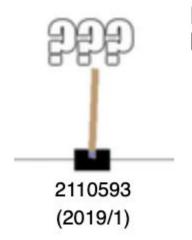
Reinforcement Learning

Introduction

Mycourseville & github

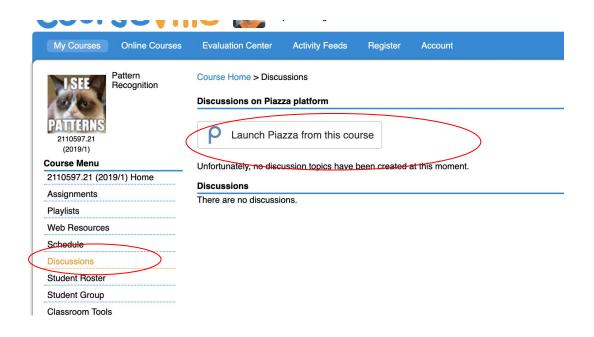
2110593 (2019/1)

https://github.com/ekapolc/RL_course_2019

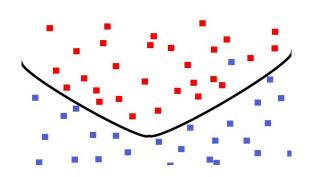


Reinforcement Learning

Piazza



Syllabus

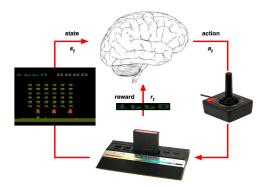


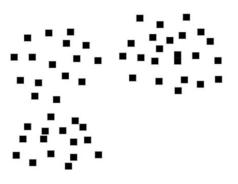
Supervised Learning





Reinforcement Learning

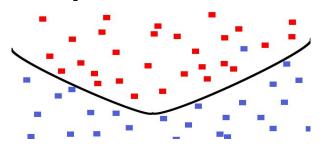




Unsupervised Learning



Supervised Learning

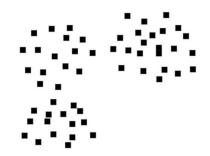




- Observe:
 - \circ $(x_1, y_1), (x_2, y_2), ...$
- Objective:
 - Input an unseen x_{new}
 - O What is y_{new}?

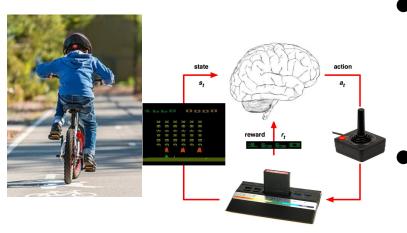
Unsupervised Learning

- Observe:
 - \circ $X_1, X_2, X_3, X_4, \dots$
- Objective:
 - \circ What is P(x)?
 - What is a good representation of x?
 - What can we learn from P(x)?





Reinforcement Learning (RL)



- Observe:
 - \circ The states (x_1, x_2, x_3, \dots)
 - \circ The reward (r_1, r_2, r_3, \dots)
- Can also take actions
 - o a₁, a₂, a₃, ...
- What are the best actions?
 - Such that we will receive highest accumulative rewards

What is RL?

- 1) A problem
- 2) A community working on 1)
- 3) Methods produced by 2) which can be applicable to other problems

