

# **QUANTITATIVE APTITUDE**



INDE	X
	4 <b>b</b>

INDEX	
1. Number System	. (3 - 8)
(i) Sum of series	
(ii) Finding the sum "upto n terms"	
(iii) Finding A Number	
2. Problem of Ages	. (9 - 11)
3. Time and Work	(12 - 14)
4. Time and Distance	(15 - 21)
(i) Problem on Train	
(ii) Trains Meeting	
5. Clock	(22 - 24)
6. Percentage	(25 - 26)
7. Profit & Loss	(27 – 28)
8. Ratio and Proportion	(29 – 30)
9. Simple Interest & Compound Interest	(31 - 32)
(i) Simple Interest	
(ii) Compound Interest	
10. Average	(33 – 35)
(i) Average Speed	
11. Probability	(36 - 37)
(i) Coins	
(ii) Dice	
12. Permutation	(38 - 39)

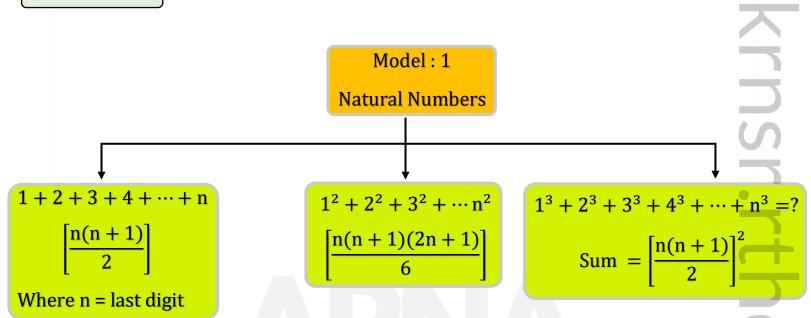


13. Combination	(40 - 41)
14. Square & Cube Roots	[42 - 43)
15. Logarithms	
Solutions(	[46 <b>-</b> 56]



# **NUMBER SYSTEM**

# **SUM OF SERIES**





 $1 + 3 + 5 + 7 \dots + 33$ 

 $(x^2)$ 

where  $\left[x = \frac{n+1}{2}\right]$ 

n = last digit

 $2 + 4 + 6 + 8 \dots + 50$ 

x(x+1)

where  $\left[x = \frac{n}{2}\right]$ 

n = last digit

51 + 53 + 55 ... + 65

Case: When series doesn't

Start from 1 or 2 and start

From in between



**Q.1** 
$$1+2+3+\cdots +30=?$$

**Sol.** 
$$\frac{n(n+1)}{2} = \frac{30 \times 31}{2}$$
$$= 15 \times 31$$
$$= 45$$

$$0.2 1^2 + 2^2 + 3^2 + \cdots + 12^2 = ?$$

Sol. 
$$\frac{n(n+1)(2n+1)}{6} = \frac{12 \times 13 \times 25}{6}$$
$$= 50 \times 13$$
$$= 650$$

$$0.3 1^3 + 2^3 + 3^3 + \cdots + 9^3 = ?$$

Sol. 
$$\left[\frac{n(n+1)}{2}\right]^2 = \left(\frac{9 \times 10}{2}\right)^2$$
$$= 45^2$$
$$= 2025$$

Q.4 
$$1+3+5+\cdots+49=?$$

**Sol.** 
$$x^2$$

We know, 
$$x = \frac{n+1}{2}$$

$$=\frac{49+1}{2}$$

$$= 25$$

$$\therefore x^2 = (25)^2$$

$$= 625$$

**Q.5** 
$$2+4+6+\cdots+5+58=?$$

**Sol.** 
$$x(x + 1)$$

We Know, 
$$x = \frac{n}{2}$$

$$=\frac{58}{2}$$

$$= 29$$

$$x(x+1) = 29(29+1)$$

$$= 29 \times 30$$

# <rnsr.rthd@gmail.com</pre>

(rnsr.rthc

$$Q.6 51 + 53 + 55.... + 99 = ?$$

**Sol.** 
$$(1+3+5+\cdots 99)-(1+3+5\cdots +49)$$

For 
$$1 + 3 + 5 + \dots 99$$

by using formula: x<sup>2</sup>

Trick: 
$$x = \frac{n+1}{2}$$
  
 $= \frac{99+1}{2}$   
 $x = 50$   
 $x^2 = (50)^2$   
 $= 2500$ 

For 
$$1 + 3 + 5 \dots + 49$$

Solving: 
$$(1+3+5+\cdots 99) - (1+3+5\cdots +49)$$

$$= 2500 - 625$$

$$= 1875$$

Trick: x<sup>2</sup>

$$x = \frac{x+1}{2}$$
$$= \frac{49+1}{2}$$
$$= 25$$

$$x^2 = (25)^2$$

This method can be used when series starts from random number in between. That is series doesn't starts from 1, 2 etc.

Q.7 
$$10^2 + 11^2 + 12^2 + \cdots + 20^2 = ?$$



# FINDING THE SUM "UPTO N TERMS"

**Formula**: 
$$S_n = \frac{n}{2} [2a + (n-1)d]$$

where  $a = 1^{st}$  Digit, d = difference,  $n = n^{th}$  term

# Q.8 Find the sum

$$1 + 3 + 5 + 7 + 9 \cdots$$
 upto 15 terms

**Sol.** 
$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$S_{15} = \frac{15}{2}[2(1) + (15 - 1)2]$$

$$=\frac{15}{2}[2+28]$$

$$=\frac{15}{2}\times30$$

= 225 {d = difference, so difference between any 2 digits as per question is 2}

In this, we don't know what exactly us 15th term, so we used formula of Arithmetic Progression

# **Question to Practice**

Q.9 Find the sum of first 19 terms of the sequence 2, 7, 12, 17, ...?

# (rnsr.rthc

# FINDING A NUMBER

# Q.10 What is two third of half of 369?

**Sol.** 
$$\frac{2}{3} \times \frac{1}{2} \times 369 = ?$$
 = 123

# Q.11 If one-third of one-fourth of a number is 15, then three-tenth of the number is?

Sol. 
$$\frac{1}{3} \times \frac{1}{4} \times x = 15$$
$$x = 15 \times 4 \times 3$$
$$x = 180$$

Now, three-tenth of this number

$$= \frac{3}{10} x$$

$$= \frac{3}{10} \times 180$$

$$= 54$$

# Q.12 If the sum of two numbers, one of which is $\frac{2}{5}$ times the other is so, then the numbers are?

**Sol.** Let's take first no. 
$$= x$$

Then according to question, second no. =  $\frac{2}{5}x$ 

$$x + \frac{2}{5}x = 50$$

$$\frac{5x + 2x}{5} = 50$$

$$7x = 250$$

$$x = \frac{250}{7}$$

$$\therefore$$
 first no. = x

$$=\frac{250}{7}$$

Second no. = 
$$\frac{2}{5}x$$

$$=\frac{2}{5}\times\frac{250}{7}$$

$$=\frac{100}{7}$$



Q.13 If  $\frac{1}{2}$  is added to a number & the sum is multiple by 3, the result is 21 then the number is?

**Sol.** Let the no. be x

$$\left(\frac{1}{2} + x\right) \times 3 = 21$$

$$\frac{3}{2} + 3x = 21$$

$$3x = 21 - \frac{3}{2}$$

$$3x = \frac{42 - 3}{2}$$

$$3x = \frac{39}{2} \Rightarrow \boxed{x = \frac{13}{2}}$$

**Question to Practice** 

Q.14 If  $4/5^{th}$  of a number exceeds its  $3/4^{th}$  by 8, then the number is

Q.15 If 3/4 of a number is 7 more then 1/6 of the number, then 5/2 of the number is?

# \_ APNA COLLEGE

# **PROBLEMS ON AGES**

Q.16 The present ages of A and B are in the ratio 4 : 5 and after 5 years they will be in the ratio 5 : 6. The present age A is?

