

# TP2 Report

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We had the goal to identify the 2 ciphertexts (of the 20 ones provided) that used the same key for OTP (One Time Pad) encryption.

Unfortunately, we can't say for sure that this work was completed successfully, since the only guess we have can't be confirmed. If the letter frequency in the plaintexts texts match the values we assumed ([english alphabet letter frequency](#)).

In this *One Time Pad*, instead of XOR of the bytes, the operation was oriented to the addition of alphabetic characters with rotation on overflow (mod 26).

```
'A' + 'B' = 'B' 'B' + 'C' = 'D' 'Z' + 'B' = 'A'
```

## Our Attempt

With 20 ciphertexts we wanted to find any direct relation between 2 texts, for this we first tried to subtract ciphertext1 (c1) and ciphertext2 (c2) (for every possible pair in the 20 texts).

```
c1: ciphertext 1
c2: ciphertext 2
t1: plaintext 1
t2: plaintext 2
k: reused key
k1: random key 1
k2: random key 2
```

Case A

With same key

$c1 = t1 + k$

$c2 = t2 + k$

$c2 - c1 = (t2 + k) - (t1 + k)$

$c2 - c1 = (t2 - t1)$

Case B

With random keys

$c1 = t1 + k1$

$c2 = t2 + k2$

$c2 - c1 = (t2 + k2) - (t1 + k1)$

$c2 - c1 = (t2 - t1) + (k2 - k1)$

As we can see with same keys the subtraction of the ciphertexts cancel the addition of the keys and the result is only the difference between texts 1 and 2.

On the other hand, the subtraction of ciphers with random keys results in the difference between texts 1 and 2, and the additional subtraction of random keys. This is a randomness feeder for the end result.

With this we can say that in the case B the  $c2 - c1$  will have an extra factor of randomness.

In the English alphabet we have different letter frequencies. Assuming that `t1` and `t2` have a similar letter frequency to the table we listed below, we can assume that the probability that the subtraction of 2 equal letters is higher for english texts than for random strings.

## Letter Frequency

E	T	A	O	I	N	S	R	H	D	L	U	C
12.02	9.10	8.12	7.68	7.31	6.95	6.28	6.02	5.92	4.32	3.98	2.88	2.71

M	F	Y	W	G	P	B	V	K	X	Q	J	Z
2.61	2.30	2.11	2.09	2.03	1.82	1.49	1.11	0.69	0.17	0.11	0.10	0.07

Since the Case B has a randomness feeder with the addition of the subtraction of different keys, the  $c_2 - c_1$  of Case A will have a higher chance of having the letter **A** than Case B.

Finally we tested this with python code to count letter **A** occurrences to verify this theory and sorted the results.

## Results

```
$ python main.py | sort
. . .
231 (15,20):
232 (4,13):
240 (7,20):
244 (12,20):
248 (3,14):
371 (6,14):
Highest: (6, 14, 371)
```

Analyzing the results we can verify that the subtraction of ciphertexts **6** and **14** had more **A** occurrences than any other ciphertexts combinations and thus making us believe that these were the two that were encrypted with the same key.

However, we took the assumption that the letter frequency in both plaintexts matched with the letter frequency in the english alphabet. In case this isn't true, then the result might not be correct and the reason the number 371 is so high is just coincidence.