IS593: Language-based Security

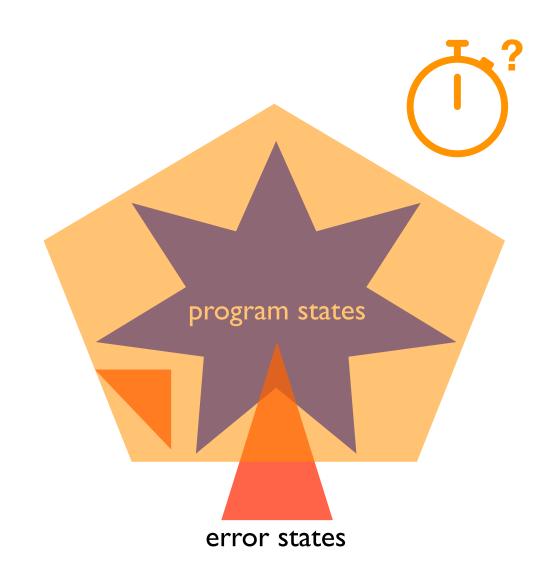
8. Advanced Iteration Techniques

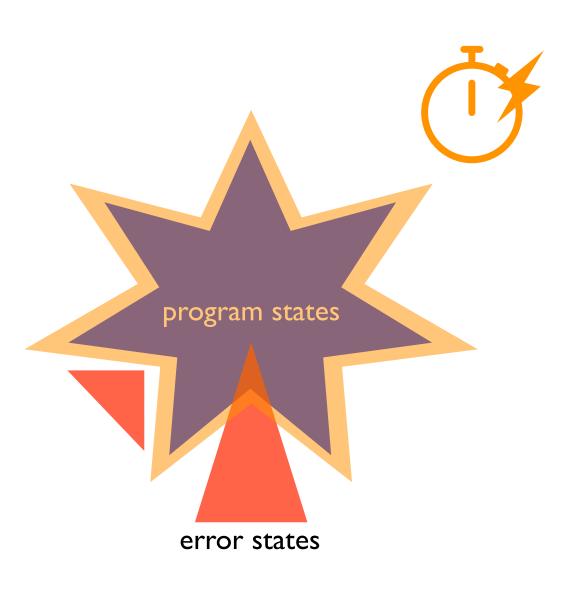
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Advanced Analysis Techniques

- So far, our focus most has been sound abstract semantics
- From now on, we will cover several advanced techniques to achieve efficient and accurate analysis





Iteration Strategies

- Loop invariant inference: sequences of abstract iterations
 - Compute weaker and weaker abstract states until stabilization (via join and widening)
- "Loop is evil": a main source of imprecision in static analysis
- Needs for techniques to improve the precision