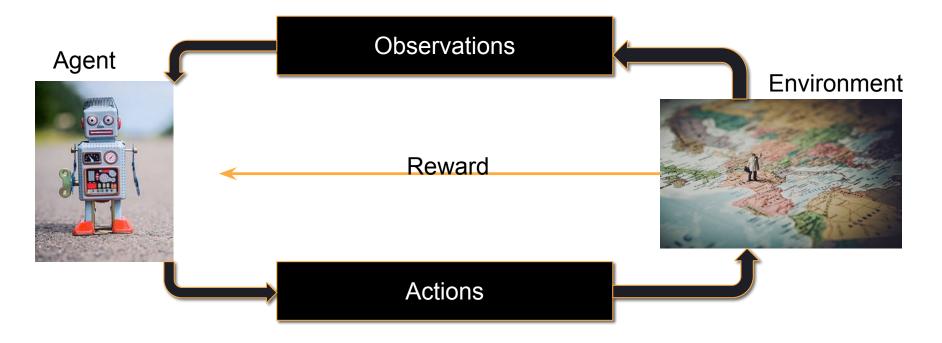


Benjamin Van Roy

Professor at Stanford University; Research Lead at DeepMind, Mountain View

Topic: Reinforcement Learning

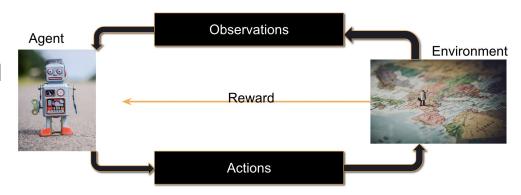
RL problem



Difference between RL and other modes of learning

- Sequential decisions
- You have a goal vs
 You have means to get there
- No concept of "training set" and "test set"
- "Passive" vs "Active" learning





RL(DeepMind)'s goal



Even a 4-1 victory for Lee Se-dol would represent a major achievement for DeepMind, a British company acquired by Google for a reported \$400 million in 2014. The unit's <u>ultimate mission is no less than to "solve intelligence,"</u> with potential uses ranging from healthcare to robotics, but attaining the long-sought computer science dream of a world-beating Go program would catapult DeepMind to the forefront of AI research.

https://www.theverge.com/2016/3/8/11178462/google-deepmind-go-challenge-ai-vs-lee-sedol



https://www.youtube.com/watch?v=wiOopO9jTZw



https://blog.openai.com/openai-five/

https://youtu.be/eHipy j29Xw



https://deepmind.com/blog/article/alphastar-mastering-real-time-strategy-game-starcraft-ii



https://ai.facebook.com/blog/pluribus-first-ai-to-beat-pros-in-6-player-poker/

https://www.youtube.com/watch?v=u90TbxK7VEA

RL and Artificial General Intelligence





Statement from a Slashdot post about the AlphaGo victory: "We know now that we don't need any big new breakthroughs to get to true Al"

That is completely, utterly, ridiculously wrong.

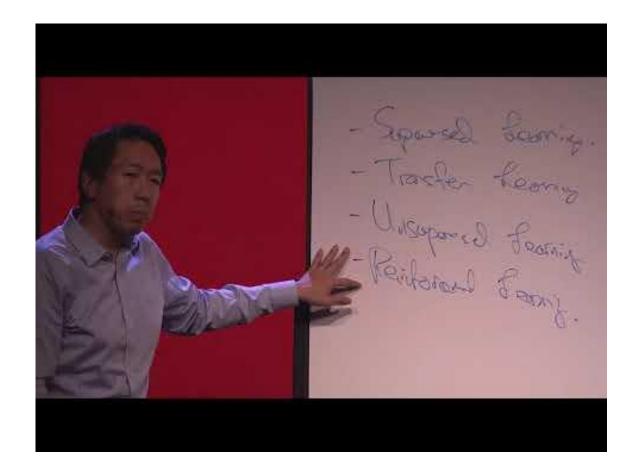
As I've said in previous statements: most of human and animal learning is unsupervised learning. If intelligence was a cake, unsupervised learning would be the cake, supervised learning would be the icing on the cake, and reinforcement learning would be the cherry on the cake. We know how to make the icing and the cherry, but we don't know how to make the cake.

We need to solve the unsupervised learning problem before we can even think of getting to true Al. And that's just an obstacle we know about. What about all the ones we don't know about?

#deeplearning #AI #AlphaGo

RL and \$\$\$

"The excitement and PR hype behind reinforcement learning is a bit disproportionate relative to the economic value it's creating today" - Andrew Ng



https://craft.co/deepmind/metrics

DeepMind Income Statement

FY, 2016

FY, 2017

Annual

GBP

	200 A	
Revenue	40.3m	54.4m
Revenue growth, %		35%
General and administrative expense	163.8m	333.9m
Operating expense total	163.8m	333.9m
Depreciation and amortization	863.5k	1.9m
EBIT	(123.5m)	(279.4m)
EBIT margin, %	(307%)	(513%)
Interest expense	2.0m	2.6m
Pre tax profit	(126.6m)	(281.9m)
Income tax expense	32.6m	(20.3m)
Net Income	(93.9m)	(302.2m)

RL use cases

Go, chess, starcraft, dota, poker

Finance (https://www.jpmorgan.com/global/LOXM)...

