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Assignment 9

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I. PAPOULIS-CHAPTER-15

Question 15-7: Show that the sums $s_n = x_1 + x_2 + ... + x_n$ of independent zero mean random variables form a martingale.

Solution: Given,

$$s_n = x_1 + x_2 + \dots + x_n$$
 (I.1)

where, x_n are i.i.d. random variables. We have

$$s_{n+1} = s_n + x_{n+1} (I.2)$$

so that,

$$E\{s_{n+1}|s_n\} = E\{s_n + x_{n+1}|s_n\}$$
 (I.3)

$$= s_n + E\{x_{n+1}\}$$
 (I.4)

$$= s_n \tag{I.5}$$

Hence, $\{s_n\}$ represents a Martingale.