# Feature Overlap/ Feature Interaction

How overlapping features work in maxent models



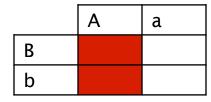
## **Feature Overlap**

- Maxent models handle overlapping features well.
- Unlike a NB model, there is no double counting!

**Empirical** 

	Α	a
В	2	1
b	2	1

	Α	a
В		
b		



	Α	a
В		
b		

A = 2/3		
	Α	a
В	1/3	1/6
b	1/3	1/6

A = 2/3		
	Α	a
В	1/3	1/6
b	1/3	1/6

	Α	a
В		
b		

_	Α	a
В	$\lambda_{A}$	
b	$\lambda_{A}$	

	Α	а
В	λ' _ + λ' ' _ A	
b	λ' _ + λ' ' _ A	



## **Example: Named Entity Feature Overlap**

Grace is correlated with PERSON, but does not add much evidence on top of already knowing prefix features.

### **Local Context**

	Prev	Cur	Next
State	Other	???	???
Word	at	Grace	Road
Tag	IN	NNP	NNP
Sig	Х	Xx	Xx

Feature Weights

Feature Type	Feature	PERS	LOC
Previous word	at	-0.73	0.94
Current word	Grace	0.03	0.00
Beginning higram	<i>-C</i>	0.45	-0.04
Current POS tag	NNP	0.47	0.45
Prev and cur tags	IN NNP	-0.10	0.14
Previous state	Other	-0.70	-0.92
Current signature	Xx	0.80	0.46
Prev state, cur sig	O-Xx	0.68	0.37
Prev-cur-next sig	x-Xx-Xx	-0.69	0.37
P. state - p-cur sig	O-x-Xx	-0.20	0.82
Total:		-0.58	2.68



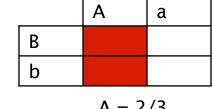
## **Feature Interaction**

 Maxent models handle overlapping features well, but do not automatically model feature interactions.

**Empirical** 

	Α	a
В	1	1
b	1	0

	Α	a
В		
b		



	Α	a
В		
b		

$$AII = 1$$
 $A = a$ 
 $B = 1/4 = 1/4$ 
 $b = 1/4 = 1/4$ 

A = 2/3		
	Α	a
В	1/3	1/6
b	1/3	1/6

B = 2/3		
A a		
В	4/9	2/9
b	2/9	1/9

	Α	a
В	0	0
b	0	0

	Α	a
В	$\lambda_{A}$	
b	$\lambda_{A}$	

	Α	a
В	$\lambda_A + \lambda_B$	$\lambda_{B}$
b	$\lambda_{A}$	



### **Feature Interaction**

• If you want interaction terms, you have to add them:

**Empirical** 

	Α	a
В	1	1
b	1	0

	Α	a
В		
b		

A = 2/3		
	Α	a
В	1/3	1/6
b	1/3	1/6

	Α	a
В		
b		

B = 2/3		
A a		
В	4/9	2/9
b	2/9	1/9

_	Α	a
В		
b		

AB = 1/3		
	Α	a
В	1/3	1/3
b	1/3	0

• A disjunctive feature would also have done it (alone):

	Α	a
В		
b		

	Α	a
В	1/3	1/3
b	1/3	0



## **Quiz Question**

- Suppose we have a 1 feature maxent model built over observed data as shown.
- What is the constructed model's probability distribution over the four possible outcomes?

Empirical

	Α	a
В	2	1
b	2	1

**Features** 



**Expectations** 

### **Probabilities**

	Α	a
В		
b		



### **Feature Interaction**

- For loglinear/logistic regression models in statistics, it is standard to do a greedy stepwise search over the space of all possible interaction terms.
- This combinatorial space is exponential in size, but that's okay as most statistics models only have 4–8 features.
- In NLP, our models commonly use hundreds of thousands of features, so that's not okay.
- Commonly, interaction terms are added by hand based on linguistic intuitions.



## **Example: NER Interaction**

Previous-state and current-signature have interactions, e.g. P=PERS-C=Xx indicates C=PERS much more strongly than C=Xx and P=PERS independently.

This feature type allows the model to capture this interaction.

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