

Data Structure and Algorithms [CO2003]

Chapter 5 - Stack and Queue

Lecturer: Duc Dung Nguyen, PhD. Contact: nddung@hcmut.edu.vn

Faculty of Computer Science and Engineering Hochiminh city University of Technology

Contents



- 1. Basic operations of Stacks
- 2. Implementation of Stacks
- 3. Applications of Stack
- 4. Basic operations of Queues
- 5. Implementation of Queue
- 6. Applications of Queue

Outcomes



- L.O.2.1 Depict the following concepts: (a) array list and linked list, including single link and double links, and multiple links; (b) stack; and (c) queue and circular queue.
- L.O.2.2 Describe storage structures by using pseudocode for: (a) array list and linked list, including single link and double links, and multiple links; (b) stack; and (c) queue and circular queue.
- L.O.2.3 List necessary methods supplied for list, stack, and queue, and describe them using pseudocode.
- L.O.2.4 Implement list, stack, and queue using C/C++.

Outcomes



- L.O.2.5 Use list, stack, and queue for problems in real-life, and choose an appropriate implementation type (array vs. link).
- L.O.2.6 Analyze the complexity and develop experiment (program) to evaluate the efficiency of methods supplied for list, stack, and queue.
- L.O.8.4 Develop recursive implementations for methods supplied for the following structures: list, tree, heap, searching, and graphs.
- L.O.1.2 Analyze algorithms and use Big-O notation to characterize the computational complexity of algorithms composed by using the following control structures: sequence, branching, and iteration (not recursion).

Basic operations of Stacks

Linear List Concepts



General list:

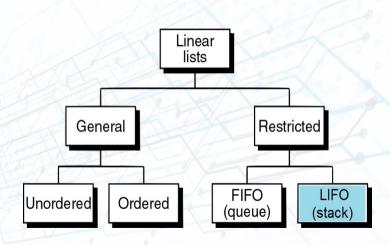
- No restrictions on which operation can be used on the list.
- No restrictions on where data can be inserted/deleted.

Restricted list:

- Only some operations can be used on the list.
- Data can be inserted/deleted only at the ends of the list.

Linear list concepts





Stack



Definition

A stack of elements of type T is a finite sequence of elements of T, in which all insertions and deletions are restricted to one end, called the top.

Stack is a Last In - First Out (LIFO) data structure.

LIFO: The last item put on the stack is the first item that can be taken off.





Basic operations of Stacks



Basic operations:

- Construct a stack, leaving it empty.
- Push an element: put a new element on to the top of the stack.
- Pop an element: remove the top element from the top of the stack.
- Top an element: retrieve the top element.

Basic operations of Stacks



Extended operations:

- Determine whether the stack is empty or not.
- Determine whether the stack is full or not.
- Find the size of the stack.
- Clear the stack to make it empty.

Basic operations of Stacks: Push



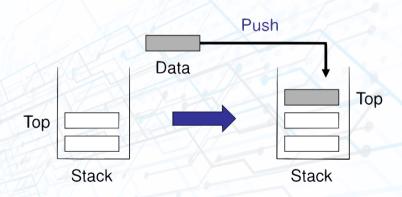


Figure 1: Successful Push operation



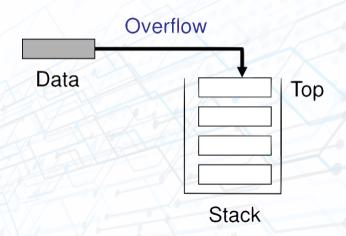


Figure 2: Unsuccessful Push operation. Stack remains unchanged.

Basic operations of Stacks: Pop



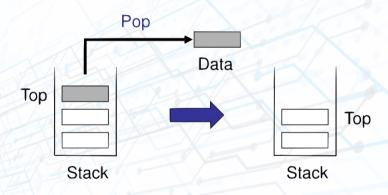


Figure 3: Successful Pop operation



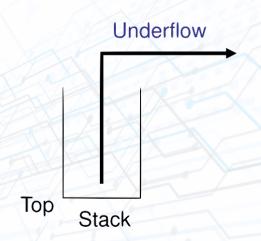


Figure 4: Unsuccessful Pop operation. Stack remains unchanged.

