



Here is the code for the binary search function:

```
def binary_search(L, v):
    """ (list, object) -> int

    Precondition: L is sorted from smallest to largest, and
    all the items in L can be compared to v.

    Return the index of the first occurrence of v in L, or
    return -1 if v is not in L.

    >>> binary_search([2, 3, 5, 7], 2)
    0
    >>> binary_search([2, 3, 5, 5], 5)
    2
    >>> binary_search([2, 3, 5, 7], 8)
    -1
    """

    b = 0
    e = len(L) - 1

    while b <= e:
        m = (b + e) // 2
        if L[m] < v:
            b = m + 1
        else:
            e = m - 1

    if b == len(L) or L[b] != v:
        return -1
    else:
        return b
```

In the above function, the main while loop continues to loop as long as  $b$  is less than  $e$ . Once  $b$  is greater than  $e$ , then our search is complete. Inside the loop, we first set  $m$  to the middle index between index  $b$  and index  $e$ . Inside the while loop, there is an if statement. If the item at position  $m$  is less than  $v$ , then we advance  $b$  to be the index just to the right of  $m$ . However, if the item at index  $m$  is greater than  $v$ , then we decrease  $e$  so that it is the index to the left of  $m$ .

Finally, at the end of our function, we have one last if statement. When the while loop ends, there are two reasons why it might have ended. First, if all the items in the list are less than  $v$ , then  $b$  will end up being equal to the length of the list, and will refer to an index outside of the list; we check whether  $b$  is equal to the length of  $L$ , and if it is, then we return  $-1$ . Finally, we check the item at location  $b$ . After all, it is possible that  $v$  is not contained in the list. If  $L[b]$  is equal to  $v$ , then we return  $b$ . Otherwise we will return  $-1$ .

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