



# Biomedical Engineering

## 生醫工程

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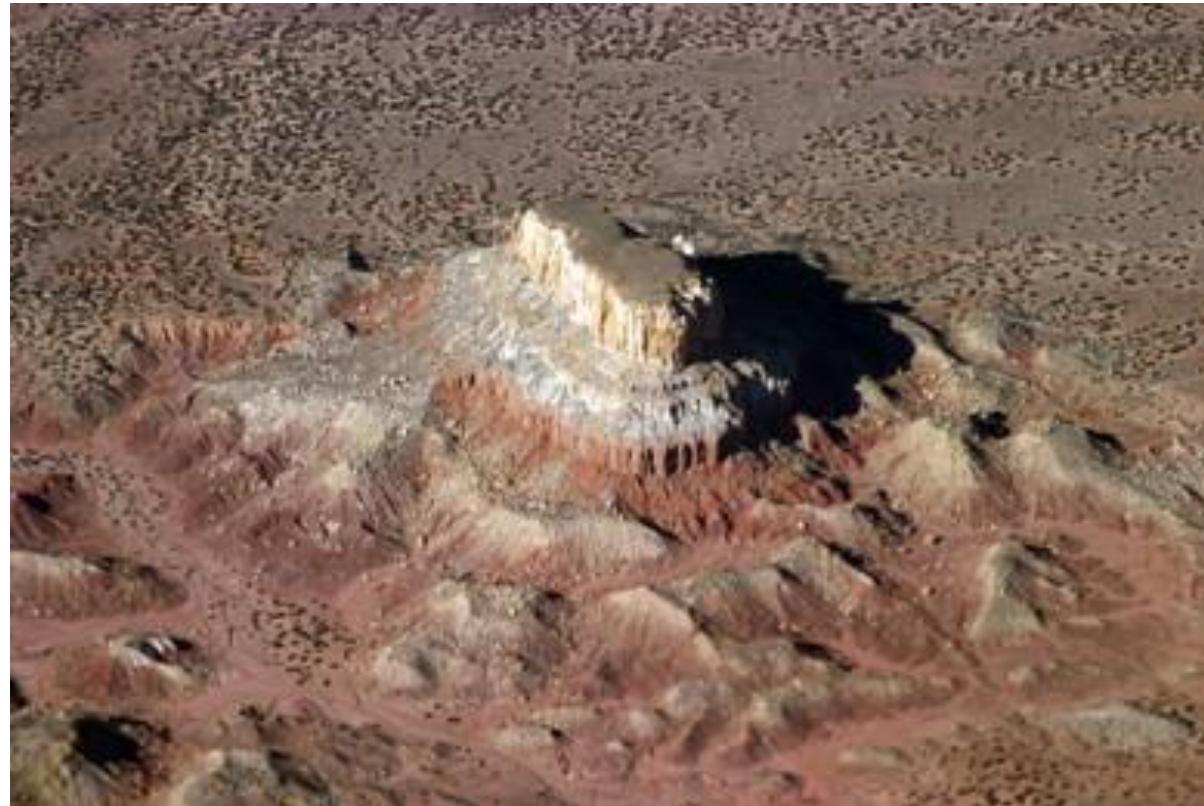
Spring 2024

# Biomedical Engineering

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(1) Review heat flow in 2D



(2) Landscape evolution

## Example for Heat Flow

$$\alpha^2 \left( \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} \right) = \frac{\partial u}{\partial t}$$

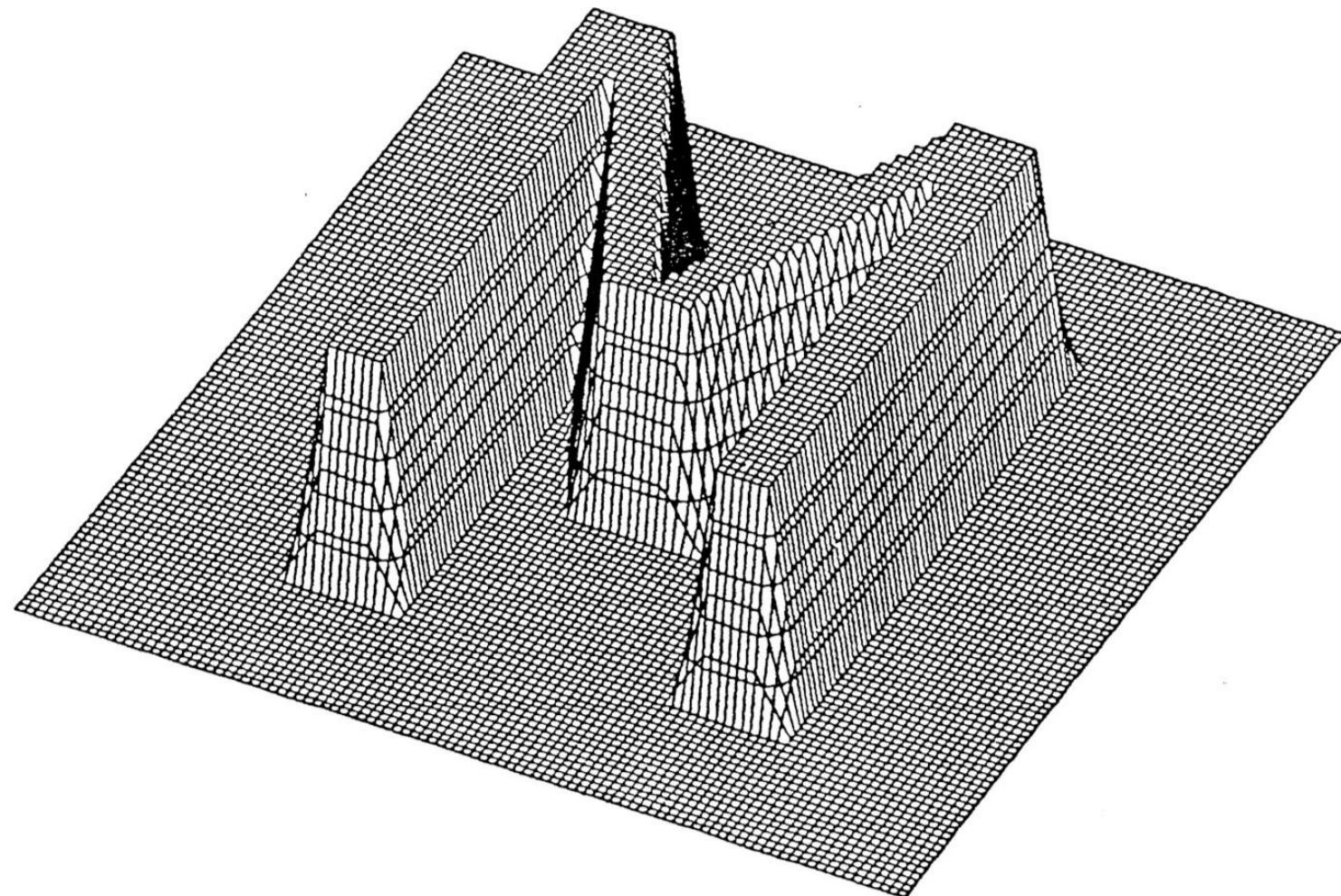


Figure 3.2:  $t = 0$

## Example in 2D

$$\alpha^2 \left( \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} \right) = \frac{\partial u}{\partial t}$$

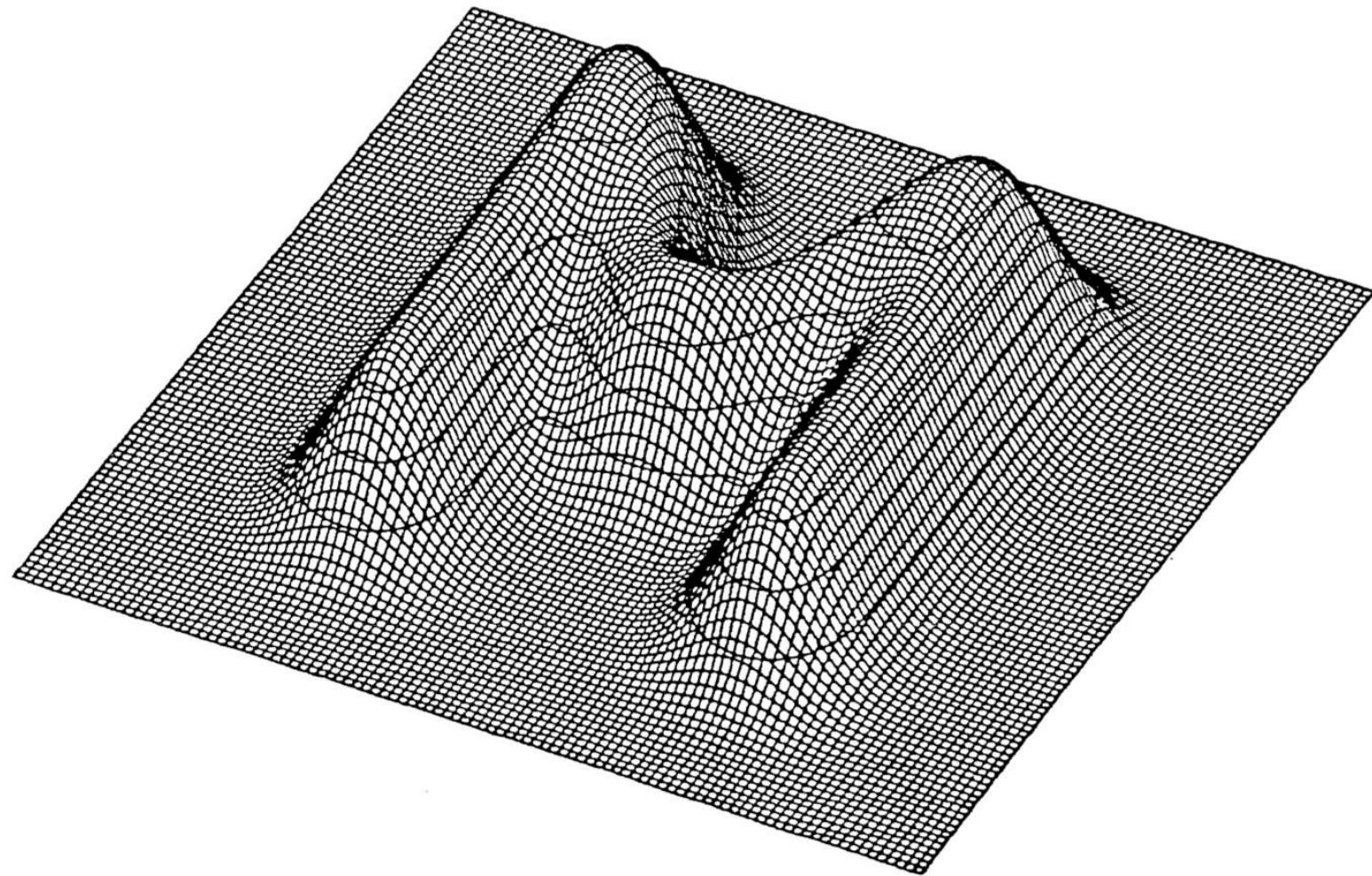


Figure 3.3:  $t = 0.001$

## Example in 2D

$$\alpha^2 \left( \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} \right) = \frac{\partial u}{\partial t}$$

