + (B - A).unit() + (C - A).unit();
    Point BX = B + (A - B).unit() + (C - B).unit();

    Point CC = lineIntersection(A, AX, B, BX);
    double r = abs(area(A, B, CC) / dist(A, B));

    printf("%.6lf,%.6lf,%.6lf\n", CC.x, CC.y, r);
}

vector<Point> TangentLineThroughPoint(Point P, Point C, long double r) {
    vector<Point> X;

    long double h2 = (C - P).mod2();
    if (h2 < r * r)
        return X;
    else {
        long double d = sqrt(h2 - r * r);

        long double m1 = (r * (P.x - C.x) + d * (P.y - C.y)) / h2;
        long double n1 = (P.y - C.y - d * m1) / r;

        long double n2 = (d * (P.x - C.x) + r * (P.y - C.y)) / h2;

```

```

        long double m2 = (P.x - C.x - d * n2) / r;

        X.push_back(C + Point(m1, n1) * r);
        if (d != 0) X.push_back(C + Point(m2, n2) * r);

        return X;
    }
}

void TangentLineThroughPoint() {
    int xc, yc, r, xp, yp;
    scanf("%d %d %d %d %d", &xc, &yc, &r, &xp, &yp);

    Point C(xc, yc), P(xp, yp);

    double hyp = dist(C, P);
    if (hyp < r)
        printf("[]\n");
    else {
        double d = sqrt(hyp * hyp - r * r);

        double m1 = (r * (P.x - C.x) + d * (P.y - C.y)) / (r * r + d * d);
        double n1 = (P.y - C.y - d * m1) / r;
        double ang1 = 180 * atan(-m1 / n1) / PI + EPS;
        if (ang1 < 0) ang1 += 180.0;

        double n2 = (d * (P.x - C.x) + r * (P.y - C.y)) / (r * r + d * d);
        double m2 = (P.x - C.x - d * n2) / r;
        double ang2 = 180 * atan(-m2 / n2) / PI + EPS;
        if (ang2 < 0) ang2 += 180.0;

        if (ang1 > ang2) swap(ang1, ang2);

        if (d == 0)
            printf("%.6lf]\n", ang1);
        else
            printf("%.6lf,%.6lf]\n", ang1, ang2);
    }
}

void CircleThroughAPointAndTangentToALineWithRadius() {
    int xp, yp, x1, y1, x2, y2, r;
    scanf("%d %d %d %d %d %d", &xp, &yp, &x1, &y1, &x2, &y2, &r);

    Point P(xp, yp), A(x1, y1), B(x2, y2);

    Vector V = (B - A).ort() * r / (B - A).mod();

    Point X[2];
    int cnt = 0;

    Point H1 = P + (B - A).ort() * cross(P - A, B - A) / (B - A).mod2() + V;
    double d1 = abs(r + cross(P - A, B - A) / (B - A).mod());

```

```

if (d1 - EPS <= r) {
    double k = sqrt(abs(r * r - d1 * d1));

    X[cnt++] = Point(H1 + (B - A).unit() * k);

    if (k > EPS) X[cnt++] = Point(H1 - (B - A).unit() * k);
}

Point H2 = P + (B - A).ort() * cross(P - A, B - A) / (B - A).mod2() - V;
double d2 = abs(r - cross(P - A, B - A) / (B - A).mod());

if (d2 - EPS <= r) {
    double k = sqrt(abs(r * r - d2 * d2));

    X[cnt++] = Point(H2 + (B - A).unit() * k);

    if (k > EPS) X[cnt++] = Point(H2 - (B - A).unit() * k);
}

sort(X, X + cnt);

if (cnt == 0)
    printf("[]\n");
else if (cnt == 1)
    printf("[(%6lf,%6lf)]\n", X[0].x, X[0].y);
else if (cnt == 2)
    printf("[(%6lf,%6lf),(%6lf,%6lf)]\n", X[0].x, X[0].y, X[1].x, X[1].y);
}

void CircleTangentToTwoLinesWithRadius() {
    int x1, y1, x2, y2, x3, y3, x4, y4, r;
    scanf("%d %d %d %d %d %d %d %d", &x1, &y1, &x2, &y2, &x3, &y3, &x4, &y4,
        &r);

