

$$1 \leq i \leq m, \quad 1 \leq j \leq n.$$

A_i : Atk of Friendly i^{th}

B_i : HP of Friendly i^{th}

P_j : Atk of Enemy j^{th}

Q_j : HP of Enemy j^{th}

m : num of friendly minions

n : num of enemy minions

X_{ij} : whether i^{th} friendly minion attacked j^{th} enemy minion.

Y_i : whether i^{th} friendly minion survived.

Z_j : whether j^{th} enemy minion survived.

S_i : score of i^{th} friendly minion

$C_j = \sum_{k=1}^m (X_{kj} \cdot A_k)$: Total atk that j^{th} enemy took

$D_i = \sum_{k=1}^n (X_{ik} \cdot P_k)$: Atk that i^{th} friendly minion took

$$C, Q, Z, M = \infty$$

if $Q - C \leq 0$ then $z = 0$

if $Q - C > 0$ then $z = 1$

$$Q - C \leq 0 \Rightarrow !(Q - C > 0) \Rightarrow Q - C + (1 - z) \cdot M > 0 \text{ must imply } z = 0$$

$$Q - C > 0 \Rightarrow !(Q - C \leq 0) \Rightarrow Q - C - z \cdot M \leq 0 \text{ must imply that } z = 1$$

$$\begin{cases} Q - C + (1 - z) \cdot M > 0 \\ Q - C - z \cdot M \leq 0 \end{cases} \Rightarrow \begin{cases} Q - C + M - z \cdot M > 0 \\ Q - C - z \cdot M \leq 0 \end{cases} \quad Q, M \text{ is constant}$$

$$\begin{cases} Q + M > C + zM \\ Q \leq C + zM \end{cases} \Rightarrow Q \leq C + M \cdot z < Q + M$$

$$1. \quad Q_j \leq C_j + M \cdot z_j < Q_j + M \quad \forall 1 \leq j \leq n$$

$$D, B, \gamma, M = \infty$$

$$2. B_i \leq D_i + M \cdot \gamma_i < B_i + M \quad \forall 1 \leq i \leq m$$

$$3. \sum_{k=1}^n (x_{ik}) \leq 1 \quad \forall 1 \leq i \leq m$$

Total $2m+n$ constraints.

$$1. \sum_{k=1}^n (x_{ik}) \leq 1 \quad \forall 1 \leq i \leq m$$

$$2. B_i \leq D_i + M \cdot y_i < B_i + M \quad \forall 1 \leq i \leq m$$

$$3. Q_j \leq C_j + M \cdot z_j < Q_j + M \quad \forall 1 \leq j \leq n$$

$$\#1 \quad \text{Min: } \sum_{k=1}^n (P_k \cdot Z_k) \Rightarrow \text{Optimal Value } O^*$$