Basic operations of Stacks: Top



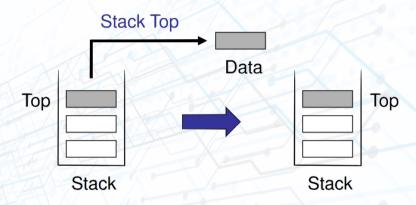


Figure 5: Successful Top operation. Stack remains unchanged.



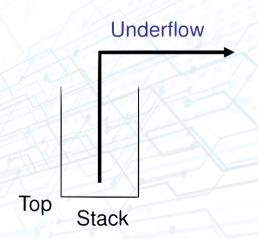
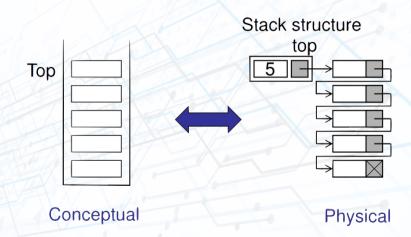


Figure 6: Unsuccessful Top operation. Stack remains unchanged.

Implementation of Stacks

Linked-list implementation

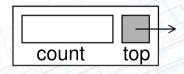




Linked-list implementation

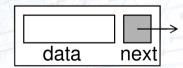


Stack structure



stack
 count <integer>
 top <node pointer>
end stack

Stack node structure



node
 data <dataType>
 next <node pointer>
end node

Linked-list implementation in C++



```
template <class ItemType>
struct Node {
   ItemType data;
   Node<ItemType> *next;
};
```

Linked-list implementation in C++



```
template < class List ItemType>
class Stack {
  public:
    Stack();
   ~Stack():
    void Push (List Item Type dataln);
    int Pop(List ItemType &dataOut);
    int GetStackTop(List ItemType &dataOut);
    void Clear();
    int IsEmpty();
    int GetSize():
    Stack < List Item Type >* Clone();
    void Print2Console();
  private:
    Node<List ItemType>* top;
    int count:
};
```

Create an empty Linked Stack

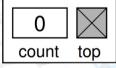




? ? count top

(no stack)

After



(empty stack)

Create an empty Linked Stack



Algorithm createStack(ref stack <metadata>)

Initializes the metadata of a stack

Pre: stack is a metadata structure of a stack

Post: metadata initialized

stack.count = 0

stack.top = null

return

End createStack

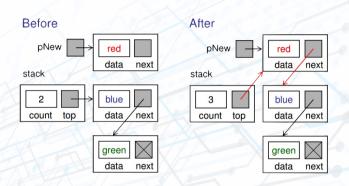
Create an empty Linked Stack



```
template <class List_ItemType>
Stack<List_ItemType>::Stack(){
   this ->top = NULL;
   this ->count = 0;
}

template <class List_ItemType>
Stack<List_ItemType>::~Stack(){
   this ->Clear();
}
```





- 1. Allocate memory for the new node and set up data.
- 2. Update pointers:
 - Point the new node to the top node (before adding the new node).
 - Point top to the new node.
- 3. Update count



Algorithm pushStack(ref stack <metadata>, val data <dataType>) Inserts (pushes) one item into the stack

Pre: stack is a metadata structure to a valid stack data contains value to be pushed into the stack

Post: data have been pushed in stack

Return true if successful; false if memory overflow



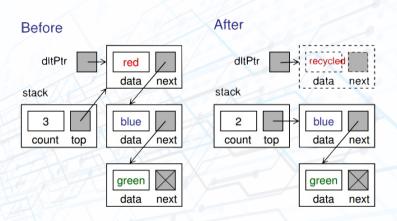
```
if stack full then
   success = false
else
   allocate (pNew)
   pNew -> data = data
   pNew -> next = stack.top
   stack.top = pNew
   stack.count = stack.count + 1
   success = true
end
return success
End pushStack
```





- Push is successful when allocation memory for the new node is successful.
- There is no difference between push data into a stack having elements and push data into an empty stack (top having NULL value is assigned to pNew->next: that's corresponding to a list having only one element).