    Point A1(x1, y1), B1(x2, y2), A2(x3, y3), B2(x4, y4);

    Vector V1 = (B1 - A1).ort() * r / (B1 - A1).mod();
    Vector V2 = (B2 - A2).ort() * r / (B2 - A2).mod();

    Point X[4];
    X[0] = lineIntersection(A1 + V1, B1 + V1, A2 + V2, B2 + V2);
    X[1] = lineIntersection(A1 + V1, B1 + V1, A2 - V2, B2 - V2);
    X[2] = lineIntersection(A1 - V1, B1 - V1, A2 + V2, B2 + V2);
    X[3] = lineIntersection(A1 - V1, B1 - V1, A2 - V2, B2 - V2);

    sort(X, X + 4);
    printf("[(%6lf,%6lf),(%6lf,%6lf),(%6lf,%6lf),(%6lf,%6lf)]\n", X[0].x,
        X[0].y, X[1].x, X[1].y, X[2].x, X[2].y, X[3].x, X[3].y);
}

void CircleTangentToTwoDisjointCirclesWithRadius() {
    int x1, y1, r1, x2, y2, r2, r;

```

```

scanf("%d %d %d %d %d %d %d", &x1, &y1, &r1, &x2, &y2, &r2, &r);

Point A(x1, y1), B(x2, y2);

r1 += r;
r2 += r;

double d = dist(A, B);

if (d > r1 + r2 || d < max(r1, r2) - min(r1, r2))
    printf("[]\n");
else {
    double a = (r1 * r1 - r2 * r2 + d * d) / (2.0 * d);
    double b = d - a;
    double c = sqrt(abs(r1 * r1 - a * a));

    Vector V = (B - A).unit();
    Point H = A + V * a;

    Point P1 = H + V.ort() * c;
    Point P2 = H - V.ort() * c;

    if (P2 < P1) swap(P1, P2);

    if (P1 == P2)
        printf("[(%6lf,%6lf)]\n", P1.x, P1.y);
    else
        printf("[(%6lf,%6lf),(%6lf,%6lf)]\n", P1.x, P1.y, P2.x, P2.y);
}
}

```

4 Strings

4.1 Trie

```

#include <bits/stdc++.h>
using namespace std;

template <int alphabet_size>
struct TrieNode {
    int n_words, n_prefixes;
    int child[alphabet_size] = {0};

    TrieNode() : n_words(0), n_prefixes(0) { }
};

template <int alphabet_size>

```

```

struct Trie {
    static constexpr int npos = -1;
    using TNode = TrieNode<alphabet_size>;
    vector<TNode> nodes;

    Trie() { nodes.emplace_back(); }

    /*
    ** Maps the given char to an unsigned integer
    ** inside the range [0..alphabet_size)
    */
    int char_to_child(char c) {
        int result = c - '0';
        //assert(0 <= result && result < alphabet_size);
        return result;
    }

    /*
    ** Adds the given word to the trie
    */
    void add_word(const char *s) {
        int current = 0;

        for (int i = 0; s[i]; i++) {
            nodes[current].n_prefixes += 1;

            int next_child = char_to_child(s[i]);

            int next_node = nodes[current].child[next_child];
            if (next_node == 0) {
                next_node = nodes.size();
                nodes[current].child[next_child] = next_node;
                nodes.emplace_back();
            }
            current = next_node;
        }

        nodes[current].n_prefixes += 1;
        nodes[current].n_words += 1;
    }

    /*
    ** Traverses the trie, following the content of string 's'.
    ** Returns the node ID where the traversal stopped, or
    ** Trie::npos if it couldn't follow the whole string.
    */
    int traverse(const char *s) {
        int current = 0;

        for (int i = 0; s[i]; i++) {
            int next_child = char_to_child(s[i]);

            int next_node = nodes[current].child[next_child];

```

```

            if (next_node == 0) {
                return Trie::npos;
            }

            current = next_node;
        }

        return current;
    }

    int count_prefixes(const char *s) {
        int node = traverse(s);
        int result = (node == Trie::npos ? 0 : nodes[node].n_prefixes);
        return result;
    }

    int count_words(const char *s) {
        int node = traverse(s);
        int result = (node == Trie::npos ? 0 : nodes[node].n_words);
        return result;
    }
};

```

4.2 Z Function