**Sol.** Let age be 'x'

Present after Future 
$$5 \text{ years}$$
  $5:6$ 

4x : 5x

After 5 years  $\Rightarrow 4x + 5:5x + 5 = 5:6$ 

$$\frac{4x+5}{5x+5} = \frac{5}{6} \qquad \qquad \left\{a: b = \frac{a}{b}\right\}$$

By cross Multiplication 24x + 30 = 25x + 25

$$x = 5$$

∴ Present Age of 
$$A = 4x$$
  
=  $4 \times 5$   
= 20 years

Present Age of B = 5x

$$= 5 \times 5$$
$$= 25 \text{ years}$$

Q.17 The ratio of present ages of two brothers is 1 : 2 and 5 years back, the ratio was 1 : 3 what will be the ratio of their ages after 5 years?

Present

1:3

$$x - 5$$
:  $2x - 5 = 1$ : 3

$$\frac{x-5}{2x-5} = \frac{1}{3}$$

$$3x - 15 = 2x - 5$$

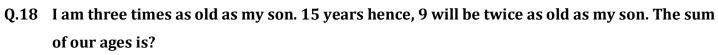
$$x = 10$$

After 5 years, ratio of their ages

$$\Rightarrow$$
 x + 5: 2x + 5

$$\therefore x = 10$$

$$10 + 5:2(10) + 5$$



$$3x$$
  $x$ 

After 15 years

$$3x + 15$$
  $x + 15$ 

$$3x + 15 = 2(x + 15)$$

$$3x + 15 = 2x + 30$$

$$x = 15$$

Son age (x) = 15 years

Father age 
$$(3x) = 3 \times 15$$

$$= 45 \text{ years}$$

$$\therefore$$
 Sum of their ages =  $45 + 15$ 

$$= 60$$
 years

# Q.19 10 years ago daughter's age was two-fifth of her mother's age that time. while 10 years hence her age will be three-fifth of her mother's age then Find the difference in the ages of the two

**Sol.** Let daughter's age 
$$= x$$

$$(x-10) = \frac{2}{5}(y-10) \rightarrow (1)$$

10 year hence

$$(x + 10) = \frac{3}{5}(y + 10) \rightarrow (2)$$

An solving equ. (1)

$$5x - 50 = 2y - 20$$

$$5x - 2y = 30 \rightarrow (3)$$

On solving equ. (2)

$$5x + 50 = 3y + 30$$

$$5x - 3y = 20 \rightarrow (4)$$

Solving equ. (3) & (4)

$$5x - 2y = 30$$

$$-5x + 3y = 20$$

$$y = 50$$

$$5x - 2y = 30$$

$$5x - 100 = 30$$

$$x = 26$$

Difference of ages = Mother age - daughter age = 50 - 26= 24

- Q.20 4 years ago, the ratio of the ages of A and B was 2: 3 and after 4 years, it will become 5: 7. Find their present ages
- Q.21 The present age of a father is 3 year more than three times the age of his son. 3 years hence, father's age will be lo year more than twice the age of son. The father's present age is?

# **TIME AND WORK**

# **Based On Chain Rule**

Formula 1:

$$P = No. of person$$

$$\frac{P_1 H_1 D_1}{P_2 H_2 D_2} = \frac{W_1}{W_2}$$

H = No. of hours

$$\frac{\mathbf{I}_1 \mathbf{I}_1 \mathbf{D}_1}{\mathbf{P}_2 \mathbf{H}_2 \mathbf{D}_2} = \frac{\mathbf{w}_1}{\mathbf{w}_2}$$

D = No. of days

Formula 2:

$$w = Work$$

$$P_1H_1D_1 = P_2H_2D_2$$

Q.22 15 min can type 3240 pages in 6 days working 2 hours per day. How many men would be required to type 5400 pages working 4 hours per day for 3 days?

**Sol.** 
$$P_1 = 15$$
,  $W_1 = 3240$ ,  $H_1 = 2$ ,  $D_1 = 6$ 

$$P_2 = ?$$
,  $w_2 = 5400$ ,  $H_2 = 4$ ,  $D_2 = 3$ 

$$\frac{P_1 H_1 D_1}{P_2 H_2 D_2} = \frac{w_1}{w_2}$$

$$\frac{15\times2\times6}{\times\times4\times3} = \frac{3240}{5400}$$

$$\frac{15}{x} = \frac{81}{135}$$

$$x = \frac{135 \times 15}{81}$$

$$x = 25$$

$$\therefore$$
 No. of men required = 25

Q.23 39 persons can repair a road in 12 days working 5 hours a day. In how many days will 30 persons working 6 hours a day Complete the work?

**Sol.** 
$$P_1 = 39$$

$$P_1 = 39$$
  $D_1 = 12$   $H_1 = 5$  hours

$$P_2 = 30$$
  $D_2 = ?$   $H_2 = 6$  hours

$$H_2 = 6 \text{ hours}$$

$$P_1H_1D_1 = P_2H_2D_2$$

$$39 \times 5 \times 12 = 30 \times x \times 6$$

$$x = 13$$



- Q.24 Ajay & Sunil together can complete a piece of work in 10 days, Sunil & Sanjay in 15 days & Sanjay and Ajay. They worked together for 6 days, and then Ajay leaves. Sunil and Ajay worked for 4 more days, and Sunil leaves How long will Sanjay take to complete the work?
- **Sol.** Work done in 1 day:

Ajay + sunil = 
$$\frac{1}{10}$$

Sunil + Sanjay = 
$$\frac{1}{15}$$

Sanjay + Ajay = 
$$\frac{1}{20}$$

$$2 \text{ Sunil} + 2 \text{ Ajay} + 2 \text{ Sanjay} = \frac{1}{10} + \frac{1}{15} + \frac{1}{20}$$

Sunil + Ajay + Sanjay = 
$$\frac{1}{2} \left[ \frac{13}{60} \right]$$

Sunil + Ajay + Sanjay = 
$$\frac{13}{120}$$
 ... (1)

Work done in 6 days = 
$$\frac{13}{20} \times 6$$

$$=\frac{13}{20}$$

Work done in 4 days = 
$$\frac{1}{15} \times 4$$

By Sunil & Ajay = 
$$\frac{4}{15}$$

: Sunil left after 4 days, Ajay left after 6 days

Remaining work = 
$$1 - \begin{bmatrix} Work done \\ in 6 days \end{bmatrix} + \begin{bmatrix} Work done \\ in 4 days \end{bmatrix}$$

$$=1-\left[\frac{13}{20}+\frac{4}{15}\right]$$

$$=1-\frac{55}{60}$$

Remaining work =  $\frac{1}{2}$  [to be completed by Sanjay alone]

No. of days required, from equ. (1)

Sanjay + 
$$\underbrace{\text{Ajay + Sunil}}_{120} = \frac{13}{120}$$

$$Sanjay + \boxed{\frac{1}{10}} = \frac{13}{20}$$

(given in question)

That Ajay & Sunil take 10 days

Sanjay = 
$$\frac{13}{120} - \frac{1}{10}$$

Sanjay 
$$=\frac{1}{120}$$

⇒ Sanjay can complete yob in 120 days.

We know, Remaining work =  $\frac{1}{12}$ 

∴ Days req. to complete 
$$\frac{1}{12}$$
 work by Sanjay =  $120 \times \frac{1}{12}$ 

Sanjay will take 10 days to complete work

- Q.25 'A' can complete 2/3 of a work in 4 days & 'B' can complete 3/5 of the work in 6 days. In how many days can both A and B together complete the work?
- Q.26 If 72 men can build a wall of 280 m length in 21 days, how many men could take 18 days to build a similar type of wall of length 100 m?



# **TIME AND DISTANCE**

- Q.27 Two friends started for a place one by motorcycle and other by car. The speed of motorcycle is 30 km/hr. and that of car is 24 km/hr. The first one takes 6hr. 12 min to reach the destination. Find the time of reaching of second one.
  - (A) 8:00 hr.
- (B) 7.25 hr.
- (C) 7.50 hr.
- (D) 7.75 hr.

- **Sol.** Motorcycle: 30 km/hr.
- 6 hr./2min.
- $\Rightarrow$  1 hr. = 30 km
- $\therefore$  Distance for 6 hrs. = 6 × 30 km

$$= 180 \text{ km}$$

1 hr. = 60 min

60 mins = 30 km

$$1 \min = \frac{3\emptyset}{6\emptyset} = \frac{1}{2} \text{ km}$$

$$\therefore$$
 Distance for 12 min =  $\frac{1}{2} \times 12$ 

$$= 6 \text{ km}$$

Distance covered in 6 hrs. 12 min = 180 + 6

$$= 186 \text{ km}$$

Speed = 24 km/hr.