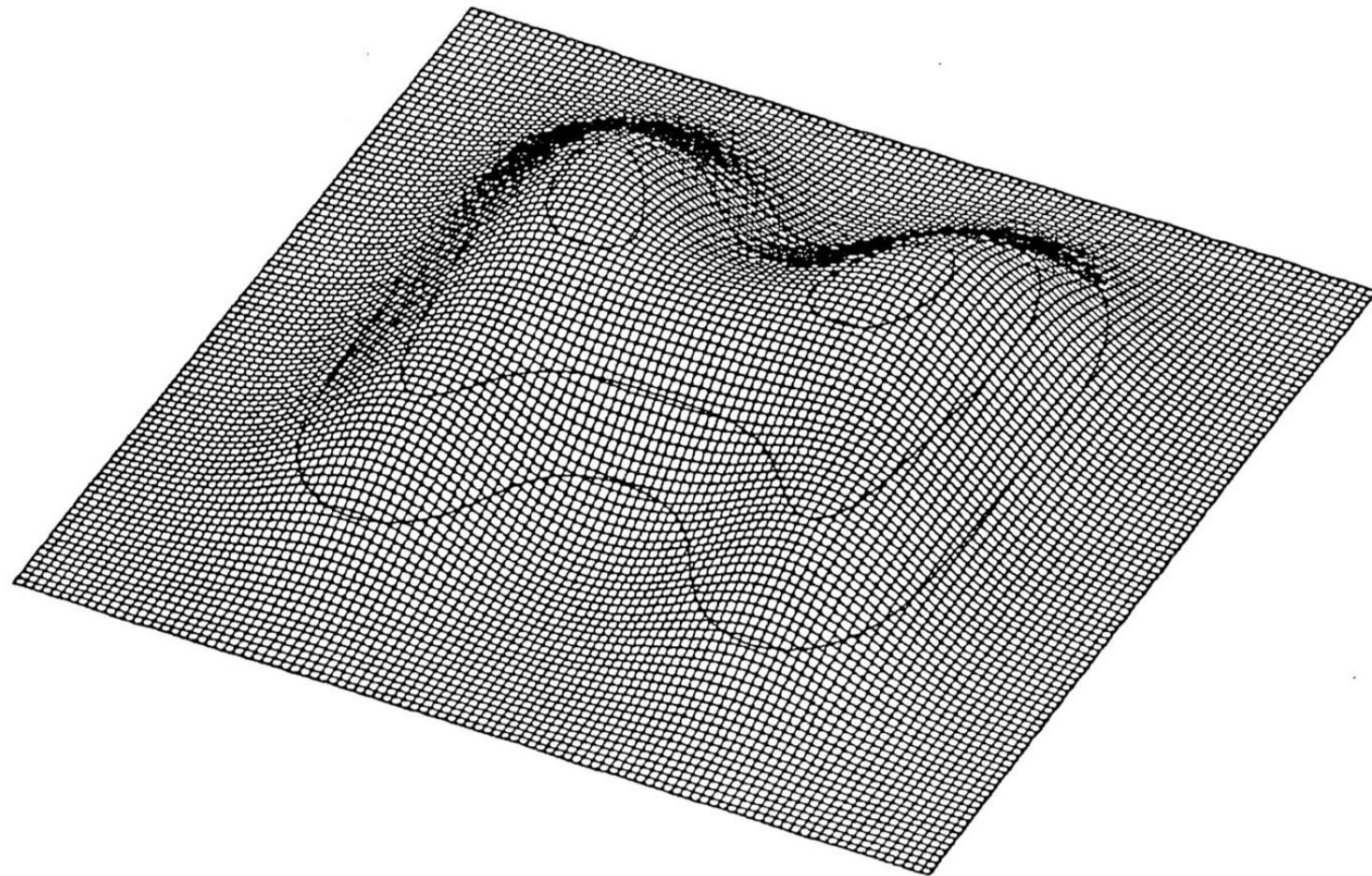


Figure 3.4:  $t = 0.004$

## Example in 2D

$$\alpha^2 \left( \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} \right) = \frac{\partial u}{\partial t}$$

