

Discrete Response Model

Lecture 1

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Maximum Likelihood Estimation (1)

Maximum Likelihood Estimation

Suppose w = 4 and n = 10. Given this observed information, we would like to find the corresponding parameter value for π that produces the largest probability of obtaining this particular sample.

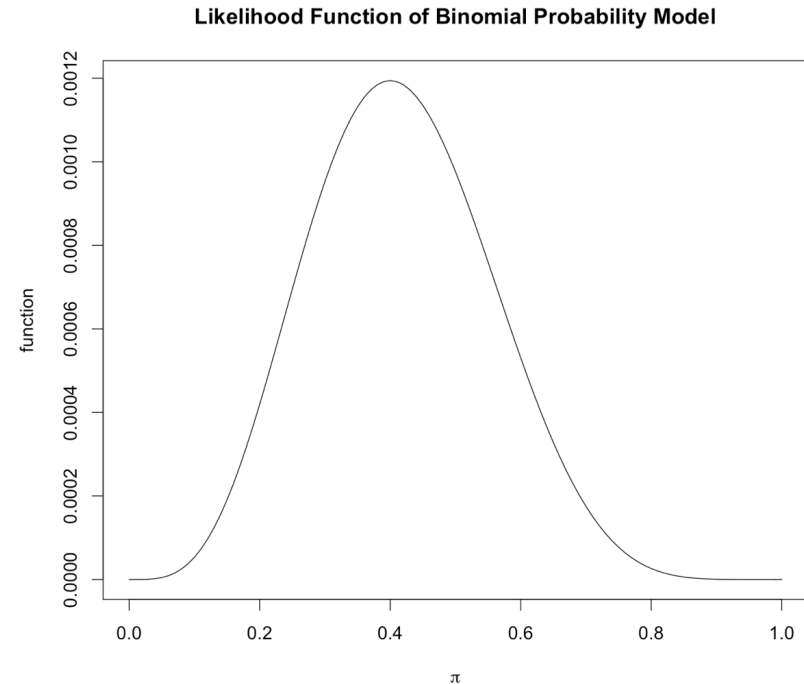
The following table can be formed to help find this parameter value:

| π | $L(\pi y_1, \dots, y_n)$ |
|-------|----------------------------|
| 0.2 | 0.000419 |
| 0.3 | 0.000953 |
| 0.35 | 0.001132 |
| 0.39 | 0.001192 |
| 0.4 | 0.001194 |
| 0.41 | 0.001192 |
| 0.5 | 0.000977 |

Maximum Likelihood Estimation (in R)

```
> sum.y<-4
> n<-10
> # Try different values of pi
> pi<-c(0.2, 0.3, 0.35, 0.39, 0.4, 0.41, 0.5)
> Lik<-pi^sum.y*(1-pi)^(n-sum.y)
> data.frame(pi, Lik)
```

| | pi | Lik |
|---|------|--------------|
| 1 | 0.20 | 0.0004194304 |
| 2 | 0.30 | 0.0009529569 |
| 3 | 0.35 | 0.0011317547 |
| 4 | 0.39 | 0.0011918935 |
| 5 | 0.40 | 0.0011943936 |
| 6 | 0.41 | 0.0011919211 |
| 7 | 0.50 | 0.0009765625 |

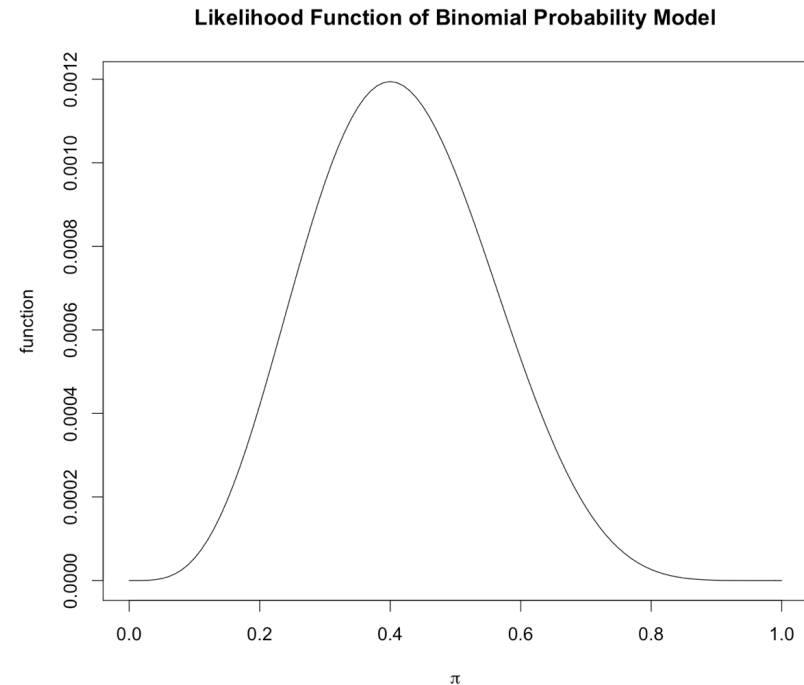


```
#Likelihood function plot
curve(expr = x^sum.y*(1-x)^(n-sum.y), xlim = c(0,1),
      xlab = expression(pi), ylab = "Likelihood
      function", main="Likelihood Function of Binomial Probability Model")
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Note that $\pi = 0.4$ is the “most plausible” value of π for the observed data because this maximizes the likelihood function. Therefore, 0.4 is the maximum likelihood estimate (MLE).

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