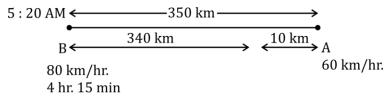
Time = DIstance/Speed

$$=\frac{186}{24}$$

$$\Rightarrow$$
 Time = 7.75 hr.

- Q.28 Kamal left for the City A from City B at 5:20 AM He travelled at a speed of 80Km/ hr. for 4 hrs. 1 min. After that, the speed was reduced to 60 km/hr. If the distance between two cities is 350 km, at what time did hamal reach City A
  - (A) 9: 20 AM
- (B) 9: 25 AM
- (C) 9:35 AM
- (D) 9:45 AM

Sol.



$$1 \text{ hr.} = 80 \text{ km}$$

Distance = Speed  $\times$  Time

 $= 80 \times 4 \text{ hr.}$ 

= 320 km

1 hr. = 80 km

60 min = 80 km

$$1 \min = \frac{8\emptyset}{6\emptyset}$$

$$15 \text{ mins} = \frac{8^4}{g_{2_1}} \times 15^5$$

= 20 km

So Total distance travelled in 4 hr. 15 min = 320 + 20

= 340 km

Given, Total distance between A to B = 350 km

& distance travelled by B = 340 km From 4 hrs. 15 min

So remining distance = 350 - 340

= 10 km

Given speed = 60 km/hr.

$$\Rightarrow$$
 1 hr. = 60 km

$$\Rightarrow$$
 60 min = 60 km

$$\Rightarrow 1 \min = 1 \text{ km}$$

$$\therefore 10 \text{ km} = 10 \text{ min}$$

So 10 mins more to reach city A to travel 350 km

So total time = 4 hrs. 15 mins

+ 10 mins

4 hrs. 25 mins

Journey started at 5: 20 AM

$$+ 4:25$$

9:45 AM



- Q.29 A man goes to his office by Scorer at a speed of 30 Km/hr. & reaches 6 min earlier. The goes at a speed of 24 km/hr., he reaches 5 minutes late. The distance of his office is
  - (A) 20 Km

(B) 21 km

(C) 22 km

(D) 24 km

Sol.

$$T_1 \sim T_2 = 11 \text{ min}$$

$$\frac{D}{S} \sim \frac{D}{S} = 11 \text{min}$$

$$\frac{D}{30 \text{ km/hr.}} - \frac{D}{24 \text{ km/hr.}} = 11 \text{ min}$$

$$\frac{D}{30 \text{ km/kr.}} - \frac{D}{24 \text{ km/kr.}} = \frac{11}{60} \text{kr.}$$

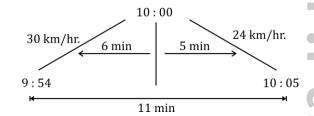
$$\frac{4D - 5D}{12\emptyset} = \frac{11}{6\emptyset}$$

$$D = \frac{11 \times 12}{6} \text{km}$$

$$D = 22 \text{ km}$$

Just to Understand

Let's consider man goes to Office at 10:00 AM



# **Question to Practice**

Q.30 As car travelling at a speed of 40 km / hr. can complete a journey in 9 hr. How long will it take to travel the same distance at  $60 \, \text{km}$  / hr.

# APNA

# **PROBLEMS ON TRAIN**

- A 100 m long train crossed a (rock/Pole/standing man) then, the distance travelled = Length of Train by train
- A 100 m long trains crossed a (Platform / Tunnel) of length 200 m, then: The distance travelled by Train = Length of Train + Platform Length
- Subtract Train 1 overtakes Train 2
  Speed Train 1 & Train 2 running in Parallel direction
- (+)
  Add
  Speed

  Train 1 crosses Train 2
  Train 1 Train 2 proceeds towards each other
- Q.31 A train 300 m long is running at a speed of as it will cross a bridge of 200 meters in?
- **Sol.** Distance = 300 + 200, Speed = 25 m/sec. = 500 m

$$T = \frac{D}{S}$$

$$T = \frac{500 \text{ m}}{25 \text{ m/sec.}}$$

$$T = 20 \text{ sec.}$$

Q.32 On train travelling at a speed of 30 m / sec crosses a platform, 600 m long in 30 seconds. The length (in meter) of train is?

**Sol.** 
$$S = 30 \text{ m/s}$$

$$P_L = 600 \text{ m}$$

$$T = 30 \text{ sec.}$$

$$D = S \times T$$

$$\begin{cases} \text{If train crosses platform, D} = \frac{\text{Platform}}{\text{Length}} + \frac{\text{Platform}}{\text{Train}} \\ = 600 + x \end{cases}$$

$$600 + x = 30 \text{ m/sec.} \times 30 \text{ sec.}$$

$$600 + x = 900 \text{ m}$$

$$x = 300 \text{ m}$$

# **Question to Practice**

**Q.33** A train takes 18 seconds to pass through a platform 162 m long and 1 s seconds to pass through another platform 120 m long. The length of the train (in m) is:

# APNA COLLEGE

# TRAINS MEETING

# Type - I:

distance between stations, length of both Train will be given in the question

Train speed,

To find at what distance & time both Trains meet

# Formula:

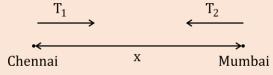
$$Distance = S_1 \left[ \frac{d + S_2 T}{S_1 + S_2} \right] km$$

Time = 
$$\left[\frac{d + S_2 T}{S_1 + S_2}\right]$$
 hours

where,  $S_1 = \text{speed of } 1^{\text{st}} \text{ Train}$ 

$$S_2$$
 = speed of  $2^{nd}$  Train

# Type - II:



To find distance between 2 stations

### Formula:

$$d\left[\frac{S_1 + S_2}{S_1 \sim S_2}\right] km$$

# Type - III:

Chennai 
$$\bullet$$
  $T_1$ 
Chennai  $\bullet$   $T_2$ 

(Trains starting from same station but there will be a delay)

To find: Distance at which both trains meet

### Formula:

$$\left[\frac{S_1 \times S_2 \times T}{S_1 \sim S_2}\right] \text{km}$$

To find: Time at which both Trains meet

Time = 
$$\left[\frac{S_1 T}{S_1 \sim S_2}\right]$$
 hours



- Q.34 Two trains start at the same time from A & B and proceeds towards B & A at 36 kmph & 42 kmph respectively. When they meet, it is found that one train has maned 48 km more than the other. What is the distance between A & B?
- Sol. Type II

$$d\left[\frac{s_1 + s_2}{s_1 \sim s_2}\right] km$$

$$=48\left[\frac{36+42}{36\sim42}\right]$$

$$=48\times\frac{78}{6}$$

$$= 48 \times 13$$

= 624 km

- Q.35 The distance between two stations A & B is 300 km. A train leaves Station 'A' at the speed of 30 km / hr. At the same time another train departs from Station B at speed of 45 km / hr. What will be the distance of the points Where both trains meet from point A?
- Q.36 A train leaves the station at 5 am at 60 km / hr. Another train leave the same station at 6:30 am at 75 km / hr. & travels in the direction of the first train. At What time and at what distance from the station will they meet?
- Sol. Type III

$$d = \left[\frac{S_1 \times S_2 \times T}{S_1 \sim S_2}\right] km$$

$$=\frac{60\times75\times\frac{3}{2}}{15}$$

$$= 450 \text{ km}$$

$$t = \left[\frac{S_1 T}{S_1 \sim S_2}\right] hours$$

$$= \left[ \frac{60 \times \frac{3}{2}}{15} \right] \text{ hours}$$

$$\left\{
\begin{array}{c}
T = 5 \text{ AM} \\
= 6:30 \text{ AM} \\
= 1\frac{1}{2} \\
= \frac{3}{2}
\end{array}
\right\}$$



