Assignment 1

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Content

1 Question 1
2 Question 2
1
3 Question 3

1 Question 1

The specific weight can be calculated as

specific weight =
$$\frac{8N}{400ml}$$
 = $20000N \cdot m^{-3}$

The density can be calculated as

$$density = \frac{8N}{400 ml \cdot 9.81 N \cdot kg^{-1}} = 2038.74 kg \cdot m^{-3}$$

The specific gravity can be calculated as

specific gravity =
$$\frac{2038.74 \text{kg} \cdot \text{m}^{-3}}{1000 \text{kg} \cdot \text{m}^{-3}} = 2.03874$$

2 Question 2

The dimension of c is $[c] = L \cdot T^{-1}$, the dimension of E_v is $[E_v] = M \cdot L^{-1} \cdot T^{-2}$, the dimension of ρ is $[\rho] = M \cdot L^{-3}$, due to that $c = E_v^a \cdot \rho^b$ is dimensionally homogeneous, we can get

$$\begin{cases} a+b=0\\ -a-3b=1 \end{cases} \Rightarrow \begin{cases} a=\frac{1}{2}\\ b=-\frac{1}{2} \end{cases}$$

So we can get the relationship between c, E_v and ρ as

$$c = \sqrt{\frac{E_v}{\rho}}$$

Therefor

$$E_v = \rho \cdot c^2 = 2000 \times 2000^2 \text{kg} \cdot \text{m}^{-1} \cdot \text{s}^{-2} = 8 \times 10^9 \text{kg} \cdot \text{m}^{-1} \cdot \text{s}^{-2}$$

3 Question 3

The dimension of Q is $[Q] = L^3 \cdot T^{-1}$, the dimension of Δp is $[\Delta p] = M \cdot L^{-1} \cdot T^{-2}$, the dimension of R and L is L, the dimension of μ is $[\mu] = M \cdot L^{-1} \cdot T^{-1}$. Considering that the equation $Q = \frac{cR^4 \Delta p}{\mu L}$ is dimensionally homogeneous, we can finally get that \mathbf{c} is a dimensionless constant. Actually this equation is called Poiseuille's law, in which c is equal to $\frac{\pi}{8}$.