High School Assignment

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1 2018-ICSE-10th board-Problem: 8(b)

Problem: If the mean of the following distribution is 24, find the value of 'a'.

| Marks | 0-10 | 10-20 | 20-30 | 30-40 | 40-50 |
|--------------------|------|-------|-------|-------|-------|
| Number of students | 7 | a | 8 | 10 | 5 |

 $\underline{\textbf{Solution}}$: Given, the mean of the following distribution is, m = 24. We know that,

$$mean(m) = \frac{\sum f_i x_i}{\sum f_i} \tag{1}$$

As per the question,

Table 1: Given data

| Intervals | Frequency (f_i) | Mid-Value (x_i) | $f_i x_i$ |
|-----------|---------------------|-------------------|----------------------------|
| 0-10 | 7 | 5 | 35 |
| 10-20 | a | 15 | 15a |
| 20-30 | 8 | 25 | 200 |
| 30-40 | 10 | 35 | 350 |
| 40-50 | 5 | 45 | 225 |
| | $\sum f_i = 30 + a$ | | $\sum f_i x_i = 810 + 15a$ |

Therefore, from equation 1, the value of mean(m = 24) can be written as,

$$24 = \frac{810 + 15a}{30 + a}$$
$$24(30 + a) = 810 + 15a$$
$$720 + 24a = 810 + 15a$$
$$9a = 90$$
$$a = 10$$

Therefore, the required value(a) is 10.