 $\because 1^{st}$  Train starts at 5 am &  $2^{nd}$  Train starts at 6:30 am

So adding 6 hrs to 6:30

 $\Rightarrow$  Both Trains meet at = 6:30

+ 6 12:30

12:30 PM



# **CLOCK**

# To Find Angle between Hour & Minute Hand

# Formula:

$$\theta = \left| 30H - \frac{11}{2}M \right|$$

H = Hour

M = Minutes

By using formula, If the angle between hour hand & minute hand is greater than 180°, then use:

360° – angle obtained by formula method

# Q.37 What is the angle between minute hand and hour hand at 1: 20?

**Sol.** Using Formula:

$$\theta = \left| 304 - \frac{11}{2} (M) \right|$$

$$\theta = \left| 30(1) - \frac{11}{2}(20) \right|$$

$$\theta = |-80|$$

$$\theta = 80^{\circ}$$

# Q.38 Find at what time between 1:00 and 2:00, the hands of clock will be together

**Sol.** 
$$\theta = 30H - \frac{11}{2}M$$

$$0 = 30 \times 1 - \frac{11}{2} M$$

$$-30 = -\frac{11}{2}M$$

$$30 = \frac{11}{2}M$$

$$M = \frac{30 \times 2}{11}$$

$$=\frac{60}{11}$$

$$=5\frac{5}{11}$$

$$\Rightarrow 1:05:\frac{5}{11}\sec$$

$$\begin{cases} \theta = 0^{\circ} \\ \text{as hands of clock} \\ \text{will be together} \end{cases}$$

For H consider lower value between which we have to find, eg – between 1 and 2 lower value is 1.



#### Find at what time between 3:00 & 4:00, the hands of clock will be at a right angle 0.39

**Sol.** 
$$\theta = 30H - \frac{11}{2}M$$

If 
$$\theta = +90^{\circ}$$

$$90 = 30 \times 3 - \frac{11}{2} (M)$$
  $\{\theta = \pm 90^{\circ}\}$ 

$$\{\theta = \pm 90^\circ\}$$

$$90 - 90 = -\frac{11}{2}M$$

$$0 = -\frac{11}{2}M \Rightarrow M = 0$$

If 
$$\theta = -90^{\circ}$$

$$-90 = 30 \times 3 - \frac{11}{2}M$$

$$-90 - 90 = -\frac{11}{2}M$$

$$\neq 180 = \neq \frac{11}{2}M$$

$$M = \frac{180 \times 2}{11}$$

$$=\frac{360}{11}$$

$$= 32 \frac{8}{11} \sec$$

# At what time between 4: 00 & 5: 00, the hands of Clock will be in opposite direction?

**Sol**. 
$$\theta = 30 \text{ H} - \frac{11}{2} \text{M}$$

$$\theta = \pm 180^{\circ}$$
 (Because opposite direction)

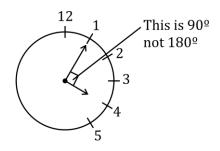
If 
$$\theta = +180^{\circ}$$

$$180 = 30 \times 4 - \frac{11}{2}M$$

$$180 = 120 - \frac{11}{2}M$$

$$60 = -\frac{11}{2}M$$

$$M = \frac{60 \times 2}{11}$$



$$\begin{cases} \text{therefore we} \\ \text{cannot consider} \\ \theta = +180^{\circ} \end{cases}$$

$$M = \frac{120}{11}$$

If we observe 4:  $10:\frac{10}{11}$  sec.

$$=10\frac{10}{11}$$

$$\Rightarrow$$
 4:10: $\frac{10}{11}$  sec.

— not Possible as it won't form 180º

If 
$$\theta = -180^{\circ}$$

$$-180 = 30 \times 4 - \frac{11}{2} \times M$$

$$-180 - 120 = -\frac{11}{2}M$$

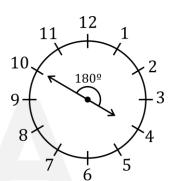
$$-300 = -\frac{11}{2}M$$

$$M = \frac{300 \times 2}{11}$$

$$=\frac{600}{11}$$

$$=54\frac{6}{11}$$

At 4: 54:  $\frac{6}{11}$  sec. the hands of clock will be in opposite direction.



- Q.41 What is the angle between minute hand and hour hand at 10:10
- Q.42 At what time between 3:00 & 4:00, will the hands of a clock be together?
- Q.43 Find at what time between 5:30 & 6:00, the hands of clock will be at right angle.

# PERCENTAGE

- Q.44 If 50% of P = 25% of Q, then P = x% of Q Find x.
  - (A) 0.5

- (B) 20
- (C) 50
- (D) 30

{Total students Present = 1000 Boys + 800 Girls = 1800}

Sol.  $50_2\%$  of P =  $25_1\%$  of Q

$$2P = Q$$

To Find: P = x% of Q

$$\frac{Q}{2} = \frac{x}{100} \times Q$$

$$x = \frac{100}{2}$$

$$x = 50$$

- In an examination, there were 1000 boys & 800 girls. 60 % of the boys and 50 % of girls passed Find the percent of Candidates failed?
- Sol. **1000** Boys

800 Girls

- 60 % Passed
- 50 % Passed
- 40 % Failed
- 50 % Failed
- $\Rightarrow \frac{40}{100} \times 1000$  $=\frac{50}{100}\times800$
- = 400 Boys Failed
  - = 400 Girls Failed
- $\Rightarrow$  400 (Boys) + 400(girls) = 800 failed
- Total students who failed % of candidates =  $\frac{1}{\text{Total students paresent in exam}}$

$$=\frac{800}{1800}\times100$$

- Rath spends 40 % of her salary on food, 20 % on house rent and, 10 % on entertainment & 0.46 10 % on conveyance. If her savings at the end of a month are Rs 1500, then her salary per month (in Rs) is:
- Sol.

Savings: 100 % - expenditure

- = 100 % [40 % + 20 % + 10 % + 10 %]
- = 100% 80%
- = 20 %
- 20% = 1500



$$x = \frac{1500 \times 10\emptyset}{2\emptyset}$$

$$x = 7500$$

**Question to Practice** 

Q.47 If 20 % of (P + Q) = 50 % of (P: Q)

(A) 7:8

(B) 7:3

(C) 7:5

(D) 5:7

Q.48 For an examination, it in required its get 36 % of maximum marks to pass. A student got 113 marks for the examination are?

Q.49 30 % of 2800 =?

# **PROFIT & LOSS**

# Formula:

$$\% \text{ gain} = \frac{\text{SP} - \text{CP}}{\text{CP}} \times 100$$

$$\{SP = Selling Price \}$$
  
 $\{CP = cost Rice \}$ 

$$CP = cost Rice$$

$$\% loss = \frac{CP - SP}{CP} \times 100$$

$$CP = \frac{100}{100 - loss \%} \times SP$$

$$CP = \frac{100}{100 + gain \%} \times SP$$

$$SP = \frac{100 + gain \%}{100} \times CP$$

$$SP = \frac{100 - loss \%}{100} \times CP$$

% change = 
$$a + b + \frac{ab}{100}$$

a = 1st Selling Price

b = 2<sup>nd</sup> Selling Price

#### By selling a cycle for Rs 4860, a student loses 19 % His cost Price is? 0.50

Sol. 
$$CP = \frac{100}{100 - Loss \%} \times SP$$

$$= \frac{100}{100 - 19} \times 4860$$

$$= \frac{100}{81} \times 4860$$

CP = 6000

# Q.51 By selling a cell phone for Rs 2400, a shopkeeper makes a profit of 25%. Then, his profit percentage if he had sold it for Rs 2040, is?

Sol. 
$$CP = \frac{100}{100 + 25} \times 2400$$
  
=  $\frac{100}{125} \times 2400$ 

$$125$$
  $CP = 1920$ 

If 
$$SP = 2040$$
, gain  $\% = ?$ 

# $\left\{ :: CP = \frac{100}{100 + gain \%} \times SP \right\}$

Q.52 Rehaan purchased a bike for Rs 54,000. He sold it a Loss of 8%. with that money he again purchased another bike & sold it at a profit of 10%. What is his overall loss/ Profit?