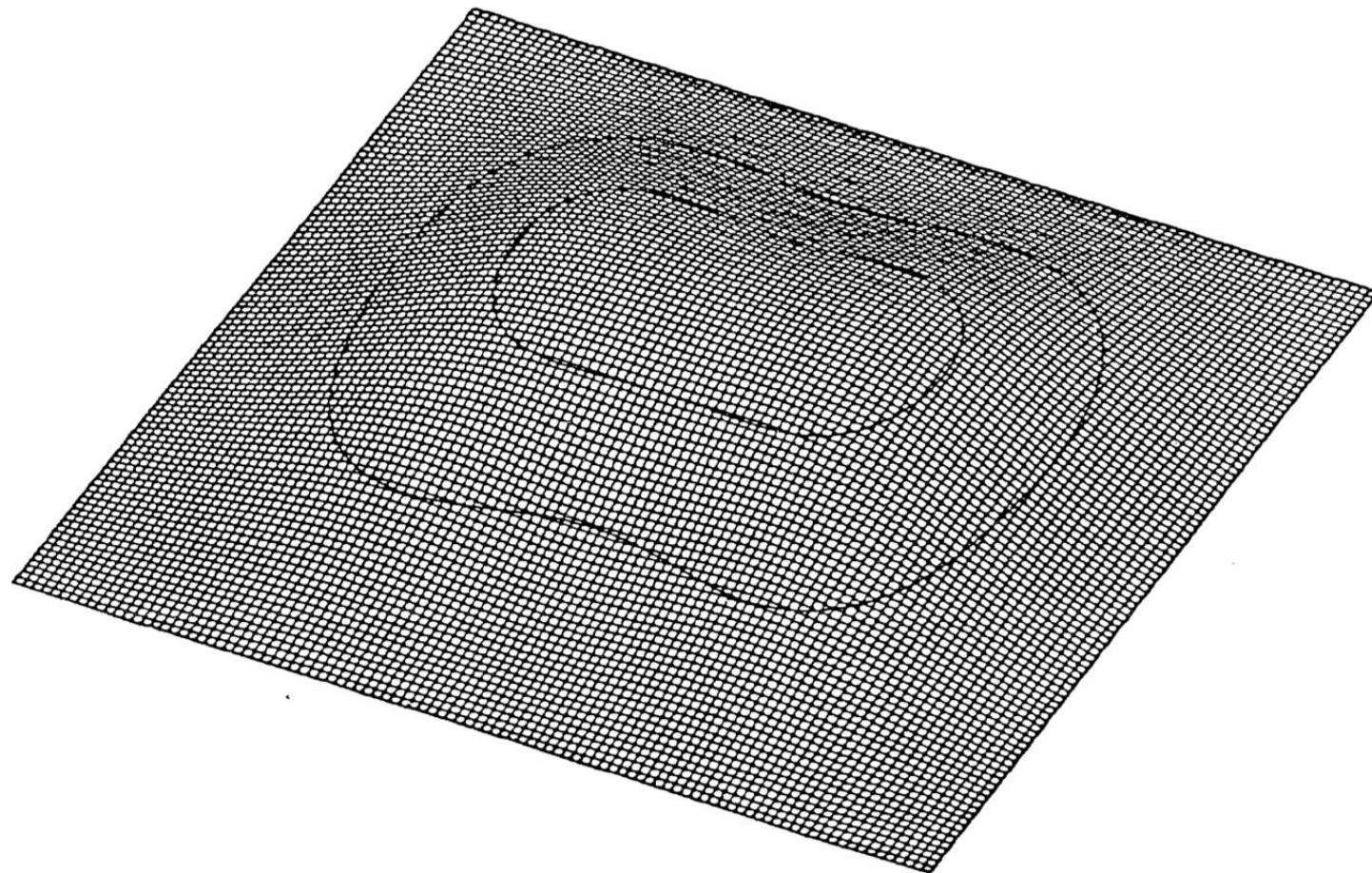
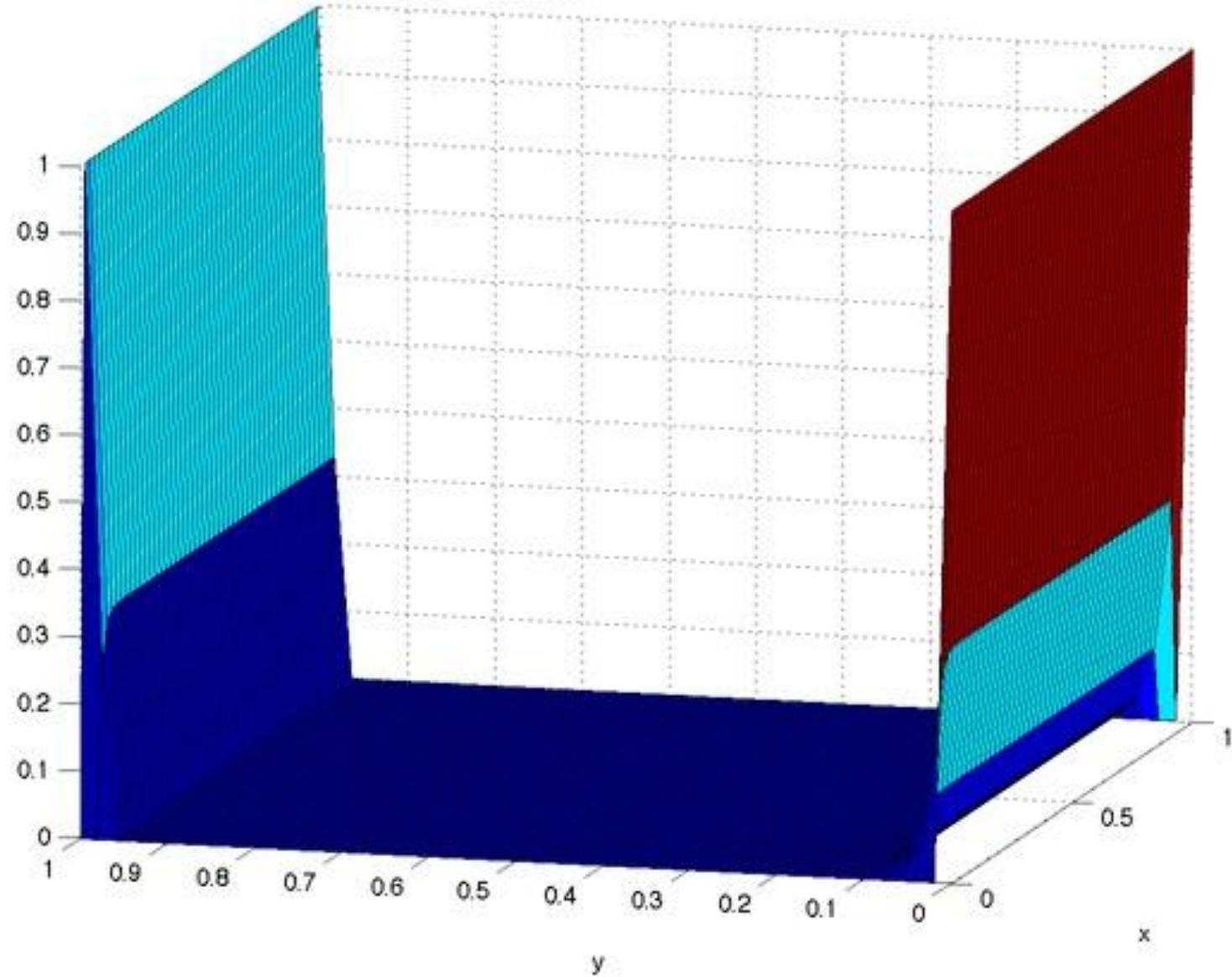
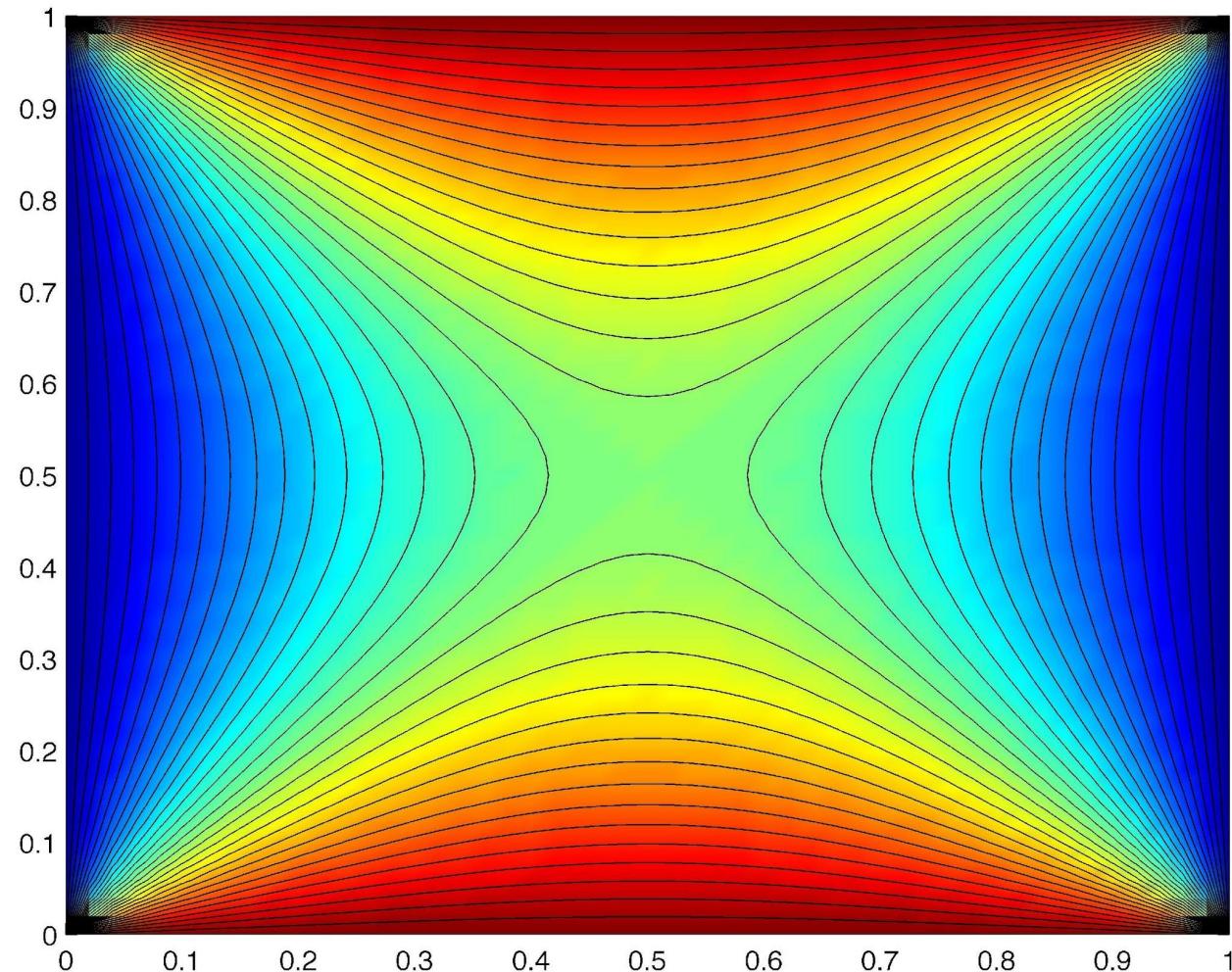