```

/*
** Given a string S of length n, the Z Algorithm produces
** an array Z where Z[i] is the length of the longest substring
** starting from S[i] which is also a prefix of S, i.e. the
** maximum k such that S[j] = S[i + j] for all 0 <= j < k.
** Note that Z[i] = 0 means that S[0] != S[i].
*/
void z_func(const string &s) {
    const int length = s.size();
    int left = 0, right = 0;

    vector z(length);
    z[0] = 0;

    for (int i = 1; i < length; i++) {
        if (i > right) {
            int j;
            for (j = 0; i + j < length && s[i + j] == s[j]; j++)
                ;
            z[i] = j;
            left = i;
            right = i + j - 1;
        } else if (z[i - left] < right - i + 1)
            z[i] = z[i - left];
    }
}

```

```

    else {
        int j;
        for (j = 1; right + j < length && s[right + j] == s[right - i + j]; j++)
            ;
        z[i] = right - i + j;
        left = i;
        right = right + j - 1;
    }
}

return z;
}

```

4.3 Minimum String Rotation

```

int minimumExpression(string s) {
    s = s + s;
    int len = s.size(), i = 0, j = 1, k = 0;
    while (i + k < len && j + k < len) {
        if (s[i + k] == s[j + k])
            k++;
        else if (s[i + k] > s[j + k]) {
            i = i + k + 1;
            if (i <= j) i = j + 1;
            k = 0;
        } else if (s[i + k] < s[j + k]) {
            j = j + k + 1;
            if (j <= i) j = i + 1;
            k = 0;
        }
    }
    return min(i, j);
}

```

4.4 Knuth Morris Pratt

```

#define MAX_L 70
int f[MAX_L];

void prefixFunction(string P) {
    int n = P.size(), k = 0;
    f[0] = 0;

    for (int i = 1; i < n; ++i) {
        while (k > 0 && P[k] != P[i]) k = f[k - 1];
    }
}

```

```

        if (P[k] == P[i]) ++k;
        f[i] = k;
    }
}

int KMP(string P, string T) {
    int n = P.size(), L = T.size(), k = 0, ans = 0;

    for (int i = 0; i < L; ++i) {
        while (k > 0 && P[k] != T[i]) k = f[k - 1];
        if (P[k] == T[i]) ++k;

        if (k == n) {
            ++ans;
            k = f[k - 1];
        }
    }

    return ans;
}

```

5 Data Structures

5.1 Ranged Fenwick Tree

```

#include <iostream>
#include <algorithm>
#include <vector>
#include <cstring>
using namespace std;

```

*// Implementation based on the code provided at Petr's blog. Nevertheless,
// an easy and helpful explanation can be found in TopCoder's forums
// <http://petr-mitrichev.blogspot.com/2013/05/fenwick-tree-range-updates.html>
// <http://apps.topcoder.com/forums/?module=RevisionHistory&messageID=1407869>*

```

template <typename T>
class RangedFenwickTree {
public:
    RangedFenwickTree() {}

    RangedFenwickTree(unsigned int n) { Init(n); }

    T Query(int at) const {
        T mul = 0, add = 0;
        int start = at;
        while (at >= 0) {
            mul += dataMul[at];
        }
    }
}

```



```

    add += dataAdd[at];
    at = (at & (at + 1)) - 1;
}
return mul * start + add;
}

T QueryInterval(int x, int y) const { return Query(y) - Query(x - 1); }

void Update(int x, int y, T delta) {
    InternalUpdate(x, delta, -delta * (x - 1));
    if (y + 1 < (int)this->size()) InternalUpdate(y + 1, -delta, delta * y);
}

unsigned int size() const { return dataMul.size(); }

void Init(unsigned int n) {
    dataMul.assign(n, 0);
    dataAdd.assign(n, 0);
}

vector<T> dataMul, dataAdd;

private:
void InternalUpdate(int x, T mul, T add) {
    for (int i = x; i < (int)this->size(); i = (i | (i + 1))) {
        dataMul[i] += mul;
        dataAdd[i] += add;
    }
}
};

// Extension of the Ranged Fenwick Tree to 2D
template <typename T>
class RangedFenwickTree2D {
public:
    RangedFenwickTree2D() {}