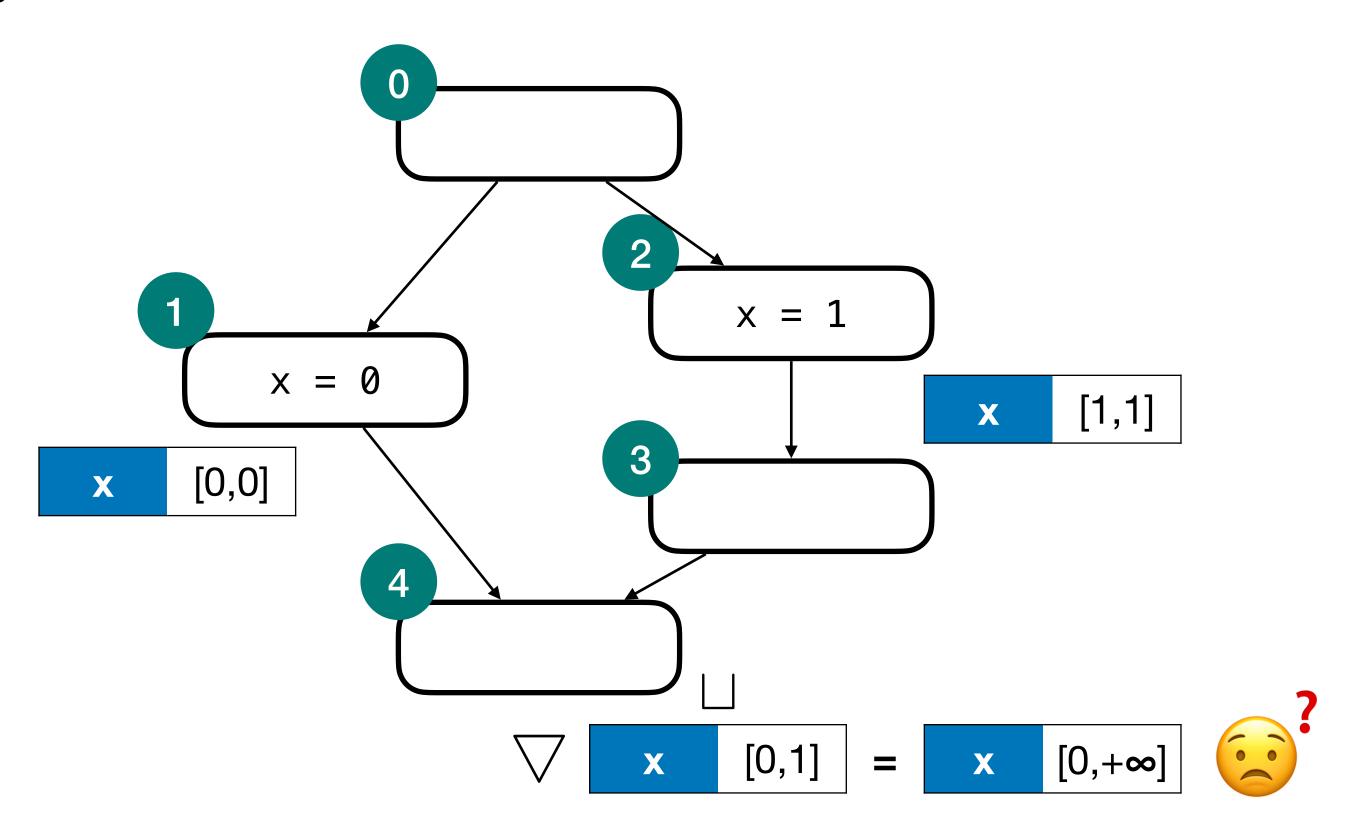
Problem 1: Overused Widening

Recall the worklist algorithm

```
X, R: \mathbb{L} \to \mathbb{M}^{\sharp}
F^{\sharp}: (\mathbb{L} \to \mathbb{M}^{\sharp}) \to (\mathbb{L} \to \mathbb{M}^{\sharp})
Worklist: \wp(\mathbb{L})
begin
     Worklist \leftarrow \mathbb{L}
    X \leftarrow \bot
    repeat
                                 Widening Everywhere?
        X \leftarrow X \nabla F^{\sharp}(X|_{Worklist})
         Worklist \leftarrow \{l \in \mathbb{L} \mid X(l) \not\sqsubseteq R(l)\}
    until Worklist = \emptyset
    return R
end
```

Problem 1: Overused Widening

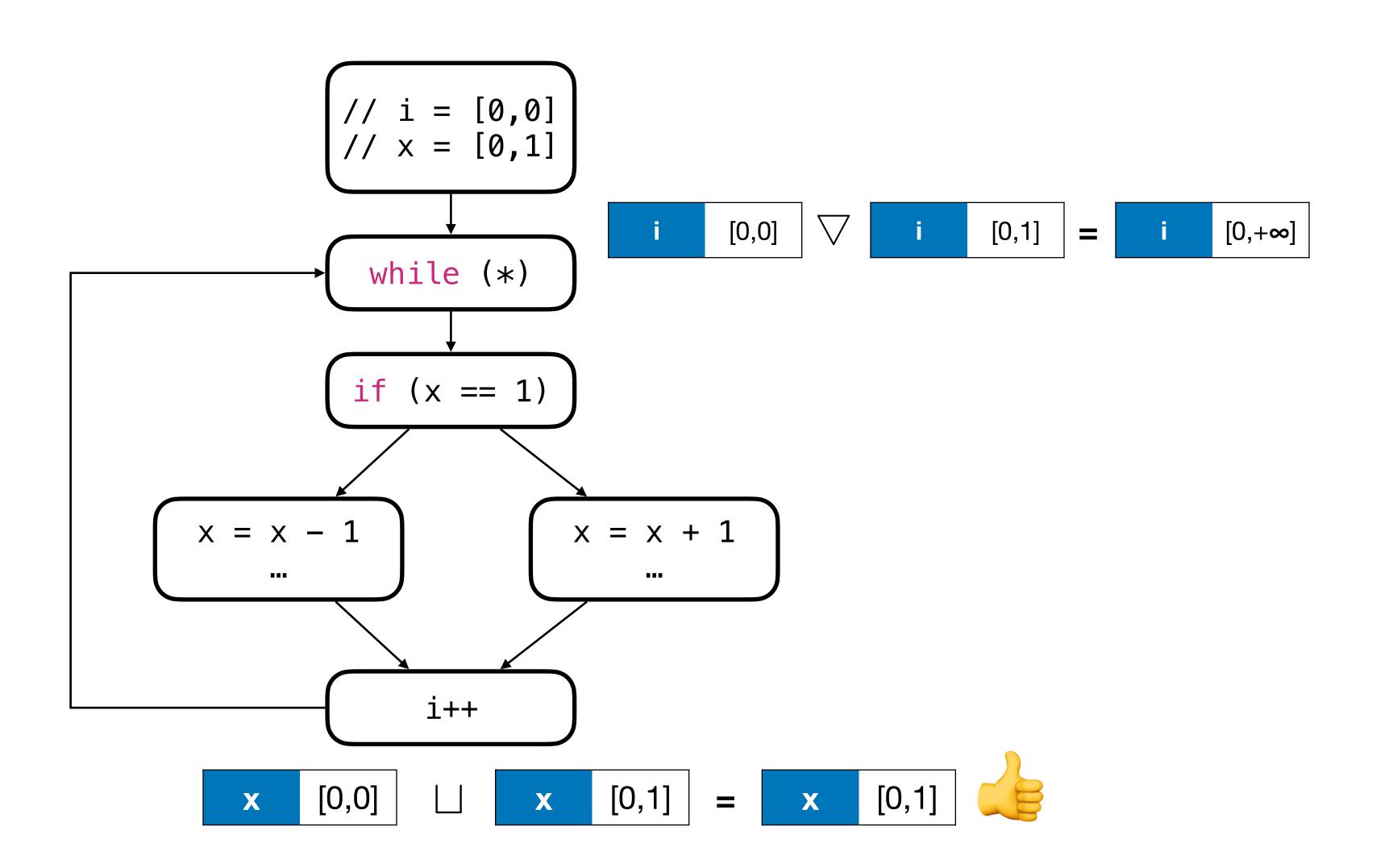
Consider an analysis with the interval abstract domain