Figure 3.5:  $t = 0.01$

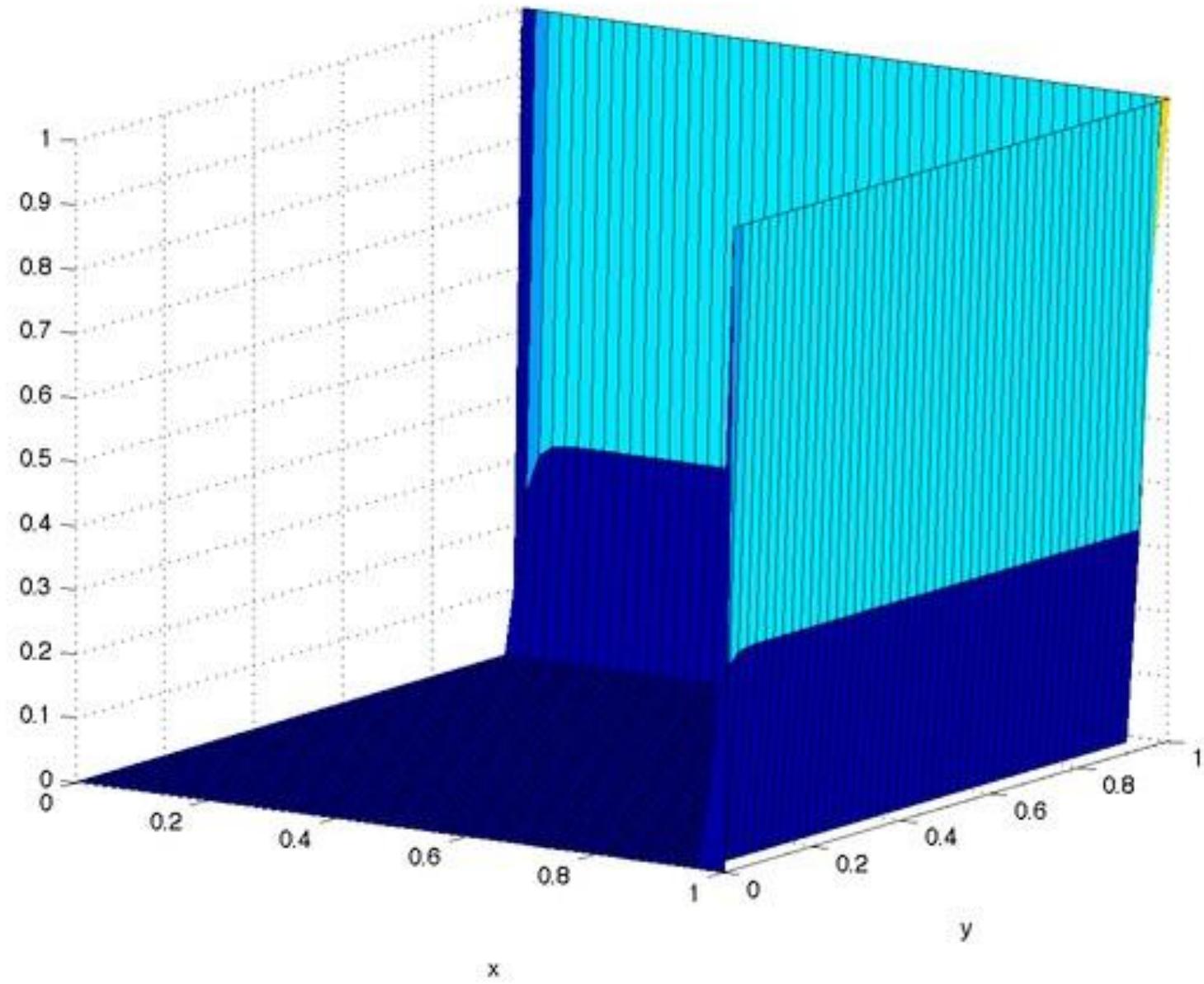
# Method 1: Jacobi Method



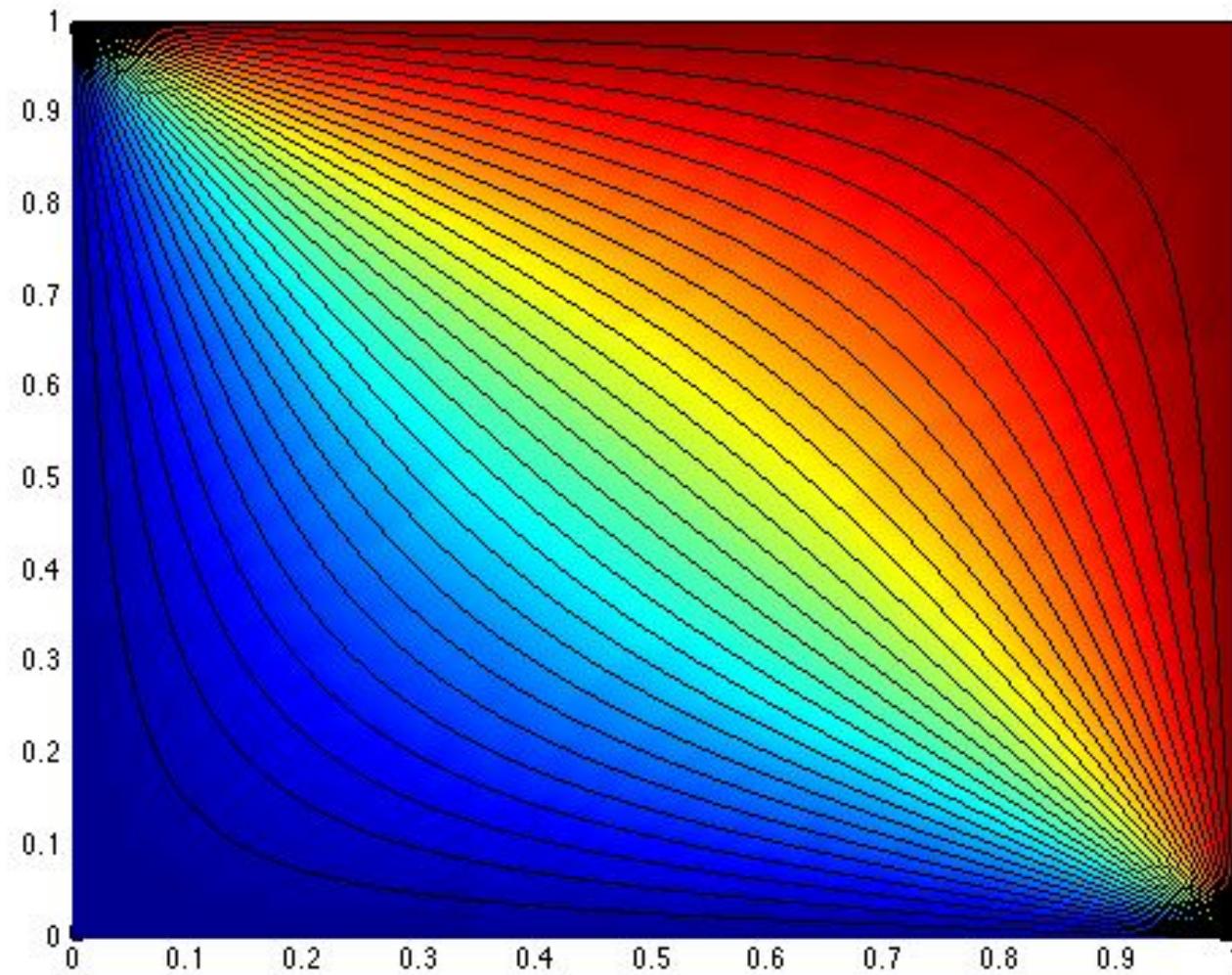
# Contour Plot of the Stationary State



# Different boundary conditions



# Contour Plot of Stationary State (Different boundary conditions)



# What processes contributed to this formation?

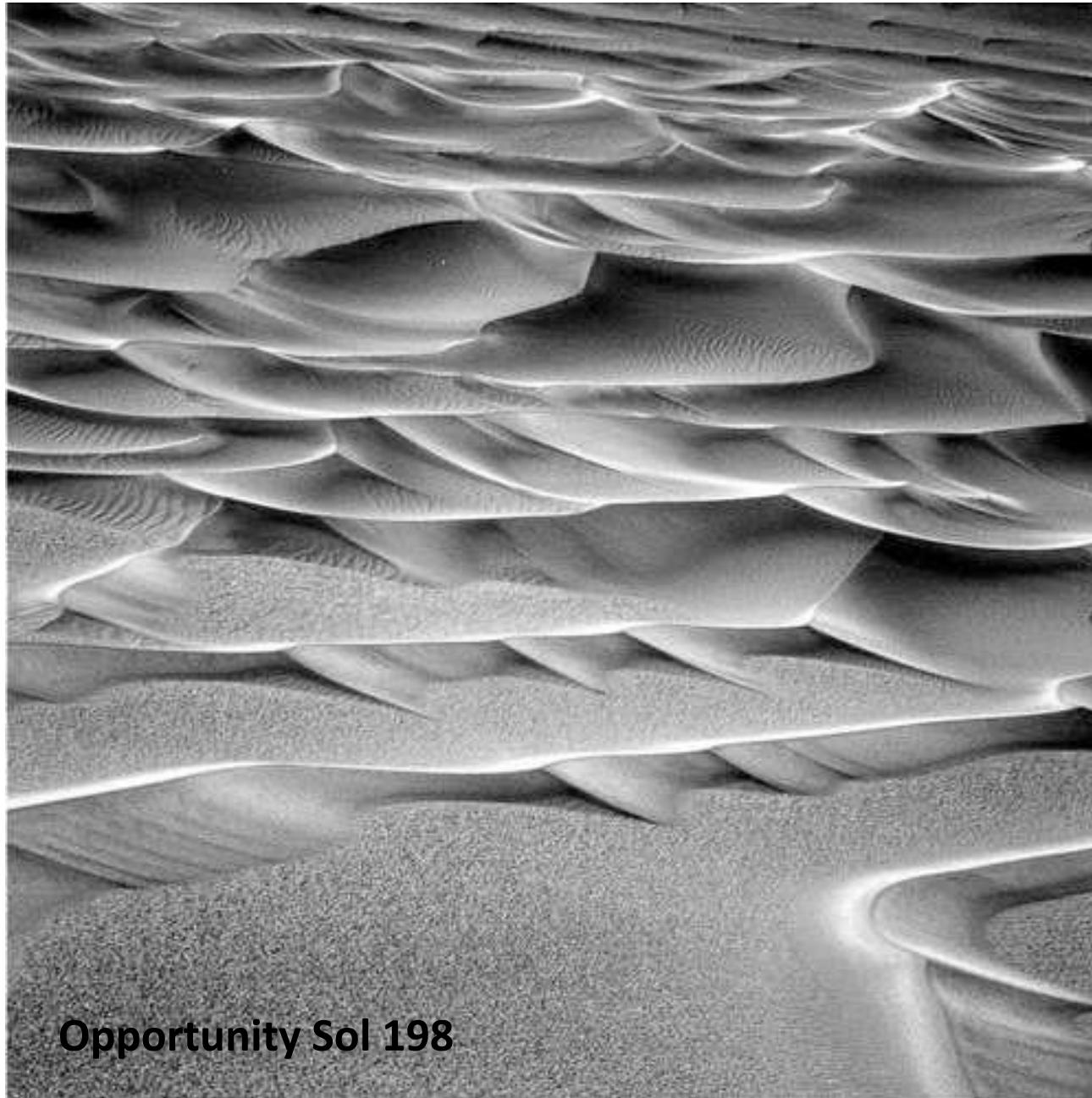
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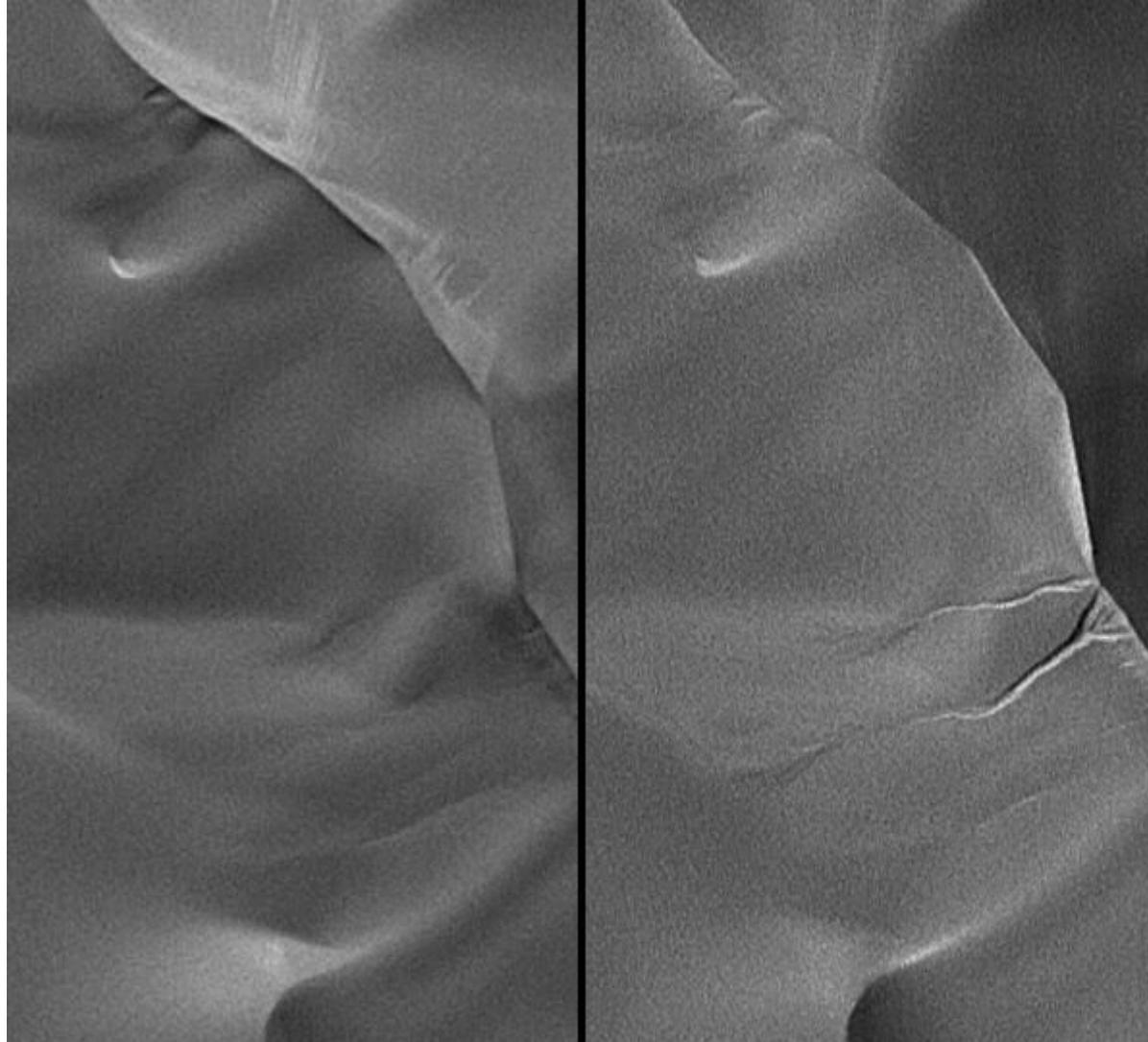


