

# 銀河における星形成則

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# Outline

## 1. Introduction

- Star formation in galaxies
- Relation between SFR and gas density

## 2. Star formation law in GMC scale

## 3. Dependence on surface density of gas

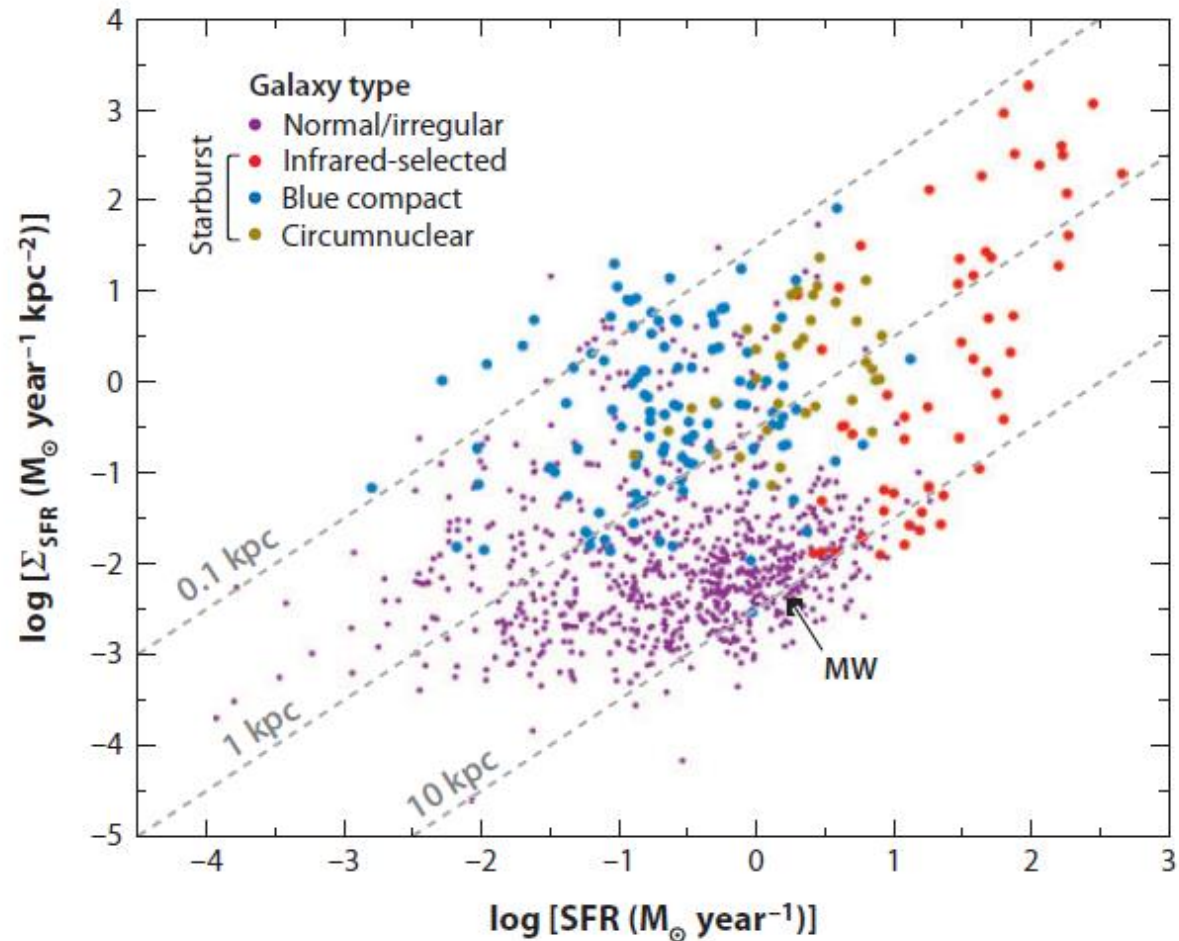
- High density regime
- Low density regime

## 4. Dependence on volume density of gas

# 1. Introduction

# Star formation in galaxies

- Normal galaxies
  - $\text{SFR} < 20 M_{\odot} \text{yr}^{-1}$
  - $\Sigma_{\text{SFR}} = \text{const.}$
- Starburst galaxies
  - $\text{SFR}, \Sigma_{\text{SFR}}$ :  
 $10^2$ - $10^3$  times higher  
than normal galaxies



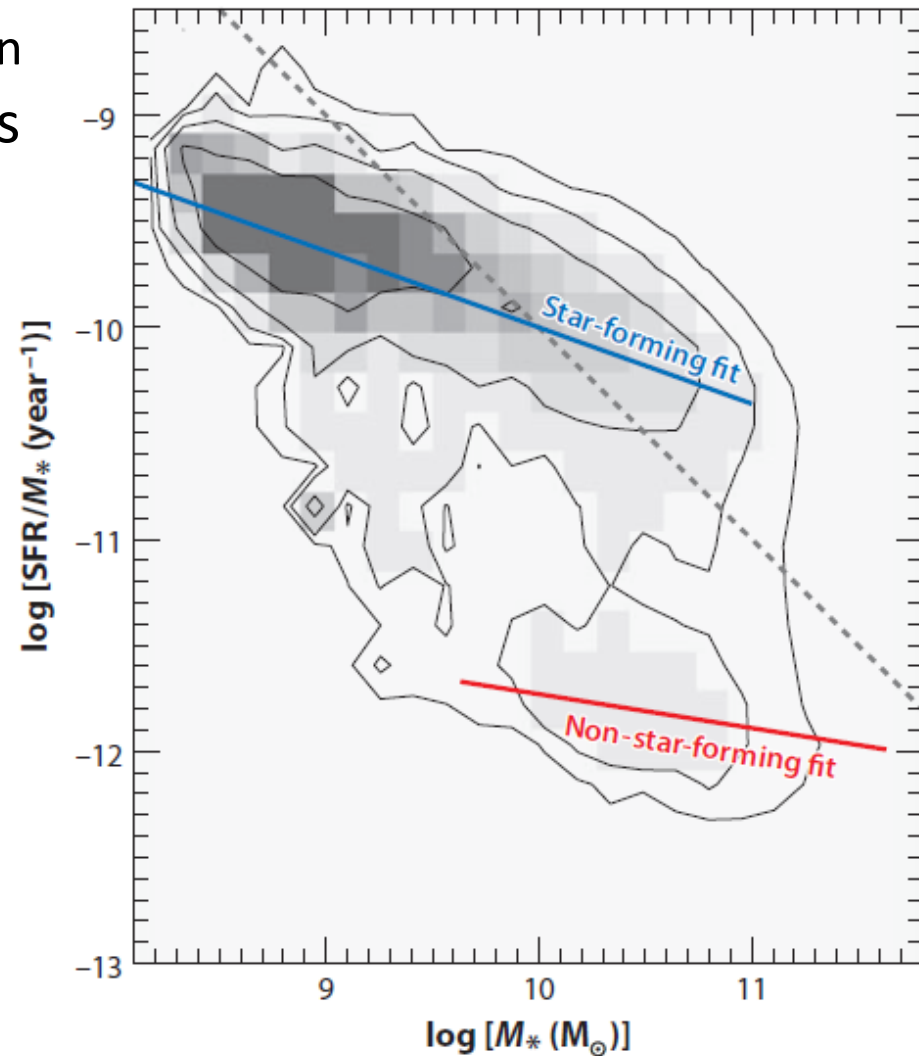
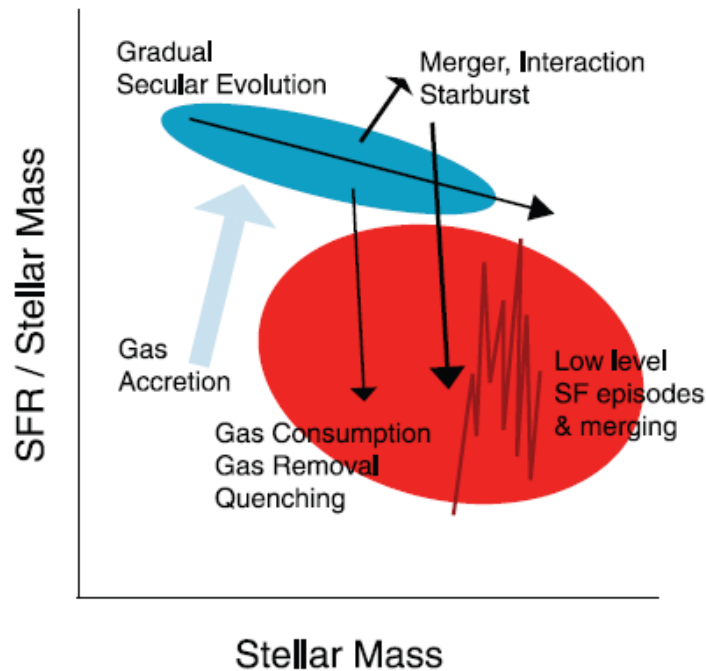
Kennicutt & Evans (2012)

# Stellar mass vs. specific Star Formation Rate (SFR/ $M_*$ )

- Bimodality

- Blue sequence: star formation
- Red sequence: non star formation
- sSFR decreases with stellar mass
  - Difference in quantity (SFR) ?
  - quality (SFE) ?

How do galaxies evolve from blue to red?



Schimoinovich et al. (2007)

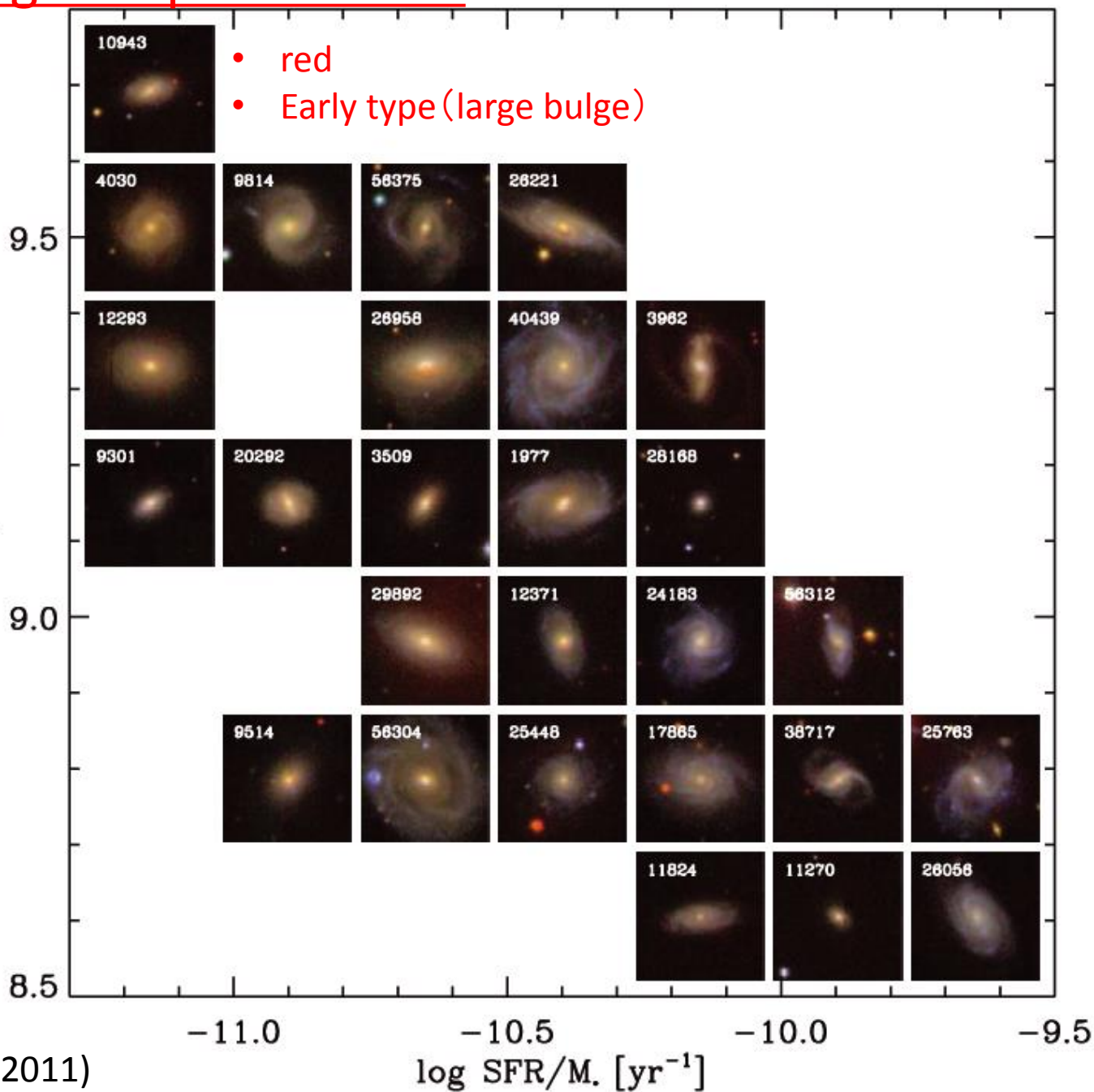
# sSFR vs. gas depletion time

Low SFE



$$t_{\text{dep}}(\text{H}_2) = \frac{M(\text{H}_2)}{\text{SFR}}$$

$\log t_{\text{dep}}(\text{H}_2) [\text{yr}]$

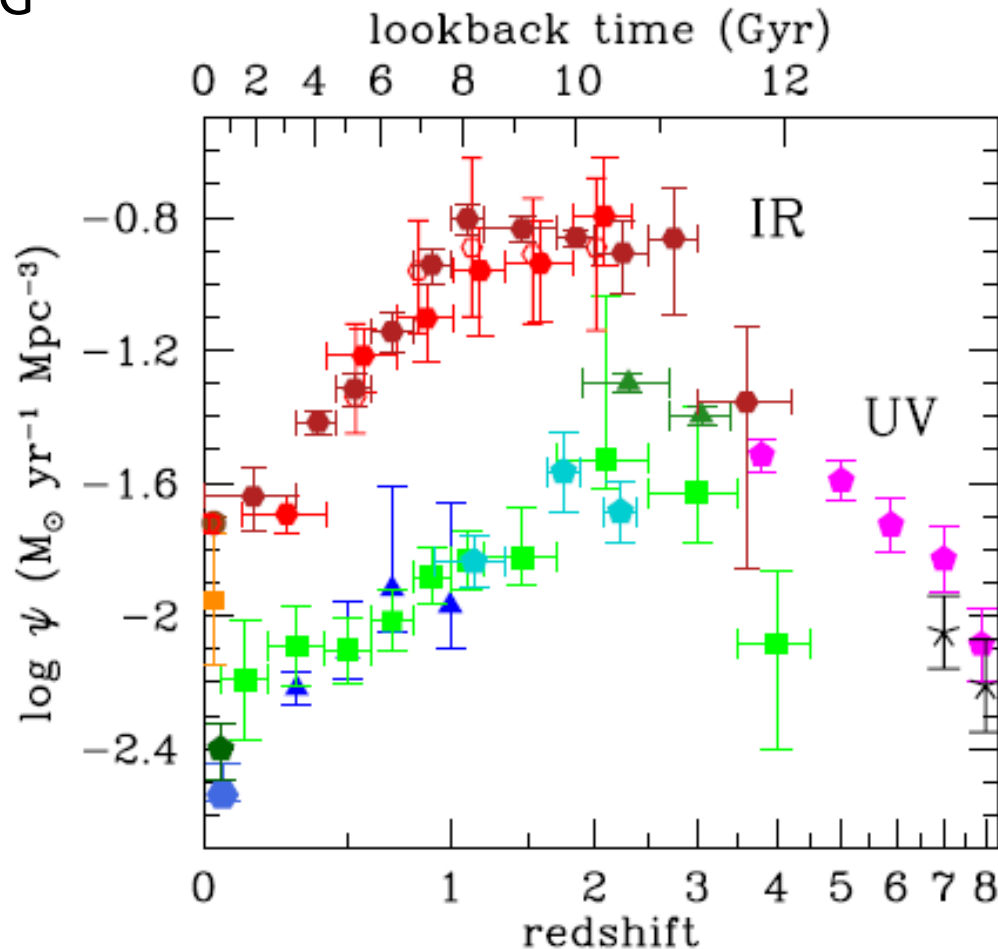


COLD GASS

Saintonge et al. (2011)

# Cosmic star formation history

- SFR density ( $M_{\odot}\text{yr}^{-1}\text{Mpc}^{-3}$ )
  - Peak at  $z=1-3$
  - (U)LIRG



Madau&Dickinson(2014)

# Relation between SFR and gas density

**Schmidt law**: SFR vs. gas volume density

$$\rho_{\text{SF}} \propto \rho_{\text{gas}}^N \quad N \approx 2 \text{ (Schmidt 1959)}$$



**Kennicutt-Schmidt law**:

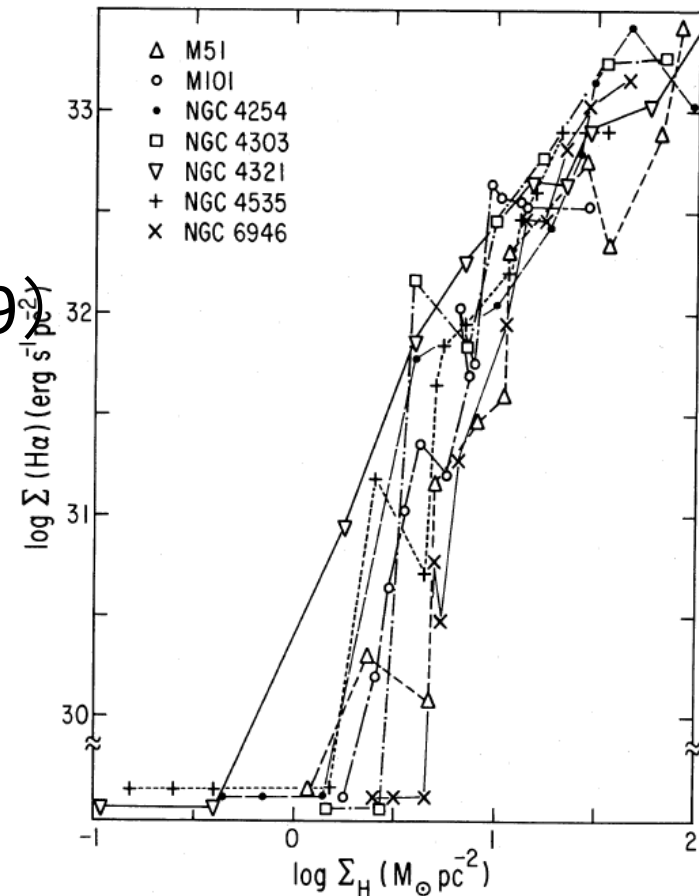
Gas surface density (Kennicutt 1989)

$$\Sigma_{\text{SFR}} \propto \Sigma_{\text{gas}}^N \quad N = 1.3 \pm 0.3$$

- Critical surface density for star formation

- Relation between properties of galaxies and star formation

- Global
- Radial distribution (sub-kpc scale)