- 1. dltPtr holds the element on the top of the stack.
- 2. top points to the next element.
- 3. Recycle dltPtr. Decrease count by 1.

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 ${\bf Algorithm}\ {\tt popStack}({\tt ref\ stack\ < metadata>,\ ref\ dataOut\ < dataType>)}$

Pops the item on the top of the stack and returns it to caller

Pre: stack is a metadata structure to a valid stack

dataOut is to receive the popped data

Post: data have been returned to caller

Return true if successful; false if stack is empty



```
if stack empty then
   success = false
else
   dltPtr = stack.top
   dataOut = stack.top -> data
   stack.top = stack.top -> next
   stack.count = stack.count - 1
   recycle(dltPtr)
   success = true
end
return success
End popStack
```





- Pop is successful when the stack is not empty.
- There is no difference between pop an element from a stack having elements and pop the only-one element in the stack (dltPtr->next having NULL value is assigned to top: that's corresponding to an empty stack).

Stack Top



Algorithm stackTop(ref stack <metadata>, ref dataOut <dataType>)
Retrieves the data from the top of the stack without changing the stack

Pre: stack is a metadata structure to a valid stack

dataOut is to receive top stack data

Post: data have been returned to caller

Return true if successful; false if stack is empty

Stack Top



Stack Top



Destroy Stack



Algorithm destroyStack(ref stack <metadata>)
Releases all nodes back to memory

Pre: stack is a metadata structure to a valid stack

Post: stack empty and all nodes recycled

Destroy Stack



```
if stack not empty then
   while stack.top not null do
       temp = stack.top
       stack.top = stack.top -> next
       recycle(temp)
   end
end
stack.count = 0
return
End destroyStack
```

Destroy Stack



```
template <class List_ItemType>
void Stack<List_ItemType>::Clear() {
  Node<List_ItemType>* temp;
  while (this->top!= NULL){
    temp = this->top;
    this->top = this->top->next;
    delete temp;
}
this->count = 0;
}
```

isEmpty Linked Stack



Algorithm isEmpty(ref stack <metadata>)

Determines if the stack is empty

Pre: stack is a metadata structure to a valid stack

Post: return stack status

Return true if the stack is empty, false otherwise

if count = 0 then

Return true

else

Return false

end

End isEmpty

isEmpty Linked Stack



```
template <class List_ItemType>
int Stack<List_ItemType>::IsEmpty() {
  return (count == 0);
}

template <class List_ItemType>
int Stack<List_ItemType>::GetSize() {
  return count;
}
```

isFull Linked Stack



Print Stack



```
template <class List_ItemType>
void Stack<List_ItemType>::Print2Console() {
  Node<List_ItemType>* p;
  p = this->top;
  while (p != NULL){
    cout << p->data << "\";
    p = p->next;
  }
  cout << endl;
}</pre>
```

Using Stack



```
int main(int argc, char* argv[]){
   Stack<int> *myStack = new Stack<int >();
   int val;
   myStack->Push(7);
   myStack->Push(9);
   myStack->Push(10);
   myStack->Push(8);
   myStack->Print2Console();
   myStack->Pop(val);
   myStack->Print2Console();
   delete myStack;
   return 0;
}
```



Implementation of array-based stack is very simple. It uses top variable to point to the topmost stack's element in the array.

- 1. Initialy top = -1;
- 2. push operation increases top by one and writes pushed element to storage[top];
- 3. pop operation checks that top is not equal to -1 and decreases top variable by 1;
- 4. getTop operation checks that top is not equal to -1 and returns storage[top];
- 5. isEmpty returns boolean if top == -1.



```
#include <string>
using namespace std;
class ArrayStack {
private:
  int top;
  int capacity;
  int *storage;
public:
  ArrayStack(int capacity) {
    storage = new int[capacity];
    this -> capacity = capacity;
    top = -1;
```



```
~ArrayStack() {
  delete[] storage;
void push (int value) {
  if (top = capacity - 1)
    throw string ("Stack is overflow");
  top++:
  storage[top] = value;
void pop(int &dataOut) {
  if (top == -1)
    throw string ("Stack is wempty");
 dataOut = storage[top];
 top --:
```



```
int getTop() {
  if (top == -1)
    throw string("Stack_is_mempty");
  return storage[top];
}

bool isEmpty() {
  return (top == -1);
}

bool isFull() {
  return (top == capacity -1);
}
```



