## LAB II

# Random magnet model: avalanches and hysteresis

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## Plan

Algorithm

2 Tasks and hints

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## **Process**

- each spin flips when it can gain energy
- its local field  $J \sum_{i(i)} s_j + h_i + H(t)$  at site *i* changes sign
- spin can be triggered by
  - 1) one of the neighbours flips
  - 2) increase of H(t)

## Slowly changing the external field:

- search for the unflipped spin that is next to flip
- jump the field H just enough to flip
- propagate the avalanche.

Use J = 1 and periodic boundary conditions.

## Block code: draft

#### Propagating an avalanche

- (1) Find the triggering spin i for the next avalanche, which is the unflipped site with the largest internal field  $J \sum_{j \text{ nbr to } i} s_j + h_i$  from its random field and neighbors.
- (2) Increment the external field *H* to minus this internal field, and push the spin onto a first-in–first-out queue
- (3) Pop the top spin off the queue.
- (4) If the spin has not been flipped,\* flip it and push all unflipped neighbors with positive local fields onto the queue.
- (5) While there are spins on the queue, repeat from step (3).
- (6) Repeat from step (1) until all the spins are flipped.

## Task 1

Benchmark: calculate mean size of the first avalanche with 1000 realizations of disorder for  $100 \times 100$  lattice and R = 0.7, 0.9, 1.4.

Optional: while developing your code plot the system/magnetic field configurations for a better insight.

#### Example results:

```
R = 1.4 mean_size = 1.042(1)

R = 0.9 mean_size = 1.39(1)

R = 0.7 mean_size = 660(30)
```

## Task 2

- **A)** Display the avalanches. While forming an avalanche assign the count number to the sites visited. Make a "pixel" plot of all the avalanches from the whole run, mark the avalanches with different colors. Use disorder strength R = 0.9, 1.4, 2.1.
- **B)** Perform the simulation on a  $300 \times 300$  system with R = 0.9, 1.4, 2.1.

Plot the accumulated result for H(M) in the range  $H \in (-3,3)$  and  $M \in (-1,1)$ . Magnetization: M = np.sum(s) / (L\*\*2).

## Extra

There are many more things one can compute:

- histogram of avalanche sizes (on a log-log plot)
- colored shells (subsequent triggered neighbourhoods) of a growing avalanche
- time series of an avalanche (time is shell number)

Try at least one of those. For more details consult the literature.

One may also perform a 3D simulation (critical value is  $R_c = 2.16$ ). (The speed would incease considerably when using numba and jit, but it is not quite trivial.)

## Hints I

## We need some simple data structure

```
# lattice of spins
s = np.ones( (L, L), dtype=np.int ) * (-1)
# recording of avalanches
aval = np.zeros( (L, L), dtype=np.int )
# random magnetic fields
h_rnd = np.random.randn(L, L) * R
# ... and the local fields
h_loc = np.ones( (L, L), dtype=np.int ) * (-4.0) + h_rnd
```

## Hints II

It is useful to prepeare a routine for calulating the neighbours

Spin update: flip the spin and adjust local field of the neighbours

```
def update(i):
    s[i] = 1
    for j in neighbours(i):
        h_loc[j] += 2.0
    return
```

## Hints III

## FIFO queue is available as a Python list

```
d = []
d.append(i)
itmp = d.pop(0)
```

## Important trick to calculate the triggering spin:

## Quick way to plot the avalanches

```
plt.imshow(aval,interpolation='none',cmap=cm.gist rainbow)
```