**Sol.** % change = 
$$a + b + \frac{ab}{100}$$

a = 1<sup>st</sup> selling Price

 $b = 2^{nd}$  Selling Price

(If sold at Loss then put negative sign for a or b) (If sold at Profit then put positive sign for a or b)

$$a = -8$$
 (Loss)

$$b = +10$$
 (Profit)

% change 
$$= -8 + 10 - \frac{80}{100}$$

$$= 2 - 0.8$$

$$= 1.2\%$$

Overall Profit =  $CP \times \%$  change

$$=54000 \times \frac{1.2}{100}$$

$$= Rs.648$$

- Q.53 A Calculator is bought for Rs.350 and sold at a gain of 15% what will be the selling Price of Calculator?
- Q.54 By selling an article for Rs.720, a man loss 10% At what price should he sell at, to gain

# 

# **RATIO AND PROPORTION**

Q. 55 If A: B = 
$$\frac{1}{2}$$
:  $\frac{1}{3}$ 

and B: 
$$C = \frac{1}{2} : \frac{1}{3}$$

then A: B: C = ?

**Sol.** A: B = 
$$\frac{1}{2}$$
:  $\frac{1}{3}$  B: C =  $\frac{1}{2}$ :  $\frac{1}{3}$ 

B: 
$$C = \frac{1}{2} : \frac{1}{3}$$

Taking L.C.M.

Taking L.C.M.

$$=\frac{3:2}{6}$$

$$=\frac{3:2}{6}$$

$$A: B = 3:2$$

$$B: C = 3:2$$

Put closest value 
$$\therefore$$
 B is 3  $\therefore$  Closest to C = 3  $A : B : C$ 

$$3 : 2 : 2$$

$$3 : 2$$
By m

A: B: C  $\begin{array}{c}
\text{Put val.} \\
\text{: } B = 2 \\
\text{: } \text{closest value to } C = 2 \\
\text{: } 3 : 2 \\
\text{: } 3 : 2 \\
\text{By multiplying both ratios}
\end{array}$ Put value which is closest ∴ B = 2 ∴ closest value to C = 2

Q.56 If 
$$a : b = 5 : 7$$

and 
$$c : d = 2a : 3b$$

then 
$$ac : bd = ?$$

**Sol.** 
$$a:b=5:7$$
,  $c:d=2a:3b$ 

$$\frac{a}{b} = \frac{5}{7} \qquad \qquad \frac{c}{d} = \frac{2a}{3b}$$

$$\frac{c}{d} = \frac{2a}{3b}$$

$$\frac{ac}{bd} = ?$$

Putting above values

$$\frac{ac}{bd} = \frac{5}{7} \times \frac{2}{3} \underbrace{a}_{b}$$

$$= \frac{5}{7} \times \frac{2}{3} \times \frac{5}{7}$$

$$= \frac{5}{7} \times \frac{2}{3} \times \frac{5}{7}$$

$$\frac{ac}{bd} = \frac{50}{147}$$

Divide Rs. 1250 among A, B, C, so that A gets 2/9 of B's share and C gets 3/4 of A' share Find the shares of A, B and C.

**Sol.** Given: 
$$A = \frac{2}{9}B$$
,  $C = \frac{3}{4}A$  (Substitute value of A)

$$\frac{A}{B} = \frac{2}{9}, \qquad C = \frac{3}{42} \times \frac{2}{93} B$$

$$\boxed{A: B = 2: 9} \qquad \frac{C}{B} = \frac{1}{6}$$

$$\frac{B}{C} = \frac{6}{1}$$

$$\boxed{B: C = 6: 1}$$

Put nearest value  $\begin{array}{c|c}
A : B : C \\
\hline
2 : 9 : 9 \\
\hline
6 : 6 : 1
\end{array}$ Put nearest value  $\overline{12 : 54 : 9}$ 

On Simplifying

A: B: 
$$C = 12^4 : 54^{18} : 9^3$$
  
= 4 : 18 : 3

# **Question to Practice**

Q.58 A mixture contains alcohol & water in the ratio 4: 3. If 5 litres of water is added to mixture the ratio becomes 4:5. find the quantity of alcohol in given mixture.

Q.59 If A: 
$$B = 2:3$$

$$A: B: C = ?$$

Q.60 If 
$$3A = 5B$$

and 
$$4B = 6C$$
 then

$$A: C = ?$$

# SIMPLE INTEREST & COMPOUND INTEREST

# Simple interest

$$S \cdot I = \frac{PRT}{100}$$

$$A = P \left[ 1 + \frac{RT}{100} \right]$$

P = PrincipalT = Time DurationR = Rate of InterestA = Total amount

# **Compound Interest**

$$CI = P\left\{ \left[ 1 + \frac{R}{100} \right]^n - 1 \right\}$$

where P = PrincipalMaturity Amount R = Rate of InterestTotal amount n = no of yearsAmount becomes A = Total amount

# **Compound Interest**

(i) for half-yearly

# Formula:

$$A = P \left[ 1 + \frac{R/2}{100} \right]^{2n}$$

(ii) for Quarterly

#### Formula:

$$A = P \left[ 1 + \frac{R/4}{100} \right]^{4n}$$

Q.61 Dinesh deposit an amount of Rs 65800 to obtain simple Interest at 14% per annum for 4 years. What total amount will Dines get at the end of 4 years?

Sol. 
$$A = P \left[ 1 + \frac{RT}{100} \right]$$
  
 $A = 65800 \left[ 1 + \frac{(14 \times 4)}{100} \right]$ 



r.rthd

$$=65800 \times \left[1 + \frac{56}{100}\right]$$

$$=\frac{658\emptyset\emptyset\times156}{1\emptyset\emptyset}$$

$$= 102648$$

Q.62 'A' invested Rs. 16000 at the rate of 10%p · a fer 1 year. If the Interest is compounded half yearly, then find total amount received by A the end of the year?

**Sol.** 
$$A = P \left[ 1 + \frac{P/2}{100} \right]^{2n}$$

$$A = 16000 \left[ 1 + \frac{5}{100} \right]^2$$

$$=16000\left(\frac{105}{100}\right)^2$$

$$=16\emptyset\emptyset\emptyset\times\frac{105}{1\emptyset\emptyset}\times\frac{105}{1\emptyset\emptyset}$$

$$= 17,640$$

Q.63 Simple Interest for sum of Rs.1500 is Rs 30 in 4 year & Rs. 60 in 8 years find the rate?

Sol.

$$SI = 60 \sim 30$$

$$= 30$$

$$S.I_1 - S.I_2 = 30$$

$$\frac{PRT}{100} - \frac{PRT}{100} = 30$$

$$1500 \left[ \frac{4x}{100} - \frac{8x}{100} \right] = 30$$

$$1500 \times \frac{4x}{100} = 30$$

$$2x = 1$$

$$x = 0.5\%$$

# **Question to Practice**

Q.64 What will be the Compound Interest for sum of Rs. 8000 after 3 years at rate of 5% p.a.

# APNA COLLEGE

# **AVERAGE**

Formula: Average = 
$$\frac{\text{Sum of Observation}}{\text{Total Number of Observation}}$$

- Q.65 The average age of A, B and C is 26 years If the average age of A and C is 29 years. What is the age of B in years?
- **Sol.** given:

$$\frac{A+B+C}{3} = 26,$$
  $\frac{A+C}{2} = 29$ 
 $A+B+C = 26 \times 3$   $A+C = 29 \times 2$ 
 $A+B+C = 78$   $A+C = 54$ 

Age of B = Total -(A+C)

= 78 - 54

= 20 years.

Q.66 The average of 7 numbers is 5. If the average of first six of these numbers is 4, the seventh number is?

Sol. 
$$\begin{cases} Average = \frac{\text{Total of 7' no.}}{\text{No. of terms}} \\ 5 = \frac{\text{Total of '7' no.}}{7} \end{cases}$$

Total of '7' no.

$$=7\times5$$

$$= 35$$

$$\begin{cases} \text{Average} &= \frac{\text{Total of 6 no.}}{\text{No. of Terms}} \\ 4 &= \frac{\text{Total of 6 no.}}{6} \end{cases}$$

Total of 6 no. =  $6 \times 4$ 

$$= 24$$

$$\therefore \text{ Seventh no.} = 35 - 24$$
$$= 11$$

Q.67 The average of marks obtained by 120 candidates was 35. If the average of marks of passed Candidates was 39 & that of failed candidates was 15, the number of candidates who passed the examination is?