Robotics...but...



https://research.googleblog.com/2016/03/deep-learning-for-robots-learning-fro

https://towardsdatascience.com/applications-of-reinf@defment-learning-in-real-world-1a94955bcd12https://www.oreilly.com/ideas/practical-applications-of-reinforcement-learning-in-industry

RL use cases

Data center and resource management (https://people.csail.mit.edu/alizadeh/papers/deeprm-hotnets16.pdf System configuration https://ieeexplore.ieee.org/abstract/document/4556714/ Recommender (Bandits) https://people.cs.umass.edu/~pthomas/papers/Barto2017.pdf)

Ad bidding (https://arxiv.org/abs/1701.02490)

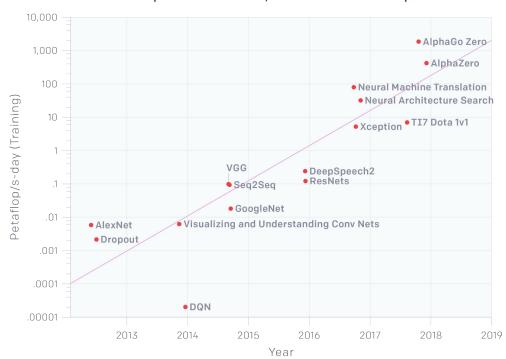
Chemistry (https://pubs.acs.org/doi/full/10.1021/acscentsci.7b00492)

Some other tasks that use algorithms from RL to help perform model training (autoML, REINFORCE)

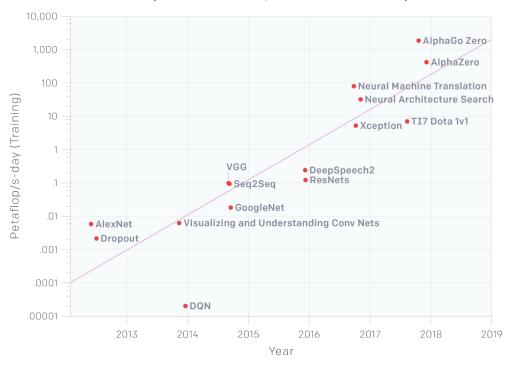




AlexNet to AlphaGo Zero: A 300,000x Increase in Compute

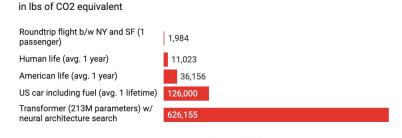


AlexNet to AlphaGo Zero: A 300,000x Increase in Compute



Common carbon footprint benchmarks

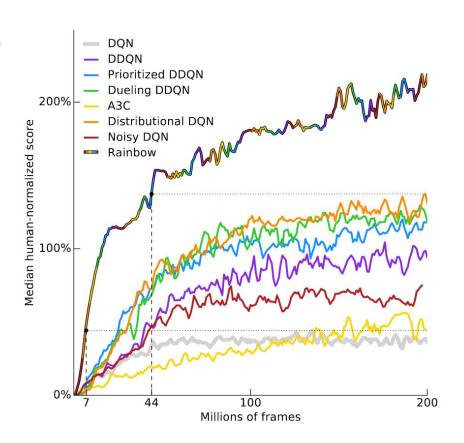
Chart: MIT Technology Review • Source: Strubell et al. • Created with Datawrapper



https://www.technologyreview.com/s/613630/training-a-sing le-ai-model-can-emit-as-much-carbon-as-five-cars-in-their-lifetimes/