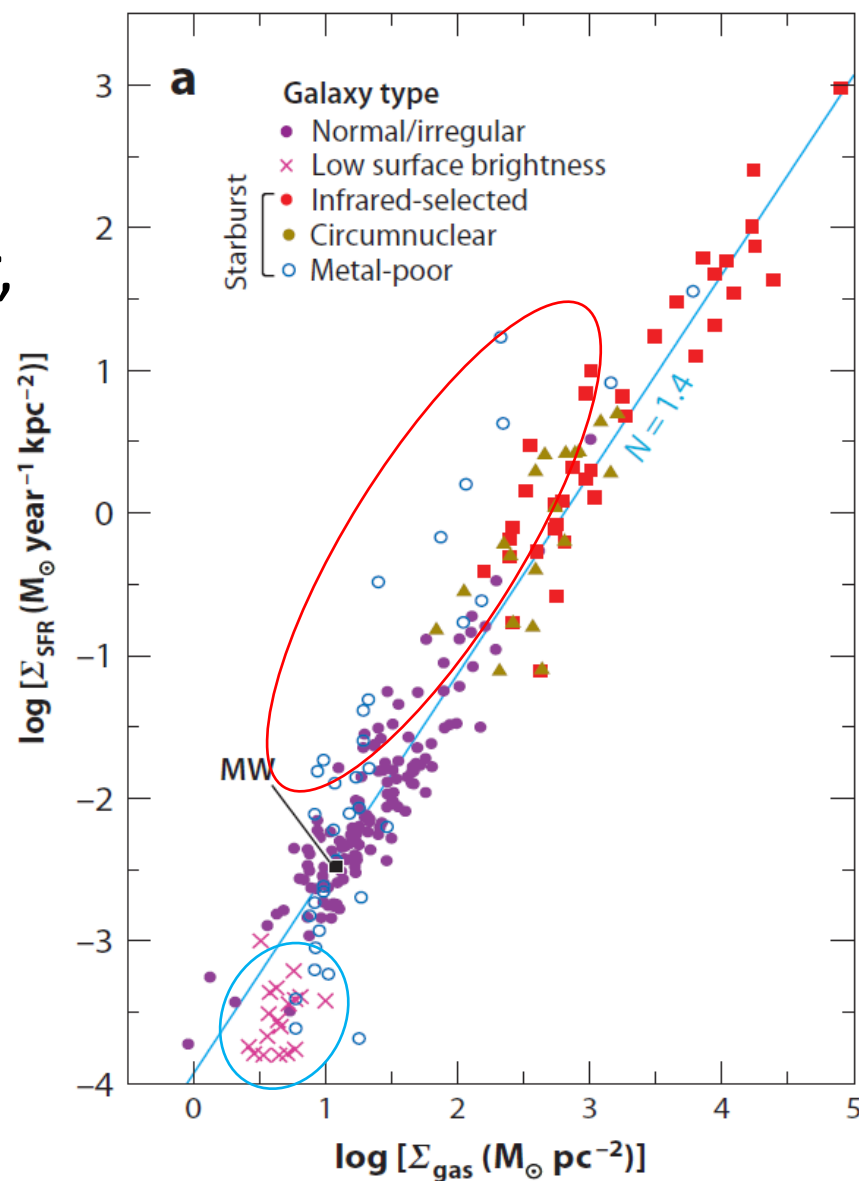


Kennicutt (1989)



# K-S law in global scale

- $\Sigma_{\text{SFR}} \propto \Sigma_{\text{gas}}^N$   $N \simeq 1.4 - 1.5$   
( $I_{\text{CO}} \rightarrow N(\text{H}_2)$  conversion factor,  
 $X_{\text{CO}} = \text{const.}$ )
- Large offset of low metallicity galaxies ( $Z < 0.3Z_{\odot}$ )
  - Difference in  $X_{\text{CO}}$ ?
- Low-Surface-Brightness galaxies: Low SFR



(Kennicutt and Evans 2012)

# K-S law with distant galaxies ( $z \geq 2$ )

- Bimodal: Starburst vs. Normal

Note: not single  $\alpha_{\text{CO}}$

$L'_{\text{CO}} \rightarrow \Sigma(\text{H}_2)$

- normal@ $z = 0.5 - 1.5$  :

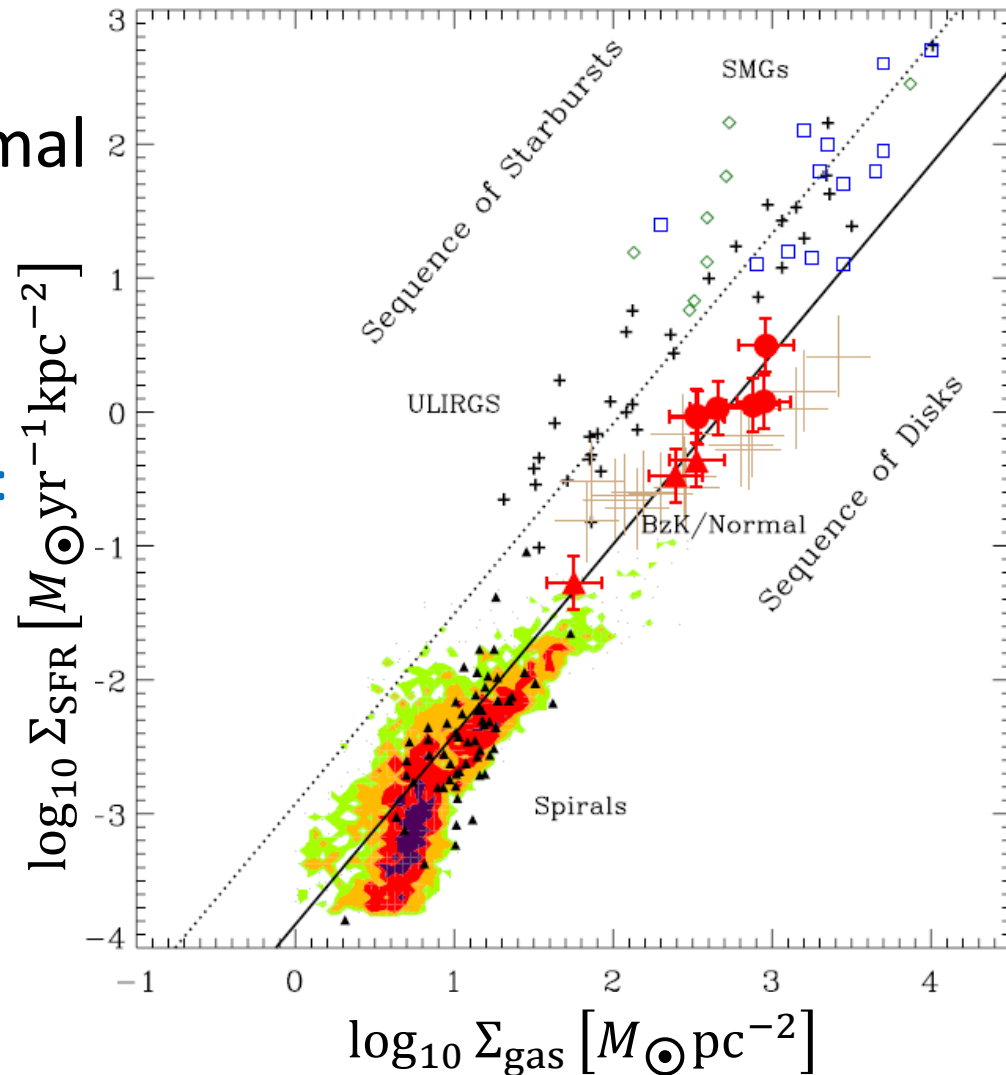
$\alpha_{\text{CO}} = 3.6$

- Local spirals :

$\alpha_{\text{CO}} = 4.6$

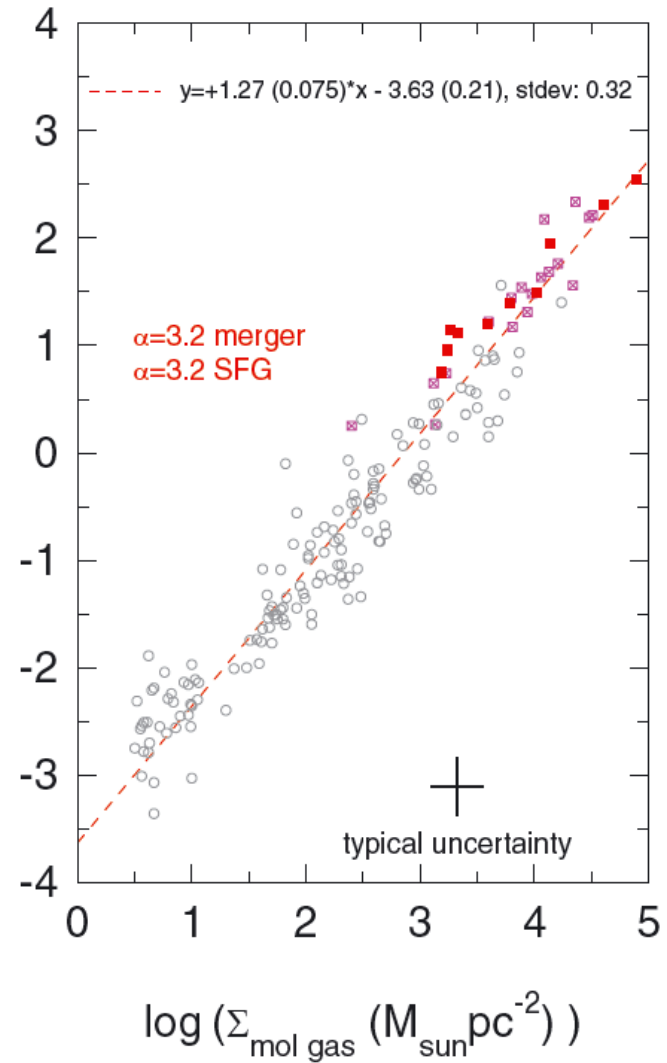
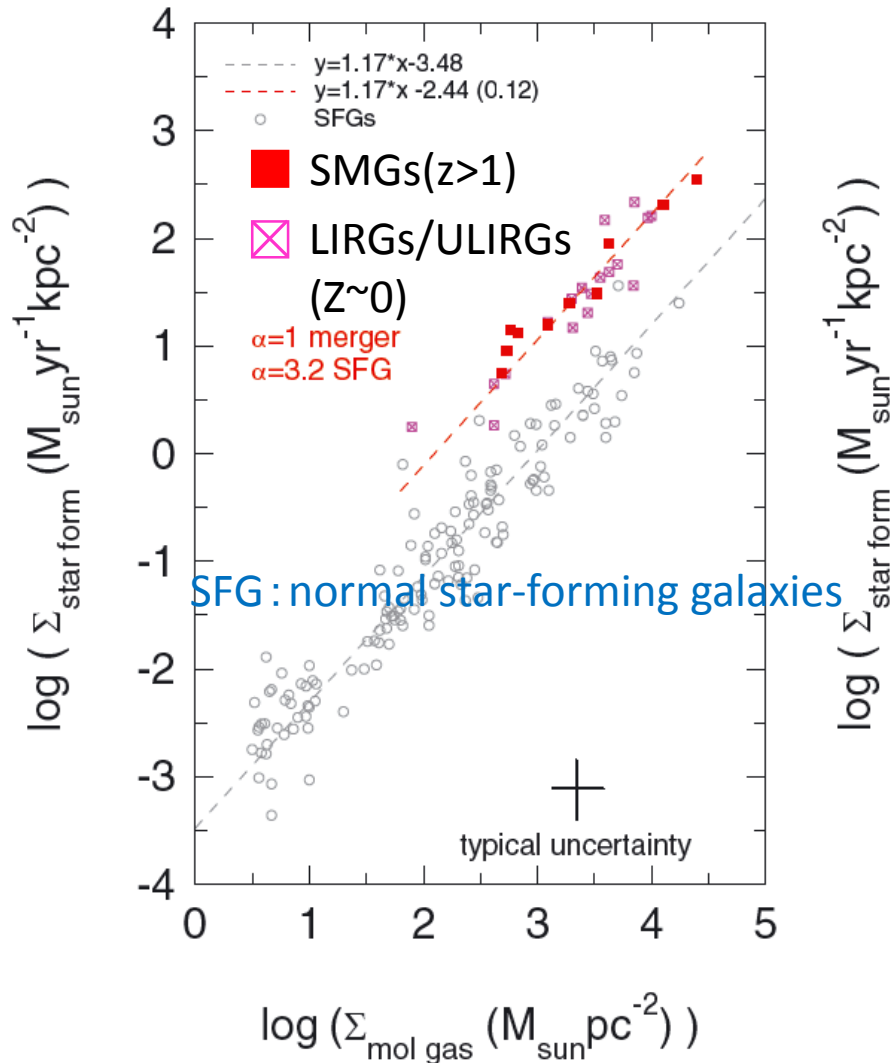
- ULIRGs, SMG/QSO :

$\alpha_{\text{CO}} = 0.8$



Daddi et al. (2010)

- Dependence on  $\alpha_{\text{CO}}$ 
  - single  $\alpha_{\text{CO}} \Rightarrow$  unimodal

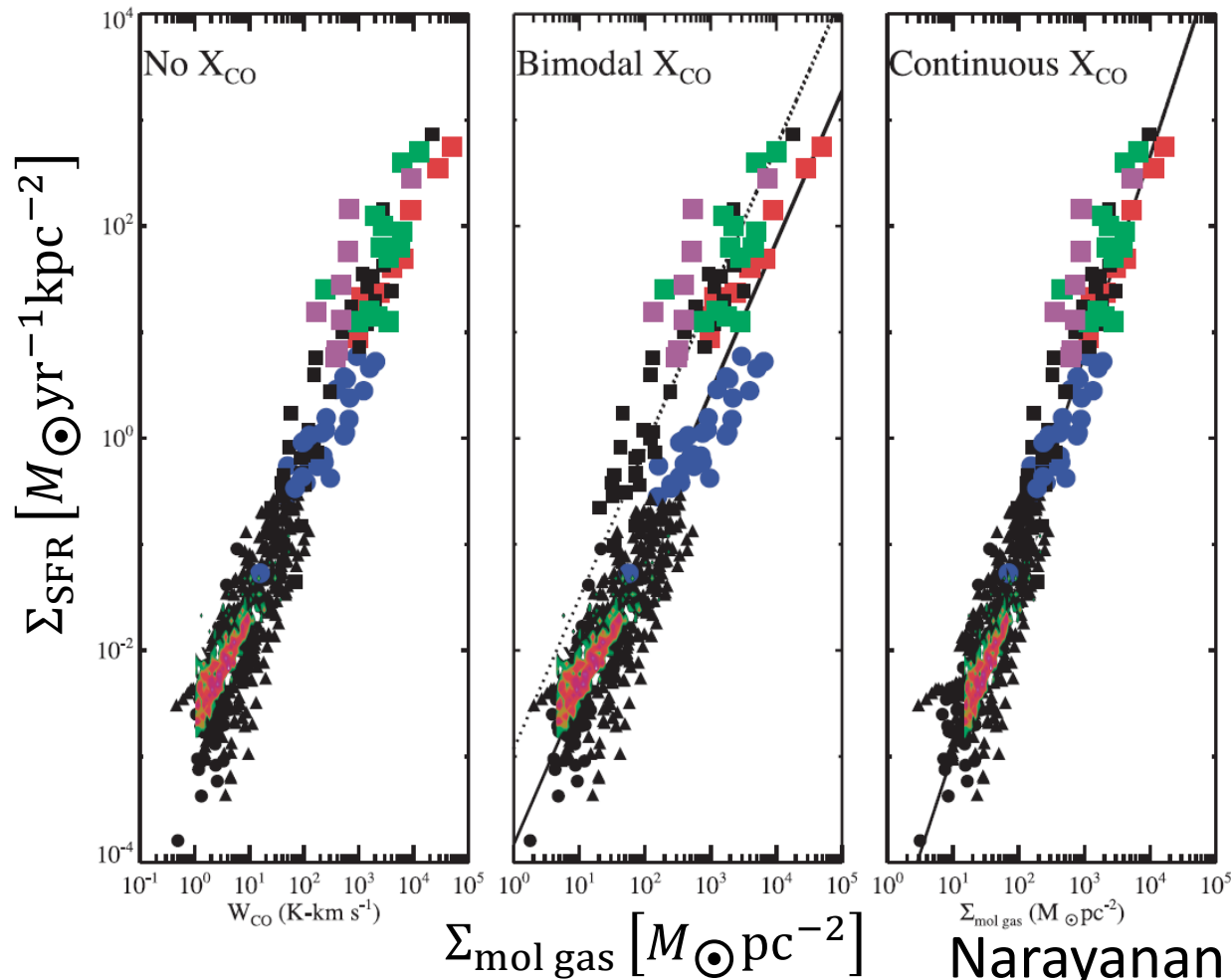


Genzel et al. (2010)

- $\alpha_{\text{CO}}$  depends on metallicity and CO intensity

$$X_{\text{CO}} = \frac{\min[4, 6.75 \times \langle W_{\text{CO}} \rangle^{-0.32}] \times 10^{20}}{Z'^{0.65}} \quad (\text{Narayanan et al. 2012})$$

Bimodal  $\Rightarrow$  Unimodal with steeper slope



Narayanan et al. (2012)

# Schmidt law by dense gas tracer

- Dense gas  $\Rightarrow$  star formation  
Critical density for excitation  
CO(1-0)  $3 \times 10^3 \text{ cm}^{-3}$  @100K  
HCN(1-0)  $4 \times 10^6 \text{ cm}^{-3}$  @30K
- SFR is proportional to dense gas mass

$$L_{\text{IR}} \propto L_{\text{HCN}}^{1.00 \pm 0.05}$$

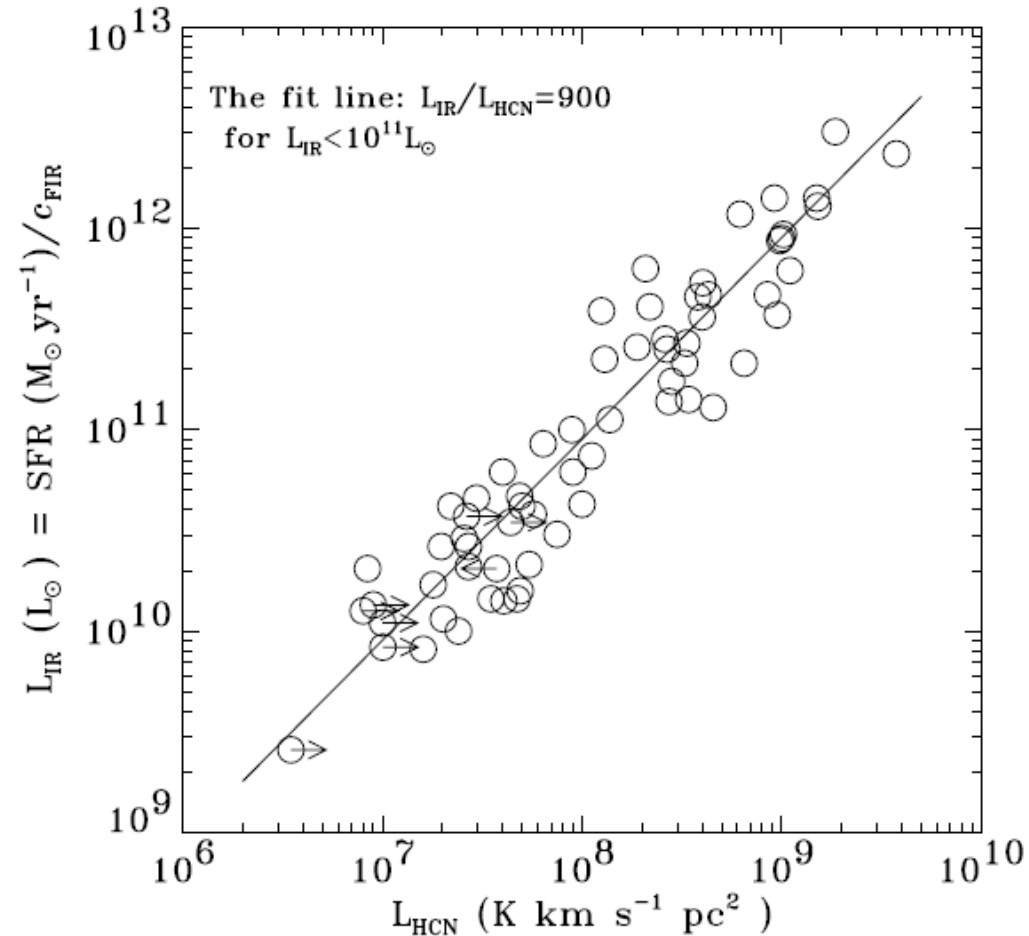
- If dense gas fraction increases with surface density of molecular gas