**Figure 1.** Aerial photograph of a landscape near Orland, California, showing quasiperiodic valley spacing of roughly 100 m. Photo by J. Kirchner.

# Erosion: Sand dunes on Mars



Sand dunes are common (wind affects landscape)



July 2002

April 2005

NASA/JPL/MSSS

Mars has an active surface

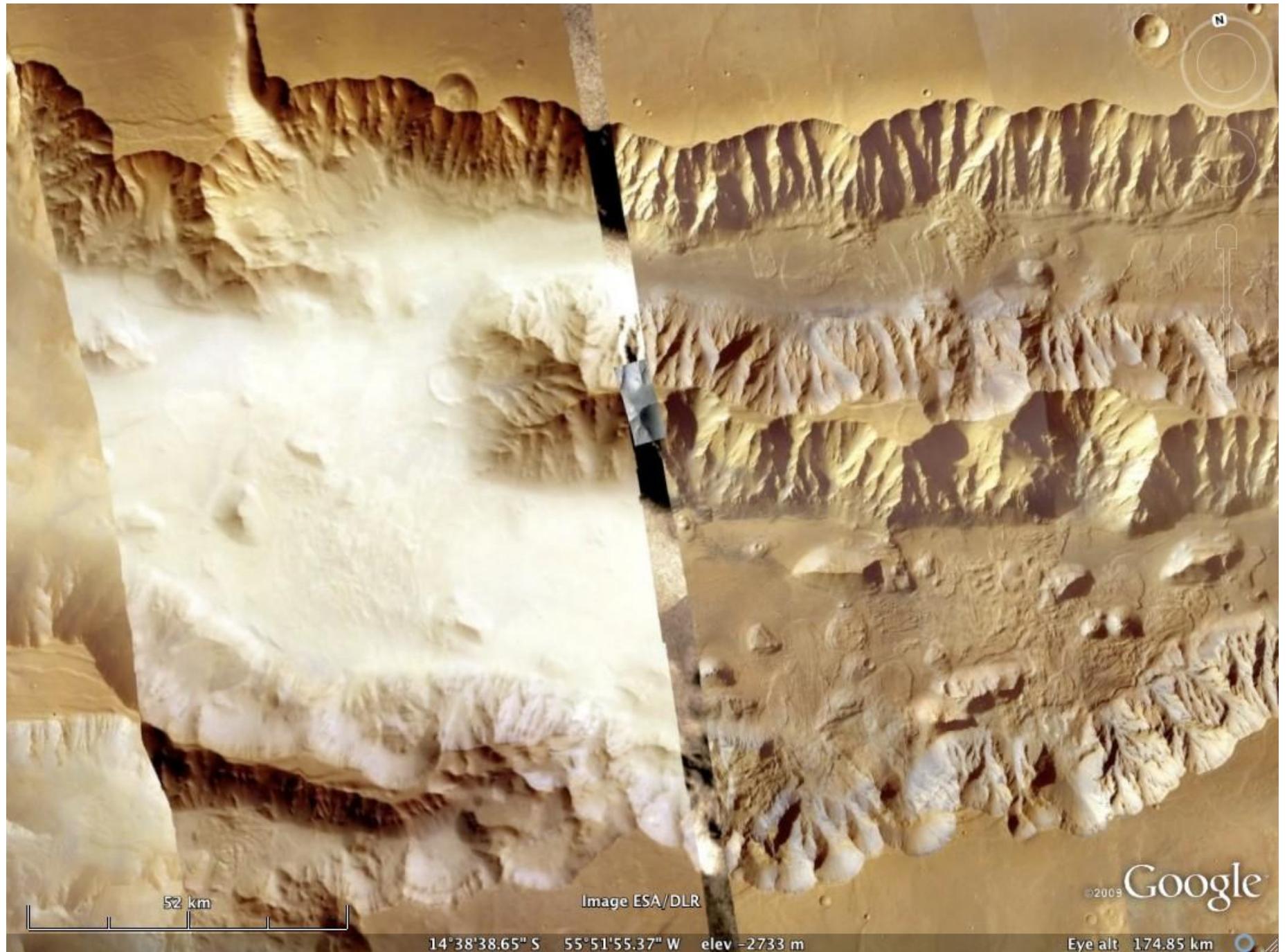
2 August 1999

27 April 2001

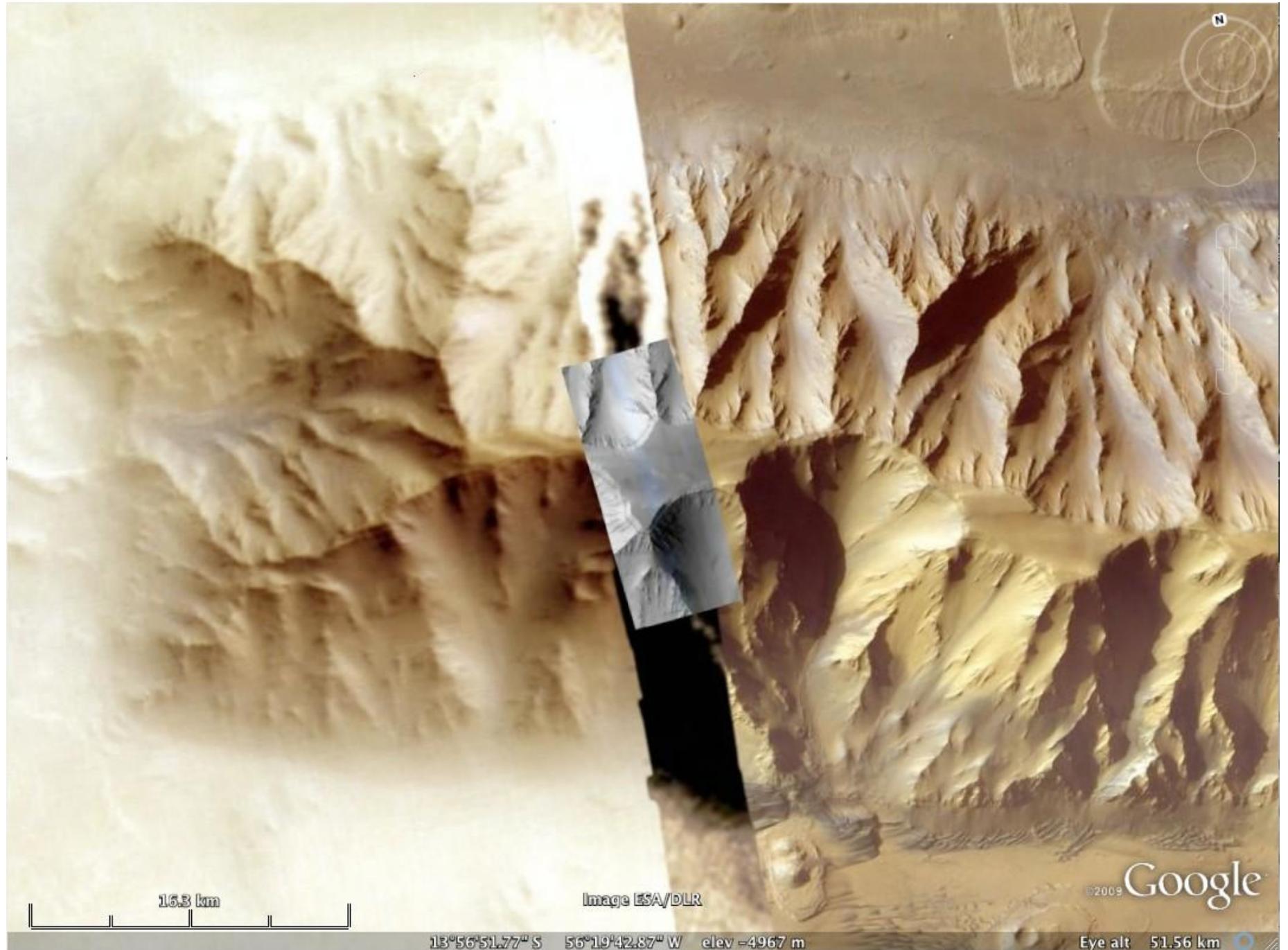