Solution: Selective Widening

- Apply widening only when the label is the target of a cycling control flow
 - e.g., while-loop heads, targets of cycling gotos, (spurious) call-cycle
- For other labels, apply the join operation instead

Case 1: Loop Heads



Case 2: Call-cycle

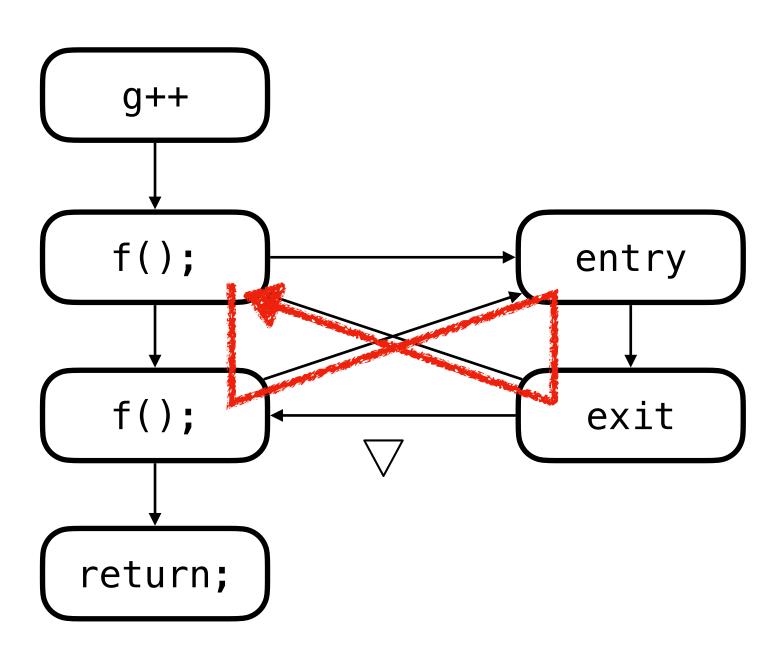
• Widening when a recursive call-cycle exists

```
void f() {
   g++;
   f();
   ...
   return;
}
```

Case 2: Call-cycle (Cont'd)

- Widening when even spurious-cycle happens
 - For example, context-insensitive analysis

```
int main() {
   g++;
   f();   // non-recursive
   f();
   return;
}
```



Caveat

- In general, cycle detection cannot be done before analysis
 - control-flow is dynamic (e.g., higher-order functions, exceptions, etc)
- Possible solutions:
 - online cycle-detection (during analysis): precise but costly
 - offline cycle-detection with pre-analysis (before analysis): imprecise but lightweight

Problem 2: Hasty Join

```
x = ?; // any value
i = 1;
while (i > 0) {
   if(x < 0 || x > 1000) {
       x = 0;
   } else {
       x = x + 1;
   }
   input(i);
}
// actually, x is in [0, 1001]
```

- The abstract value for x with a naive approach would be $[-\infty, +\infty]$
- Idea: detach the first iteration from the rest

Solution: Loop Unrolling

```
x = ?; // any value
i = 1;
while (i > 0) {
   if(x < 0 || x > 1000) {
      x = 0;
   } else {
      x = 1 + x;
   }
   input(i);
}
// actually, x is in [0, 1001]
```

```
x = ?; // any value
i = 1;
if(x < 0 || x > 1000) {
  x = 0;
} else {
  x = 1 + x;
input(i);
// x is in [0, 1001]
while (i > 0) {
  if(x < 0 | | x > 1000) {
    x = 0;
  } else {
    x = 1 + x;
  input(i);
// x is in [0, 1001]
```