Data inefficient

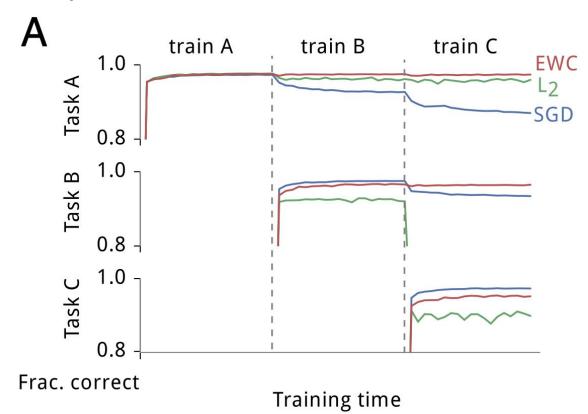
 Many use case can be better solved with supervised learning (efficiency and accuracy)



Rewards engineering is hard Sparse rewards



Catastrophic forgetting

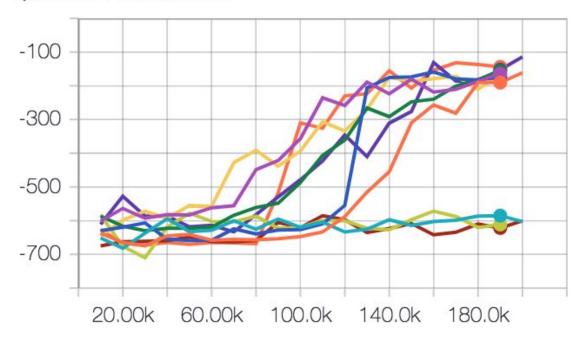


http://www.pnas.org/content/early/2017/03/13/1611835114.full.pdf?with-ds=yes

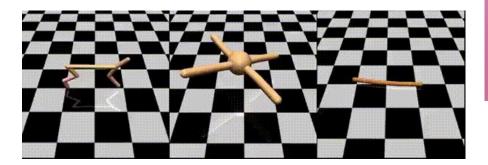
Randomness

Random initialization
Random exploration
Random environment

episode_reward/test

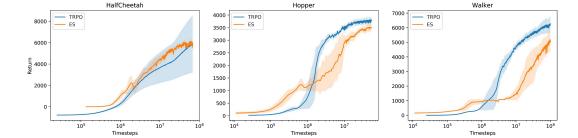


Sometimes evolution strategies might be better



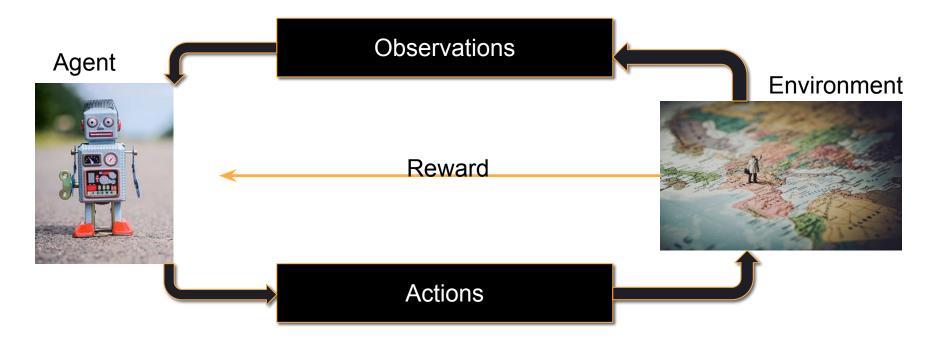
Evolution Strategies as a Scalable Alternative to Reinforcement Learning

We've <u>discovered</u> that **evolution strategies (ES)**, an optimization technique that's been known for decades, rivals the performance of standard **reinforcement learning (RL)** techniques on modern RL benchmarks (e.g. Atari/MuJoCo), while overcoming many of RL's inconveniences.



https://openai.com/blog/evolution-strategies/

RL problem



Imitation learning

Learn through experts actions

Becomes a supervised learning problem

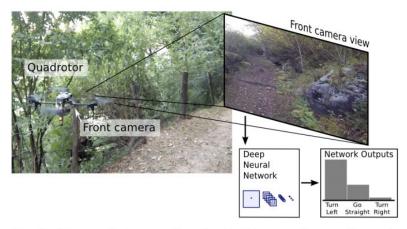


Fig. 1: Our quadrotor acquires the trail images from a forward-looking camera; a Deep Neural Network classifies the images to determine which action will keep the robot on the trail.