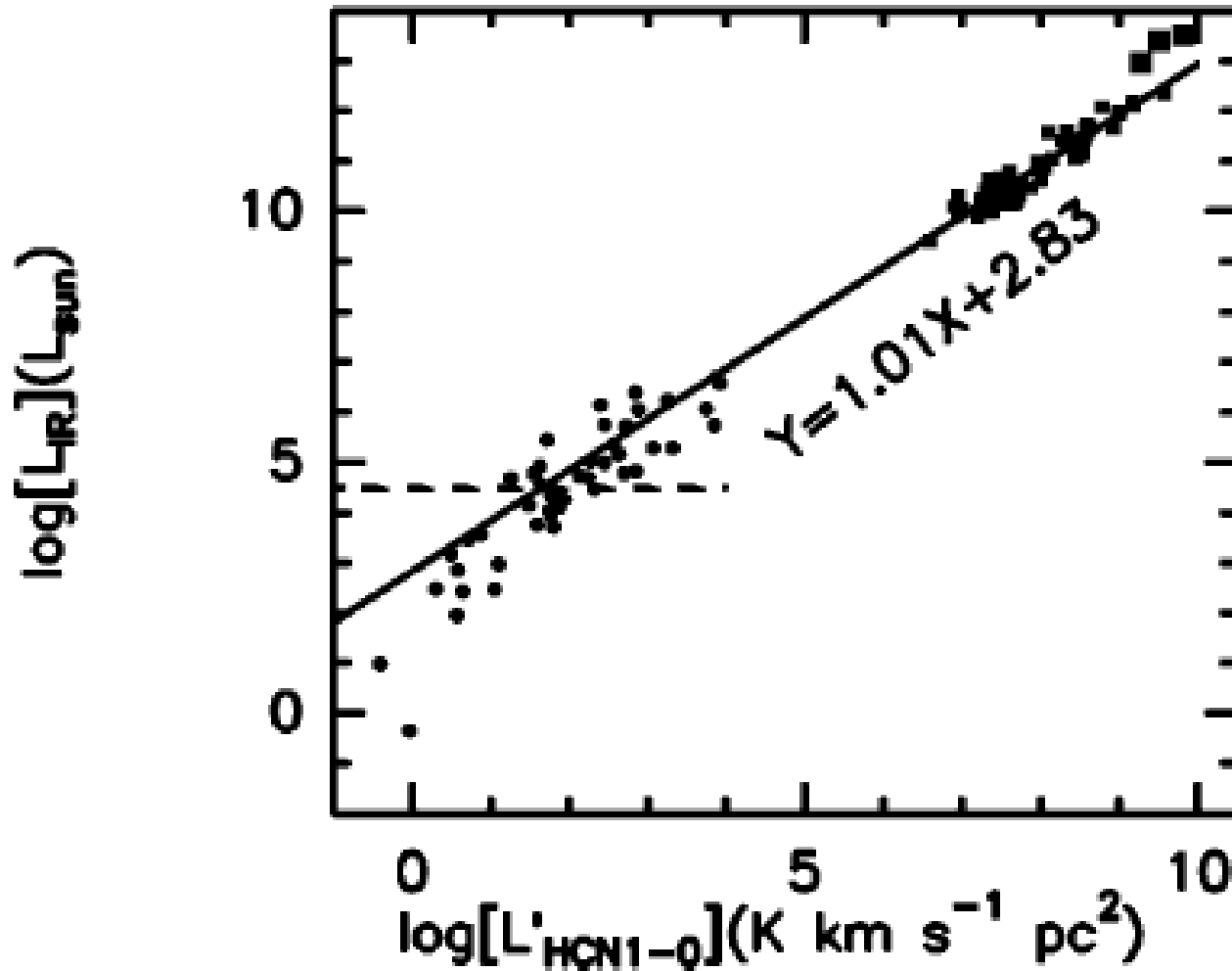
higher SFE at higher  $\Sigma_{\text{H}_2}$



$$\Sigma_{\text{SFR}} \propto \Sigma_{\text{H}_2}^{1.4} \quad (\text{non-linear for CO})$$



Gao & Solomon (2004)



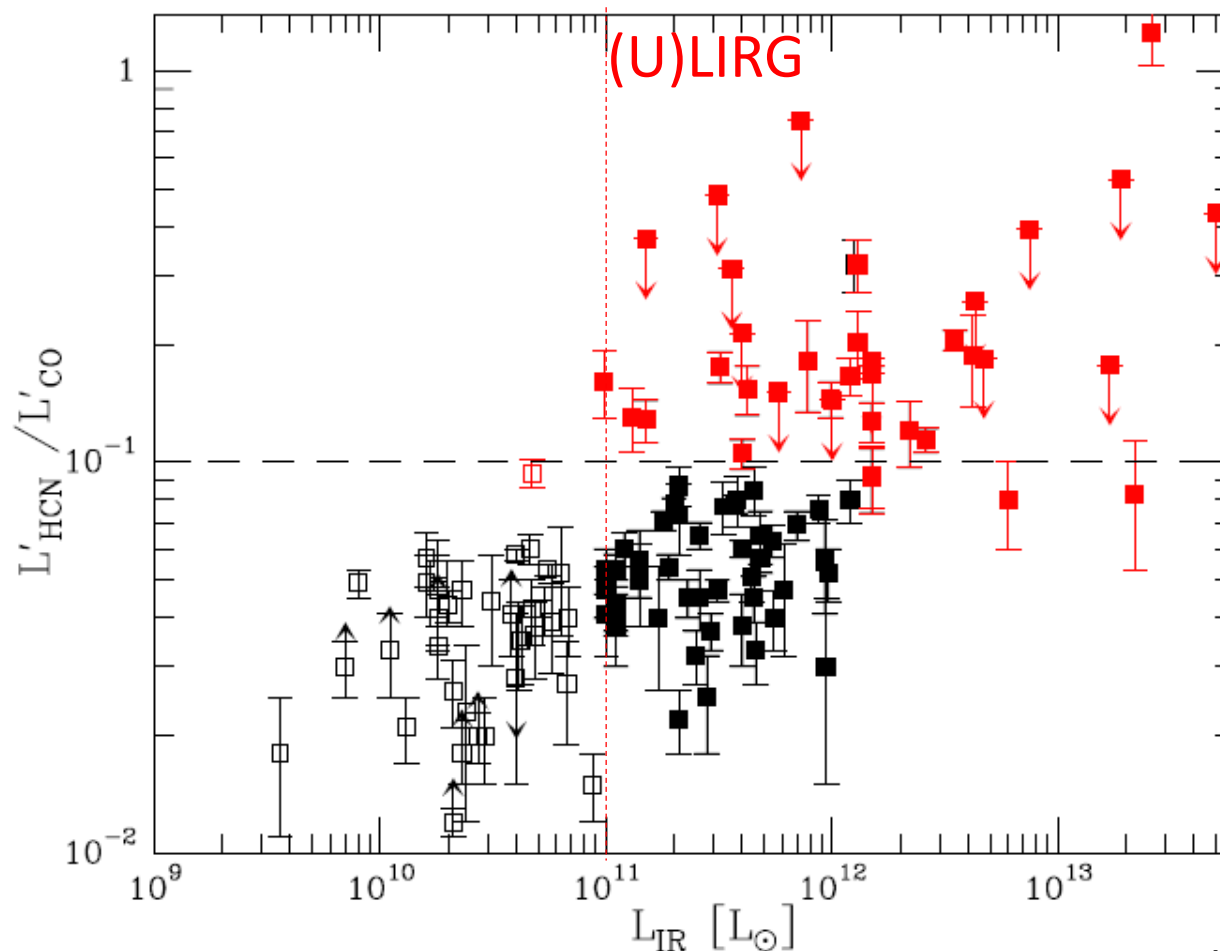
Wu et al. (2005)

- Molecular cloud core to QSOs (order of ten!)  
Same relation ( $L_{\text{IR}} \propto L_{\text{HCN}}$ )?  
 $\Rightarrow$  Star formation occurs beyond a certain critical density?

## Higher HCN/CO in (U)LIRG

e.g., for normal conversion factor,  $M_{\text{dense}} > M_{\text{gas}}$  in Arp220!

- HCN abundance?
  - Excitation by IR radiation?
- ⇒ Small HCN- $\Sigma_{\text{dense}}$  conversion factor

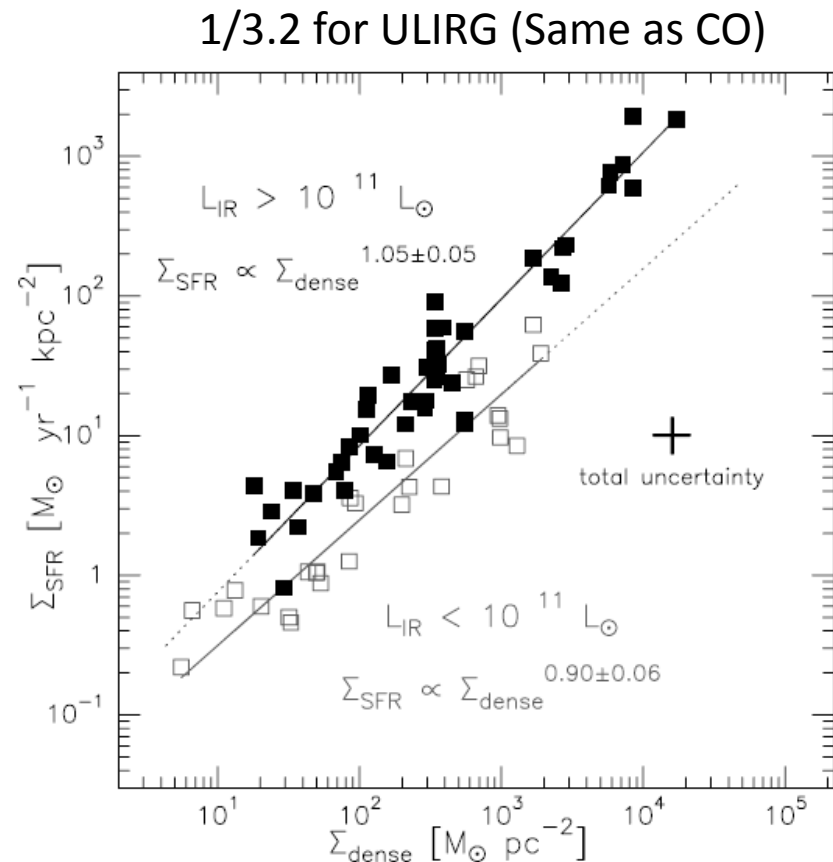
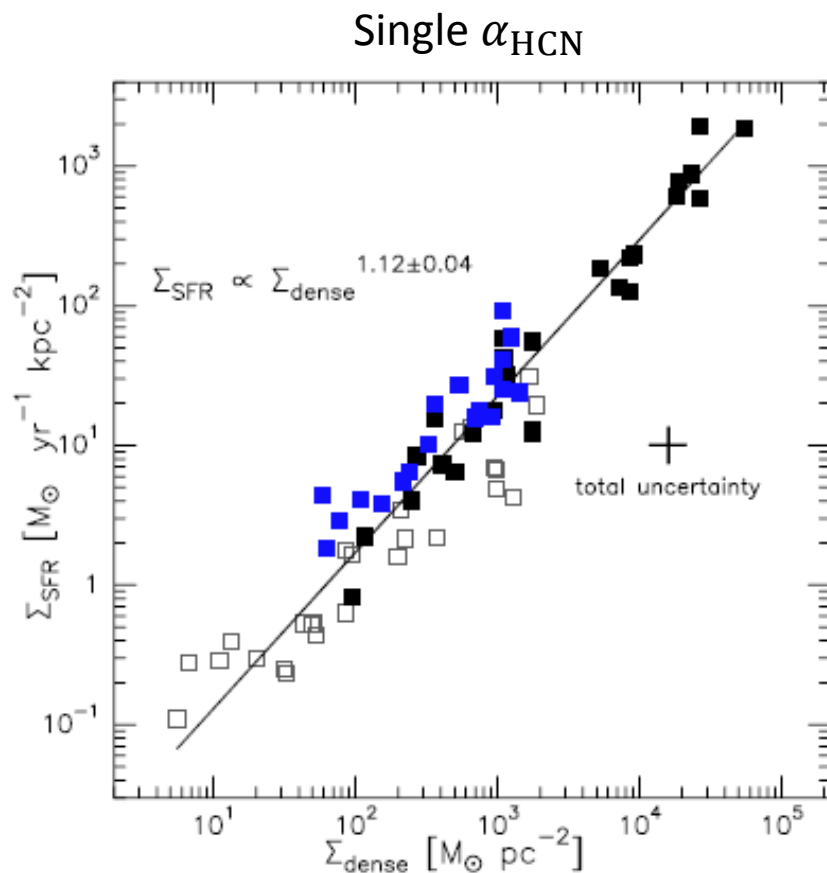


Garcia-Burillo et al. (2012)

# Difference of HCN- $\Sigma_{\text{dense}}$ conversion factor ( $\alpha_{\text{HCN}}$ ) between normal galaxies and ULIRG

$\Rightarrow N > 1$  for all

$\Rightarrow$  Bimodality in K-S law by dense gas tracer?



Garcia-Burillo et al. (2012)



# Low $\text{SFR}/M_{\text{dense}}$ near the Galactic center

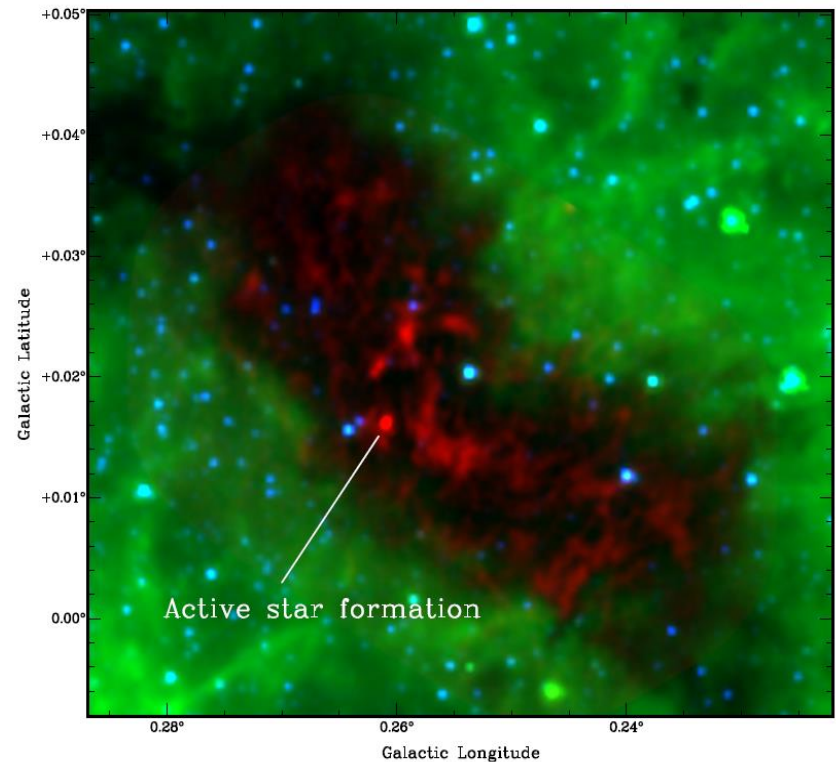
- Central Molecular Zone (CMZ) ( $R < 200$  pc)
  - Low  $\Sigma_{\text{SFR}}/\Sigma_{\text{dense}}$  (Rathborne et al. 2014)
  - G0.253+0.016: Star formation in a specific core ( $> 10^6 \text{cm}^{-3}$ )  
 $\Rightarrow$  High critical density  
for star formation?

$\Rightarrow$  Not simply  $\text{SFR} \propto M_{\text{dense}}$ ?

G0.253+0.016  
Blue:  $3.6\mu\text{m}$   
Green:  $8.0\mu\text{m}$   
Red:  $3\text{mm}$

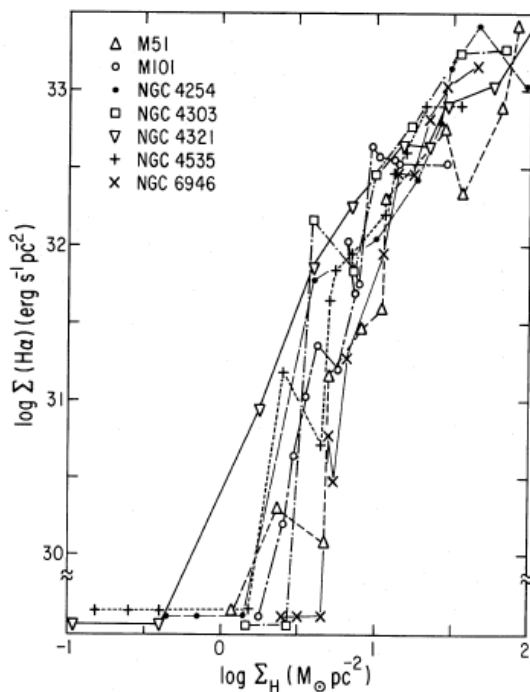
ALMA

Rathborne et al. (2014)

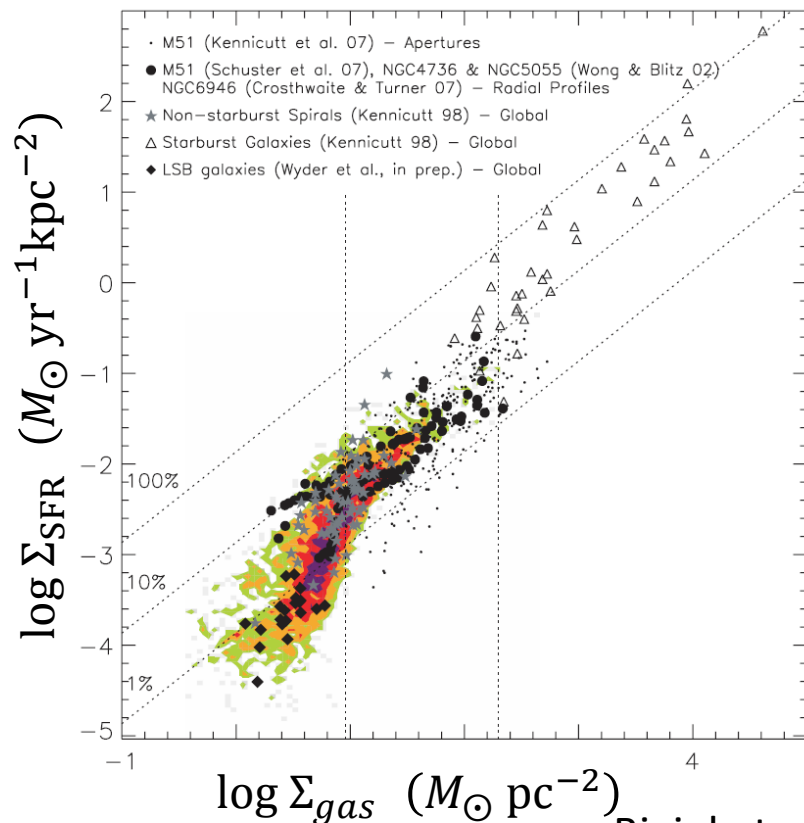


# K-S law in sub-kpc scale

- Spatially resolved K-S law
  - and average of small-scale variation
- $N=1.4-3.1$ (total gas),  $1.0-1.4$ (molecular gas)
- Critical density for star formation  $\sim$ a few  $M_{\odot} \text{ pc}^{-2}$



Kennicutt (1989)



Bigiel et al. (2008)