Problem 3: Hasty Widening

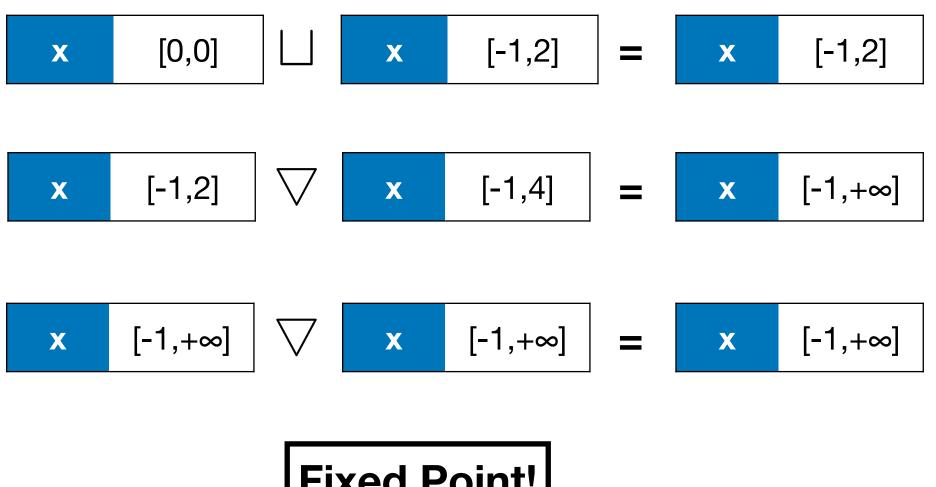
```
x = 0;
while (rand()) {
   if(rand()) {
      x = -1;
   } else {
      x = x + 2;
   }
}
// x >= -1
```

- The abstract value of x with a naive approach would be $[-\infty, +\infty]$
- Idea: delay the application of widening for the first N iterations

Solution: Delayed Widening

x = 0;while (rand()) { if(rand()) { x = -1;} else { x = x + 2; $// \times >= -1$

Delayed widening where N = 1



Problem 4: Excessive Widening

```
x = 0;
while (x <= 100) {
   if(x >= 50) {
        x = 10;
   } else {
        x = x + 1;
   }
}
// actually, x is in [0, 50]
x [0,0] \nabla x [0,2] = x [0,+∞]
```

- The abstract value of x with a naive approach is $[0, +\infty]$
- Idea: use a slower and more precise widening

Solution: Widening with Thresholds

- Take several small steps and stops at pre-defined threshold values
- For example, consider only one threshold *B*:

A naive widening operator

$$[n,p] \triangledown [n,q] = \begin{cases} [n,p] & \text{if } p \ge q \\ [n,+\infty] & \text{if } p < q \end{cases}$$

A widening with thresholds

$$[n,p] \triangledown [n,q] = \begin{cases} [n,p] & \text{if } p \ge q \\ [n,+\infty] & \text{if } p < q \end{cases}$$

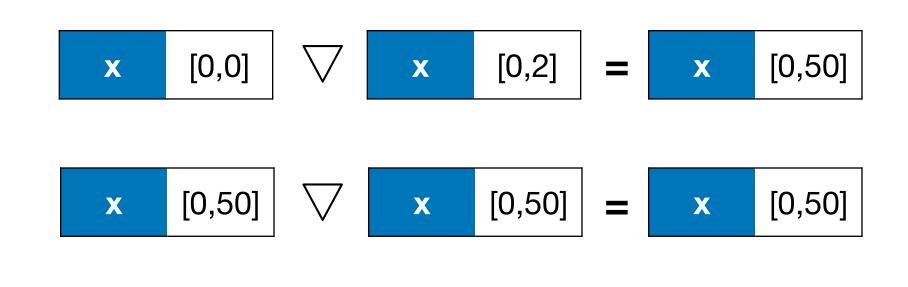
$$[n,p] \triangledown [n,q] = \begin{cases} [n,p] & \text{if } p \ge q \\ [n,B] & \text{if } p < q \le B \\ [n,+\infty] & \text{if } B < q \end{cases}$$

*only the right bounds, for brevity

Widening with Thresholds

```
x = 0;
while (x <= 100) {
   if(x >= 50) {
      x = 10;
   } else {
      x = x + 1;
   }
}
```

Thresholds = $\{50\}$



Fixed Point!

Summary

- "Loop is evil": one of the main source of imprecision
- Important to design effective iteration techniques
 - no universal solutions
 - depending on the target program's characteristics
- Need for domain knowledge (human experts or learning techniques)