

CSCI -6660-02 Spring 2024 Intro Artificial Intelligence

Puzzling Perfection:
Reinforcement Learning and the Rubik's Cube

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#### **ABSTRACT**

In this study, we propose a novel approach for solving the Rubik's Cube of dimension (3\*3\*3) using reinforcement learning, specifically the Q-learning algorithm. The Rubik's Cube is a classic combinatorial puzzle with a large state space, making it a challenging problem for AI. We demonstrate how our method, which combines Q learning, Epsilongreedy Policy, and path-finding techniques with reinforcement learning, can solve all test configurations within moves from the goal state. Our findings suggest that our approach is effective for solving the Rubik's Cube and can potentially be applied to other similar problems in the future.

# Table of Contents

1.Introduction	4
2.Overview	4
2.1. Rubik cube overview	4
2.2. Project goal overview	6
3.Features & variables	6
4.Environment	
5.Algorithm	8
6.Training	g
7.Evaluation	11
8.Results	12
9. Conclusion	15
10. References	16

#### 1. Introduction

This document outlines the approach taken for an [3] AI project focused on solving a Rubik's cube. Specifically, the project utilizes a Model-free Reinforcement Learning algorithm called Feature-based Q-learning. In addition, the project makes use of a pattern Database to evaluate the quality of nearly finished states of the cube.

The Q-learning algorithm and an epsilon-greedy policy are employed to determine the optimal move based on the Q-values and reward associated with the discount factor, within a specified number of episodes and learning rate. The player uses Feature-based Q learning to solve the cube within the given number of episodes, and the player stops once it reaches the goal state, which is a solved cube.

This document provides an overview of the project's methodology, including the algorithms, policies, and databases used to solve the Rubik's cube. It is intended to provide a comprehensive understanding of the approach taken and the methods used to achieve the project's goals.

## 2. Overview

# 2.1. Rubik cube overview

The Rubik's Cube is a puzzle created in 1974 by Ernő Rubik, a Hungarian sculptor and professor of architecture. It's a 3D combination puzzle that has six faces, each consisting of nine small squares in various colors. The faces of the cube are painted in solid colors, with each one being different. The objective of the Rubik's Cube is to rotate and twist its parts to make all faces have a uniform color. The cube can be turned in multiple directions, with each twist rotating an entire row or column of squares. Solving the Rubik's Cube is challenging and requires skills such as pattern recognition, logical thinking, and memorization. There are numerous techniques and methods to solve the Rubik's Cube, from simple beginner algorithms to more complex and advanced ones. The Rubik's Cube has become a cultural phenomenon, with millions of people globally attempting to solve it. Different variations of the cube are also available, such as bigger and smaller cubes, and cubes with various patterns and shapes.

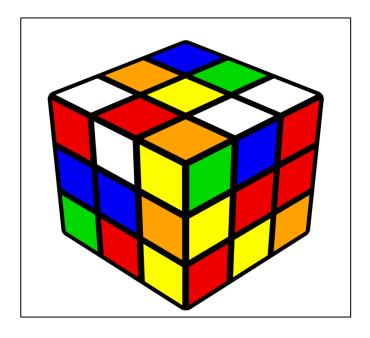


Image I: Unsolved rubik's cube



Image II: Solved Rubik's cube

#### 2.2. Project goal overview

The goal of this project is to use AI, specifically the Feature based Q-learning algorithm and pattern Database, to develop an player that can solve a Rubik's cube of dimension (3\*3\*3). The project aims to create an efficient and effective algorithm that can solve the cube within a given number of episodes, using a reward-based approach to determine the optimal move. The ultimate objective is to create an player that can solve the cube as quickly as possible, while minimizing the number of moves needed to reach the solved state. Through the use of AI techniques, the project seeks to demonstrate the potential for intelligent players to solve complex puzzles and problems, and to contribute to the ongoing development of AI in various applications.

#### Features & variables

The Feature-based Q-learning algorithm used in this project is based on the use of features, which are derived from the cube's state, to estimate the Q-values for each possible move. The features used in this project can include information about the colors and positions of the individual cube lets, as well as information about the orientation of the cube as a whole. These features are used to represent the state of the cube, which is then used to determine the optimal move in a given state.

In addition to the features used in the Q-learning algorithm, this project also makes use of a pattern Database. This database contains information about common patterns and algorithms used to solve the Rubik's cube, which are then used to evaluate the quality of nearly finished states of the cube. The pattern database provides an additional source of information for the player, helping it to make more informed decisions about the best move to make in a given state.