    RangedFenwickTree2D(unsigned int m, unsigned int n) { Init(m, n); }

    T Query(int x, int y) const {
        T mul = 0, add = 0;
        for (int i = x; i >= 0; i = (i & (i + 1)) - 1) {
            mul += dataMul[i].Query(y);
            add += dataAdd[i].Query(y);
        }
        return mul * x + add;
    }

    T QuerySubmatrix(int x1, int y1, int x2, int y2) const {
        T result = Query(x2, y2);
        if (x1 > 0) result -= Query(x1 - 1, y2);
        if (y1 > 0) result -= Query(x2, y1 - 1);
        if (x1 > 0 && y1 > 0) result += Query(x1 - 1, y1 - 1);
    }
};

```

```

    return result;
}

void Update(int x1, int y1, int x2, int y2, T delta) {
    for (int i = x1; i < (int)dataMul.size(); i |= i + 1) {
        dataMul[i].Update(y1, y2, delta);
        dataAdd[i].Update(y1, y2, -delta * (x1 - 1));
    }
    for (int i = x2 + 1; i < (int)dataMul.size(); i |= i + 1) {
        dataMul[i].Update(y1, y2, -delta);
        dataAdd[i].Update(y1, y2, delta * x2);
    }
}

void Init(unsigned int m, unsigned int n) {
    // dataMul efficient initialization
    if (dataMul.size() == m) {
        for (int i = 0; i < (int)m; i++) dataMul[i].Init(n);
    } else {
        dataMul.assign(m, RangedFenwickTree<T>(n));
    }
    // dataAdd efficient initialization
    if (dataAdd.size() == m) {
        for (int i = 0; i < (int)m; i++) dataAdd[i].Init(n);
    } else {
        dataAdd.assign(m, RangedFenwickTree<T>(n));
    }
}

vector<RangedFenwickTree<T> > dataMul, dataAdd;
};

int main() {
    // EXAMPLE USAGE
    // Solution for http://www.spoj.com/problems/USUBQSUB/

    ios_base::sync_with_stdio(0);
    cin.tie(0);

    int n, m;
    cin >> n >> m;
    RangedFenwickTree2D<long long> f(n + 1, n + 1);
    while (m--) {
        int kind, x1, y1, x2, y2;
        cin >> kind >> x1 >> y1 >> x2 >> y2;
        if (kind == 1) {
            cout << f.QuerySubmatrix(x1, y1, x2, y2) << '\n';
        } else {
            int value;
            cin >> value;
            f.Update(x1, y1, x2, y2, value);
        }
    }
}

```

```
    return 0;
}
```

5.2 Fenwick Tree

```
// Most of the implementation comes from e-maxx.ru, although several
// things can also be found on the TopCoder tutorial about BITs
// community.topcoder.com/tc?module=Static&dl=tutorials&d2=binaryIndexedTrees
// e-maxx.ru/algo/fenwick_tree
template <typename T>
class FenwickTree {
public:
    FenwickTree() {}

    FenwickTree(unsigned int n) { Init(n); }

    T Query(int x) const {
        T result = 0;
        for (int i = x; i >= 0; i = (i & (i + 1)) - 1) result += data[i];
        return result;
    }

    T QueryInterval(int x, int y) const { return Query(y) - Query(x - 1); }

    T QuerySingle(int x) const {
        T result = data[x];
        if (x > 0) {
            int y = (x & (x + 1)) - 1;
            x -= 1;
            while (x != y) {
                result -= data[x];
                x = (x & (x + 1)) - 1;
            }
        }
        return result;
    }

    void Update(int x, T delta) {
        for (int i = x; i < (int)data.size(); i = (i | (i + 1))) data[i] += delta;
    }

    unsigned int size() const { return data.size(); }

    void Init(unsigned int n) { data.assign(n, 0); }

    vector<T> data;
};
```

```
// Extension of the Fenwick Tree to 2D
template <typename T>
class FenwickTree2D {
public:
    FenwickTree2D() {}

