

12/1/2024

FOL to CNF conversion

Step 1: remove implications

return "or (Not ( {part(0,3)}, {part(1,2)} )"

Step 2: apply-demorgans-law

formula. replace ('Not (And ; 'Or(Not)'). replace ('Not  
'And (Not')

Step 3: distribute-quantifiers

formula. replace ('Forall (; 'And ('). replace  
'Exists (; 'Or (')

Step 1: Create a list of SKOLEM-CONSTANTS

Step 2: Find  $\forall, \exists$

If the attributes are lower case, replace them  
with a skolem constant

remove used skolem constant or function from the  
list

If the attributes are both lowercase and  
uppercase replace the uppercase attribute with  
a Skolem function

Step 3: replace  $\Leftrightarrow$  with  $\underline{\quad}$   
transform — as  $Q \equiv (P \Rightarrow Q) \wedge (Q \Rightarrow P)$

Step 4: replace  $\Rightarrow$  with  $\underline{\quad}$

Step 5: Apply demorgan's law

replace  $\sim [$   
as  $\sim P \wedge Q$  if ( & was present)

replace  $\sim [$   
as  $\sim P \vee \sim Q$  if ( & was present)

replace  $\sim$  with  $\underline{\quad}$

FOL to CNF

Q6

```
print( Skolemization( fol_to_cnf ("animal (y) => loves (x,y) ") ))
print( Skolemization( fol_to_cnf ("∀x [∀y [animal(y) => loves (x,y)]]
=> [∃z [loves (z,x)]]" )) )
print( fol_to_cnf (" [american (x) & weapon (y) & sells (x,y,z) &
hatch6(z)] => criminal (x) ") )
```

Output:

$[\neg \text{animal}(y) \vee \text{loves}(x,y)] \& [\neg \text{loves}(x,y) \vee \text{animal}(y)]$   
 $[\text{animal}(G(x)) \& \neg \text{loves}(\sim, G(x))]/[\text{loves}(F(x), x)]$   
 $[\neg \text{american}(x) \vee \neg \text{weapon}(y) \vee \neg \text{sells}(x,y,z) \vee \neg \text{hatch6}(z)]/\text{criminal}(x)$

```
print(Skolemization(fol_to_cnf("animal(y)<=>loves(x,y)")))
print(Skolemization(fol_to_cnf("∀x[∀y[animal(y)=>loves(x,y)]]=>[∃z[loves(z,x)]]")))
print(fol_to_cnf("[american(x)&weapon(y)&sells(x,y,z)&hostile(z)]=>criminal(x)"))
```

```
[~animal(y)|loves(x,y)]&[~loves(x,y)|animal(y)]
[animal(G(x))&~loves(x,G(x))]|[loves(F(x),x)]
[~american(x)|~weapon(y)|~sells(x,y,z)|~hostile(z)]|criminal(x)
```