# Time scale of star formation

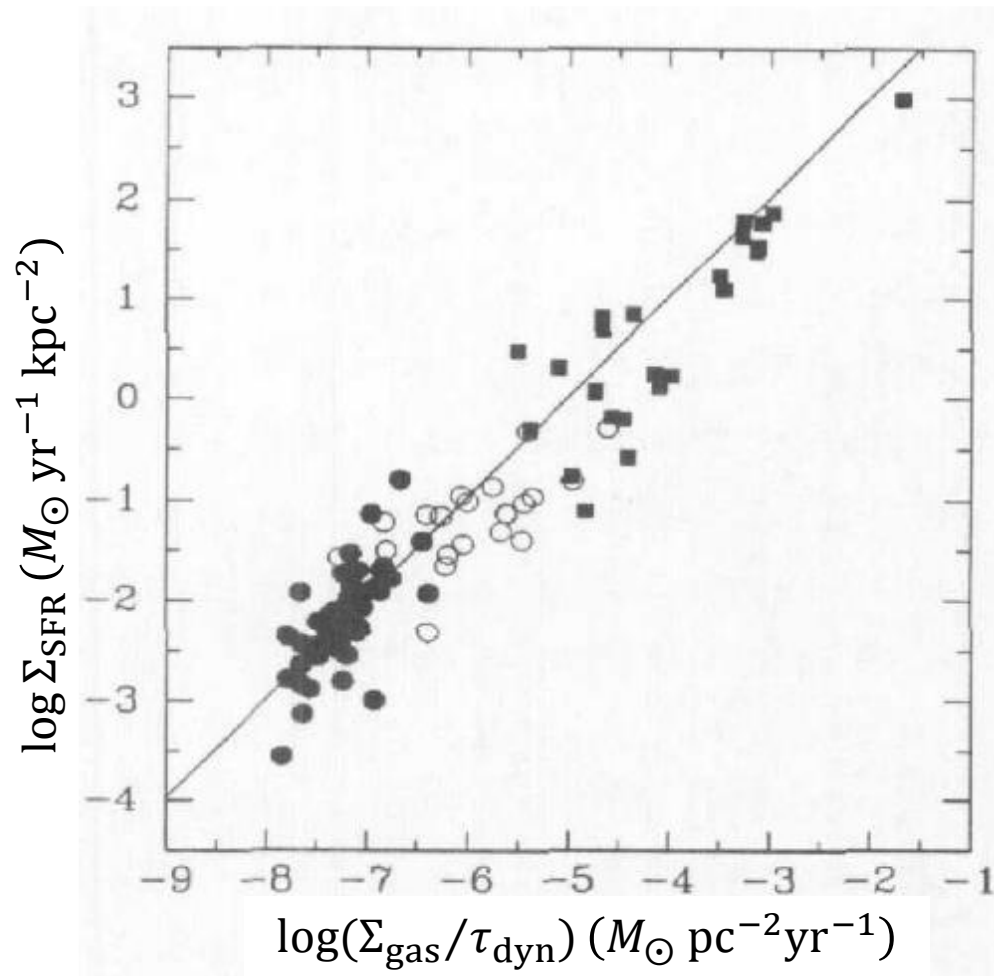
- Dynamical time  $\tau_{\text{dyn}}$ :

One disk orbit time at half of the radius of the star-forming disk

$$\Sigma_{\text{SFR}} \propto \Sigma_{\text{gas}} / \tau_{\text{dyn}}$$

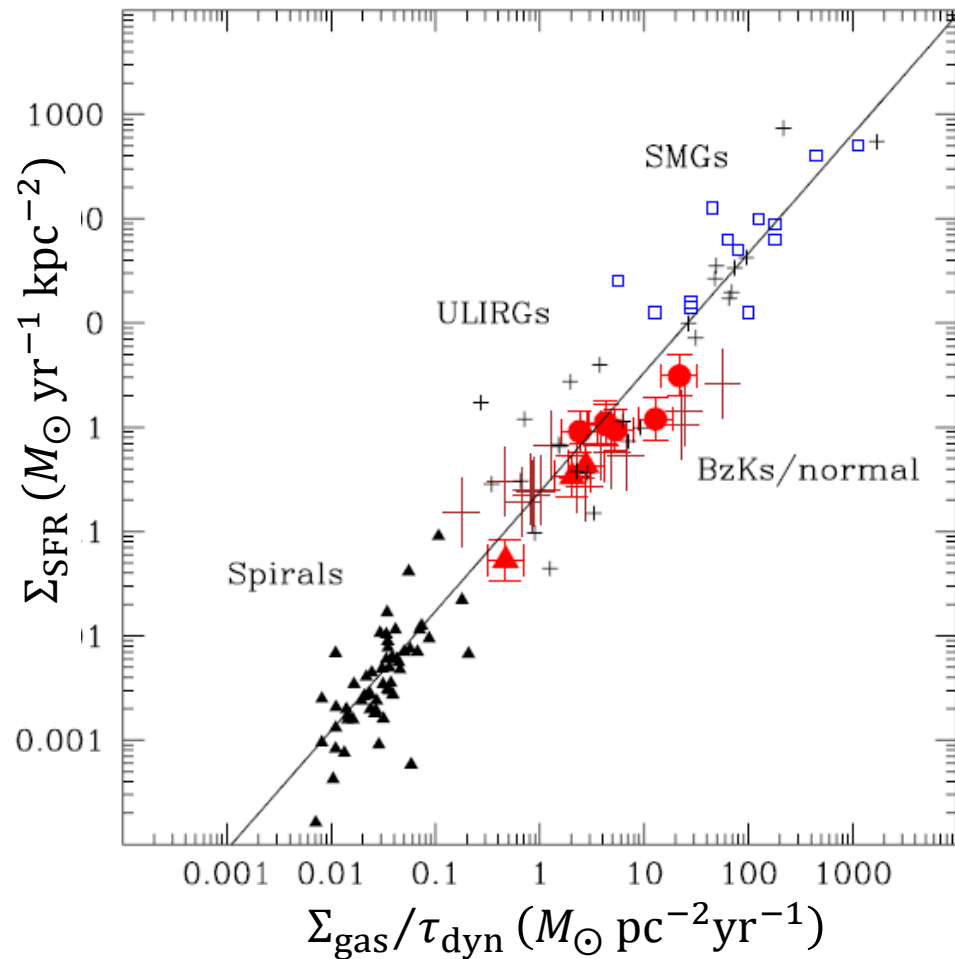
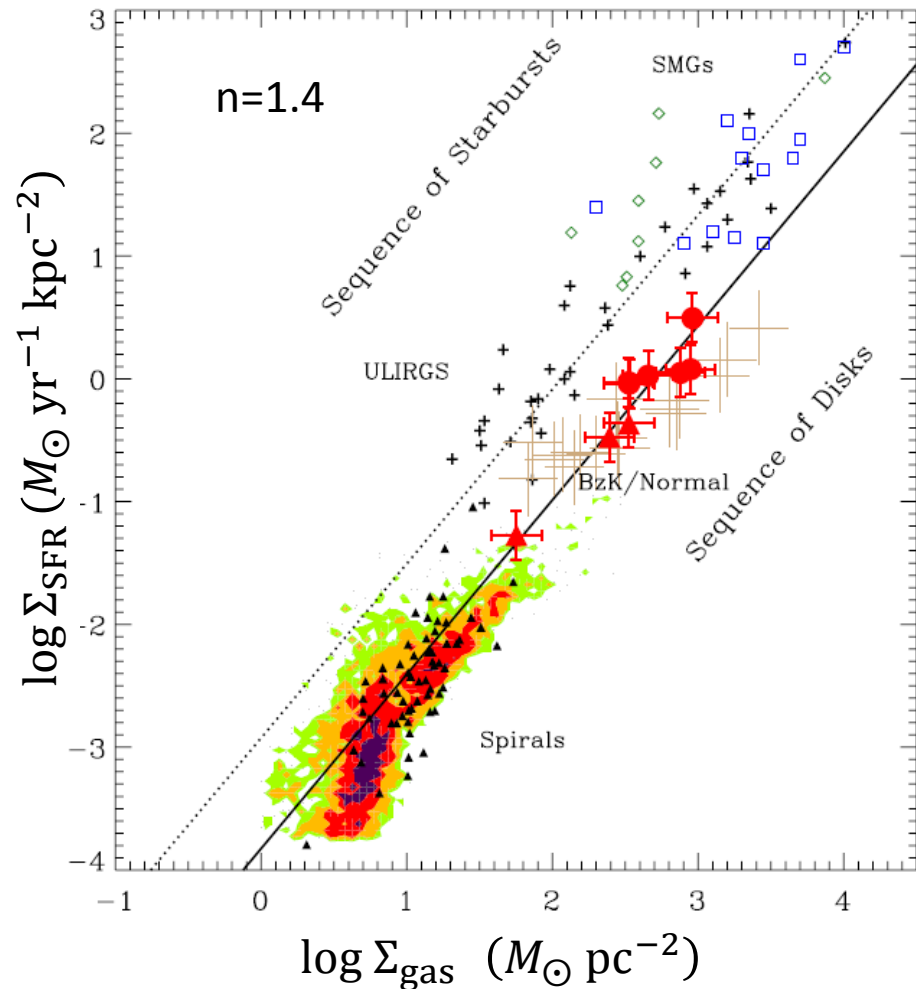
- A constant fraction of gas form stars per orbit

e.g., trigger by spiral arms?



Kennicutt (1998)

- $\Sigma_{\text{gas}}/\tau_{\text{dyn}}$ : ULIRG/SMGs bimodal  $\Rightarrow$  unimodal
  - Galactic dynamics determine the relation? (Why?)



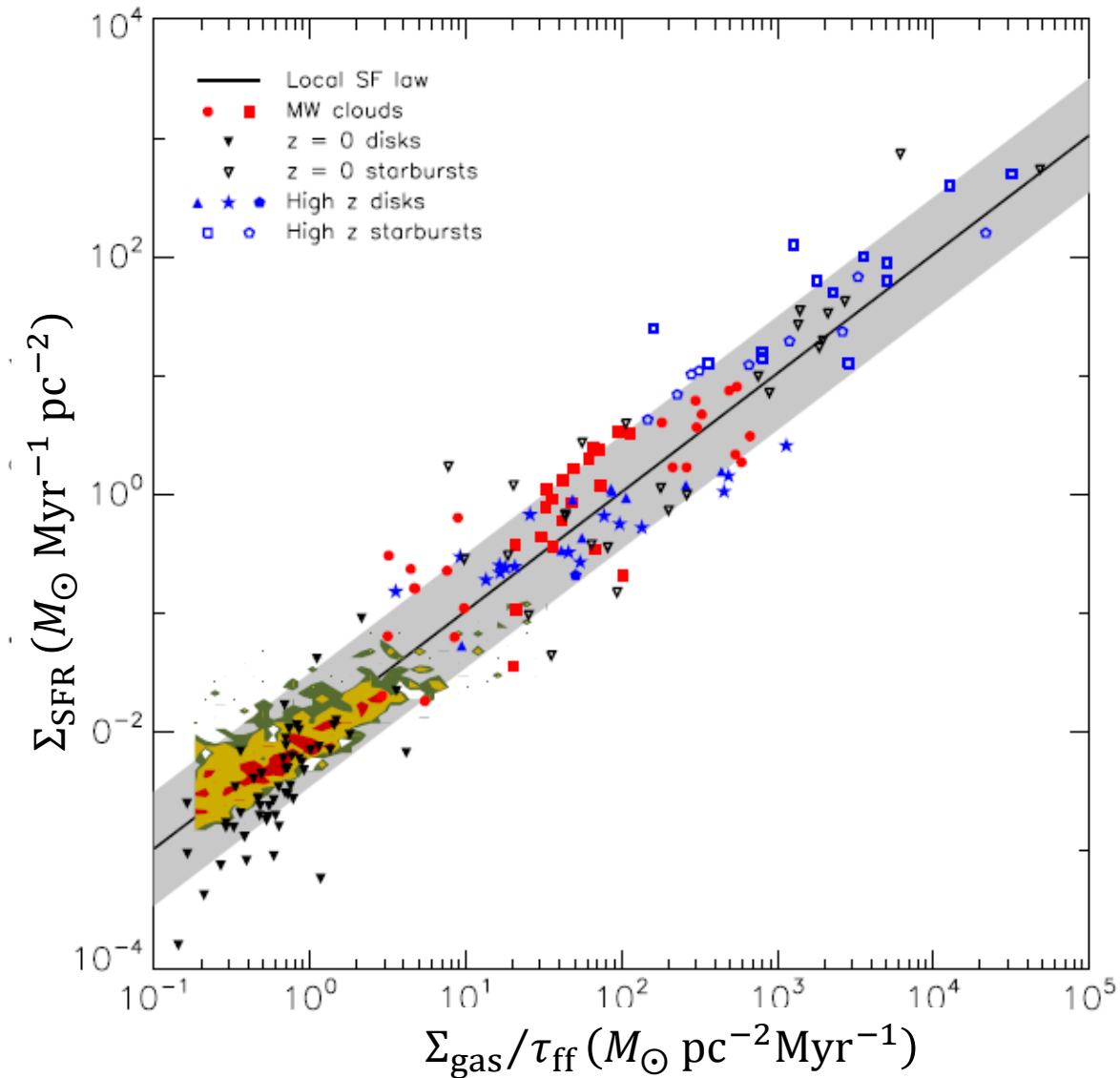
Daddi et al. (2010)

- Free fall time

$$\tau_{\text{ff}} = \sqrt{\frac{3\pi}{32G\rho}}$$

$$\Sigma_{\text{SFR}} \propto \Sigma_{\text{gas}} / \tau_{\text{ff}}$$

- SFR depends on the properties of molecular clouds?



Krumholz et al. (2012)

# Physical interpretation of K-S law (1)

$$\rho_{\text{SF}} \propto \frac{\rho_{\text{gas}}}{\tau_{\text{ff}}} \propto \frac{\rho_{\text{gas}}}{(1/\sqrt{G\rho_{\text{gas}}})} \propto \rho_{\text{gas}}^{1.5}$$

- If scale height of the galactic disk is constant

$$\Sigma_{\text{SF}} \propto \Sigma_{\text{gas}}^{1.5}$$

(But, we observe ensemble of molecular clouds.

In that case,  $\Sigma_{\text{SF}} \propto \Sigma_{\text{gas}}$ ?)

# Critical density for star formation

- Toomre criterion (Toomre 1964)
  - Critical density for gravitational instability in thin isothermal gas disk

$$\Sigma_c = \alpha \frac{\kappa \sigma}{3.36 G}$$

$\sigma$ : velocity dispersion,  $\kappa$ : epicyclic frequency

$$\kappa^2 = \left( R \frac{d\Omega^2}{dR} + 4\Omega^2 \right)_{R_g}$$

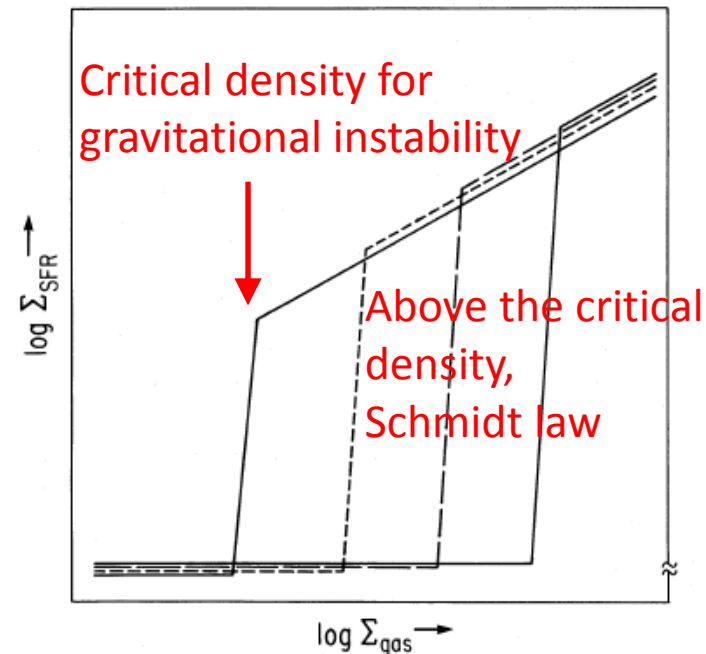
$R$ : radius,  $\Omega$ : angular velocity

- Toomre  $Q$  parameter

$$\frac{\Sigma_c}{\Sigma} = Q = \alpha \frac{\kappa \sigma}{3.36 G \Sigma}$$

$Q > 1$  : stable       $Q < 1$  : unstable

$\Sigma > \Sigma_c \Rightarrow$  star formation  
by gravitational instability?



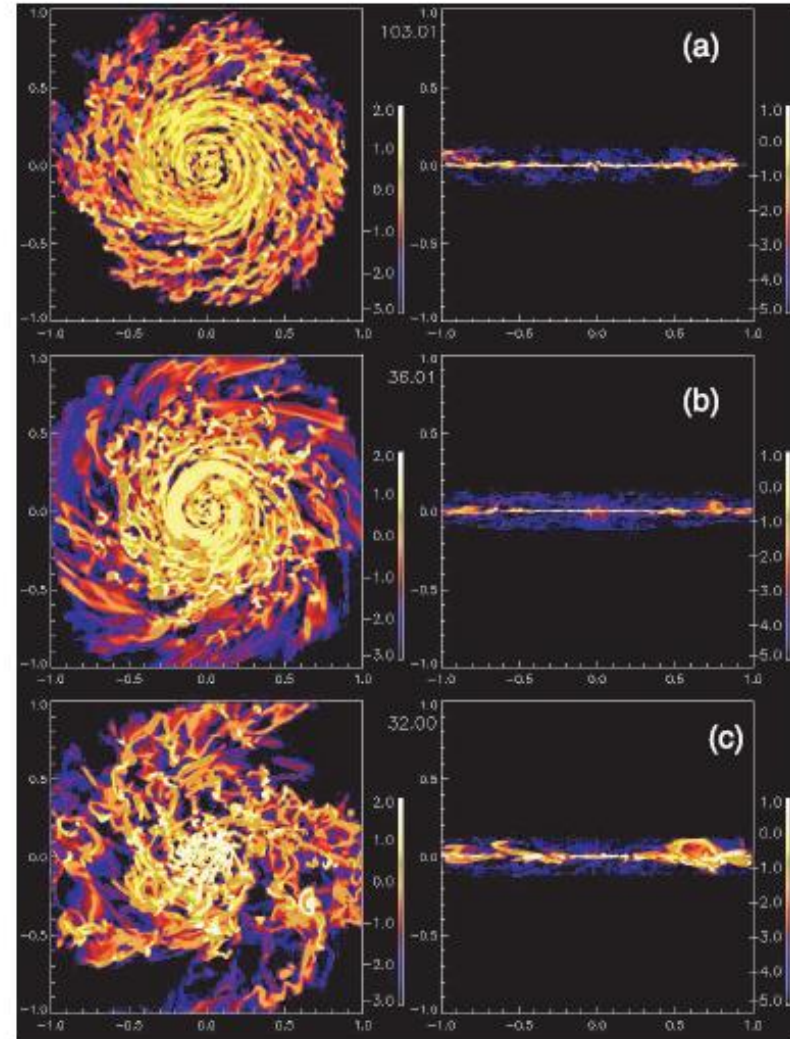
# Physical interpretation of K-S law (2)

- Three-dimensional hydrodynamic simulations

⇒ Probability distribution function (PDF) of gas density

Star formation law

⇒ Relation between PDF of gas density and SFR  
(Critical density, efficiency)

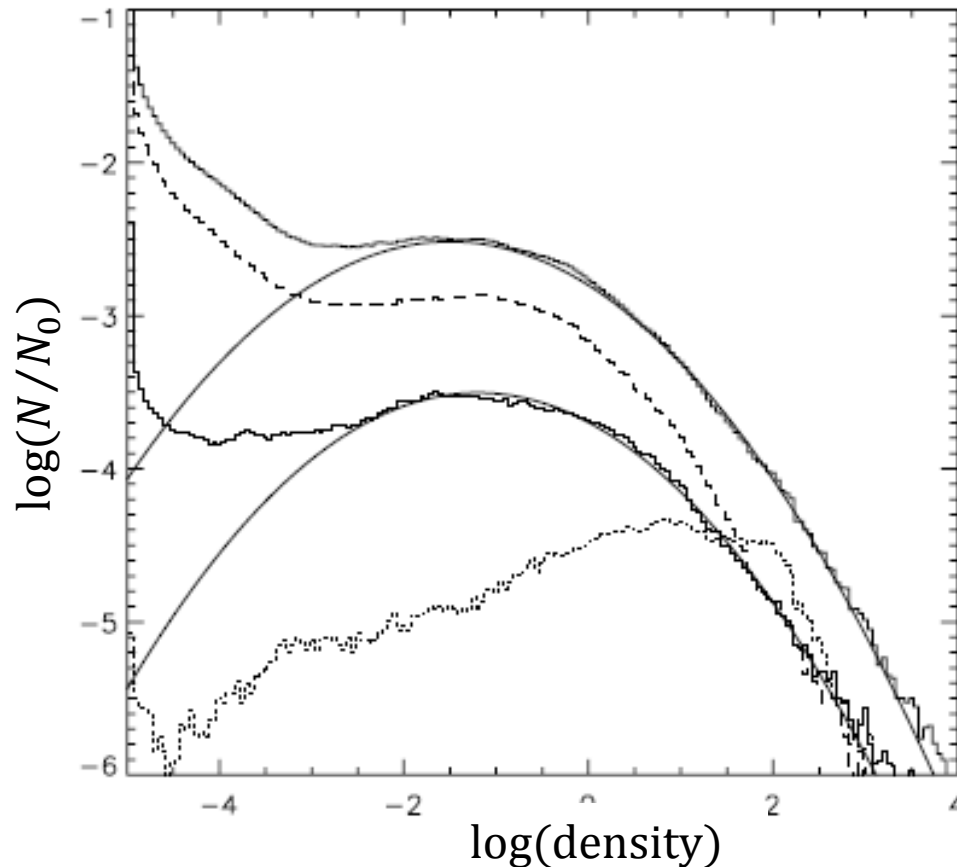


Wada & Norman (2007)