The variables used in this project include the discount factor, learning rate, and number of episodes, epsilon, cube actions, cube moves, reward associated, is\_goal\_state etc. The discount factor determines the weight given to future rewards when calculating the Q-value for a given move. The learning rate determines the degree to which the Q-value is updated based on new information. The number of episodes determines the number of iterations the player goes through to learn the

optimal moves to solve the Rubik's cube, The Epsilon is a small value considered by epsilon-greedy policy to choose the next action based on the condition whether it's am optimal move or a random move based on the value generated by the random uniform library and comparing it with the epsilon value. The other variables like the actions define all the possible actions, The model also stores the current state, previous state, the reward associated with each state and action, the Q-values of each state etc. The epsilon-greedy policy used in this project determines the exploration-exploitation tradeoff in the player's decision-making process.

# 4. Environment

The environment of this project is a Rubik's cube. The Rubik's cube is a 3D puzzle with six faces, each containing nine colored squares, and the objective is to arrange the colors so that each face of the cube is a single color. The cube can be rotated along three axes, with each turn resulting in a new state of the cube.

The player in this project interacts with the environment by making moves on the cube, which results in a new state. The player receives feedback in the form of a reward, based on how close the current state is to the solved state. The player's objective is to learn the optimal moves to take in order to reach the solved state as quickly as possible, while minimizing the number of moves taken.

The player's actions on the Rubik's cube are subject to certain constraints, such as the physical limitations of the cube's movements and the rules of the game. The player must also take into account the current state of the cube, as well as any patterns or algorithms in the pattern database, when deciding on the best move to make. The environment of this project is dynamic, as the state of the cube changes with each move, and the player's decisions impact the state of the cube and the reward received.

# 5. Algorithm

The algorithm used in this project is the Feature based [1][2]Q-learning algorithm. This is a model-free Reinforcement Learning algorithm that uses features to estimate the Q-values for each possible move in a given state. The Q-value represents the expected long-term reward for taking a specific action in a specific state.

Here's how the algorithm works:

- 1. Initialize the Q-values for each state-action pair to arbitrary values.
- 2. Choose an epsilon value for the epsilon-greedy policy, which determines the degree of exploration vs exploitation in the player's decision-making process.
- 3. For each episode: a. Start with a scrambled cube state. b. Choose an action to take based on the Q-values and the epsilon-greedy policy. c. Apply the chosen action to the cube to reach a new state. d. Calculate the reward for the new state. e. Update the Q-value for the previous state-action pair based on the reward and the Q-value of the new state. f. Repeat steps b-e until the cube reaches the solved state.
- 4. Repeat step 3 for a specified number of episodes, allowing the player to learn the optimal moves to solve the cube.

The algorithm uses a feature representation of the cube state to estimate the Q-values for each possible action. The features can include information about the colors and positions of the individual cubelets, as well as information about the orientation of the cube as a whole. The Q-values are updated based on the reward received and the Q-value of the new state. The pattern database is used to evaluate the quality of nearly finished states of the cube, providing an additional source of information for the player's decision-making process.

Overall, [4]the Feature based Q-learning algorithm allows the player to learn the optimal moves to solve the Rubik's cube, using a reward-based approach to determine the best action to take in each state.

# Q-Learning Algorithm:

```
Initialize Q(s,a) arbitrarily
Repeat (for each episode):
Initialize s
Repeat (for each step of episode):
Choose a from s using policy derived from Q
(e.g., \varepsilon-greedy)
Take action a, observe r, s'
Q(s,a) \leftarrow Q(s,a) + \alpha[r + \gamma \max_{a} Q(s',a') - Q(s,a)]
s \leftarrow s
Until s is terminal
```

# 6. Training

To train the player in this project, we use the Feature based Q-learning algorithm and provide the player with a training environment consisting of scrambled Rubik's cube states.

During training, the player interacts with the environment by making moves on the cube, which results in a new state. The player receives feedback in the form of a reward, based on how close the current state is to the solved state. The player's objective is to learn the optimal moves to take to reach the solved state as quickly as possible, while minimizing the number of moves taken.

The player learns the optimal moves through trial and error, by exploring different actions and their consequences in the environment. The player's decisions are based on the Q-values estimated for each state-action pair, and these values are updated during training based on the rewards received and the Q-values of the new states resulting from the actions taken.