    FenwickTree2D(unsigned int m, unsigned int n) { Init(m, n); }

    T Query(int x, int y) const {
        T result = 0;
        for (int i = x; i >= 0; i = (i & (i + 1)) - 1) result += data[i].Query(y);
        return result;
    }

    void Update(int x, int y, T delta) {
        for (int i = x; i < (int)data.size(); i = (i | (i + 1)))
            data[i].Update(y, delta);
    }

    void Init(unsigned int m, unsigned int n) {
        if (data.size() == m) {
            for (int i = 0; i < (int)m; i++) data[i].Init(n);
        } else {
            data.assign(m, FenwickTree<T>(n));
        }
    }

    vector<FenwickTree<T> > data;
};

/*
** BIT Linear Construction Snippet
**

class Fenwick{
    int *m, N;
public:
    Fenwick(int a[], int n);
};

Fenwick::Fenwick(int a[], int n){
    N = n;
    m = new int[N];
    memset(m, 0, sizeof(int)*N);
    for(int i=0;i<N;++i){
        m[i] += a[i];
        if((i|(i+1))<N) m[i|(i+1)] += m[i];
    }
}
*/
```

5.3 Longest Common Ancestor

```

#define MAX_N 100000
#define LOG2_MAXN 16

// NOTE : memset(parent, -1, sizeof(parent));
int N, parent[MAX_N], L[MAX_N];
int P[MAX_N][LOG2_MAXN + 1];

int get_level(int u) {
    if (L[u] != -1)
        return L[u];
    else if (parent[u] == -1)
        return 0;
    return 1 + get_level(parent[u]);
}

void init() {
    memset(L, -1, sizeof(L));
    for (int i = 0; i < N; ++i) L[i] = get_level(i);

    memset(P, -1, sizeof(P));

    for (int i = 0; i < N; ++i) P[i][0] = parent[i];

    for (int j = 1; (1 << j) < N; ++j)
        for (int i = 0; i < N; ++i)
            if (P[i][j - 1] != -1) P[i][j] = P[P[i][j - 1]][j - 1];
}

int LCA(int p, int q) {
    if (L[p] < L[q]) swap(p, q);

    int log = 1;
    while ((1 << log) <= L[p]) ++log;
    --log;

    for (int i = log; i >= 0; --i)
        if (L[p] - (1 << i) >= L[q]) p = P[p][i];

    if (p == q) return p;

    for (int i = log; i >= 0; --i) {
        if (P[p][i] != -1 && P[p][i] != P[q][i]) {
            p = P[p][i];
            q = P[q][i];
        }
    }

    return parent[p];
}

```

5.4 Segment Tree

```

#include <bits/stdc++.h>
using namespace std;

/*
** Generic segment tree with lazy propagation (requires C++11)
** Sample node implementation that supports
** Query: sum of the elements in range [a, b)
** Update: add a given value X to every element in range [a, b)
*/

struct StNode {
    using NodeType = StNode;
    using i64 = long long;
    i64 val; // Sum of the interval
    i64 lazy; // Sumation pending to apply to children

    // Used, while creating the tree, to update the Node content according to
    // the value given by the ValueProvider
    void set(const NodeType& from) {
        val = from.val;
        lazy = identity().lazy;
    }

    // Updates the Node content to store the result of the 'merge' operation
    // applied on the children.
    // The tree will always call push_lazy() on the Node *before* calling merge()
    void merge(const NodeType& le, const NodeType& ri) {
        val = le.val + ri.val;
        lazy = identity().lazy;
    }

    // Used to update the Node content in a tree update command
    void update(const NodeType& from) {
        auto new_value = from.val;
        val += (e - s) * new_value;
        lazy += new_value;
    }

    // Pushes any pending lazy updates to children
    void push_lazy(NodeType& le, NodeType& ri) {
        if (lazy == identity().lazy) {
            return;
        }

        le.lazy += lazy;
        le.val += (le.e - le.s) * lazy;

        ri.lazy += lazy;
    }
};

```

```

    ri.val += (ri.e - ri.s) * lazy;

    lazy = identity().lazy;
}

// This function should return a NodeType instance such that calling
// Y.merge(X, identity()) or Y.merge(identity(), X) for any Node X with no
// pending updates should make Y match X exactly.
static NodeType identity() {
    static auto tmp = (NodeType){0, 0};
    return tmp;
}

// Internal tree data
int son[2]; // Children of this node
int s, e; // Interval [s, e), covered by this node
};

template <class Node>
struct SegmentTree {
    using ValueProvider = function<Node(int)>;
    vector<Node> T;