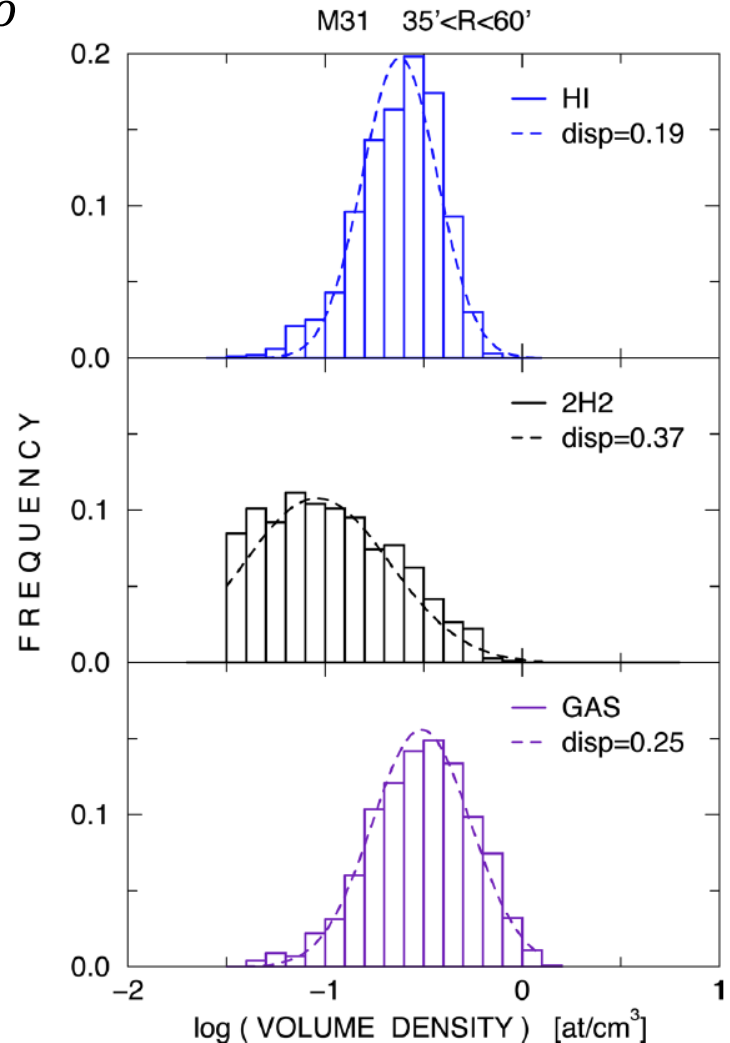


- If non-linear random processes determine density distribution  
 $\Rightarrow$  log-normal distribution (対数正規分布)

$$f(\rho)d\rho = \frac{1}{\sqrt{2\pi}\sigma} \exp\left[-\frac{\ln(\rho/\rho_0)^2}{2\sigma^2}\right] d\ln\rho$$



Numerical simulation  
 (Wada and Norman 2007)



PDF of gas density in M31  
 (Berkhuijsen & Fletcher 2015)

- If stars are formed from dense gas above  $\rho_c$  with an efficiency  $\varepsilon_c$ ,

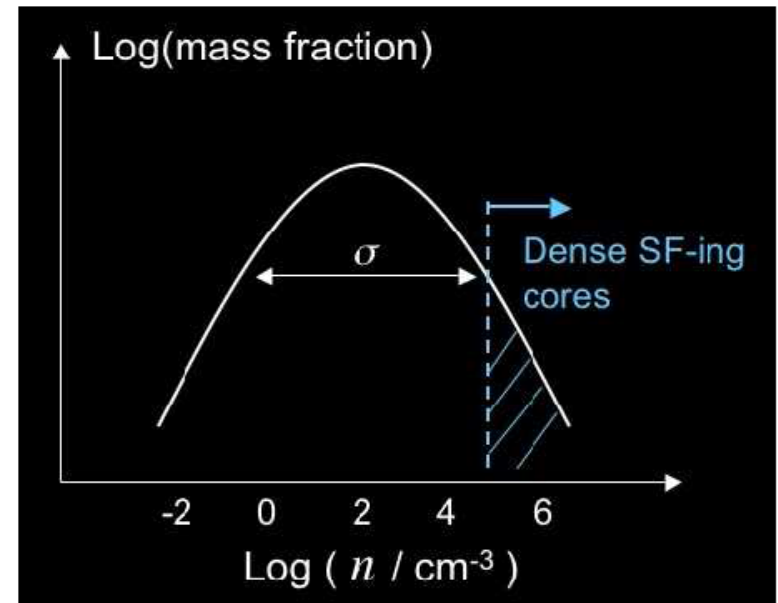
$$\dot{\rho}_* = \varepsilon_c (G \rho_c)^{1/2} f_c \langle \rho \rangle_V$$

$\varepsilon_c$ : Star formation efficiency

$\rho_c$ : Critical density for star formation

$f_c$ : Fraction of gas above critical density

$\langle \rho \rangle_V$ : Average density



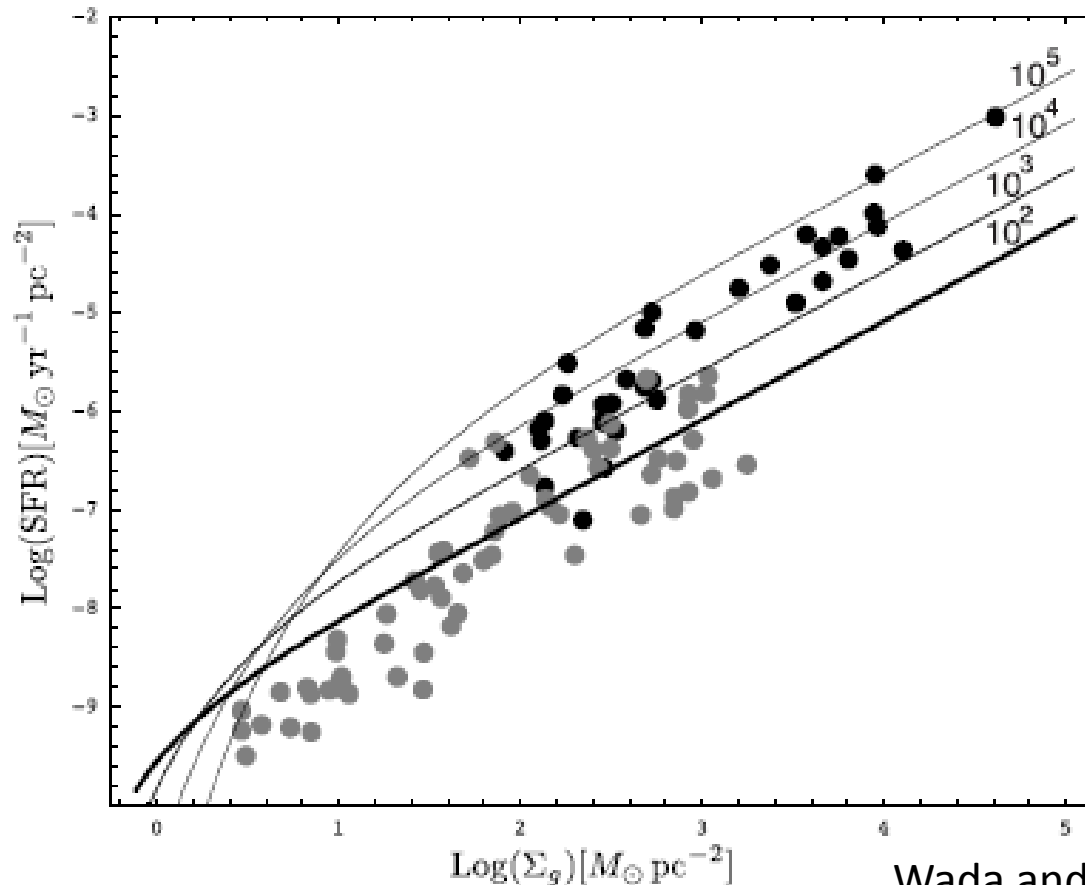
- If PDF of gas density is log-normal  $\Rightarrow f_c$

**SFR  $\Rightarrow$  a function of average density**

$$\begin{aligned} \dot{\rho}_* & \left[ \varepsilon_c, \left( \frac{\langle \rho \rangle_V}{1 M_\odot \text{pc}^{-3}} \right), \left( \frac{\rho_0}{1 \text{cm}^{-3}} \right), \left( \frac{\rho_c}{10^5 \text{cm}^{-3}} \right) \right] \\ & = 3.6 \times 10^{-7} \varepsilon_c M_\odot \text{yr}^{-1} \text{pc}^{-3} \times \left[ 1 - \text{Erf} \left( \frac{\ln(\rho_c \rho_0 / \langle \rho \rangle_V^2)}{2 [\ln(\langle \rho \rangle_V / \rho_0)]^{1/2}} \right) \right] \rho_c^{1/2} \langle \rho \rangle_V \end{aligned}$$

$$\text{Erf}(x) = \frac{2}{\sqrt{\pi}} \int_0^x e^{-t^2} dt$$

- Consistent with observations
  - Steep slop at low density regime
  - $\Sigma_{\text{SFR}} \propto \Sigma_{\text{gas}}$  at high density regime
- Difference between Normal and starburst  $\Rightarrow \varepsilon_c$ ?  
(What is the cause of the difference of  $\varepsilon_c$ ?)



Wada and Norman (2007)

# Physical interpretation of K-S law (3)

## Critical density for star formation (Krumholz and McKee 2005)

- Star formation in clouds in virial equilibrium supported by turbulence

$$\sigma_l \propto l^{0.5} \quad \sigma_l : \text{velocity dispersion, } l : \text{size of molecular cloud}$$

- PDF of gas density : log-normal
- Gravitational energy > turbulence energy  $\Rightarrow$  star formation  
 $\Rightarrow$  Jeans length  $< \lambda_s$  (velocity dispersion of turbulence = sound speed)

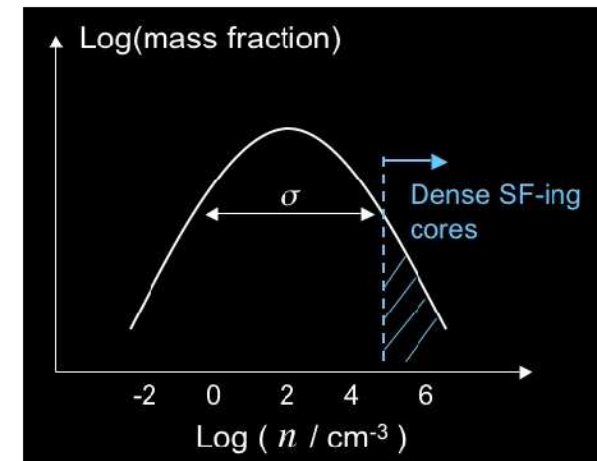
$$x = \frac{\rho}{\rho_0} > x_{crit} \equiv \left( \phi_x \frac{\lambda_{J0}}{\lambda_s} \right)^2$$

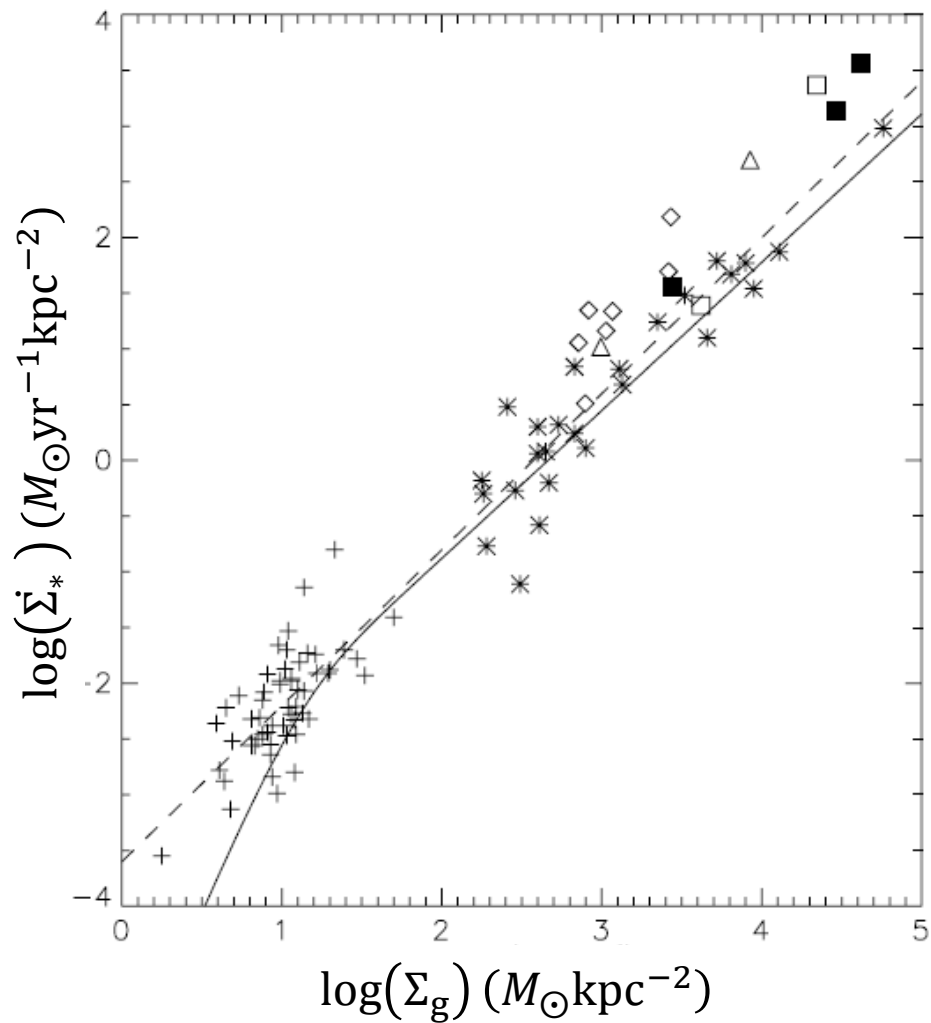
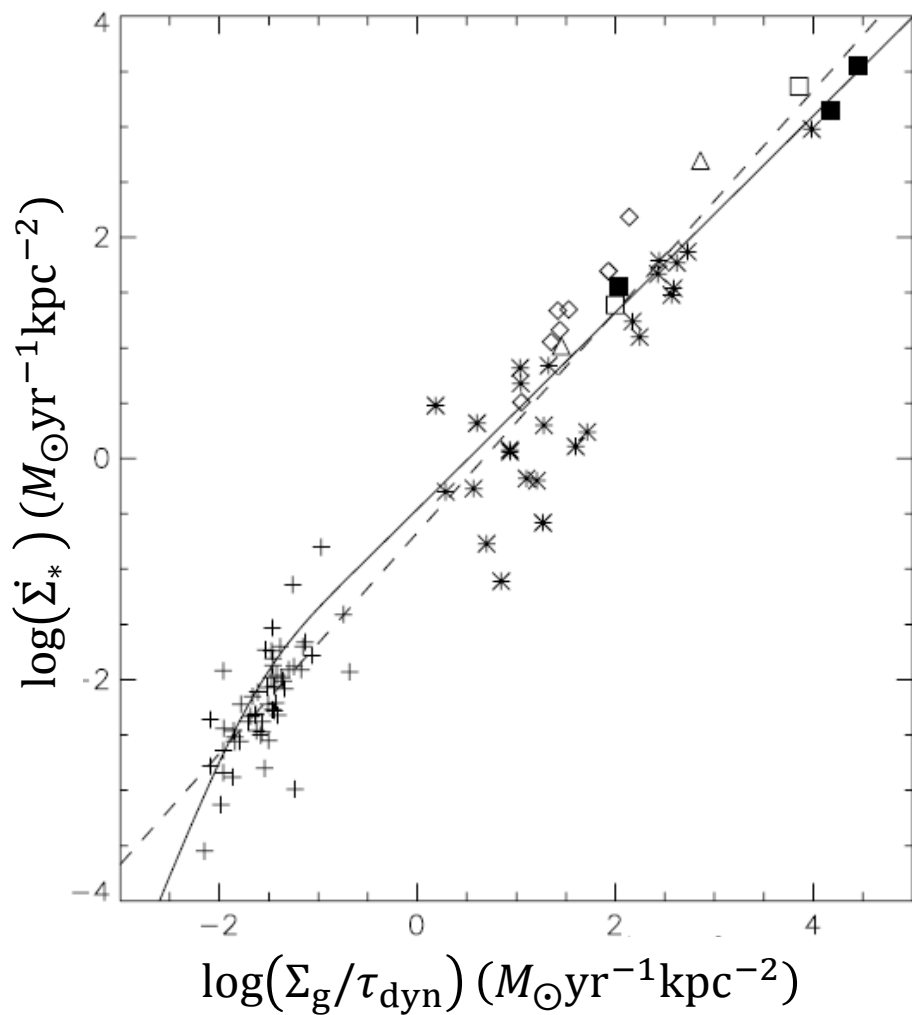
$\lambda_{J0}$  : Jeans length of average density

$\phi_x = 1.13$  : fitted by simulations

$\Rightarrow$  Spatial variation of critical density

- Small  $\lambda_s \Rightarrow$  high critical density  
e.g., Galactic center



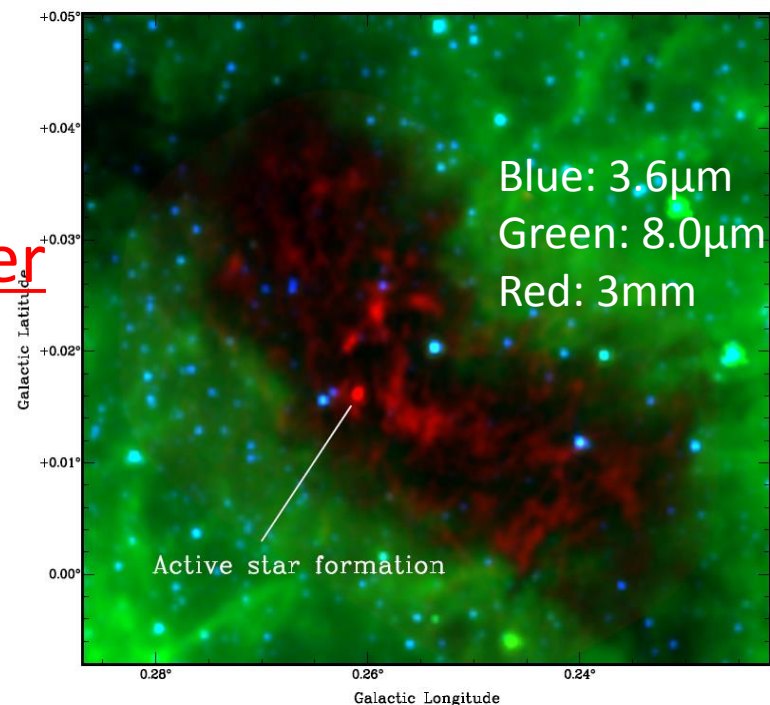


- Solid line : Krumholz & McKee (2005)
- Dashed line : Kennicutt (1998)

# Star formation near the Galactic center

(Rathborne et al. 2014) (ALMA)

- Central Molecular Zone (CMZ)
  - Low  $\Sigma_{\text{SFR}}/\Sigma_{\text{dense}}$   
⇒ High critical density for star formation
    - G0.253+0.016
      - Star formation in the core with highest density ( $> 10^6 \text{ cm}^{-3}$ )



