

HW 10 Problems

Linear mixed effect models

Consider the following model

$$y_{ij} = x'_{ij}\beta + z'_{ij}\alpha_i + e_{ij}$$

$$e_{ij} \sim N(0, \sigma^2)$$

$$x_{ij} = z_{ij} = (1, age_{ij})'$$

We can choose the following priors

$$\alpha_i \sim N_2(0, \Omega)$$

$$\beta \sim N_2(0, I)$$

$$\sigma^{-2} \sim Ga(1, 1)$$

Consider 2 different approaches for random effect covariance

(1) $\Omega \sim IW(3, I)$

(2) Let $\alpha_i = \Lambda\alpha_i^*$ where $\alpha_i^* \sim N_2(0, I)$ and define a “reasonable” conditionally-conjugate prior for Ω

To do:

Normalize y 's

Derive Gibbs in both cases and code it

Implement for provided blood pressure data and comment on between vs. within subject variance