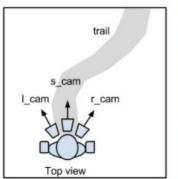








Fig. 4: *Left:* stylized top view of the acquisition setup; *Right:* our hiker during an acquisition, equipped with the three head-mounted cameras. http://rpg.ifi.uzh.ch/docs/RAL16 Giusti.pdf

Imitation learning

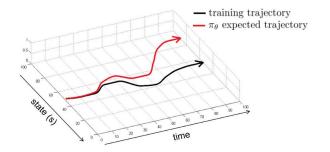
Learn through experts actions

Becomes a supervised learning problem

What if the agent goes into regions where we don't have expert's supervision?

Needs some kind of compensation of difference behavior

Can be used in conjunction with RL



Review of probabilities

Notation

Expectation (multivariate)

Correlation - correlation vs causation

Variance

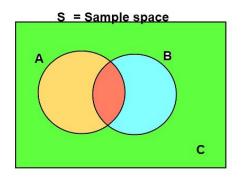
Sampling from a distribution (gaussian, uniform, softmax)

Estimation (MLE)

Conditional probability

P(A|B) probability of A given B has occurred

$$P(A \mid B) = \frac{P(A \cap B)}{P(B)}$$



Different notations P(A|B=b)

Independence

 Two events are independent (statistically independent or stochastically independent) if the occurrence of one does not affect the probability of occurrence of the other.

$$P(A \cap B) = P(A)P(B) \Leftrightarrow P(B) = P(B \mid A)$$

Bayes' Rule (Bayes's theorem or Bayes' law)

$$P(A \mid B) = \frac{P(B \mid A) P(A)}{P(B)}$$

Usefulness: We can find P(A|B) from P(B|A) and vice versa

Expected value

Expected value

$$E[x] = \int_{-\infty}^{\infty} x p(x) dx$$

$$E[g(x)] = \int_{-\infty}^{\infty} g(x) p(x) dx$$

• Variance (σ^2) (Standard Deviation = σ)

$$Var[x] = E[(x - E[x])^{2}] = \sigma^{2} = \int_{-\infty}^{\infty} (x - E[x])^{2} p(x) dx$$

$$E[(x-E[x])^2] = E[x^2] - (E[x])^2$$

Expected value and Variance properties

- E[a] = a; a is a constant.
- E[aX+b] = aE[X]+b
- $\bullet \ \mathsf{E}[X+Y] = \mathsf{E}[X] + \mathsf{E}[Y]$
- Var[a] = 0
- $Var[aX+b] = a^2Var[X]$

Conditional Expected Value

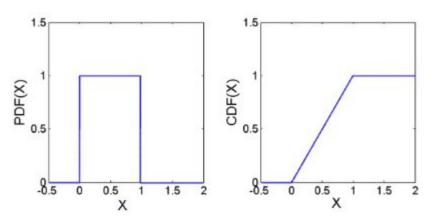
$$E[x \mid A] = \int_{-\infty}^{\infty} xp(x \mid A)dx$$
$$E[g(x) \mid A] = \int_{-\infty}^{\infty} g(x)p(x \mid A)dx$$

Cumulative Distribution Functions CDFs

Probability that the RV is less than a certain amount

$$F_X(x_0) = P(X \le x_0) = \int_{-\inf}^{x_0} p(x) dx$$
 • CDF is the integral of PDF. Differentiating CDF wrt x gives

the PDF



Useful for sampling

Joint distributions

- If we want to monitor how two events are jointly occurring, we consider the joint distribution p_{x y}(x,y)
- $p_{XY}(x,y) = p_X(x)p_Y(y)$ if x and y are independent

$$P(A) = \iint_A p_{XY}(x, y) dx dy$$

$$p_X(x) = \int_{-\infty}^{\infty} p_{XY}(x, y) dy$$

$$p_{Y}(y) = \int_{-\infty}^{\infty} p_{XY}(x, y) dx$$

Can we take expectation from a joint distribution? What about a conditional expectation?