# Slope streaks



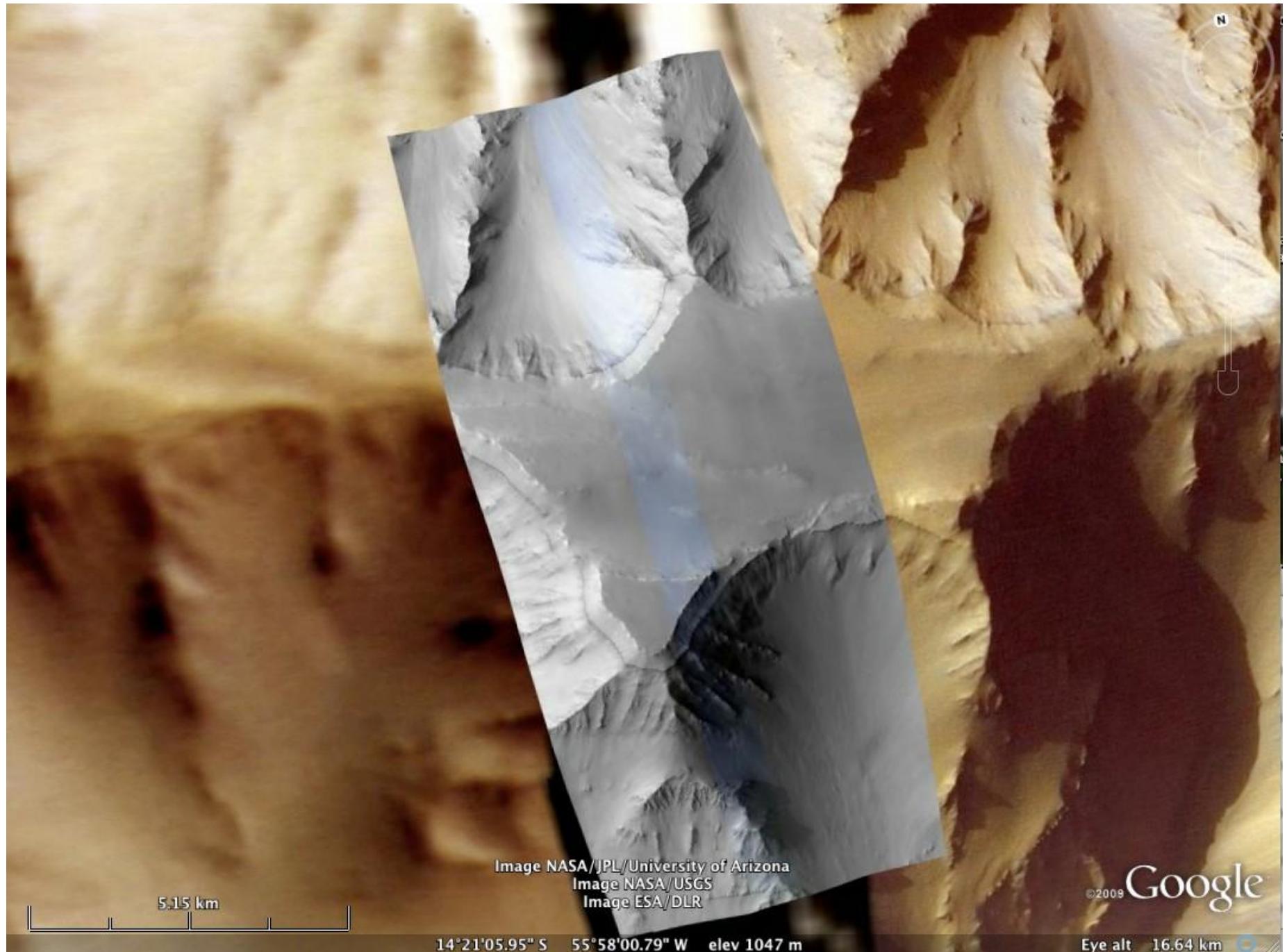
500 m



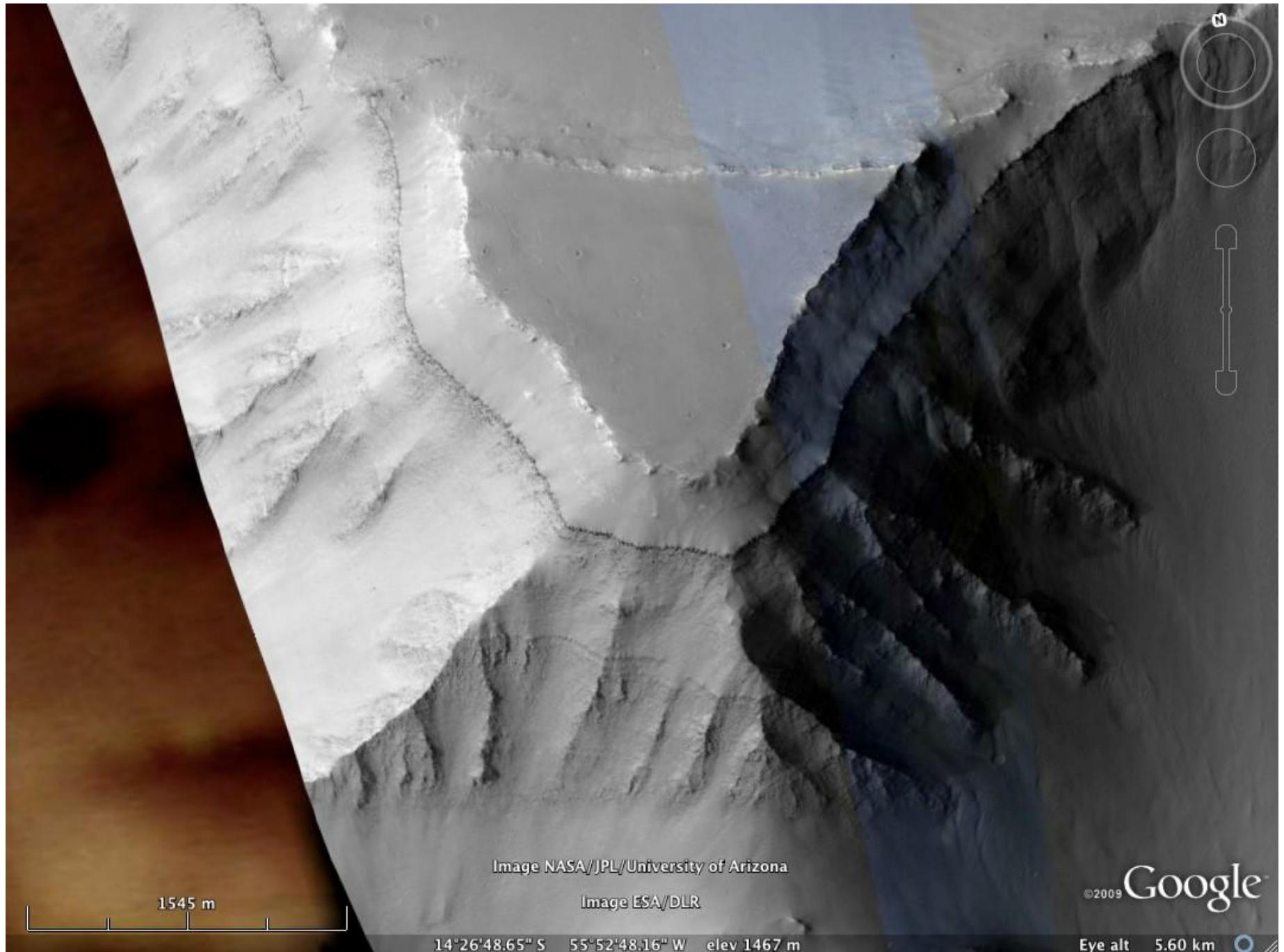
Eastern Valles Marineris: layered outcrops – Deposits of sediments from water?



Eastern Valles Marineris: layered outcrops – Deposits of sediments from water?



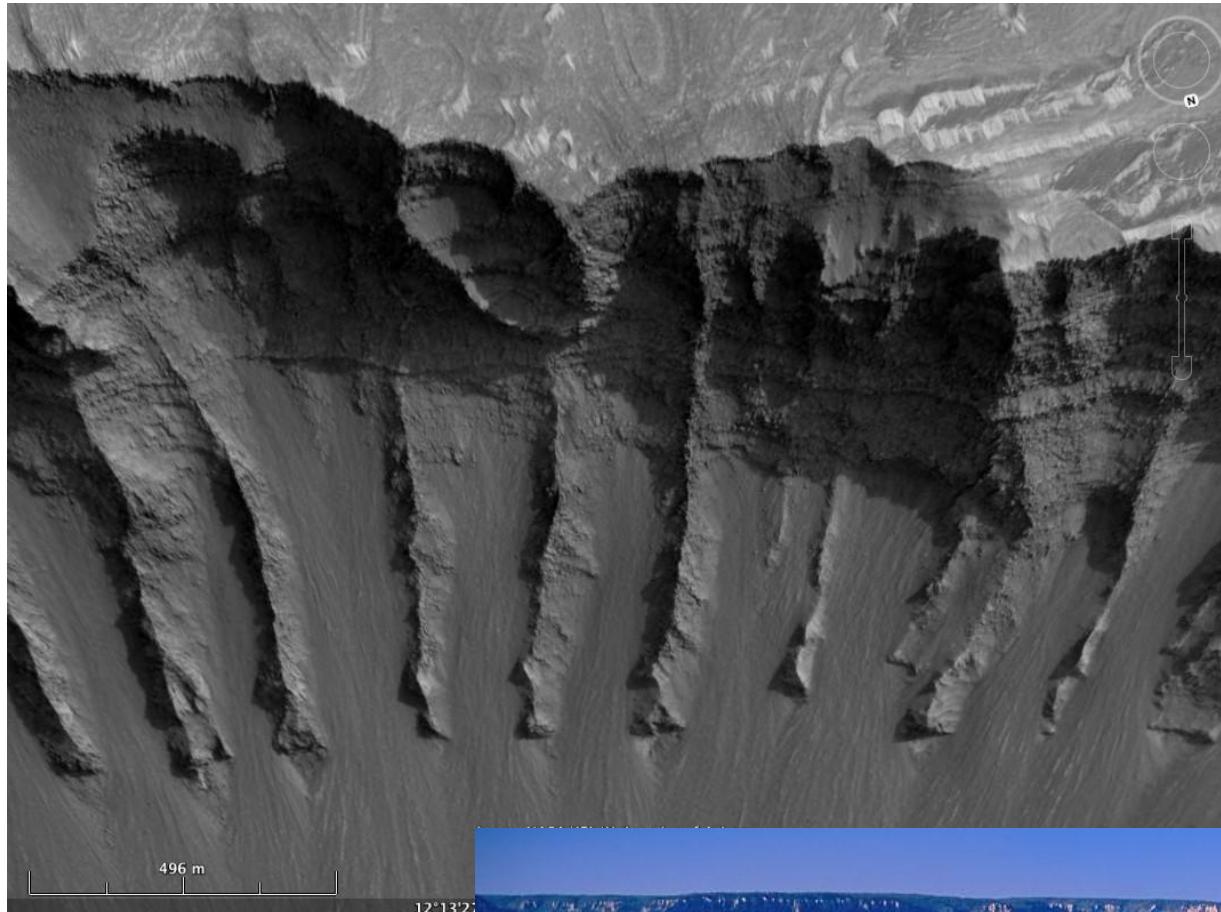
Eastern Valles Marineris: layered outcrops – Deposits of sediments from water?