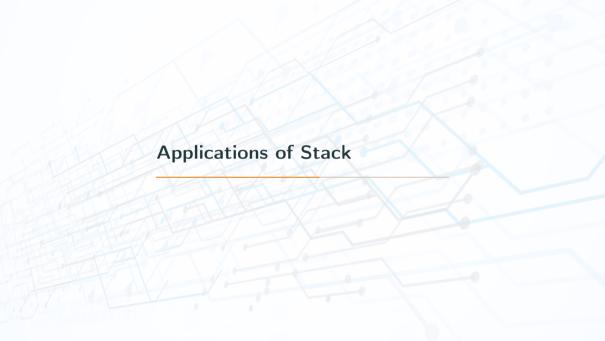
```
int getSize() {
    return top + 1;
}

void print2Console() {
    if (top > -1) {
        for (int i = top; i >= 0; i--) {
            cout << storage[i] << "u";
        }
        cout << endl;
}
}</pre>
```

Using array-based stack



```
int main(int argc, char* argv[]){
   ArrayStack *myStack = new ArrayStack(10);
   int val;
   myStack->push(7);
   myStack->push(9);
   myStack->push(10);
   myStack->push(8);
   myStack->print2Console();
   myStack->pop(val);
   myStack->print2Console();
   delete myStack;
   return 0;
}
```



Applications of Stack



- Reversing data items
 - Reverse a list
 - Convert Decimal to Binary
- Parsing
 - Brackets Parse
- Postponement of processing data items
 - Infix to Postfix Transformation
 - Evaluate a Postfix Expression
- Backtracking
 - Goal Seeking Problem
 - Knight's Tour
 - Exiting a Maze
 - Eight Queens Problem

Basic operations of Queues



Definition

A queue of elements of type T is a finite sequence of elements of T, in which data can only be inserted at one end called the rear, and deleted from the other end called the front.

Queue is a First In - First Out (FIFO) data structure.

FIFO: The first item stored in the queue is the first item that can be taken out.





Basic operations of Queues



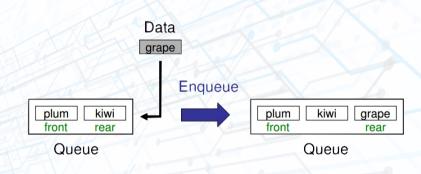
Basic operations:

- Construct a queue, leaving it empty.
- Enqueue: put a new element in to the rear of the queue.
- Dequeue: remove the first element from the front of the queue.
- Queue Front: retrieve the front element.
- Queue Rear: retrieve the rear element.



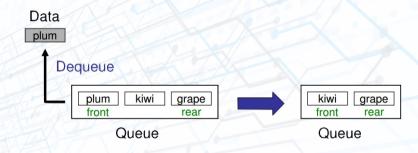
Basic operations of Queues: Enqueue





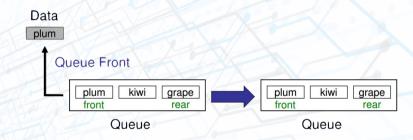
Basic operations of Queues: Dequeue





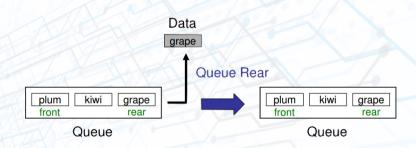
Basic operations of Queues: Queue Front





Basic operations of Queues: Queue Rear

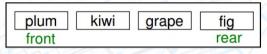




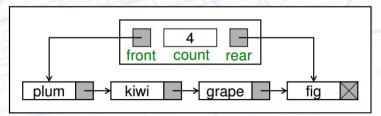
Implementation of Queue







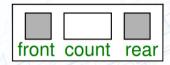




Linked-list implementation



Queue structure



Queue node structure



queue count <integer> front <node pointer> rear <node pointer> endqueue

node
 data <dataType>
 next <node pointer>
end node

Linked-list implementation in C++



```
template <class ItemType>
struct Node {
   ItemType data;
   Node<ItemType> * next;
};

template <class List_ItemType>
class Queue {
   public:
      Queue();
      ~Queue();
      ~Queue();
```