    SegmentTree(int n, const ValueProvider& vp = [] (int pos) {
        return Node::identity();
    }) {
        Node nd;
        nd.son[0] = nd.son[1] = -1;
        nd.s = 0, nd.e = n;

        T.reserve(4 * n);
        T.emplace_back(std::move(nd));

        init(vp, 0);
    }

    void init(const ValueProvider& vp, int u) {
        Node& n = T[u];

        if (n.e - n.s == 1) {
            n.set(vp(n.s));
            return;
        }

        Node le(n), ri(n);

        le.e = (n.s + n.e) / 2;
        n.son[0] = T.size();
        T.emplace_back(std::move(le));
        init(vp, n.son[0]);

        ri.s = le.e;
        n.son[1] = T.size();

```

```

        T.emplace_back(std::move(ri));
        init(vp, n.son[1]);

        n.merge(T[n.son[0]], T[n.son[1]]);
    }

    void update(int le, int ri, const Node& val, int u = 0) {
        Node& n = T[u];
        if (le >= n.e || n.s >= ri) return;

        if (n.s == le && n.e == ri) {
            n.update(val);
            return;
        }

        n.push_lazy(T[n.son[0]], T[n.son[1]]);

        update(le, min(T[n.son[0]].e, ri), val, n.son[0]);
        update(max(T[n.son[1]].s, le), ri, val, n.son[1]);
        n.merge(T[n.son[0]], T[n.son[1]]);
    }

    Node query(int le, int ri, int u = 0) {
        Node& n = T[u];
        if (n.e <= le || n.s >= ri) return Node::identity();
        if (n.s == le && n.e == ri) return n;

        n.push_lazy(T[n.son[0]], T[n.son[1]]);

        Node r1, r2, r3;
        r1 = query(le, min(T[n.son[0]].e, ri), n.son[0]);
        r2 = query(max(T[n.son[1]].s, le), ri, n.son[1]);
        r3.merge(r1, r2);
        return r3;
    }
};

/*
** USAGE SAMPLE
** http://www.spoj.com/problems/HORRIBLE/
*/
int main() {
    ios_base::sync_with_stdio(false);
    cin.tie(nullptr);

    int tc;
    cin >> tc;

    for (int cas = 1; cas <= tc; ++cas) {
        int n, c;
        cin >> n >> c;

        SegmentTree<StNode> st(n);

```

```

for (int i = 0; i < c; ++i) {
    int k, p, q;
    cin >> k >> p >> q;
    p -= 1;

    if (k == 0) {
        int v;
        cin >> v;
        st.update(p, q, (StNode){v});
    } else {
        auto sum = st.query(p, q).val;
        cout << sum << '\n';
    }
}

return 0;
}

```

6 Math

6.1 Combinations

```

long long comb(int n, int m) {
    if (m > n - m) m = n - m;

    long long C = 1;
    // C^{n}_{i} -> C^{n}_{i+1}
    for (int i = 0; i < m; ++i) C = C * (n - i) / (i + 1);
    return C;
}

// Cuando n y m son grandes y se pide comb(n, m) % MOD,
// donde MOD es un numero primo, se puede usar el Teorema de Lucas.

#define MOD 3571
int C[MOD][MOD];

void FillLucasTable() {
    memset(C, 0, sizeof(C));

    for (int i = 0; i < MOD; ++i) C[i][0] = 1;
    for (int i = 1; i < MOD; ++i) C[i][i] = 1;
    for (int i = 2; i < MOD; ++i)
        for (int j = 1; j < i; ++j) C[i][j] = (C[i - 1][j] + C[i - 1][j - 1]) % MOD;
}

```