Expectation of multivariate distributions

$$E[g(X_1, X_2)] = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} g(x_1, x_2) p_{X_1, X_2}(x_1, x_2) dx_1 dx_2$$

$$E[g(X_1)h(X_2)] = E[g(X_1)]E[h(X_2)]$$

If X_1 and X_2 independent

Sum of Random variables

- $\cdot Z = Y + X$
- What is the pdf of Z? Where Y and X continuous RVs

$$p_{X+Y}(z) = (p_X * p_Y)(z) = (p_Y * p_X)(z)$$

Central Limit Theorem (CLT)

• Suppose X₁,X₂,... is a sequence of iid (independent and identically distributed) RVs. As n approaches infinity the sum of the sequence converge in distribution to a Normal distribution.

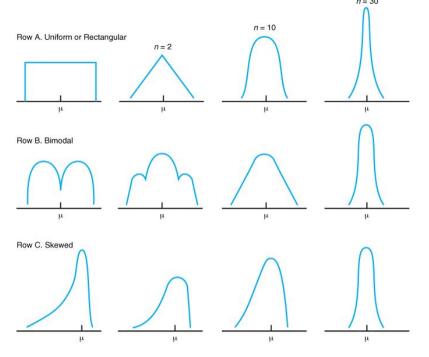
$$\sqrt{n}\left(\left(rac{1}{n}\sum_{i=1}^{n}X_{i}
ight)-\mu
ight)\overset{d}{
ightarrow}N\left(0,\sigma^{2}
ight)$$

 Other variants of CLT exists, without the independence or identically distributed assumption

CLT implications

A sum of RVs tends to become Normally distributed very

quickly



Gaussian distribution (normal distribution)

• X is normal (Gaussian): $X \sim N(\mu, \sigma^2)$

$$p(x) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-(x-\mu)^2/2\sigma^2}$$

$$E[x] = \mu$$

$$Var[x] = \sigma^2$$

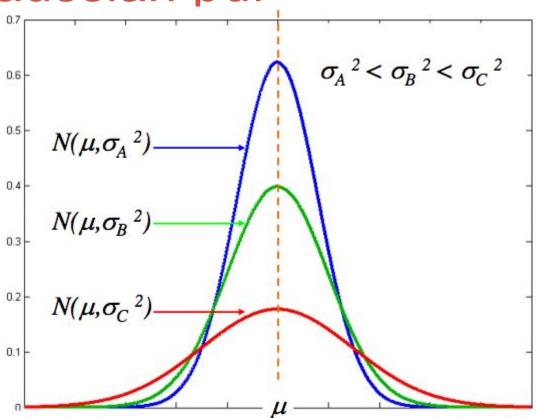
• X is Standard normal (Standard Gaussian): $X \sim N(0,1)$ when $\mu=0$, $\sigma^2=1$

$$p(x) = \frac{1}{\sqrt{2\pi}} e^{-(x-\mu)^2/2}$$

$$E[x] = 0$$

$$Var[x] = 1$$

Gaussian pdf



Linear transformation of Gaussian RV

- Normality is preserved by linear transformation. Calculation involving the normal variable is usually done in terms of standard normal.
- Let Y=aX+b, if $X\sim N(\mu,\sigma^2) \rightarrow Y\sim N(a\mu+b,a^2\sigma^2)$
- Let $Z=(X-\mu)/\sigma$, if $X\sim N(\mu,\sigma^2) \rightarrow Z\sim N(0,1)$: Standard Normal

Can you prove this?