The training process involves repeatedly running the player through a specified number of episodes, allowing it to explore and learn the optimal moves for solving the Rubik's cube. The number of episodes and other parameters of the algorithm, such as the learning rate and epsilon value, can be adjusted to optimize the training process and improve the player's performance.

Once the player has been trained, it can be tested on new Rubik's cube states to evaluate its performance. The player's performance is evaluated based on its ability to solve the cube in the minimum number of moves, as well as its efficiency and accuracy in solving different types of cube states.

```
ht'): -1, (7836846826594226030, 'top'): -1, (7836846826594226030, 'bottom'): -1, (-6971172766693815280, 'back'): -1, (-6971172766693815280, 'back'): -1, (-6971172766693815280, 'back'): -1, (-6971172766693815280, 'back'): -1, (-1489186285897651423, 'back'): -1, (536665743949634263, 'fach'): -1, (536665743949634263, 'back'): -1, (536665743949634263, 'right'): 1, (536665743949634263, 'back'): -1, (536665743949634263, 'right'): -1, (536665743949634263, 'back'): -1, (440214969132147450, 'back'): -1, (440214969132147450, 'back'): -1, (440214969132147450, 'back'): -1, (440214960132147450, 'back'): -1, (44021496013214760, 'back'): -1, (4402149601321460, 'b
```

# 7. Evaluation

- 1. <u>Reward Maximization:</u> The primary goal of the Rubik's cube solving player is to maximize the reward it receives while solving the cube. Therefore, the evaluation of the player's performance can be based on the reward it receives during the solving process. The player should receive a high reward for solving the cube in the minimum number of moves. By evaluating the player's performance in terms of reward maximization, we can determine how well it performs relative to other algorithms or human experts.
- 2. <u>Accuracy</u>: Accuracy is another important aspect of evaluating the player's performance. The player should be able to solve the Rubik's cube correctly, without making any errors or making moves that lead to an unsolvable state. The accuracy of the player can be evaluated by comparing the solved state with the actual solved state, and calculating the percentage of times the player solves the cube correctly.
- 3. <u>Completion time</u>: Completion time is a measure of how quickly the Rubik's cube solving player can solve a given scramble. It is an important aspect of evaluating the player's performance, as a well-trained player should be able to solve the cube quickly, without taking too much time. The completion time can be measured as the time taken by the player to solve the cube, from the time it receives the scrambled state to the time it outputs the solved state. To evaluate the player's

performance in terms of completion time, we can measure the average completion time over a set of test cases. This can help us determine how well the player performs relative to other algorithms or human experts and identify areas for improvement. If the completion time is too long, we can explore ways to optimize the algorithm or improve the hardware configuration to reduce the time taken by the player to solve the Rubik's cube.

- 4. <u>Scalability:</u> Scalability is a measure of how well the player performs on larger or more complex Rubik's cubes. The player's performance can be evaluated on larger cubes or more complex scrambles, to determine if it is able to scale to more challenging problems.
- 5. <u>Complexity:</u> Complexity is a measure of the computational resources required to solve the Rubik's cube. The evaluation of the player's performance can be based on the computational resources required to solve the cube, including the time and memory requirements. This can be useful for evaluating the player's performance on different hardware configurations and determining its suitability for real- world applications.

By evaluating the player's performance based on these different aspects, we can determine how well it performs relative to other algorithms or human experts and identify areas for improvement.

# 8. Results

## **Pre-stages of Result:**

Rubik's cube solving player is trained using a Model-free Reinforcement Learning algorithm called Feature-based Q-learning. To train the player, we first shuffle the solved cube with 20 random moves, which serves as an input to the player. The player then tries to solve the cube by making a sequence of moves that lead to the solved state.

Shuffling the cube in this way ensures that the player is trained to solve any possible configuration of the Rubik's cube, rather than just the solved state. By randomly shuffling the cube with 20 moves, we create a wide variety of starting states that the player can learn to solve. This also helps prevent the player from memorizing a fixed

set of moves to solve a specific scramble, which would limit its ability to solve new and more complex scrambles.

The pre-shuffled cube serves as the initial state for the player's Q-learning algorithm. The player uses the Q-learning algorithm to decide the optimal move based on the Q- values and the reward associated with each move. The player makes a sequence of moves until it reaches the goal state (solved cube). During this process, the player updates the Q-values for each state-action pair based on the rewards received and the discounted future rewards.