**Sol.** Avg = 
$$\frac{\text{Total marks obtained}}{\text{No of Students}}$$

$$35 = \frac{\text{Total marks}}{120}$$

Total marks = 
$$120 \times 35$$
  
=  $4200$ 

Let's assume no of Passed candidates as 'x'

4200 = Marks obtained by passed candidate + Marks obtained by failed Candidate

$$4200 = (x \times 39) + [(120 - x) \times 15]$$

$$4200 = 39x + 1800 - 15x$$

$$2400 = 24x$$

$$x = 100$$

 $\therefore$  Passed candidates = 100

- Q.68 Of the three numbers, the first is twice the second and the second is thrice the third. If the average of the three numbers is 10. The number are?
- Q.69 The average expenditure of a man for the first 5 months is Rs 3600 and for the next 7 months it is Rs. 3900. If he saves Rs. 8700 during the year, his average income per month is?

# **AVERAGE SPEED**

**Note 1:** If the certain distance is covered at the speed of 'x' km/hr and the same distance is covered at 'y' Km/hr.then the average speed during entire journey is:

$$\left(\frac{2xy}{x+y}\right)$$
 km/hr.

Where x, y = speed

**Note 2:** If the person covers 'A' Km at a speed of 'x' Km/hr., 'B' Km at a speed of 'y' km/hr. and 'C' km at a speed of 'z' km/hr. Find out average speed of entire journey

$$\left(\frac{A+B+C}{\frac{A}{x}+\frac{B}{y}+\frac{C}{z}}\right) \text{km/hr.}$$

where, A, B, C = distance

x, y, z = speed

Q.70 An person covers 9 km at a speed of 3 km/hr., 25 km at a speed of 5 km/hr and 30 km at a speed of 10 km/hr. Find out the average speed of the entire journey.

Sol. 
$$\left(\frac{A+B+C}{\frac{A}{x}+\frac{B}{y}+\frac{C}{z}}\right)$$
 km/hr.

Avg. speed = 
$$\left(\frac{9 + 25 + 30}{\frac{9}{3} + \frac{25}{5} + \frac{80}{10}}\right)$$

$$= \left(\frac{9+25+30}{3+5+3}\right)$$

$$=\frac{64}{11}$$

= 5.81 km/hr.

# APNA COLLEGE

### **PROBABILITY**

$$Probability = \frac{Sum of Observation}{Possibility}$$

#### "Coins"

#### **Possibility**

**1.** One Coin tossed :  $\{H, T\} = 2 \rightarrow Possibility$ 

2. Two Coins Tossed Simultaneously = {HH, HT, TH, TT} = 4

3. Three Coins Tossed Simultaneously = 
$$\begin{cases}
HHH, TTT \\
HTH, TTT \\
HHHT, TTTT \\
HHHT, TTTT \\
HHHTH, TTTT
\\
HTHH, THTT
\end{cases} = 8$$

4. Four Coins Tossed = 
$$\begin{cases}
HHTH, THTT \\
HTHH, HTTT \\
HHTTT, THHT \\
HTTH, HTHT
\end{cases}$$
= 16

Q.71 3 coins are tossed find the probability of exactly 2 heads.

Probability of exactly 2 heads =  $\frac{3}{8}$ 

#### **Question to Practice**

Q.72 3 coins are tossed find the probability of no heads?

### DICE

#### **Possible Outcomes**

(1) 1 Dice = 
$$6^n$$
 = (Where n = No. of Dice)  
=  $6^1$   
=  $6$ 

(2) 2 Dice = 
$$6^2$$
  
= 36

(3) 3 Dice = 
$$6^3$$
  
= 216

#### Q.73 In a single throw of 2 dice, find the probability of getting a total of 3 or 5

### **Sol.** Possible Outcomes

$$2 \text{ Dice} \begin{cases}
(1,1) & (1,2) & (1,3) & (1,4) & (1,5) & (1,6) \\
(2,1) & (2,2) & (2,3) & (2,4) & (2,5) & (2,6) \\
(3,1) & (3,2) & (3,3) & (3,4) & (3,5) & (3,6) \\
(4,1) & (4,2) & (4,3) & (4,4) & (4,5) & (4,6) \\
(5,1) & (5,2) & (5,3) & (5,4) & (5,5) & (5,6) \\
(6,1) & (6,2) & (6,3) & (6,4) & (6,5) & (6,6)
\end{cases}$$

Probability = 
$$\frac{6}{36}$$

$$= \frac{1}{6}$$

#### **Question to Practice**

### Q.74 In a single throw of 2 dice, what is the probability of a doublet (same number)?

### Q.75 In a single throw of 3 dice, then find the probability of getting a total of 5

Sol. Possible Outcomes = 
$$6^n$$
  
=  $6^3$   
= 216  
Total of 5:  $\{(1,1,3) \quad (1,3,1) \quad (3,1,1)\}$   
 $(2,2,1) \quad (2,1,2) \quad (1,2,2)\}$   
Probability =  $\frac{6}{216}$ 

# APNA COLLEGE

## **PERMUTATION**

#### Q.76 How many ways the word can be arranged?

- (i) Non-Repeated Letters
  - (A) CAT
  - (B) MACHINE
  - (C) GAME
  - (D) CRYSTAL
  - (E) EDUCATION

Sol. (A) CAT 
$$= 3! - \text{Total No. of letter}$$
$$= 3 \times 2 \times 1$$
$$= 6$$

(B) MACHINE = 7!  
= 
$$7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1$$
  
=  $5040$ 

(C) GAME = 4!  
= 
$$4 \times 3 \times 2 \times 1$$
  
= 24

(D) CRYSTAL = 7!  
= 
$$7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1$$
  
=  $5040$ 

(E) EDUCATION = 9!  
= 
$$9 \times 8 \times 7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1$$
  
=  $362880$ 

- (ii) Repeated Letter
  - (A) SISTER
  - (B) PERCENTAGE

Sol. (A)SISTER = 
$$\frac{6!}{2!}$$
 Total No. of letter

No. of repeated letter

$$= \frac{6 \times 5 \times 4 \times 3 \times 2 \times 1}{2 \times 1}$$

$$= 360$$

(B) PERCENTAGE = 
$$\frac{10!}{3!}$$
= 
$$\frac{10 \times 9 \times 8 \times 7 \times 6 \times 5 \times 4 \times 2 \times 2 \times 2}{2 \times 2 \times 2 \times 2}$$
= 
$$604800$$

- Q.77 How many ways the word can be arranged?
- (i) Vowel that comes together
  - (A) JUDGE
  - (B) MACHINE
- Sol. (A) JUDGE

Vowel: (UE)

JDG(UE)

we can place (UE) at following places

$$\frac{\downarrow}{J} \underbrace{J} \underbrace{D} \underbrace{\downarrow} G \underbrace{\downarrow}$$

$$= 4! \times 2!$$

No. of places Vowels (UE)

where we can [2 Letters]

place vowels (No. of ways we can re-arrange vowel)

(B) MACHINE

Vowel: (AIE)

We can place (AIE) in following places  $\downarrow M \downarrow C \downarrow H \downarrow N \downarrow$ 

$$= 5! \times 3!$$

No. of places

(No. of ways (AIE) can

where we can

be re-arrange [3 Letters])

(AIE) place vowel

- (ii) Vowels always comes together
  - (A) SISTER
- Sol. Vowels: (IE)

We can place (IE) in following places

$$\frac{1}{\sqrt{S}} \cdot \frac{1}{\sqrt{S}} \cdot \frac{$$

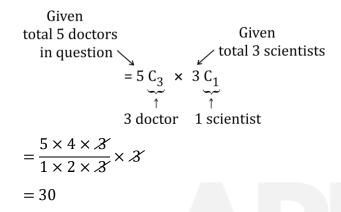
place (IE) No. of repeated vowel Letters

## COMBINATION

Q.78 Different committee's are to be made as per the requirement in each question. In how many ways can it be done?