	Solar	G0.253+0.016	
Measured			
Mean, column density PDF ( $N_0$ )	$0.5\text{--}3.0 \times 10^{21} \text{ cm}^{-2}$	$86 \pm 20 \times 10^{21} \text{ cm}^{-2}$	7, 8
Dispersion, column density PDF ( $\sigma_{\log N}$ )	0.28–0.59	$0.34 \pm 0.03$	7, 8
Critical volume density ( $\rho_{\text{crit}}$ )	<u><math>10^4 \text{ cm}^{-3}</math></u>	<u><math>&gt; 10^6 \text{ cm}^{-3}</math></u>	3, 9, 8
Predicted (relative to solar neighborhood clouds)			
Mean, column density PDF ( $N_0$ )	1	100	
Dispersion, volume density PDF ( $\sigma_{\log \rho}$ )	1	1.2	
Critical volume density ( $\rho_{\text{crit}}$ )	<u>1</u>	<u><math>10^4</math></u>	10, 11, 5

**Note.** The key properties are marked in bold.

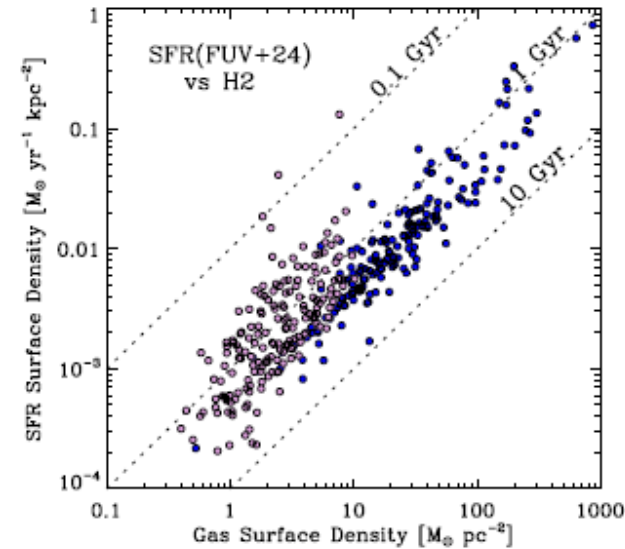
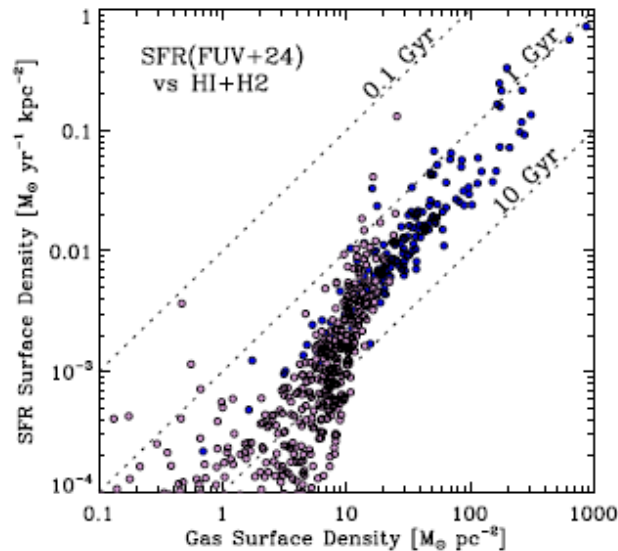
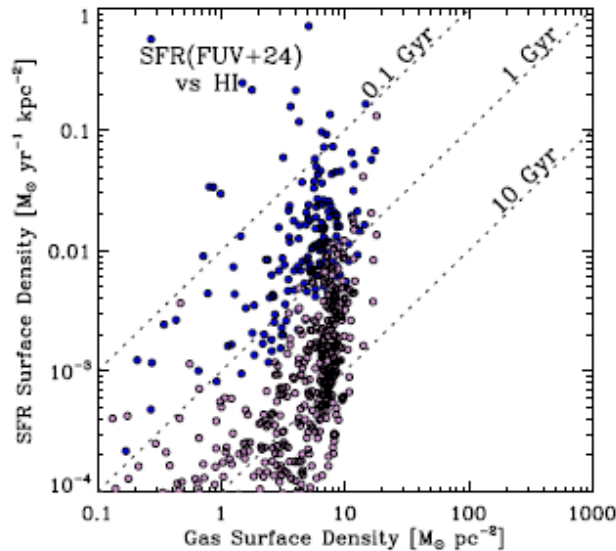
**References.** (1) Larson 2003; (2) Ao et al. 2013; (3) Lada et al. 2010; (4) Longmore et al. 2013; (5) Kruijssen et al. 2014; (6) Schneider et al. 2014; (7) Kainulainen et al. 2009; (8) this work; (9) Lada et al. 2012; (10) Krumholz & McKee 2005; (11) Padoan & Nordlund 2011.

# Physical interpretation of K-S law (4)

- SFR vs. HI: no correlation
- SFR vs.  $H_2$  :  $\Sigma_{SFR} \propto \Sigma_{H_2}^{1.0}$
- SFR vs.  $HI+H_2$  :  $\Sigma_{SFR} \propto \Sigma_{HI+H_2}^{1.6}$  + Critical density for star formation

## ⇒ Star formation: Two processes

- $HI \rightarrow H_2 \Rightarrow$  Critical density for  $H_2$  formation
- Star formation from  $H_2$  with a constant efficiency



Schruba et al. (2011)

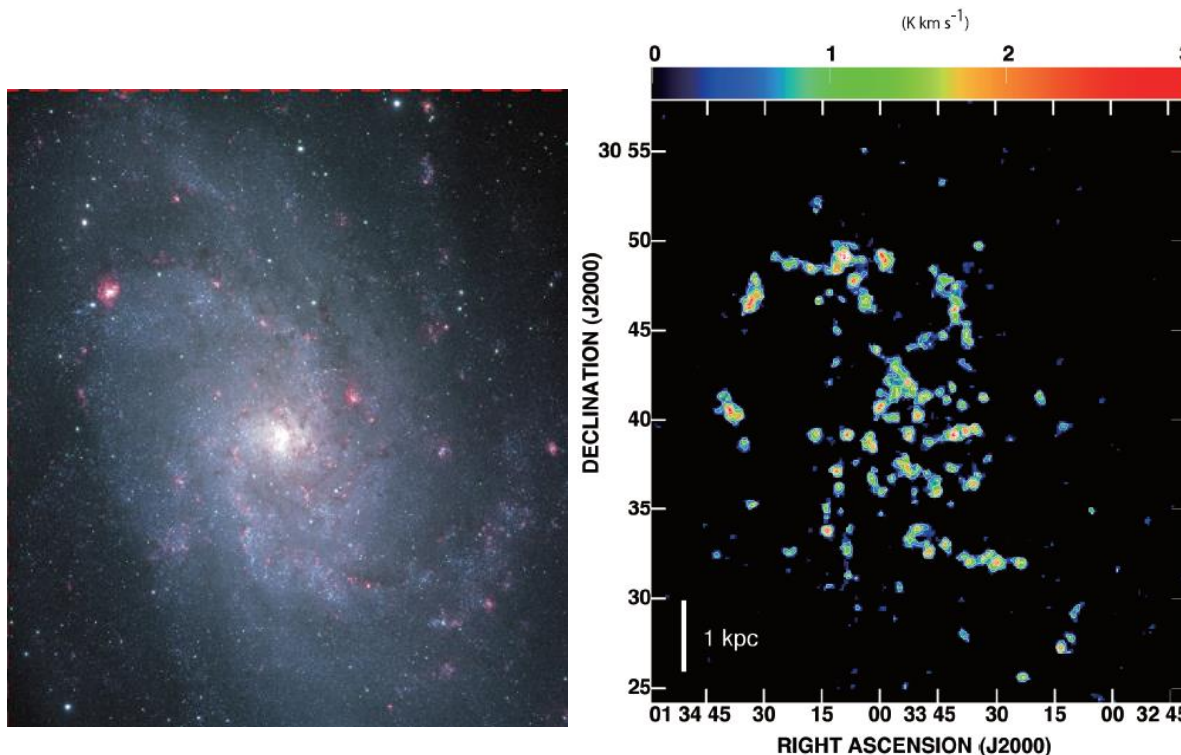
2. Star formation law in GMC scale
3. Dependence on surface density of gas
  - High density regime
  - Low density regime
4. Volume density of gas vs. SFE



## 2. K-S law in GMC scale (Onodera et al. 2009)

- K-S law
  - Global
  - Radial average

To what scale is the K-S law valid?

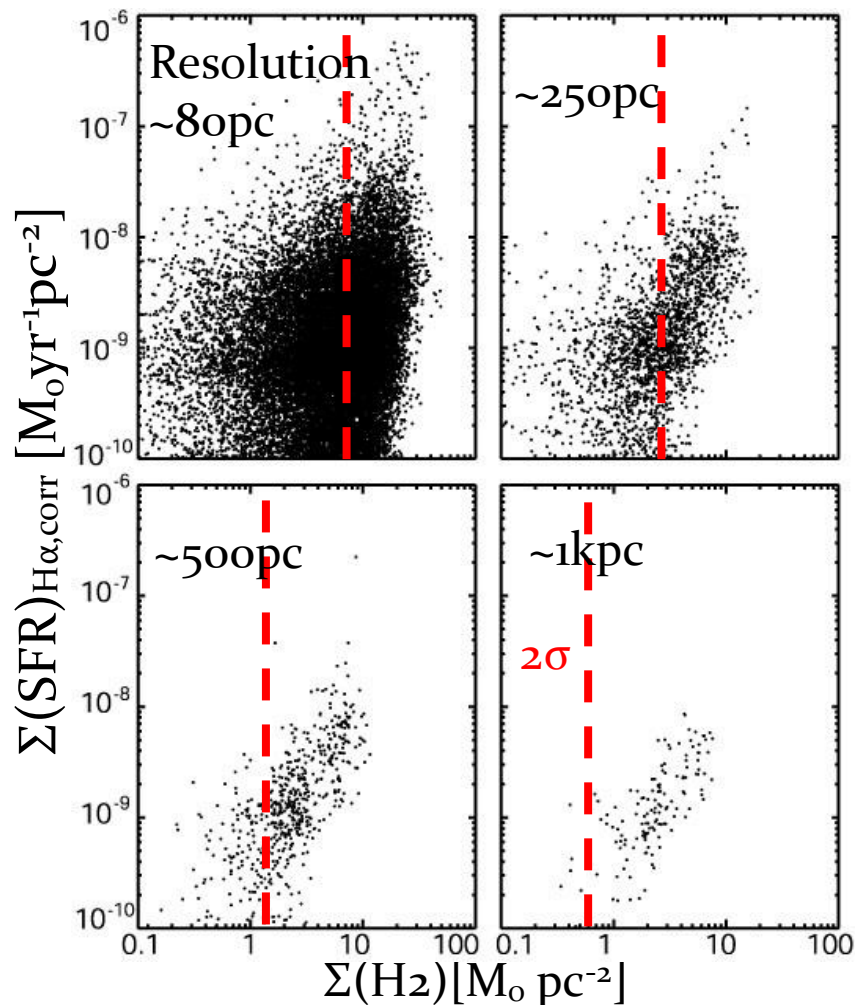


Spatial resolution  
~80 pc  
(GMC scale)

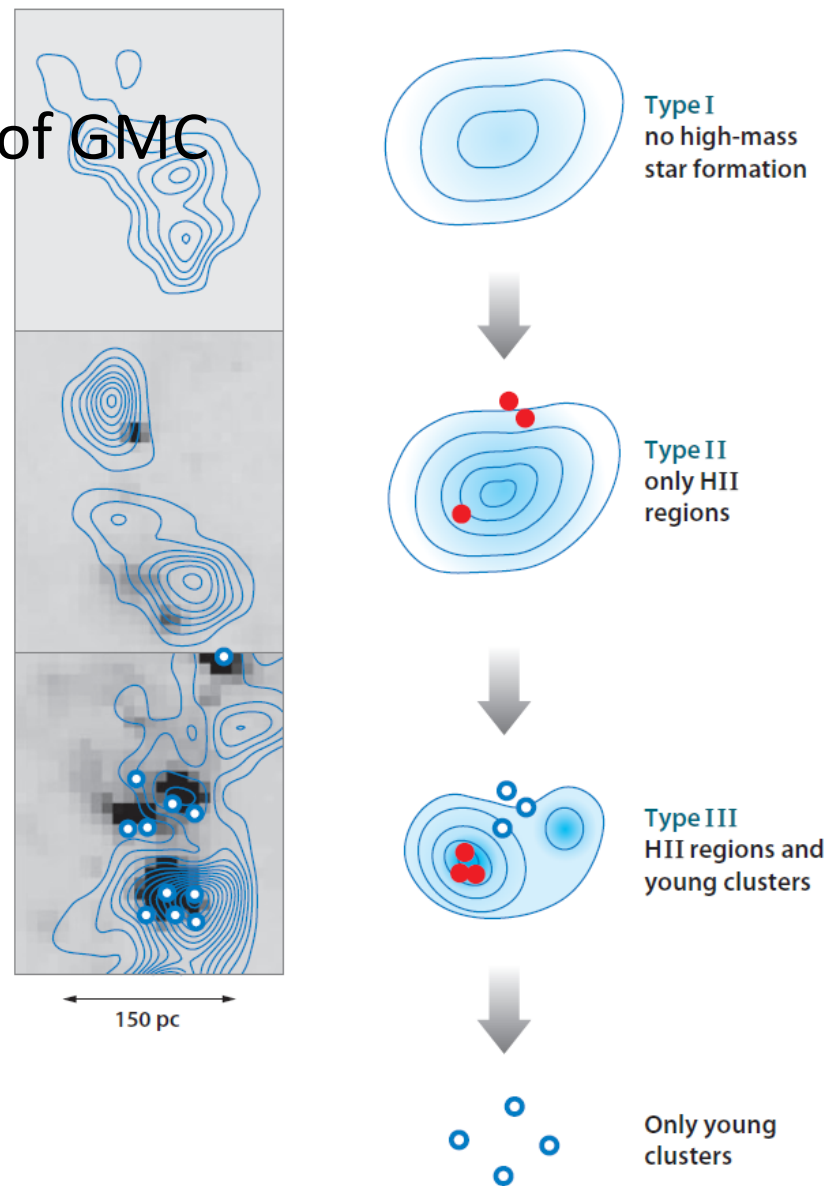
CO map of M33 (Tosaki et al. 2011)

# K-S law in GMC scale

- Breakdown of K-S law
- Difference of evolutionary stage of GMC



M33: Onodera et al. (2009)

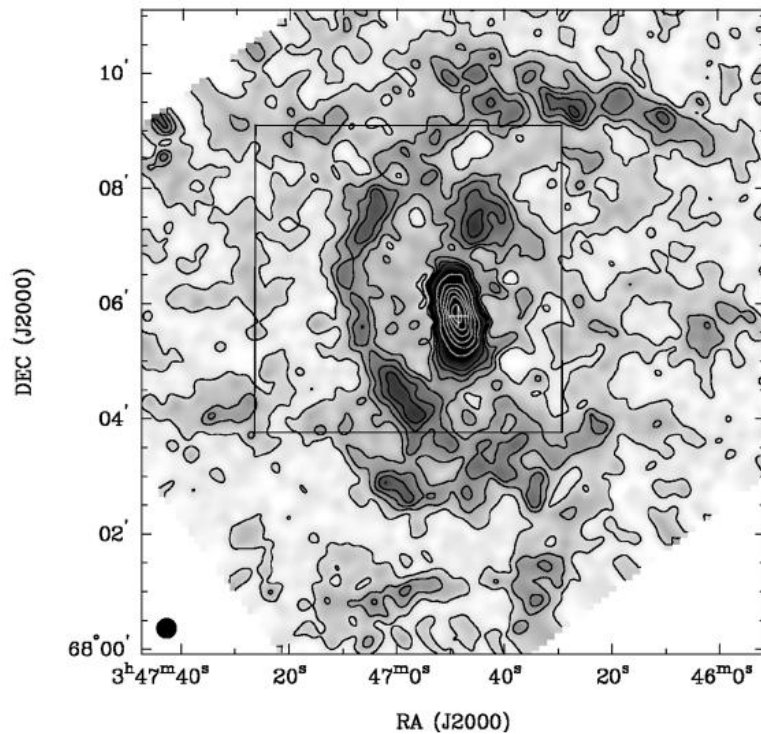


LMC: Fukui & Kawamura (2010)

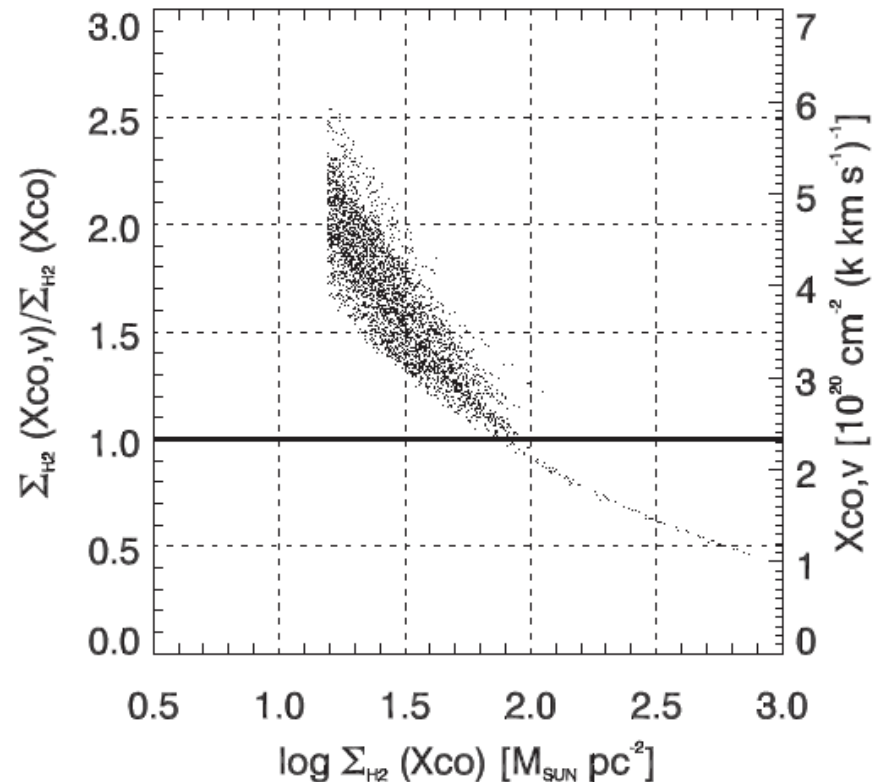
### 3. Dependence on surface density of gas K-S law at high density region (Pan et al. 2014)