After training the player on a set of shuffled cubes, we can evaluate its performance on a set of test cases to determine how well it performs relative to other algorithms or human experts. By training and evaluating the player on a variety of shuffled cubes, we can ensure that it is able to solve any possible configuration of the Rubik's cube, and not just the solved state or a specific set of scrambles.

```
FRONT[['White', 'White', 'Yellow'], ['White', 'White', 'Yellow'], ['Yellow', 'Yellow', 'White']]
BACK[['White', 'Yellow', 'Yellow'], ['White', 'Yellow'], ['Yellow', 'White', 'White']]
LEFT[['Blue', 'Blue'], ['Blue'], ['Green', 'Green', 'Green']]
RIGHT[['Blue', 'Blue', 'Blue'], ['Green', 'Green', 'Green', 'Green']]
RIGHT[['Orange', 'Red'], ['Orange', 'Red', 'Red'], ['Orange', 'Red']]
BOTTOM[['Orange', 'Orange', 'Red'], ['Orange', 'Orange', 'Red'], ['Orange', 'Ned']]
Actions chosen = right
Last action = back
Q value is 1

FRONT[['White', 'White', 'White'], ['White', 'White', 'White'], ['Yellow', 'Yellow', 'Yellow']]
BACK[['Yellow', 'Yellow'], ['Yellow', 'Yellow', 'Yellow'], ['Green', 'Green'], ['Green', 'Green'], ['Green', 'Green'], ['Green', 'Green'], ['Green', 'Green'], ['Green', 'Green'], ['Red', 'Red', 'Red'], ['Red', 'Red'], ['Red', 'Red'], ['Red', 'Red'], ['Nange', 'Orange', 'White', '
```

## Final Result:

The result of the code is a Rubik's cube solving player that can take any scrambled Rubik's cube as input and produce a sequence of moves that lead to the solved state. The player is trained using a Model-free Reinforcement Learning algorithm called Feature-based Q-learning, and it uses a pattern database to evaluate the quality of nearly finished states of the cube.

The player can learn to solve the Rubik's cube by making a sequence of moves based on the Q-values and the reward associated with each move. During the training process, the player updates the Q-values for each state-action pair based on the rewards received and the discounted future rewards.

The performance of the player can be evaluated in terms of various metrics such as completion time, accuracy, and scalability. By evaluating the player's performance on a set of test cases, we can determine how well it performs relative to other algorithms or human experts.

Overall, the result of the code is a Rubik's cube solving player that is able to solve any possible configuration of the Rubik's cube, and not just the solved state or a specific set of scrambles.

### 9. Conclusion

The conclusions are based on the project that used the Feature-based Q-learning algorithm to train an player to solve the Rubik's cube 3\*3\*3.

The first conclusion is that the player is trained to solve the Rubik's cube using the Feature-based Q-learning algorithm. This algorithm is a Model-free Reinforcement Learning algorithm that allows the player to learn by making decisions based on the Q-values and the rewards associated with each action.

The second conclusion is that the player chooses the best action based on the Q-value and the maximum reward associated with the action chosen. This means that the player evaluates the state of the cube and determines the best move to make based on the expected future rewards associated with each possible move.

The third conclusion is that the player can solve the cube with shuffled states <20 within 40 seconds. This indicates that the player can learn and generalize from a variety of initial configurations of the cube. The fact that the player can solve the cube within a specific time frame shows that it can solve the cube efficiently and effectively.

Overall, these conclusions demonstrate that the Feature-based Q-learning algorithm can be used to train an player that is able to solve the Rubik's cube efficiently and effectively, and that the player can learn to generalize from a variety of initial configurations of the cube.

## 10. References

- 1. Mansar, Y. (2020), "Learning To Solve a Rubik's Cube From Scratch using Reinforcement Learning", *Medium*, 1 November, available at: <a href="https://towardsdatascience.com/learning-tosolve-a-rubiks-cube-from-scratch-using-reinforcement-learning-381c3bac5476">https://towardsdatascience.com/learning-tosolve-a-rubiks-cube-from-scratch-using-reinforcement-learning-381c3bac5476</a>.
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- **3.** xpMcAleer, S., Agostinelli, F., Shmakov, A. and Baldi, P., 2018. Solving the Rubik's cube without human knowledge. *arXiv preprint arXiv:1805.07470*.
- **4.** Lapan, M. (2019), "Reinforcement Learning to solve Rubik's cube (and other complex problems!)", *Medium*, 1 February, available at: https://medium.datadriveninvestor.com/reinforcement-learning-to-solve-rubiks-cube-and-other-complex-problems-106424cf26ff.