8 students out of which 5 are doctors and 3 are scientist

- (i) A committee of 4 in while 3 are doctors & 1 is scientist
- **Sol.** 3 doctor & 1 scientists



- (ii) A committee of 5 in while which 3 are doctors
- **Sol.** To make committee of 5

3 are doctors (given)

$$\Rightarrow$$
 2 are scientists [5 - 3 = 2]

Committee doctor

Total

Total

5 doctors

3 scientists

5 doctors
given 
$$\searrow$$
 given
$$= 5 C_3 \times 3 C_2$$

$$= \frac{5 \times 4 \times 3}{1 \times 2 \times 3} \times \frac{3 \times 2}{1 \times 2}$$

$$= 30$$

- (iii) A committee of 2 in which there is no doctor
- **Sol.** (No doctor)

Committee of  $2 \Rightarrow$  only 2 scientists

Total 3 scientists given 
$$3 \underbrace{C_2}_{2} = \frac{3 \times 2}{1 \times 2} = 3$$
 2 scientists



### (iv) Committee of 2 unit which either both are doctors or both are scientists

**Sol.** 5 doctors 3 scientists (given)

Committee of 2

$$5 C_2 \overset{\leftarrow}{/} 3 C_2$$

either both doctor or scientist

$$=\frac{5\times4}{1\times2}+\frac{3\times2}{1\times2}$$

$$= 10 + 3$$

$$= 13$$

#### **Sol.** $384 \times ? = Perfect Square$

$$384 = 2 \times 3$$

$$=2^2\times2^2\times2^2\times2^1\times3^1$$

Perfect squares not perfect squares

To make  $2^1 \times 3^1$  perfect square,

we have to multiply it by  $2^1 \times 3^1$ 

$$\Rightarrow 2^1 \times 3^1 \times 2^1 \times 3^1$$

$$\Rightarrow \underbrace{2^2 \times 3^2}$$

(Perfect Square) (6)

 $\div$  6 is Least number to be multiplied with 384 to make it a perfect square.

#### **Question to Practice**

Q.80 What is the smallest number with which 5400 may be multiplied so that product is perfect cube?

# Q.81 Square of difference between two numbers is 9 while the sum of squares of those two number is 225 what is their product?

**Sol.** Given: 
$$(a - b)^2 = 9 \dots (1)$$

$$a^2 + b^2 = 225 \dots (2)$$

We know identity,

$$(a - b)^2 = a^2 + b^2 - 2ab$$

From (1) & (2)

$$9 = 225 - 2ab$$

$$ab = 116$$

$$ab = 58$$

$$∴$$
 Produce = 58

# APNA COLLEGE

### **LOGARITHM**

#### Q.82 Find the value of:

(A) 
$$\log_5(25)$$

**Sol.** 
$$\log_5(5)^2 = 2 \times \log_5(5)$$
  
= 2 × 1  
= 2

(B) 
$$\log_{81} 3$$

**Sol.** 
$$81 = 3^4$$

$$\log_{3} 4(3) = \frac{1}{4} \times \log_{3}(3)$$
$$= \frac{1}{4} \times 1$$
$$= \frac{1}{4}$$

(C) 
$$\log_{\sqrt{7}} \left( \frac{1}{243} \right)$$

**Sol.** 
$$\frac{1}{243} = \frac{1}{(7)^3} = 7^{-3}$$
 (1)

$$\sqrt{7} = 7^{1/2}$$

$$\log_{7^{1/2}}(7^{-3}) = -3 \times \log_{7^{1/2}}(7)$$
$$= -3 \times \frac{1}{2}\log_{7} 7$$
$$= -3 \times 2 \times 1 = -6$$

**Sol.** 
$$1000 = 10^3$$

• 
$$0001 = \frac{1}{1000} = \frac{1}{10^4} = 10^{-4}$$

$$\log_{10} -410^{3} = 3 \times \frac{1}{(-4)} \log_{10} 10$$
$$= -\frac{3}{4} \times 1$$
$$= -\frac{3}{4}$$



$$(E) \qquad log_2 \left( \frac{512 \times 256}{32} \right)$$

**Sol.** 
$$32 = 2^5; 256 = 2^8$$

$$512 = 2^9$$

$$= \log_2 \frac{(2^9 \times 2^8)}{2^5}$$

$$= \log_2(2^9 \times 2^3)$$

$$= \log_2(2^{12})$$

$$= 12 \times \log_2(2)$$

$$= 12 \times 1 \Rightarrow 12$$

#### Q.83 Find the value of y, if $log_v(25/9) = -2$

**Sol.** 
$$\log_{v}(25/9) = -2$$

$$a^m = x [log_a(x) = m]$$

$$y^{-2} = \frac{25}{9}$$

$$y^2 = \frac{9}{25}$$

$$y = \frac{3}{5}$$

#### Q.84 Find the value of:

$$\log\left(\frac{15}{16}\right) - \log\left(\frac{27}{45}\right) + \log\left(\frac{48}{75}\right)$$

#### Sol. Product Rule:

$$\log_a(xy) = \log_a(x) + \log_a(y)$$

#### **Quotient Rule:**

$$\log_{a}(x/y) = \log_{a}(x) - \log_{a}(y)$$

$$\log\left(\frac{15}{16}\right) - \underbrace{\log\left(\frac{27}{45}\right)}_{\downarrow} + \underbrace{\log\left(\frac{48}{75}\right)}_{\downarrow}$$

Quotient Rule Product Rule

$$\log\left(\frac{15^{1}}{16} \times \frac{45^{8}}{27_{8_{1}}} \times \frac{48^{3^{1}}}{75}\right)_{8_{1}}$$

$$= \log 1 = 0$$

**Sol. 7** 
$$(1^2 + 2^2 + \dots + 20^2) - (1^2 + \dots + 9^2)$$

(Total) – (First)

$$=\frac{n(n+1)(2n+1)}{6}-\frac{n(n+1)(2n+1)}{6}$$

$$=\frac{20\times21\times41}{6}-\frac{9(10)(19)}{6}$$

$$= 2870 - (15 \times 19)$$

$$= 2585$$

**Sol. 9** 
$$a = 2$$

$$d = 7 - 2 = 5$$

$$n = 9$$

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$S_{19} = \frac{19}{2} [2(2) + (19 - 1)5]$$

$$=\frac{19}{2}[4+(18\times5)]$$

$$=\frac{19}{2}\times 94=893$$

#### **Sol. 14** Let the no. be x

$$\frac{4}{5}x - \frac{3}{4}x = 8$$

$$\frac{16x - 15x}{20} = 8$$

$$x = 160$$

#### **Sol. 15** Let the no. be x

First no.-second no. = 7

$$\frac{3}{4}x - \frac{1}{6}x = 7$$

$$\frac{3x}{4} - \frac{x}{6} = 7$$

$$\frac{9x - 2x}{12} = 7$$

$$x = 12$$

 $\frac{5}{3}$  of the number

$$\Rightarrow \frac{5}{3}x$$

$$=\frac{5}{3}\times12$$

$$= 20$$

#### Sol. 20

Past 4 years

Past age + 1

Past Present Future

2: 3 ? 5: 7

2x: 3x 5x: 7x

$$\frac{2x + 8}{3x + 8} = \frac{5}{7}$$

$$14x + 56 = 15x + 40$$

$$x = 6$$

Present ages, of A & B.