Linked-list implementation in C++

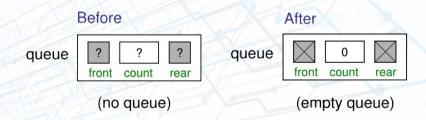


```
void Enqueue(List_ItemType dataIn);
int Dequeue(List_ItemType &dataOut);
int GetQueueFront(List_ItemType &dataOut);
int GetQueueRear(List_ItemType &dataOut);
void Clear();
int IsEmpty();
int GetSize();
void Print2Console();

private:
   Node<List_ItemType> *front, *rear;
int count;
```

Create Queue





Create Queue



Algorithm createQueue(ref queue <metadata>) Initializes the metadata of a queue

Pre: queue is a metadata structure of a queue

Post: metadata initialized

queue.count= 0

queue.front = null

queue.rear = null

return

End createQueue

Create Queue



```
template <class List_ItemType>
Queue<List_ItemType>::Queue(){
   this->count = 0;
   this->front = NULL;
   this->rear = NULL;
}

template <class List_ItemType>
Queue<List_ItemType>::~Queue(){
   this->Clear();
}
```

Enqueue: Insert into an empty queue



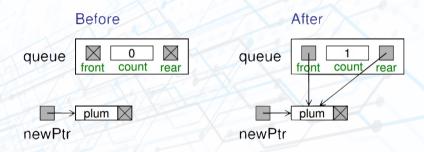


Figure 7: Insert into an empty queue

Enqueue: Insert into a queue with data



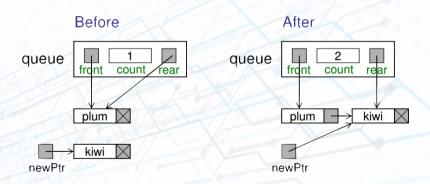


Figure 8: Insert into a queue with data

Enqueue



Algorithm enqueue(ref queue <metadata>, val data <dataType>) Inserts one item at the rear of the queue

Pre: queue is a metadata structure of a valid queue data contains data to be inserted into queue

Post: data have been inserted in queue

Return true if successful, false if memory overflow

Enqueue



```
if queue full then
   return false
end
allocate (newPtr)
newPtr -> data = data
newPtr -> next = null
if queue.count = 0 then
   queue.front = newPtr // Insert into an empty queue
else
   queue.rear -> next = newPtr // Insert into a queue with data
end
queue.rear = newPtr
queue.count = queue.count + 1
return true
```

Enqueue



Dequeue: Delete data in a queue with only one item



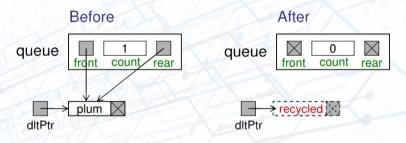


Figure 9: Delete data in a queue with only one item

Dequeue: Delete data in a queue with more than one item



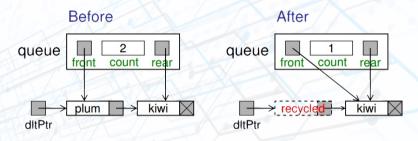


Figure 10: Delete data in a queue with more than one item

Dequeue



Algorithm dequeue(ref queue <metadata>, ref dataOut <dataType>) Deletes one item at the front of the queue and returns its data to caller

Pre: queue is a metadata structure of a valid queue dataOut is to receive dequeued data

Post: front data have been returned to caller

Return true if successful, false if memory overflow

Dequeue



```
if queue empty then
   return false
end
dataOut = queue.front -> data
dltPtr = queue.front
if queue.count = 1 then
   // Delete data in a queue with only one item
   queue.rear = NULL
end
queue.front = queue.front -> next
queue.count = queue.count - 1
recycle (dltPtr)
return true
```