- Dependence of  $X_{\text{CO}}$  on metallicity and CO intensity

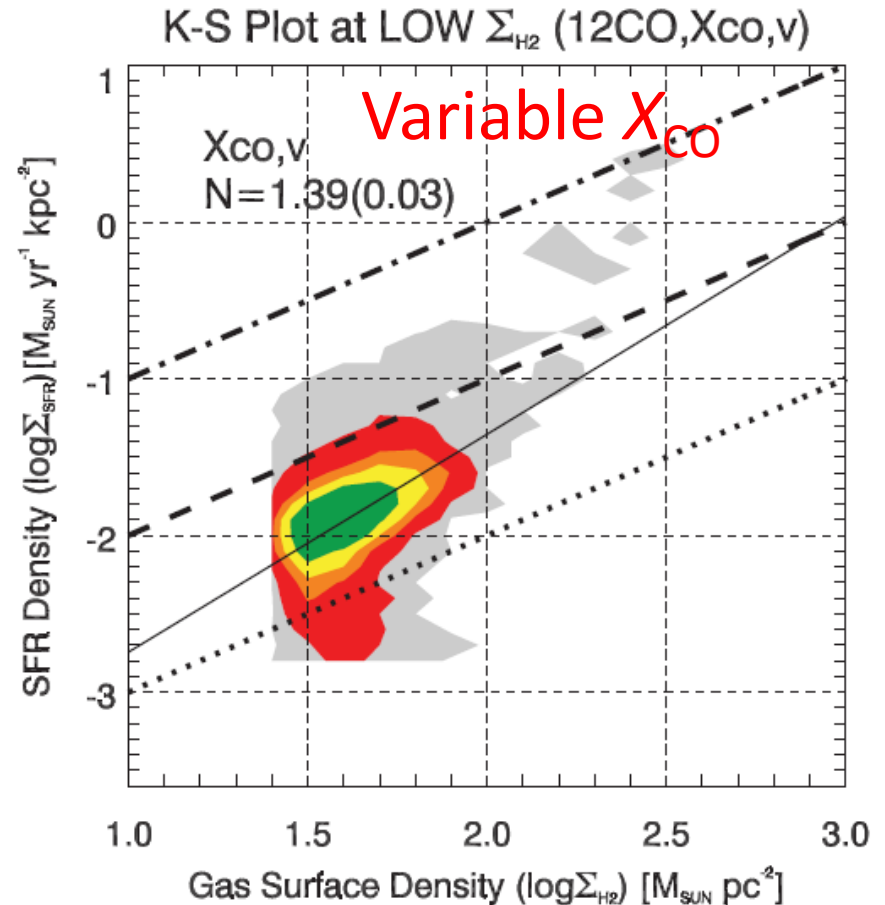
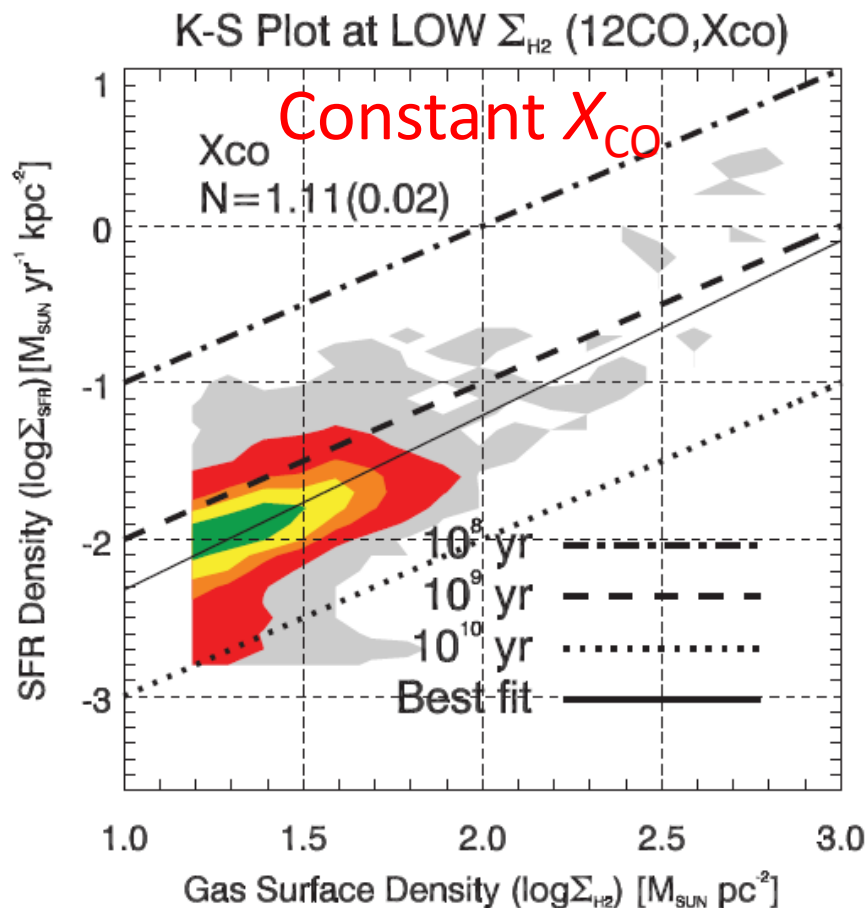
$$X_{\text{CO},v} = \frac{\min[4, 6.75 \times \langle W_{\text{CO}} \rangle^{-0.32}] \times 10^{20}}{Z'^{0.65}} \quad (\text{Narayanan et al. 2012})$$



$^{12}\text{CO}$  map of IC342  
(Kuno et al. 2007)



- K-S law taking account of dependence of  $X_{\text{CO}}$  on metallicity and CO intensity
  - Higher power at high density region



# Comparison with optically thin $^{13}\text{CO}$

- $^{12}\text{CO}$

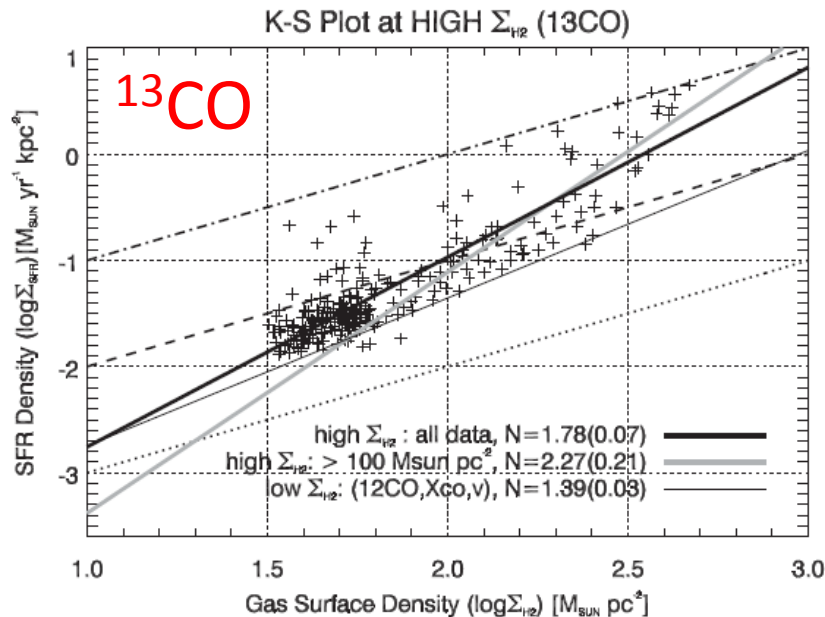
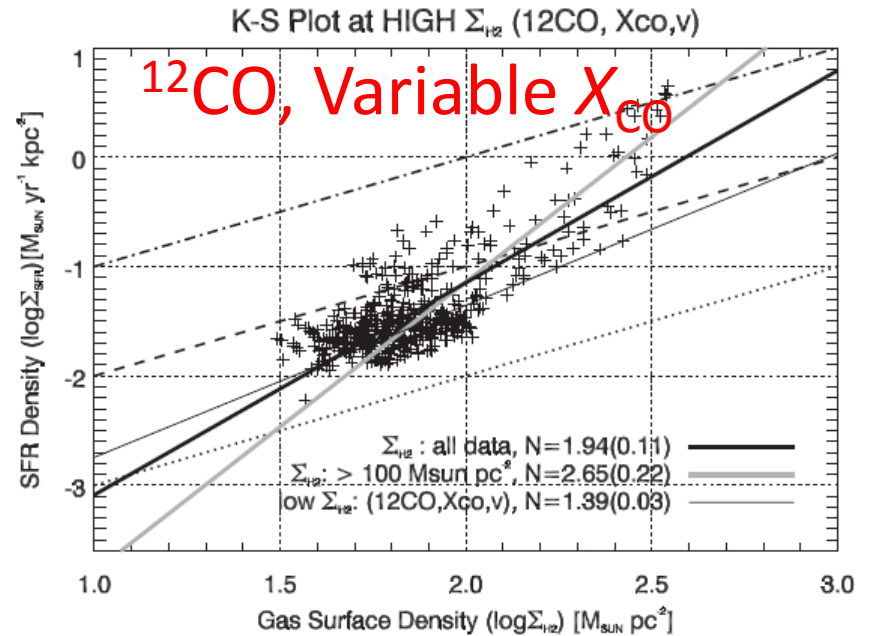
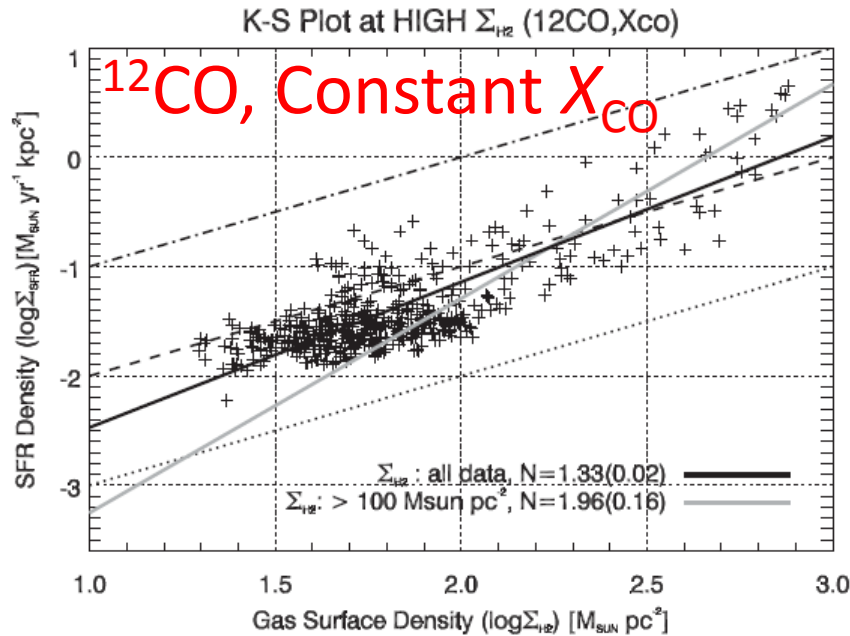
- Optically thick
  - Conversion factor  $\Rightarrow$  Gas mass

- $^{13}\text{CO}$

- Optically thin
  - LTE  $\Rightarrow$  Gas mass
- Abundance variation
  - Radial variation: center  $\Rightarrow$  high  $^{13}\text{CO}/^{12}\text{CO}$
- Temperature variation
  - Dust temperature  $\Rightarrow$  Gas temperature



- Comparison with optically thin  $^{13}\text{CO}$

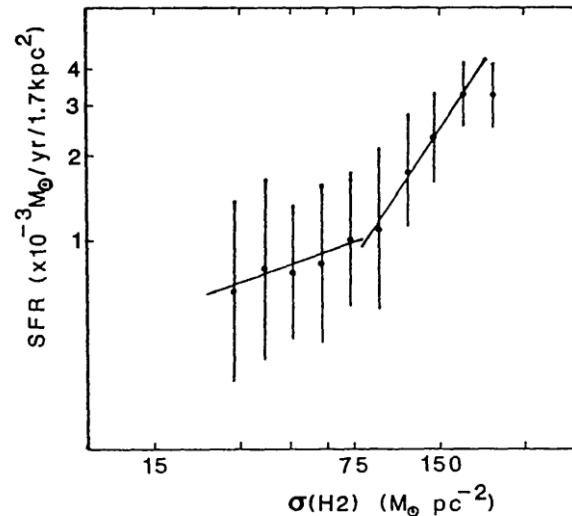


Same trend in  $^{13}\text{CO}$  K-S law  
[power, N]

	[all]	[>100Mo/pc <sup>2</sup> ]
$^{12}\text{CO}, X_{\text{CO}}$	1.33	1.96
$^{12}\text{CO}, X_{\text{CO},v}$	1.94	2.65
$^{13}\text{CO}$	1.78	2.27

## • Star formation mechanisms

- Low density region: Gravitational instability
- High density region: Cloud-cloud collision



M51

(Nakai, Kuno et al. 1991)

## • GMC properties

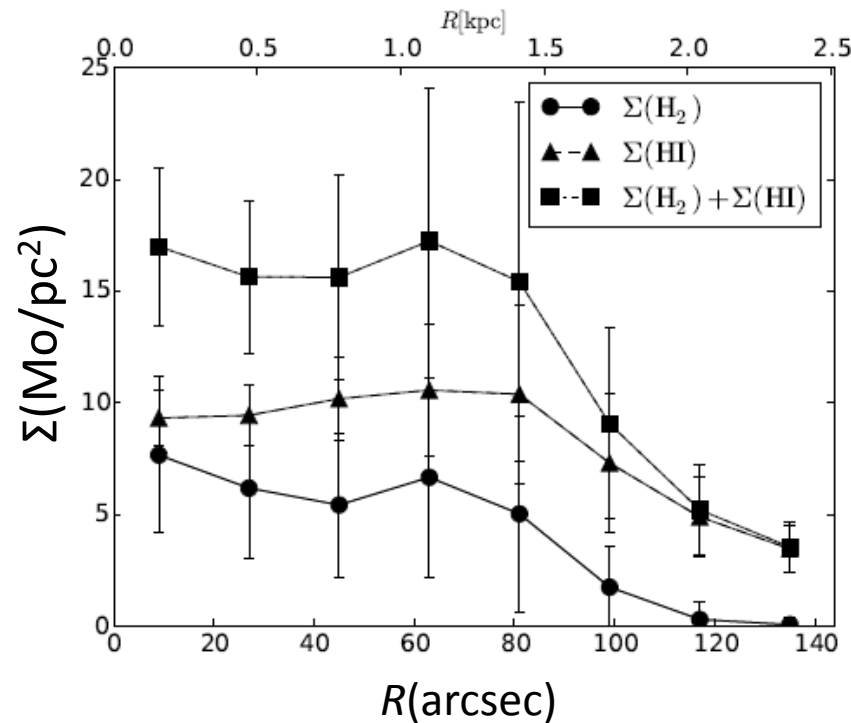
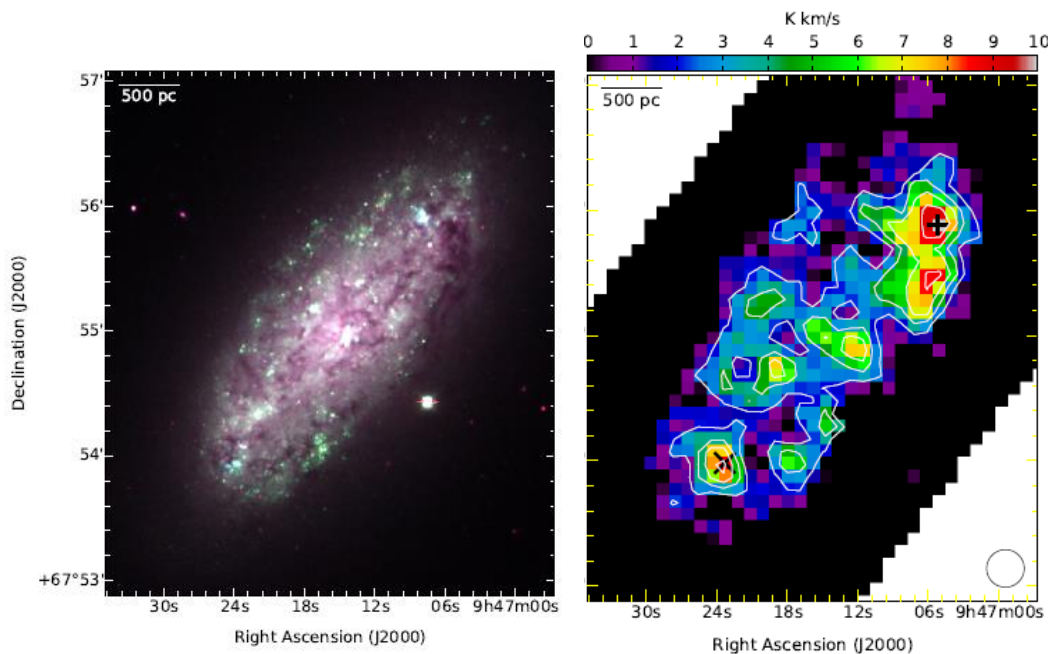
- High density region: ISM pressure  $\Rightarrow$  High density  
 $\Rightarrow$  Short free fall time  
(Krumholz et al. 2009)

# 3. Dependence on surface density of gas

## K-S law at low density region (Hatakeyama et al. 2017)

- NGC 2976
  - Nearby (3.56Mpc)
  - HI dominant

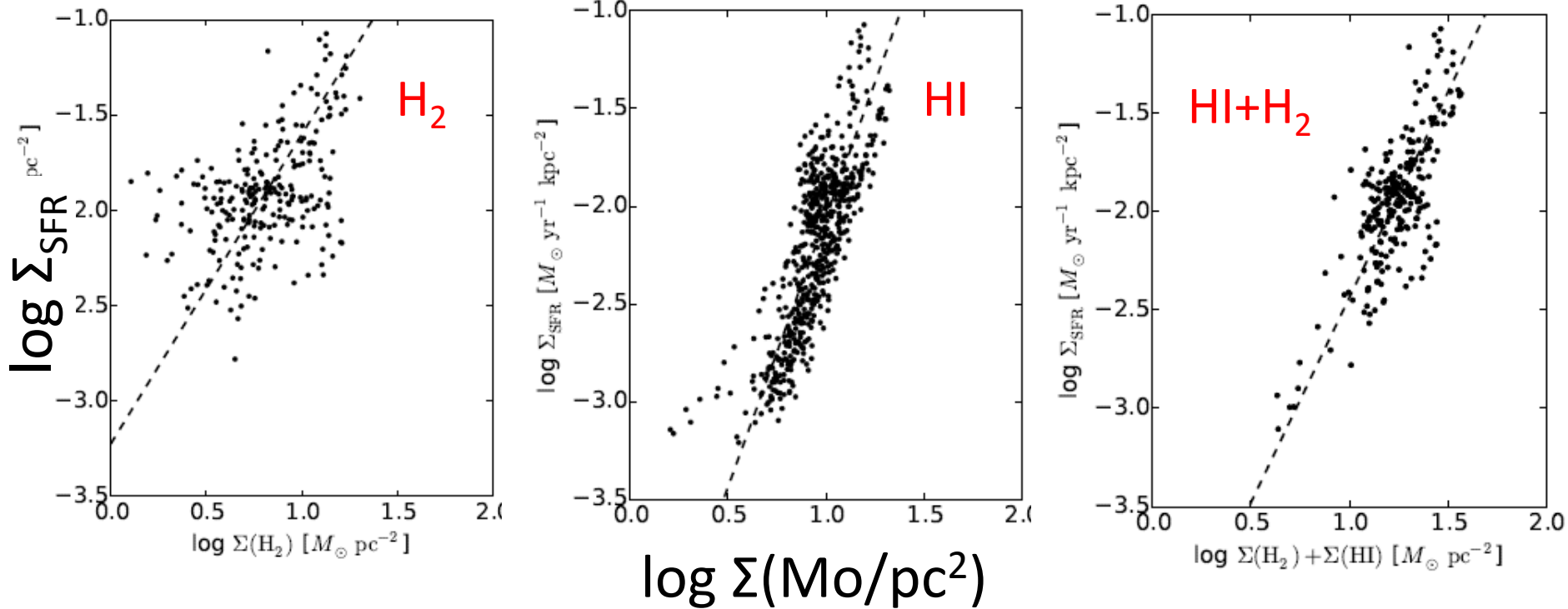
Good sample :  $\text{HI} \Rightarrow \text{H}_2 \Rightarrow \text{Star formation}$



$I_{\text{CO}}$  map obtained with NRO 45-m telescope



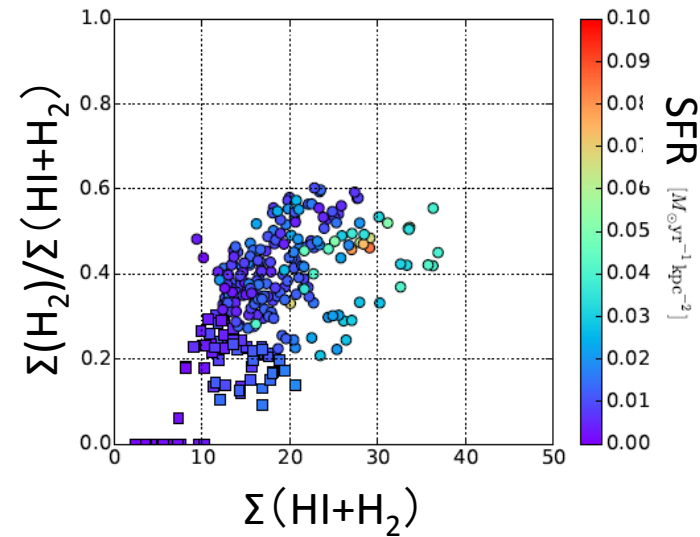
# K-S law at low density region



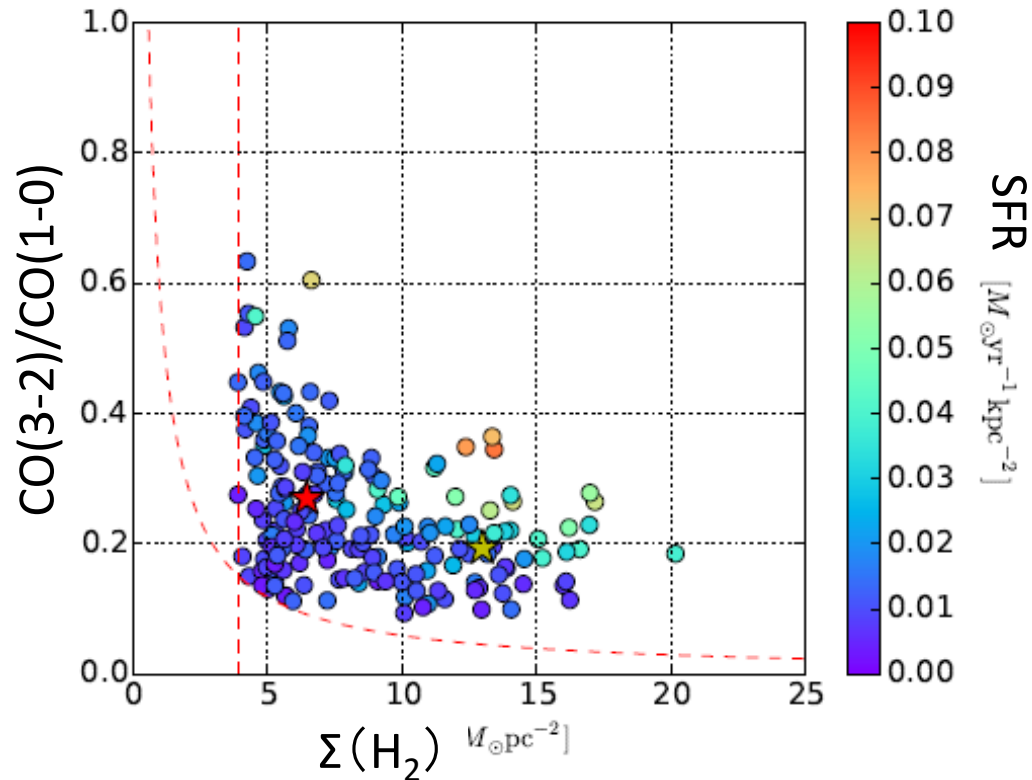
## • HI

- Saturated at  $\Sigma \approx 10 M_{\odot} \text{pc}^{-2}$
  - Correlation with SFR (photoionization)?
- $\Rightarrow$  Power:  $\text{HI}+\text{H}_2 > \text{H}_2$

$\text{H}_2$  formation



- $\Sigma(H_2) > 10 M_\odot \text{pc}^{-2} \Rightarrow$  star formation?
- Diffuse clouds  $\Rightarrow$  Self gravitating clouds ?

