

McCulloch-Pitts Neural Model

February 2, 2023

McCulloch-Pitts Neural Model for AND case

Step 1: Generate a vector of inputs and a vector of weights.

```
[ ]: import numpy as np

input_table = np.array([
    [0,0],
    [0,1],
    [1,0],
    [1,1]
])
print(f'Input Table:\n{input_table}')
```

Input Table:

```
[[0 0]
 [0 1]
 [1 0]
 [1 1]]
```

```
[ ]: weights = np.array([1,1])
print(f'weights: {weights}')
```

weights: [1 1]

Step 2: Compute the dot product between the matrix of inputs and weights

```
[ ]: dot_products = np.dot(input_table, weights)
print(f'Dot products: {dot_products}')
```

Dot products: [0 1 1 2]

Step 3: Define the threshold activation function

```
[ ]: def linear_threshold_gate(dot, threshold):
    if dot >= threshold:
        return 1
    else:
        return 0
```

Step 4: Compute the output based on the threshold value

```
[ ]: T = 2
     for i in range(0,4):
         activation = linear_threshold_gate(dot_products[i], T)
         print(f'Activation: {activation}')
```

Activation: 0
 Activation: 0
 Activation: 0
 Activation: 1

McCulloch-Pitts Neural Model for OR case

For OR case, Threshold can be 1 or greater than 1

```
[ ]: input_table = np.array([
    [0,0],
    [0,1],
    [1,0],
    [1,1]
])
     print(f'Input Table:\n{input_table}')
```

Input Table:
 [[0 0]
 [0 1]
 [1 0]
 [1 1]]

```
[ ]: weights = np.array([1,1])
     print(f'weights: {weights}')
```

weights: [1 1]

```
[ ]: dot_products = np.dot(input_table, weights)
     print(f'Dot products: {dot_products}')
```

Dot products: [0 1 1 2]

```
[ ]: T = 1
     for i in range(0,4):
         activation = linear_threshold_gate(dot_products[i], T)
         print(f'Activation: {activation}')
```

Activation: 0
 Activation: 1
 Activation: 1
 Activation: 1

For NOR case, Threshold will be 0 and weights will be negative

```
[ ]: input_table = np.array([
    [0,0],
    [0,1],
    [1,0],
    [1,1]
])
print(f'Input Table:\n{input_table}')
```

Input Table:

```
[[0 0]
 [0 1]
 [1 0]
 [1 1]]
```

```
[ ]: weights = np.array([-1,-1])
print(f'weights: {weights}')
```

weights: [-1 -1]

```
[ ]: dot_products = np.dot(input_table, weights)
print(f'Dot products: {dot_products}')
```

Dot products: [0 -1 -1 -2]

```
[ ]: T = 0
for i in range(0,4):
    activation = linear_threshold_gate(dot_products[i], T)
    print(f'Activation: {activation}')
```

Activation: 1
Activation: 0
Activation: 0
Activation: 0