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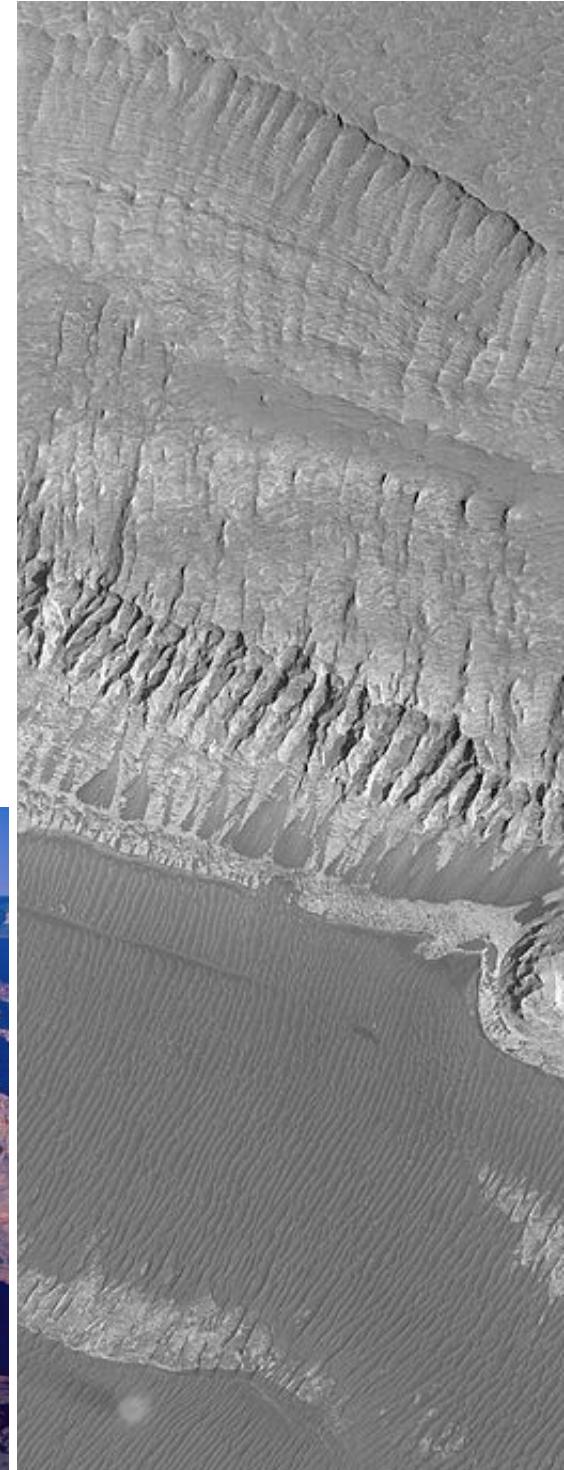


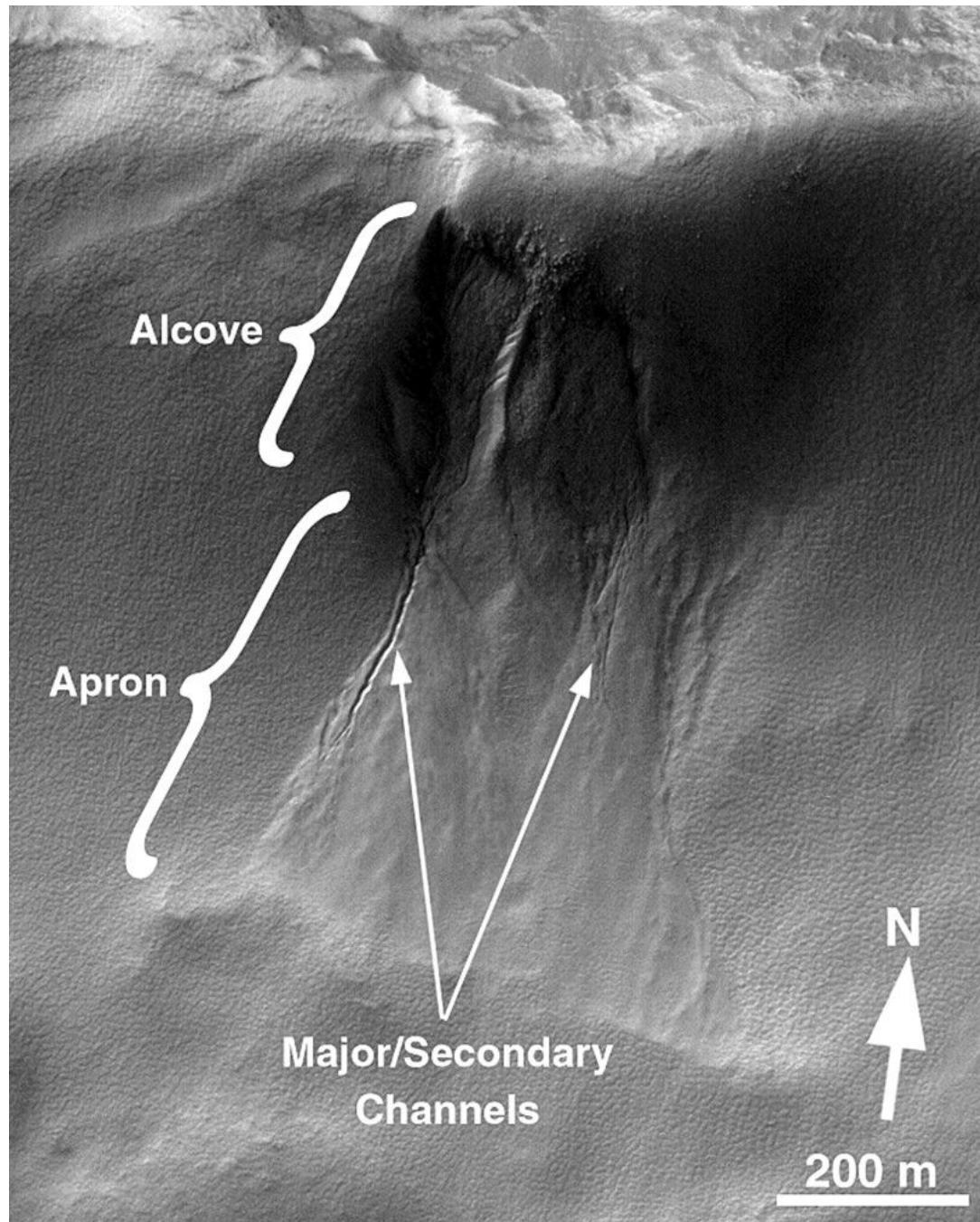
Eastern Valles Marineris: layered outcrops – Deposits of sediments from water?