Summation of 2 Gaussian RVs

- X mean m₁ variance σ₁²
- Y mean m_2 variance σ_2^2
- X and Y are independent

• X+Y is normally distributed with mean $m_1 + m_2$ variance $\sigma_1^2 + \sigma_2^2$

Covariance of multivariate distributions

$$-cov(X_1,X_2) = E[(X_1-m_1)(X_2-m_2)]$$

$$-cov(X_1,X_2) = E[(X_1)(X_2)] - m_1m_2$$

- Covariance with itself is just the Variance
- Correlation

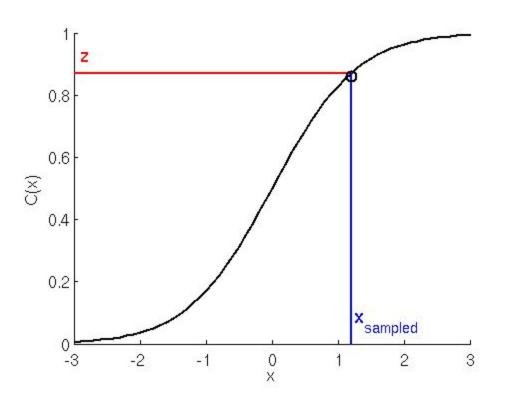
$$\rho = \frac{cov(X_1, X_2)}{\sqrt{V(X_1)V(X_2)}}$$

Covariance matrix

- Given a set of RVs, X₁ X₂ ... X_n
- The covariance matrix is a matrix which has the covariance of the i and j RV in position (i,j)

```
\Sigma = \begin{bmatrix} \mathrm{E}[(X_1 - \mu_1)(X_1 - \mu_1)] & \mathrm{E}[(X_1 - \mu_1)(X_2 - \mu_2)] & \cdots & \mathrm{E}[(X_1 - \mu_1)(X_n - \mu_n)] \\ \mathrm{E}[(X_2 - \mu_2)(X_1 - \mu_1)] & \mathrm{E}[(X_2 - \mu_2)(X_2 - \mu_2)] & \cdots & \mathrm{E}[(X_2 - \mu_2)(X_n - \mu_n)] \\ \vdots & \vdots & \ddots & \vdots \\ \mathrm{E}[(X_n - \mu_n)(X_1 - \mu_1)] & \mathrm{E}[(X_n - \mu_n)(X_2 - \mu_2)] & \cdots & \mathrm{E}[(X_n - \mu_n)(X_n - \mu_n)] \end{bmatrix}.
```

Sampling using the inverse of the CDF



Draw from a uniform random generator

Look at the inverse of the CDF for the new x

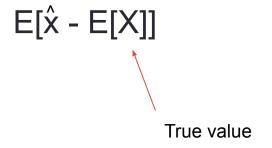
Estimation

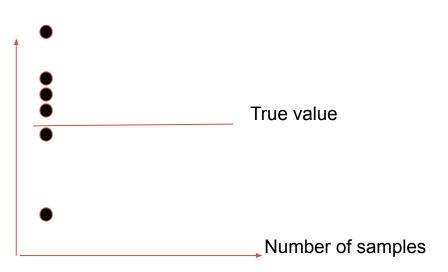
Bias and variance of estimators

Estimation

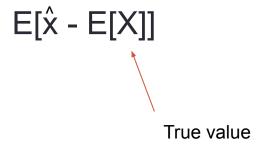
Given observations $x_1, x_2, x_3, ..., x_n$ Find the sample mean and sample variance

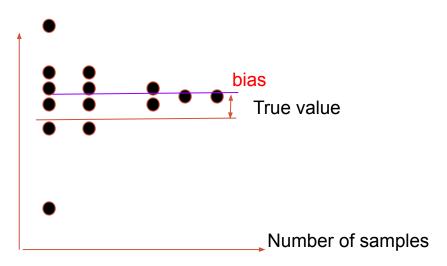
Estimator bias



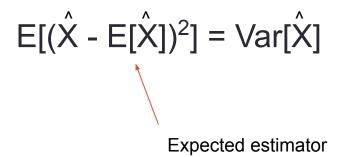


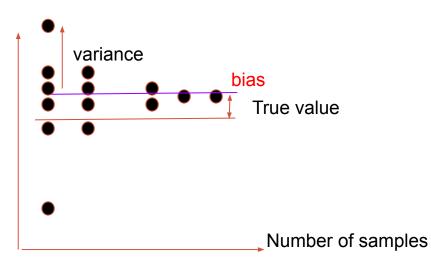
Estimator bias





Estimator variance





Summary

What is RL Probability review

Homework

Read chapter 1 of Sutton Answer questions 1.1-1.5