$$\#2 \quad \text{Max: } \sum_{k=1}^m (S_k)$$

m more columns

$$\text{and } O \cdot \sum_{k=1}^n (P_k \cdot Z_k) \leq O^*$$

1 more row

$$S(i) = A_i \cdot (B_i - D_i) \cdot Y_i$$

$$\gamma, S, A, B, D, M = \infty$$

$$\text{if } \gamma = 0 \text{ then } S = 0$$

$$\text{if } \gamma = 1 \text{ then } S = A \cdot (B - D)$$

$$0 \leq S \leq \gamma \cdot M$$

$$A(B-D) - (1-\gamma)M \leq S \leq A(B-D) + (1-\gamma)M$$

$$S \geq 0$$

$$S - \gamma \cdot M \leq 0$$

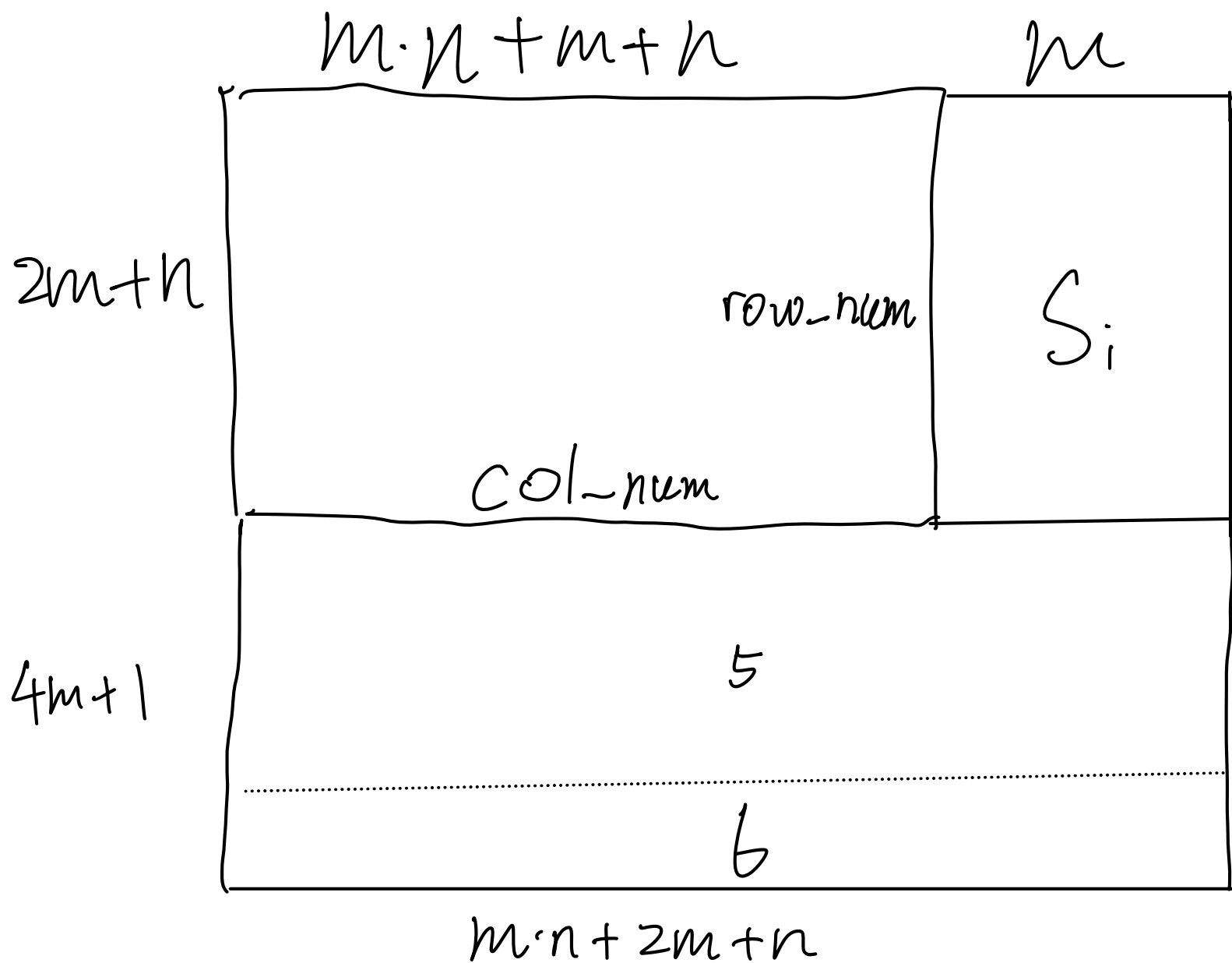
$$S + AD - \gamma M \geq AB - M$$

$$S + AD + \gamma M \leq AB + M$$

5.
$$\left. \begin{array}{l} S_i \geq 0 \\ S_i - Y_i M \leq 0 \\ S_i + A_i D - Y_i M \geq A_i B_i - M \\ S_i + A_i D + Y_i M \leq A_i B_i + M \end{array} \right\} \forall 1 \leq i \leq m, 4m \text{ more rows}$$

Thus $(m \cdot n + m + n) + m = m \cdot n + 2m + n$ cols

$(2m + n) + 1 + 4m = 6m + n + 1$ rows



GRB test sample

$\begin{matrix} \bigcirc & \bigcirc \\ 2 & 3 & 4 & 4 \end{matrix}$

$n=2$

$\begin{matrix} \bigcirc & \bigcirc & \bigcirc \\ 2 & 1 & 2 & 1 \end{matrix}$

$m=3$