Dequeue



```
template <class List_ItemType>
int Queue<List_ItemType>::Dequeue(List_ItemType &dataOut){
  if (count == 0)
    return 0;
  dataOut = front->data;
  Node<List_ItemType>* dltPtr= this->front;
  if (count == 1)
    this->rear = NULL;
  this->front = this->front->next;
  this->count--;
  delete dltPtr;
  return 1;
}
```

Queue Front



```
template <class List_ItemType>
int Queue<List_ItemType>::GetQueueFront(List_ItemType &dataOut){
  if (count == 0)
    return 0;
  dataOut = this->front->data;
  return 1;
}
```

Queue Rear



```
template <class List_ItemType>
int Queue<List_ItemType>::GetQueueRear(List_ItemType &dataOut){
  if (count == 0)
    return 0;
  dataOut = this->rear->data;
  return 1;
}
```

Destroy Queue



Algorithm destroyQueue(ref queue <metadata>) Deletes all data from a queue

Pre: queue is a metadata structure of a valid queue

Post: queue empty and all nodes recycled

Return nothing

Destroy Queue



```
if queue not empty then
   while queue.front not null do
      temp = queue.front
      queue.front = queue.front->next
      recycle(temp)
   end
end
queue.front = NULL
queue.rear = NULL
queue.count = 0
return
End destroyQueue
```

Destroy Queue



```
template <class List_ItemType>
void Queue<List_ItemType>::Clear() {
  Node<List_ItemType>* temp;
  while (this->front != NULL){
    temp = this->front;
    this->front= this->front->next;
    delete temp;
  }
  this->front= NULL;
  this->count = 0;
}
```

Queue Empty



```
template <class List_ItemType>
int Queue<List_ItemType>::IsEmpty() {
  return (this->count == 0);
}

template <class List_ItemType>
int Queue<List_ItemType>::GetSize() {
  return this->count;
}
```

Print Queue



```
template <class List_ItemType>
void Queue<List_ItemType>::Print2Console(){
  Node<List_ItemType>* p;
  p = this->front;
  cout << "Front:_";
  while (p!= NULL){
    cout << p->data << "_";
    p = p->next;
}
  cout << endl;
}</pre>
```

Using Queue



```
int main(int argc, char* argv[]){
   Queue<int> *myQueue = new Queue<int >();
   int val;
   myQueue—>Enqueue(7);
   myQueue—>Enqueue(9);
   myQueue—>Enqueue(10);
   myQueue—>Enqueue(8);
   myQueue—>Print2Console();
   myQueue—>Print2Console();
   delete myQueue;
   return 1;
}
```



```
#include <string>
using namespace std;
class ArrayQueue {
private:
  int capacity;
  int front;
  int rear;
  int *storage;
public:
  ArrayQueue(int capacity) {
    storage = new int[capacity];
    this -> capacity = capacity;
    front = -1:
    rear = -1:
```



```
~ArravQueue() {
  delete[] storage:
void enQueue(int value) {
  if(isFull()) throw string("Queue_is_full");
  if (front == -1) front = 0;
  rear++:
  storage[rear % capacity] = value;
void deQueue(int &valueOut) {
  if (isEmpty())
    throw string ("Queue is empty");
  valueOut = storage[front % capacity];
  front++:
```



```
int getFront() {
  if (isEmpty())
    throw string("Queue_is_empty");
  return storage[front % capacity];
}
int getRear() {
  if (isEmpty())
    throw string("Queue_is_empty");
  return storage[rear % capacity];
}
```



```
bool isEmpty() {
  return (front > rear || front == -1);
}
bool isFull() {
  return (rear - front + 1 == capacity);
}
int getSize() {
  return rear - front + 1;
}
```

Using Array-based queue



```
int main(int argc, char* argv[]){
   ArrayQueue *myQueue = new ArrayQueue(10);
   int val;
   myQueue—>enQueue(7);
   myQueue—>enQueue(9);
   myQueue—>enQueue(10);
   myQueue—>enQueue(8);
   myQueue—>deQueue(val);
   delete myQueue;
   return 1;
}
```

Applications of Queue

Applications of Queue



- Polynomial Arithmetic
- Categorizing Data
- Evaluate a Prefix Expression
- Radix Sort
- Queue Simulation