$$2x + 4 \Rightarrow 2(16) + 4$$

$$3x + 4 \Rightarrow 3(16) + 4$$

#### **Sol. 21**

<u>Son</u>

<u>Father</u>

Present age

X

3 + 3x

Future age

x + 3

3x + 6

After 10 years,

$$3x + 6 = 10 + 2(x + 3)$$

$$3x + 6 = 10 + 2x + 6$$

$$x = 10$$

 $\therefore$  Father Present age = 3 + 3x

$$= 3 + 3(10)$$

= 33 years

**Sol.25** 

'A': 
$$\frac{2}{3}$$
 of work = 4 days

1 work done by 'A' =  $4 \times \frac{3}{2}$ 

$$A = 6 \text{ days}$$

'B': 
$$\frac{3}{5}$$
 of work = 6 days

1 work done by 'B' =  $6 \times \frac{5}{3}$ 

$$B = 10 \text{ days}$$

$$A + B = ?$$

$$=\frac{1}{6}+\frac{1}{10}$$

$$=\frac{3^4}{30_{15}}\Rightarrow\frac{4}{15}$$

$$=\frac{4}{15}$$

Final answer will be reciprocal  $\Rightarrow \frac{15}{4}$  days

$$=3\frac{3}{4}$$
 days

$$P_1 = 72$$
  $D_1 = 21$   $w_1 = 280$ 

$$P_2 =$$

$$D_2 = 18$$

$$P_2 = ?$$
  $D_2 = 18$   $w_2 = 100$ 

We know, 
$$\frac{P_1H_1D_1}{P_2H_2D_2} = \frac{w_1}{w_2}$$

But in above question nothing is mentioned about no. of hours

$$\therefore \text{ we use } \frac{P_1 D_1}{P_2 D_2} = \frac{w_1}{w_2}$$

$$\frac{72 \times 21}{x \times 18} = \frac{280}{100}$$

$$\frac{6}{x} = \frac{1}{5}$$

$$x = 6 \times 5$$

$$x = 30$$

No. of men required = 30

#### **Sol.30**

$$40 \text{ km/hr.} \times 9 = 360 \text{ km}$$

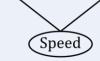
(: Distance = Speed 
$$\times$$
 Time)

$$60 \text{ km/hr.} \times ? = 360 \text{ km}$$

time = 
$$\frac{360}{60}$$

time = 6 hr.

#### **Sol.33**



$$S_1 = S_2$$

$$\frac{D}{T} = \frac{D}{T}$$

(Length of Train + Platform Length) \_ Length of Train + Platform Length

Time

$$\frac{x + 162}{18_6} = \frac{x + 120}{15_5}$$

$$5x + 810 = 6x + 720$$

$$x = 90 \text{ m}$$

#### Sol.35 Type – I

$$d = S_1 \left[ \frac{d + s_1 t}{s_1 + s_2} \right] km$$

t = Time difference

$$= T_1 \sim T_2$$

= 0 (: beth trains start at same time)

$$d = 30 \left[ \frac{300 + 30(0)}{30 + 45} \right]$$

$$=30\left[\frac{300}{75}\right]$$

$$=\frac{9000}{75}$$

= 120 km

**Sol. 41** 
$$\theta = \left| 30H - \frac{11}{2}(M) \right|$$

$$\theta = \left| 30(10) - \frac{11}{2}(10) \right|$$

$$\theta = |300 - 55|$$

$$\theta = 245^{\circ}$$

$$\because$$
 angle  $> 180^{\circ}$ 

$$= 115^{\circ}$$

**Sol. 42** 
$$\theta = \left| 30H - \frac{11}{2}(M) \right|$$

$$0^{\circ} = 30 \times 3 - \frac{11}{2} M$$

$$0 = 90 - \frac{11}{2}M$$

$$-90 = -\frac{11}{2}M$$

$$M = \frac{90 \times 2}{11}$$

$$=\frac{180}{11}$$

$$=16\frac{4}{11}$$

$$\Rightarrow$$
 3: 16:  $\frac{4}{11}$  sec.

# **Sol. 43** $\theta = 30H - \frac{11}{2}M$

$$\theta = \pm 90^{\circ}$$

If 
$$\theta = -90^{\circ}$$

$$-90 = 30 \times 5 - \frac{11}{2}M$$

$$-90 - 150 = -\frac{11}{2}M$$

$$240 = \frac{11}{2} M$$

$$M = \frac{480}{11}$$

$$=43\frac{7}{11}$$

Between 5:30 & 6:00, the hands of clock will be at right angle at 5:43:7/11 sec.

**Sol.47** 20% of 
$$(P + Q) = 50\%$$
 of  $(P - Q)$ 

$$2(P+Q) = 5(P-Q)$$

$$2P + 2Q = 5Q - 5Q$$

$$2Q + 5Q = 5P - 2P$$

$$7Q = 3P$$

$$\frac{P}{Q} = \frac{7}{3}$$

**Sol.48** Pass Mark = 
$$113 + 85$$

$$= 198$$

$$100\% = x$$

$$36x = 198 \times 100$$

$$x = \frac{198 \times 100}{36}$$

$$x = 550$$

**Sol. 49** 
$$=\frac{30}{100} \times 2800$$

$$=30\times28$$

$$= 840$$

Sol. 53 SP = 
$$\frac{100 + P\%}{100} \times CP$$
  
=  $\frac{100 + 15}{100} \times 350$   
=  $\frac{115}{100} \times 350$ 

$$SP = 402.5$$

Sol. 54 CP = 
$$\frac{100}{100 - \text{Loss\%}} \times \text{SP}$$
  
=  $\frac{100}{90} \times 720$   
=  $800$   
SP =  $\frac{100 + \text{gain \%}}{100} \times \text{CP}$   
=  $\frac{100 + 5}{100} \times 800$   
 $|\text{SP} = 840|$ 

**Sol. 58** Alcohol: Water 
$$= 4:3$$

$$= 4x: 3x$$

Alcohol = 4x, water = 3x

Given: 5 litres of water is added

$$\frac{4x}{3x+5} = \frac{4}{5}$$

$$4x \times 5 = 4(3x + 5)$$

$$20x = 12x + 20$$

$$8x = 20$$

$$x = 20/8$$

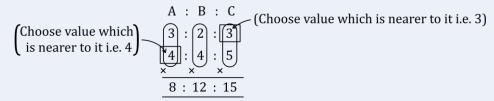
$$x = 5/2$$

Quantity of alcohol = 4x

$$= 4^2 \times \frac{5}{2}$$

= 10 litres

**Sol.59** A: B = 2: 3, B: 
$$C = 4:5$$



A: B: 
$$C = 8: 12: 15$$

**Sol.60** 
$$3A = 5B$$
,

$$4B = 6C$$

$$\frac{A}{B} = \frac{5}{3} \qquad \qquad \frac{B}{C} = \frac{6}{4}$$

$$\frac{B}{C} = \frac{6}{4}$$

$$A: B = 5: 3$$

$$B: C = 6: 4$$

A : B : C - Put nearest value Put nearest value -30 : 18 : 12

But we want A: C

On Simplifying  $\Rightarrow 30^5: 12^2$ 

$$\Rightarrow$$
 A: C = 5:2

**Sol. 64** 
$$A = P \left[ 1 + \frac{R}{100} \right]^n$$

$$=8000 \left[1 + \frac{5}{100}\right]^3$$

$$=8000 \left[ \frac{105}{100} \right]^3$$

$$=8\emptyset\emptyset\emptyset\times\frac{105}{1\emptyset\emptyset}\times\frac{105}{10\emptyset}\times\frac{105}{100}$$

$$= 21 \times 21 \times 21$$

$$A = 9261$$

$$A = P + I$$

$$9261 = 8000 + I$$

$$I = 9261 - 8000$$

$$I = 1261$$

$$C. I. = Rs. 1261$$

**Sol.68** Third = 
$$x$$

$$Second = 3x$$

$$First = 2(3x)$$

$$= 6x$$

$$\frac{6x+3x+x}{3}=10$$

$$10x = 10 \times 3$$

$$10x = 30$$

$$x = 3$$

First number = 6x

$$=6\times3$$

$$= 18$$

Second number = 3x

$$= 3 \times 3$$

Third number = x

$$= 3$$

#### **Sol.69** Total expenditure = $3600 \times 5$

$$= 18,000$$

Next 7 months =  $3900 \times 7$ 

$$= 27,300$$

Total Income for 12 months = 18,000 + 27,300 + 8,700

$$\therefore \text{ Arg. Income per month} = \frac{54000}{12}$$

$$= Rs. 4,500$$

Probability of no heads  $=\frac{1}{8}$ 

#### **Sol.74** Possible Outcomes

Probability = 
$$\frac{6}{36}$$
  
=  $\frac{1}{36}$ 

**Sol.80** 
$$5400 = 2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 5 \times 5$$

$$=2^3\times3^3 \times 5^2$$

Perfect cube not perfect cube

 $\therefore$  To make  $5^2$  a perfect cube, we have to multiply it by 5

$$=5^2\times(5)$$

$$= 5^3$$

 $\div$  Smallest number to be multiplied with 5400 to make it perfect cube.