```

int comb(int n, int k) {
    long long ans = 1;

    while (n != 0) {
        int ni = n % MOD, ki = k % MOD;
        n /= MOD;
        k /= MOD;
        ans = (ans * C[ni][ki]) % MOD;
    }

    return (int)ans;
}

```

6.2 Chinese Remainer Theorem

```

// rem y mod tienen el mismo numero de elementos
long long chinese_remainder(vector<int> rem, vector<int> mod) {
    long long ans = rem[0], m = mod[0];
    int n = rem.size();

    for (int i = 1; i < n; ++i) {
        int a = modular_inverse(m, mod[i]);
        int b = modular_inverse(mod[i], m);
        ans = (ans * b * mod[i] + rem[i] * a * m) % (m * mod[i]);
        m *= mod[i];
    }

    return ans;
}

```

6.3 Deterministic Miller Rabin

```

/*
** Deterministic Miller-Rabin
** if n < 3,825,123,056,546,413,051, it is enough to test
** a = 2, 3, 5, 7, 11, 13, 17, 19, and 23.
*/
#include <bits/stdc++.h>
using namespace std;
typedef unsigned long long ll;

vector<ll> mr_values({2, 3, 5, 7, 11, 13, 17, 19, 23});

ll mulmod(ll a, ll b, ll n) {

```

```

ll erg = 0;
ll r = 0;
while (b > 0) {
    // unsigned long long gives enough room for base 10 operations
    ll x = ((a % n) * (b % 10)) % n;
    for (ll i = 0; i < r; i++) x = (x * 10) % n;
    erg = (erg + x) % n;
    r++;
    b /= 10;
}
return erg;
}

ll fastexp(ll a, ll b, ll n) {
    if (b == 0) return 1;
    if (b == 1) return a % n;
    ll res = 1;
    while (b > 0) {
        if (b % 2 == 1) res = mulmod(a, res, n);
        a = mulmod(a, a, n);
        b /= 2;
    }
    return res;
}

bool mrtest(ll n) {
    if (n == 1) return false;
    ll d = n - 1;
    ll s = 0;
    while (d % 2 == 0) {
        s++;
        d /= 2;
    }
    for (ll j = 0; j < (ll)mr_values.size(); j++) {
        if (mr_values[j] > n - 1) continue;
        ll ad = fastexp(mr_values[j], d, n);
        if (ad % n == 1) continue;
        bool notcomp = false;
        for (ll r = 0; r <= max(0ull, s - 1); r++) {
            ll rr = fastexp(2, r, n);
            ll ard = fastexp(ad, rr, n);
            if (ard % n == n - 1) {
                notcomp = true;
                break;
            }
        }
        if (!notcomp) {
            return false;
        }
    }
    return true;
}

```

```

bool isprime(ll n) {
    if (n <= 1) return false;
    if (n == 2) return true;
    if (n % 2 == 0) return false;
    return mrtest(n);
}

```

6.4 Big Integer

```

string trim_zeros(const string& a) {
    size_t idx = 0;
    while (a[idx] == '0' && idx < a.size()) idx++;
    if (idx == a.size()) idx--;
    return a.substr(idx);
}

string big_sub(const string& n1, const string& n2) {
    string a = trim_zeros(n1);
    string b = trim_zeros(n2);

    bool minus = false;
    if (esMayor(b, a)) {
        swap(a, b);
        minus = true;
    }

    int i, j, d = (a.length() - b.length());
    for (i = b.length() - 1; i >= 0; i--) {
        if (a[i + d] >= b[i])
            a[i + d] -= b[i] - '0';
        else {
            j = -1;
            while (a[i + d + j] == '0') {
                a[i + d + j] = '9';
                j--;
            }
            a[i + d + j]--;
            a[i + d] += 10 - b[i] + '0';
        }
    }

    return (minus ? "-" : "") + trim_zeros(a);
}

string big_add(const string& a, const string& b) {
    int LA = a.size(), LB = b.size(), L = max(LA, LB), carry = 0;

```

```

string x = string(L, '0');

while (L--> 0) {
    LA--;
    LB--;

    if (LA >= 0) carry += a[LA] - '0';
    if (LB >= 0) carry += b[LB] - '0';

    if (carry < 10)
        x[L] = '0' + carry, carry = 0;
    else
        x[L] = '0' + carry - 10, carry = 1;
}

if (carry) x = '1' + x;
return x;
}

string big_mult(string a, string b) {
    if (a == "0" || b == "0")
        return "0";
    else if (a.size() == 1) {
        int m = a[0] - '0';

        string ans = string(b.size(), '0');

        int lleva = 0;

        for (int i = b.size() - 1; i >= 0; i--) {
            int d = (b[i] - '0') * m + lleva;
            lleva = d / 10;
            ans[i] += d % 10;
        }
        if (lleva) ans = (char)(lleva + '0') + ans;
        return ans;
    } else if (b.size() == 1)
        return big_mult(b, a);
    else {
        string ans = "0";
        string ceros = "";
        for (int i = a.size() - 1; i >= 0; i--) {
            string s = big_mult(string(1, a[i]), b) + ceros;
            ceros += "0";
            ans = big_add(ans, s);
        }
        return ans;
    }
}

```

6.5 Factorial Prime Factors