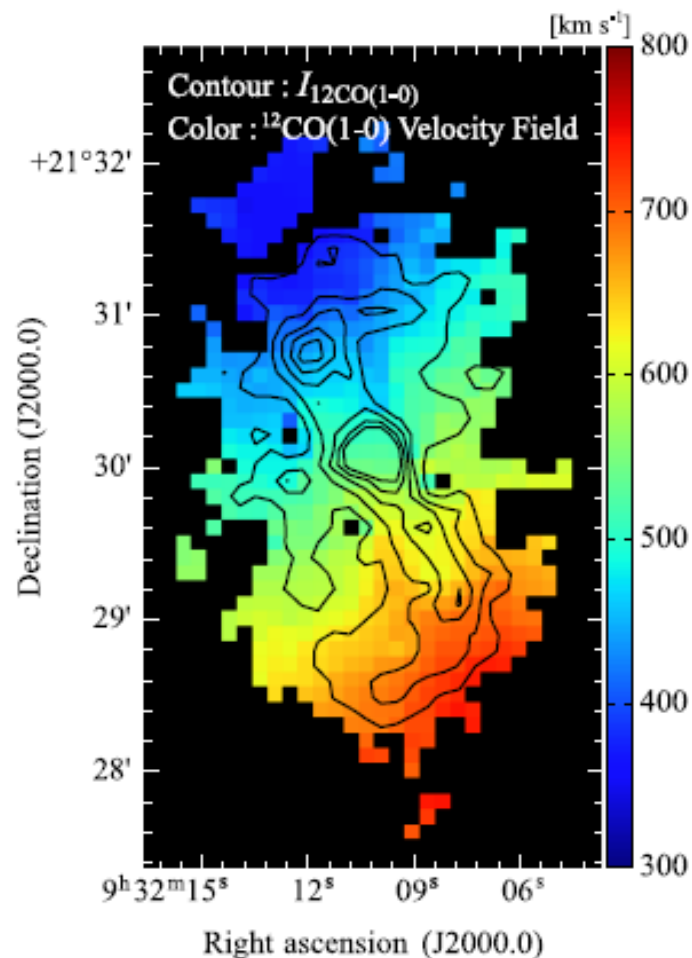
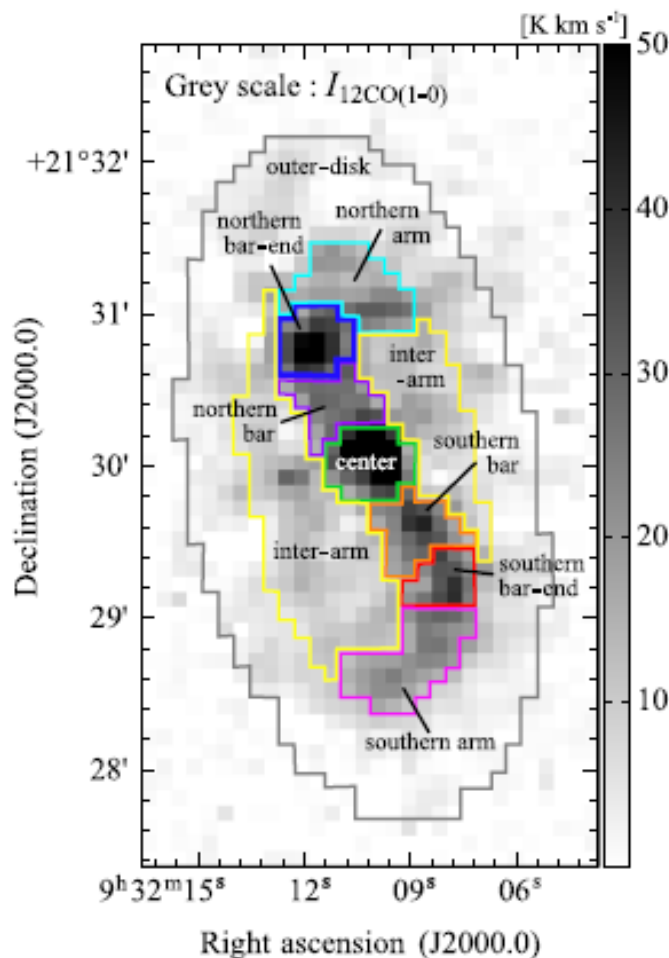


## Star formation process

- $\Sigma(\text{HI}) > 10 M_\odot \text{pc}^{-2} : \quad \text{HI} \Rightarrow \text{H}_2$  (diffuse clouds)
- $\Sigma(\text{H}_2) > 10 M_\odot \text{pc}^{-2} : \quad \text{H}_2 \Rightarrow$  self gravitating clouds  $\Rightarrow$  star

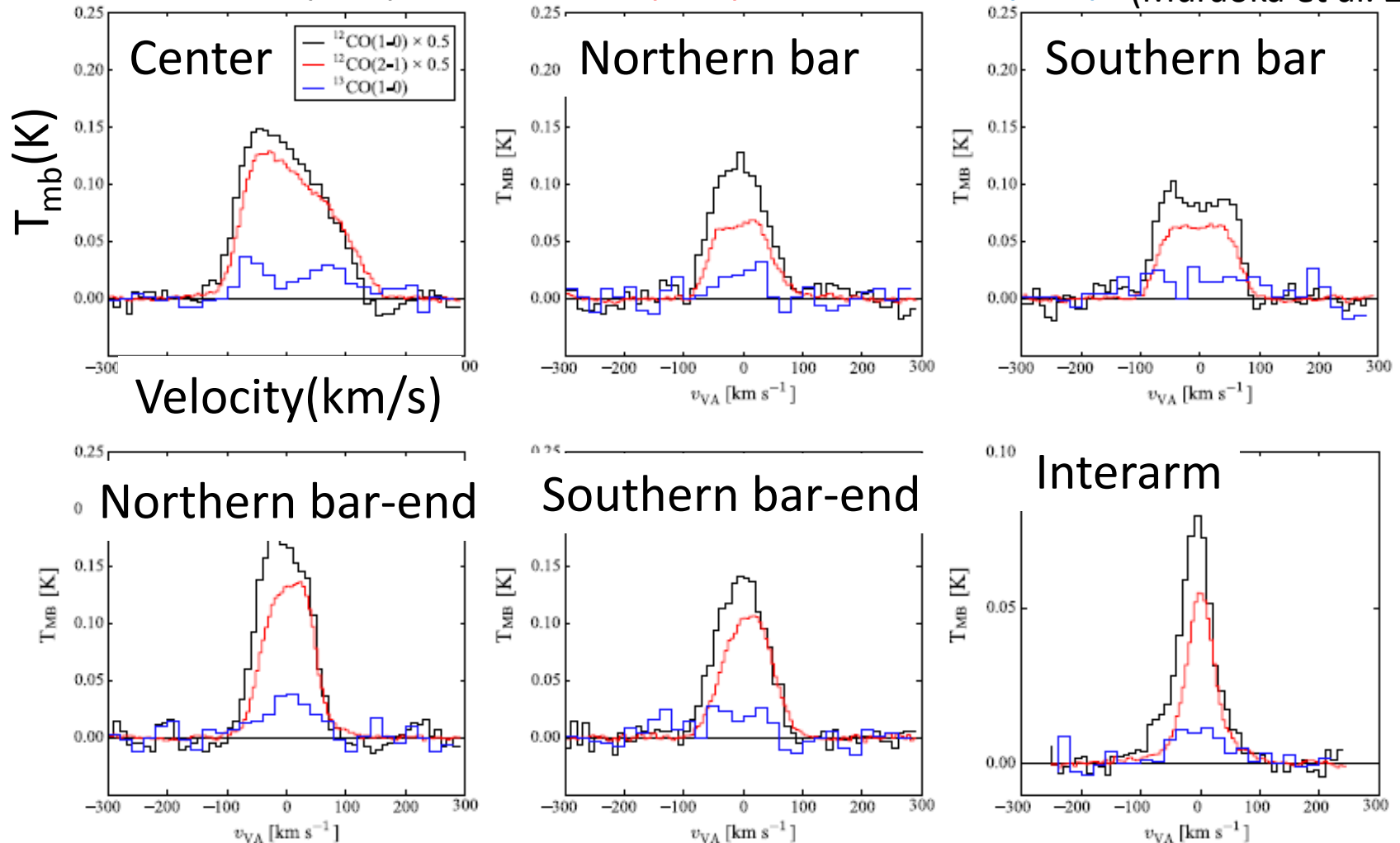
# 4. Volume density of gas vs. SFE (Muraoka et al. 2016)

- NGC 2903
- $^{12}\text{CO}+^{13}\text{CO}$  mapping (COMING)  $\Rightarrow$  Physical properties



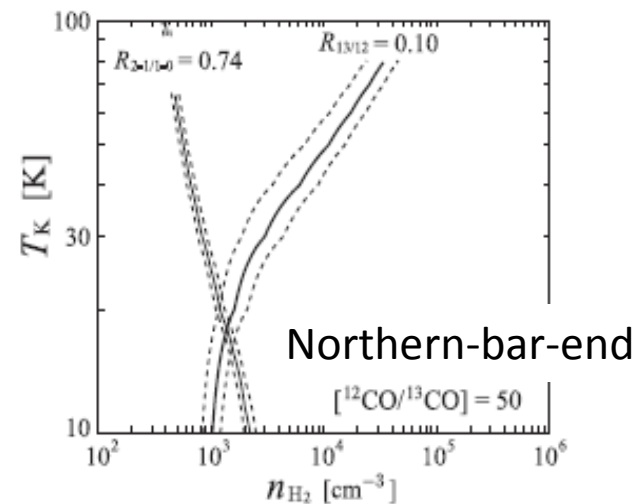
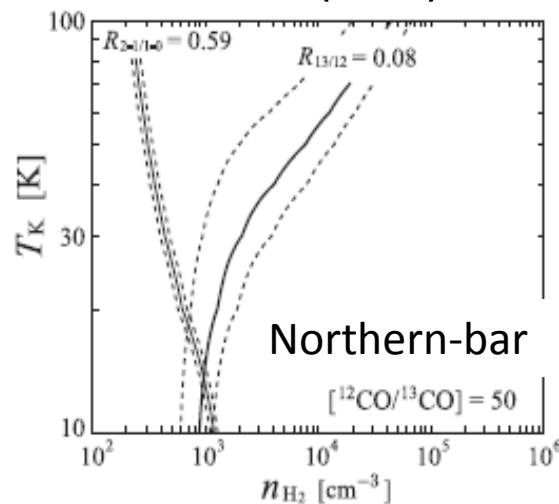
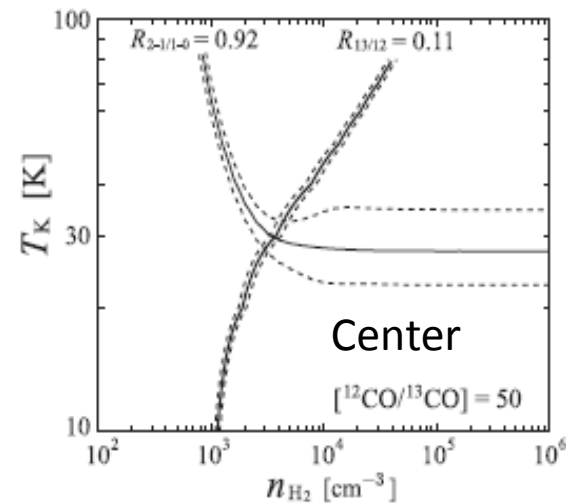
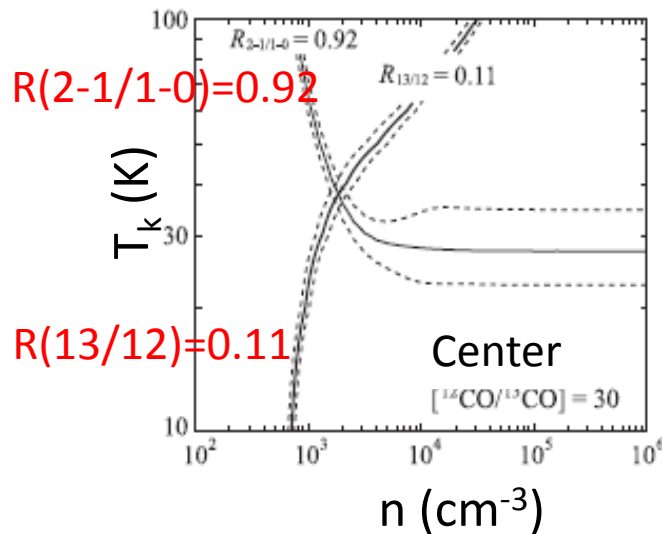
- Detection of  $^{13}\text{CO}$  by stacking using  $^{12}\text{CO}$  velocity

Black:  $^{12}\text{CO}(1-0)$ , Red:  $^{12}\text{CO}(2-1)$ , Blue:  $^{13}\text{CO}(1-0)$  (Muraoka et al. 2016)



( $^{12}\text{CO}(2-1)$ : IRAM 30-m Leroy et al. 2009)

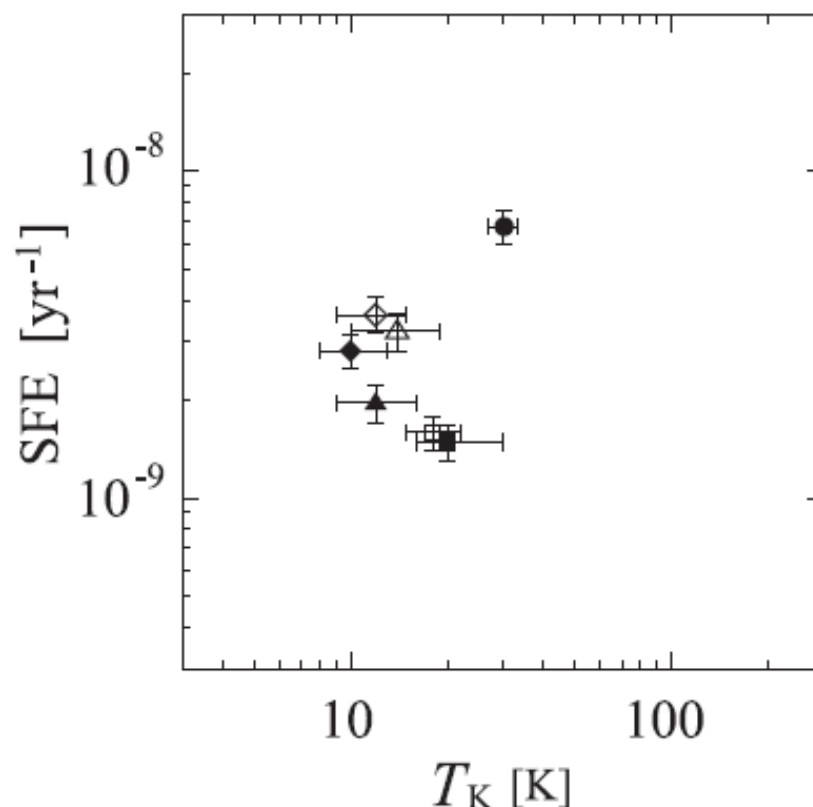
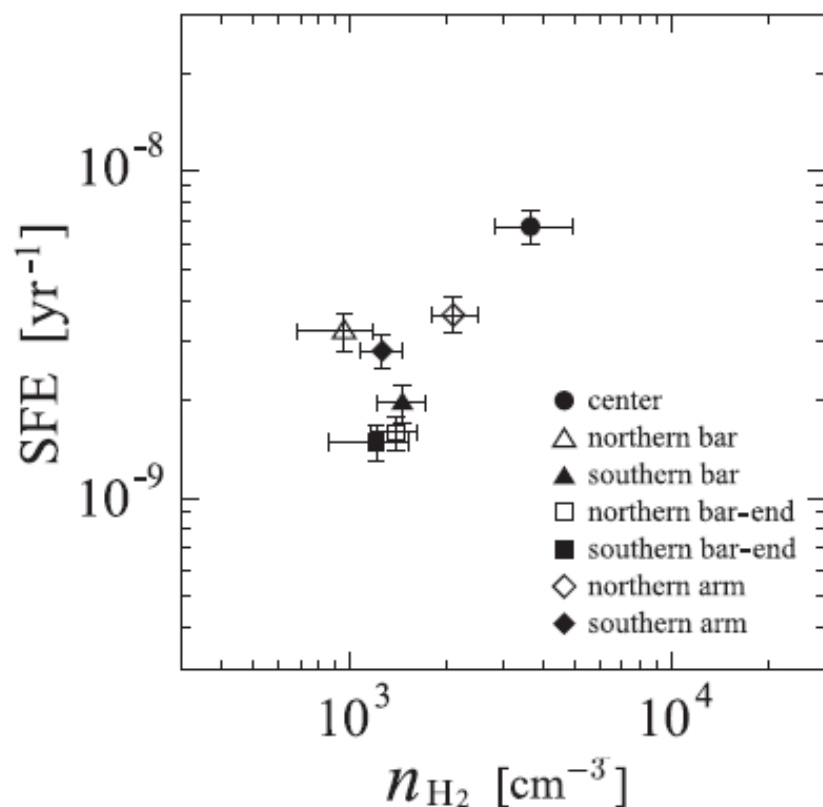
- Large Velocity Gradient (LVG) model
  - Abundance, Velocity gradient  $\Rightarrow$  density, temperature



(Muraoka et al. 2016)

# Volume density of molecular gas vs. SFE

- Higher volume density  $\Rightarrow$  Higher SFE



# Summary

- Star formation law: one of the most fundamental relations to understand galaxy evolution
  - Gas phase (total gas, molecular gas, dense gas)
  - Galaxy type (e.g., normal vs. starburst)
  - Time scale of star formation
  - Spatial variation in galaxies  
(relation with galactic structures, such as spiral arm and bar)
  - Surface density  $\Rightarrow$  volume density
  - Effect of variation in conversion factor  $X_{\text{co}}$