# Week 9 Live Session

w203 Instructional Team
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#### Announcements

Feedback about Quiz 1.

Remember that Lab 3 is being released this week.

### Common hypothesis testing errors

For each of the following scenarios, explain the key error in the statistical procedure.

- a) Bill hypothesizes that the average student drinks between 100 and 200 grams of caffeine during a take-home lab. He measures mean caffeine intake for a random sample of 50 lab-takers, then computes the p-value associated with his hypothesis.
- b) Mike likes peanuts. Mike likes peanuts so much that he conducts a study to show how peanut allergies are an NIH sponsored hoax. He recruits 20 toddlers and randomly assigns each into two groups: peanut butter and brown sugar paste. To Mike's delight, he fails to find evidence for a difference between the groups (p = .34). Mike concludes by accepting the null hypothesis (that peanut allergies do not exist).
- c) Anne replicates Mike's study and estimates a p-value of .03, she concludes that the alternative hypothesis has a 97% chance of being true.
- d) Tim asks 50 passengers on the 8am Staten Island Ferry to complete his survey about attitudes toward atheists. He finds a statistically significant difference between attitudes toward atheists and attitudes toward scientologists (p = .04). Huzzah! Tim concludes that the US public is more fearful of atheists than scientologists.

#### Comparing Means

The file united\_states\_senate\_2014\_v2.csv contains data on the 100 members of the US senate that served in 2014. We will consider this group to be a sample (for example, from some generative process that creates senators).

```
S = read.csv("united_states_senate_2014_v2.csv")
summary(S)
```

```
##
             Senator.Names
                               Gender
                                                State
                                                                  Party
                            Female:20
##
    Alan Franken
                     : 1
                                         Alabama
                                                   : 2
                                                          Democrat
                            Male:80
##
    Amy Klobuchar
                     : 1
                                         Alaska
                                                    : 2
                                                          Independent: 2
##
   Angus King
                     : 1
                                         Arizona
                                                    : 2
                                                          Republican:45
    Barbara Boxer
##
                                         Arkansas
##
    Barbara Mikulski: 1
                                         California: 2
    Benjamin Cardin: 1
##
                                         Colorado
##
    (Other)
                     :94
                                         (Other)
                                                    :88
##
               Religion
                          Campaign.Money.Raised..millions.of...
##
                                 : 0.100
    Protestant
                    :49
                          Min.
##
    Catholic
                    :27
                          1st Qu.: 4.575
```

```
##
    Jewish
                    :10
                          Median: 7.550
##
    Other Christian: 7
                          Mean
                                  : 9.645
##
   Mormon
                    : 2
                          3rd Qu.:13.800
##
  Unaffiliated
                    : 2
                                  :44.200
                          Max.
##
    (Other)
                    : 3
##
  Campaign.Money.Spent..millions.of...
                                             NRA.Rating
          : 0.200
   Min.
                                           Α
                                                   :34
    1st Qu.: 2.975
                                           F
##
                                                   :34
##
    Median : 6.000
                                                   : 9
                                                   : 5
##
    Mean
           : 8.227
    3rd Qu.:12.225
                                           AQ
                                                   : 5
                                                   : 3
##
           :43.400
                                           C
    Max.
##
                                            (Other):10
```

You will be placed in a breakout room and assigned a single question to investigate using this dataset. Each question involves a comparison of means.

In your breakout rooms, examine the data and decide what type of test is most appropriate. You may select a paired or an unpaired test. You may also select a parametric or a nonparametric test. Conduct your test and interpret your results.

- Room 1: Is there a difference between the amount of money a senator raises and the amount spent?
- Room 2: Do female Democratic senators raise more or less money than female Republican senators?
- Room 3: Do protestant Senators spend more or less money than non-protestant senators?
- Room 4: Does the NRA prefer male senators or female senators?
- Room 5: Choose your own question to investigate.

#### **Demonstration of Confidence Intervals**

The following exercise is meant to demonstrate what the confidence level in a confidence interval represents. For this exercise, we will assume a standard normal population distribution and simulate what happens when we draw a sample and compute a confidence interval.

Your task is to complete the following function so that it,

- 1) simulates and stores n draws from a standard normal distribution
- 2) based on those draws, computes a valid confidence interval with confidence level  $\alpha$ .

Your function should return a vector of length 2, containing the lower bound and upper bound of the confidence interval.

```
sim_conf_int = function(n, alpha) {
    # Your code to
    # 1. simulate n draws from a standard normal dist.
    # 2. compute a confidence interval with confidence level alpha
    return(c(-1,1)) # replace with the interval you compute.
}
```

When your function is complete, you can use the following code to run your function 100 times and plot the results.

```
many_conf_int = function(m, n, alpha) {
  results = NULL
  for(i in 1:m) {
    interval = sim_conf_int(n, alpha)
```

```
results = rbind(results, c(interval[1], interval[2], interval[1]<0 & interval[2]>0))
  }
  resultsdf = data.frame(results)
  names(resultsdf) = c("low", "high", "captured")
  return(resultsdf)
}
n = 20
cints = many_conf_int(100, n, .05)
plot(NULL, type="n",xlim=c(1,100),ylim=c(min(cints$low), max(cints$high)), xlab="Trial",ylab=expression
abline(h = c(0, qt(0.975, n-1)/sqrt(n), qt(0.025, n-1)/sqrt(n)), lty = <math>c(1,2,2), col = "gray")
points(cints$high, col = 2+cints$captured, pch = 20)
points(cints$low, col = 2+cints$captured, pch = 20)
for(i in 1:100)
   {
     lines(c(i,i), c(cints$low[i],cints$high[i]), col = 2+cints$captured[i], pch = 19)
title(expression(paste("Simulation of t-Confidence Intervals for ", mu,
                          " with Sample Size 20")))
legend(0,-.65, legend = c(expression(paste(mu, "Captured")),
                             expression(paste(mu, "Not Captured"))), fill = c(3,2))
```

## Simulation of t–Confidence Intervals for $\mu$ with Sample Size 20