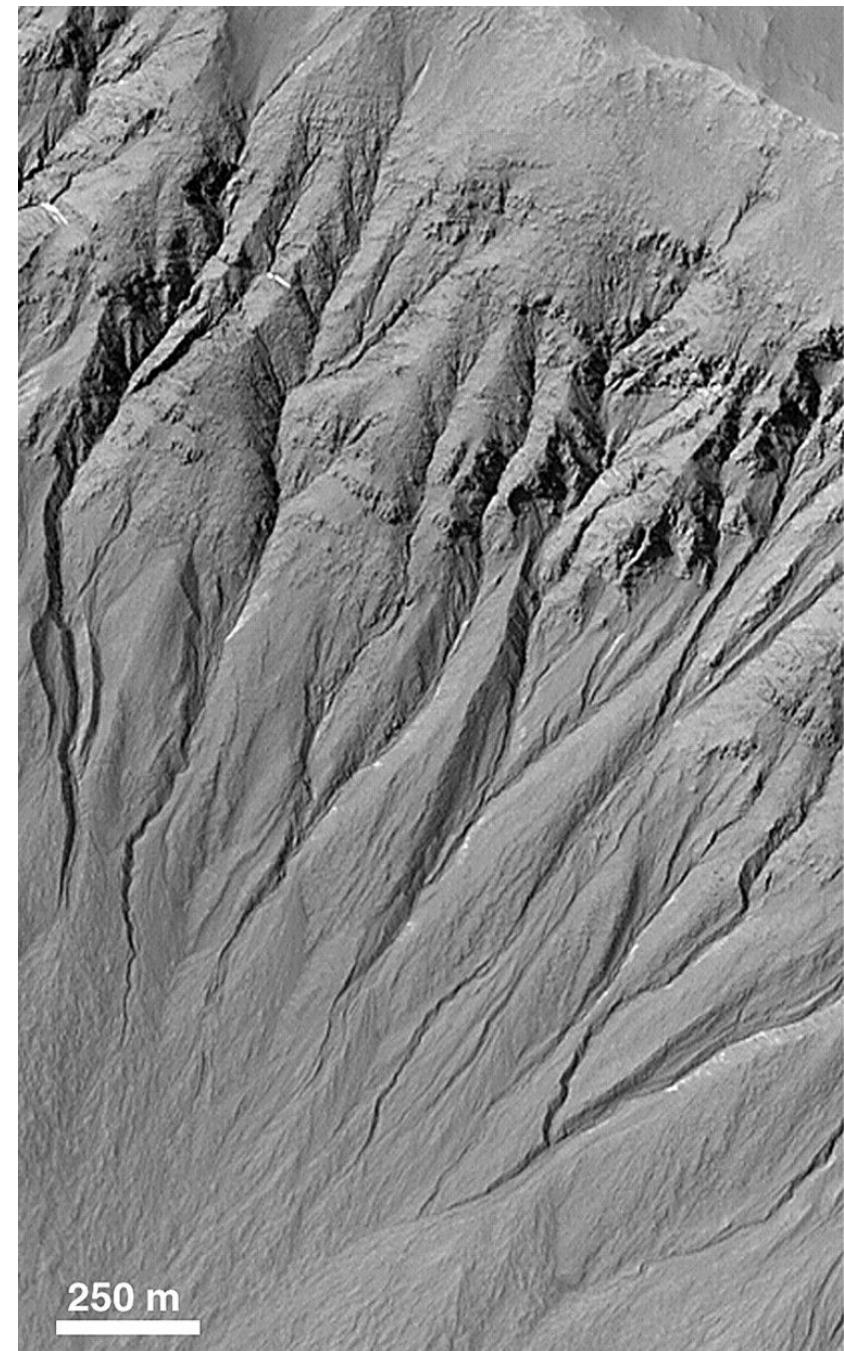
Layered structure  
in Grand Canyon  
vs. Valles  
Marineris on Mars

Deposits of  
sediments from  
water?

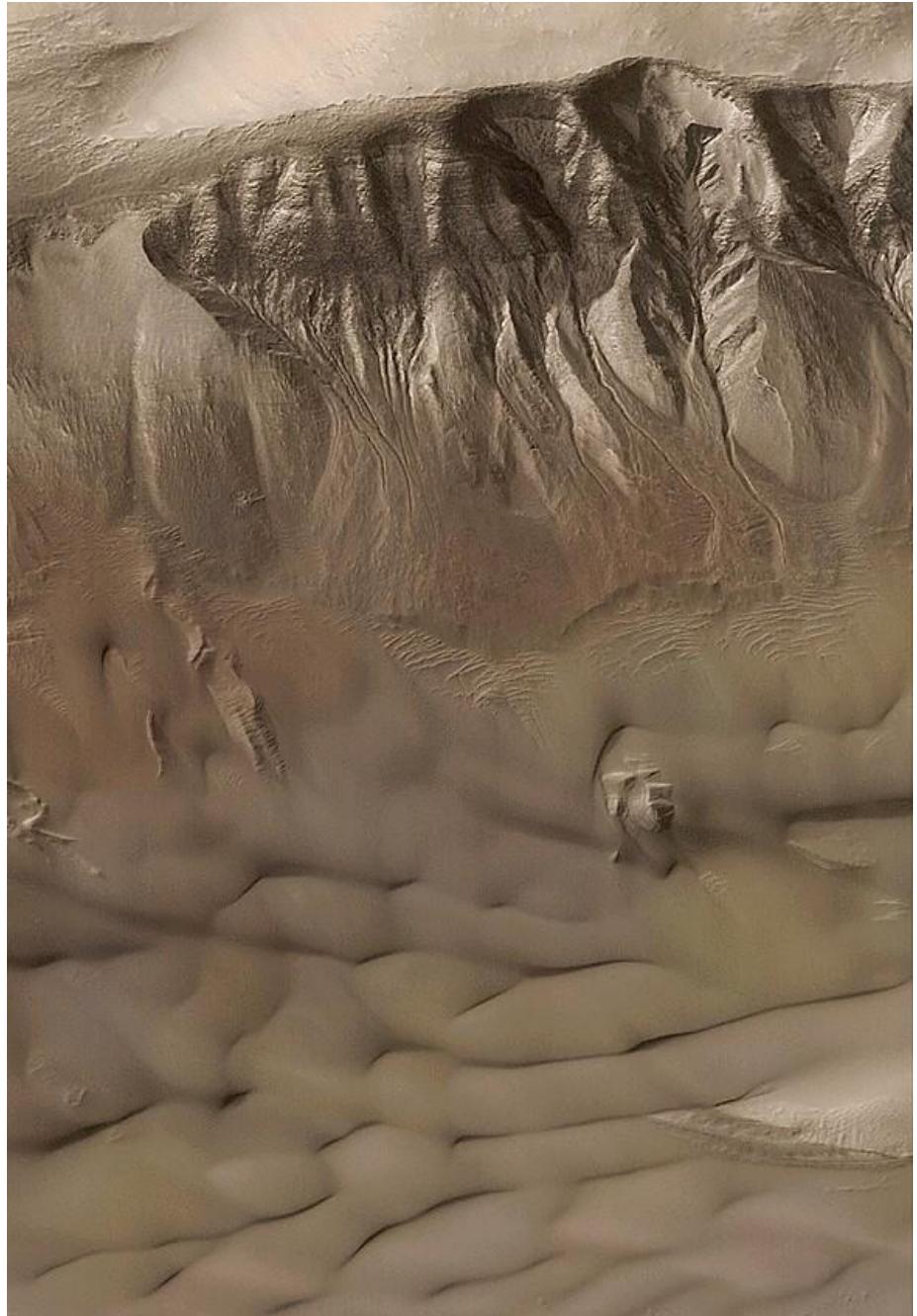




Martian gullies



Recent surface water??



Mars Gullies



Recent surface water??

# A landslide on Mars in action!

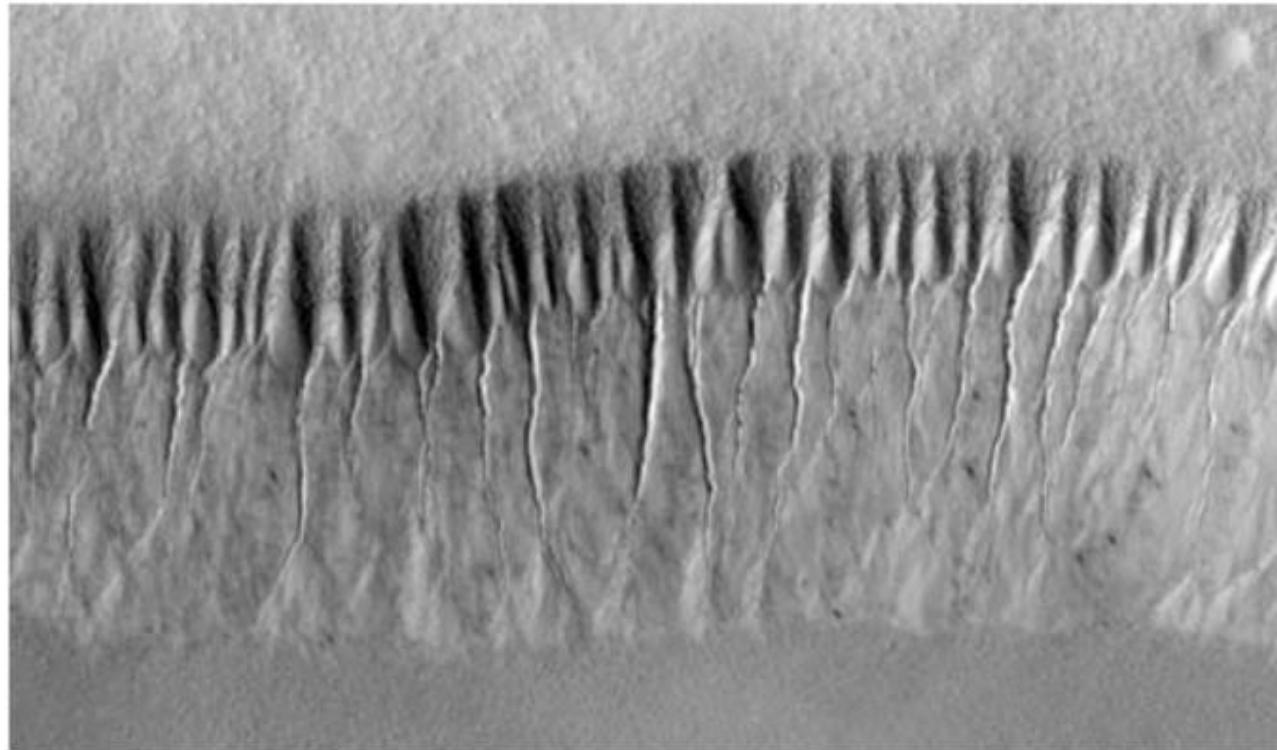


NASA/JPL |

## Hang Onto Your Hat

This false-color image released by NASA shows an active avalanche on Mars. Taken by the Reconnaissance Orbiter on Feb. 19, 2008, the image shows tan clouds billowing away from the foot of a towering slope, where ice and dust have just cascaded down.

**Mars Reconnaissance Orbiter (HiRISE)**



**Figure 3.** Detail of Mars Orbiter Camera image R0502476 showing evenly spaced erosional features incised into a debris slope at the edge of a depression near  $70.7^{\circ}\text{S}$ ,  $355.7^{\circ}\text{W}$ . Image width is approximately 6.5 km. The rim of the depression is toward the top of the image; the floor is toward the bottom. Valleys, channels, and depositional fans appear to have been created by repeated debris flows [Malin and Edgett, 2000]. The convex profiles of the intervening ridges may be a signature of slope-dependent creep driven by cyclical deposition and sublimation of ground ice [Perron et al., 2003]. Image courtesy of NASA/JPL/MSSS.