```

vector<int> primes; // Filled with prime numbers <= n (at least)

void factorial_prime_factor(const int n, vector<int>& v) {
    v.clear();
    for (size_t i = 0; primes[i] <= n && i < primes.size(); i++) {
        const int& p = primes[i];
        double q = (n / (double)p);
        int d = int(q);

        while (q >= p) {
            q /= p;
            d += int(q);
        }

        v.push_back(d);
    }
}

```

6.6 Extended Gcd

```

// a*x + b*y = gcd(a,b)
int extGcd(int a, int b, int &x, int &y) {
    if (b == 0) {
        x = 1;
        y = 0;
        return a;
    }

    int g = extGcd(b, a % b, y, x);
    y -= a / b * x;
    return g;
}

// ASSUME: gcd(a, m) == 1
int modInv(int a, int m) {
    int x, y;
    extGcd(a, m, x, y);
    return (x % m + m) % m;
}

```

6.7 Least Significant Bit Position

```
// http://supertech.csail.mit.edu/papers/debruijn.pdf
int lsbpos(unsigned int v) {
    static const int t[32] = {0, 1, 28, 2, 29, 14, 24, 3, 30, 22, 20,
        15, 25, 17, 4, 8, 31, 27, 13, 23, 21, 19,
        16, 7, 26, 12, 18, 6, 11, 5, 10, 9};
    return t[((unsigned int)((v & -v) * 0x077CB531U)) >> 27];
}
```

7 General

7.1 Longest Increasing Subsequence

```
#include <vector>
/* Finds longest strictly increasing subsequence. O(n log k) algorithm. */
void find_lis(vector<int> &a, vector<int> &b) {
    vector<int> p(a.size());
    int u, v;

    if (a.empty()) return;

    b.push_back(0);
    for (size_t i = 1; i < a.size(); i++) {
        // If next element a[i] is greater than last element of current longest
        // subsequence a[b.back()], just push it at back of "b" and continue
        if (a[b.back()] < a[i]) {
            p[i] = b.back();
            b.push_back(i);
            continue;
        }
        // Binary search to find the smallest element referenced by b which is just
        // bigger than a[i]
        // Note : Binary search is performed on b (and not a). Size of b is always
        // <= k and hence contributes O(log k) to complexity.
        for (u = 0, v = b.size() - 1; u < v;) {
            int c = (u + v) / 2;
            if (a[b[c]] < a[i])
                u = c + 1;
            else
                v = c;
        }
        // Update b if new value is smaller then previously referenced value
        if (a[i] < a[b[u]]) {
            if (u > 0) p[i] = b[u - 1];
            b[u] = i;
        }
    }
    for (u = b.size(), v = b.back(); u--; v = p[v]) b[u] = v;
}
```

7.2 Inversion Counting

```
int v[MAX], sortedV[MAX];

// Merge sort with inversion counting
long long mergeSort(int *V, int lo, int hi) {
    if (lo >= hi) {
        return 0;
    } else {
        int m1 = (lo + hi) / 2, m2 = m1 + 1;
        long long r = 0, rA, rB;
        int i = lo, j = m2, k = 0;

        rA = mergeSort(V, lo, m1);
        rB = mergeSort(V, m2, hi);

        while (i <= m1 && j <= hi) {
            if (V[j] < V[i]) {
                r += (m1 - i + 1);
                sortedV[k++] = V[j++];
            } else {
                sortedV[k++] = V[i++];
            }
        }

        if (i > m1) {
            i = j;
            j = hi;
        } else {
            j = m1;
        }

        while (i <= j) {
            sortedV[k++] = V[i++];
        }

        memcpy(V + lo, sortedV, (hi - lo + 1) * sizeof(int));

        return r + rA + rB;
    }
}
```