

MESF6910J, Term 2, 2017-2018

Final Project Report

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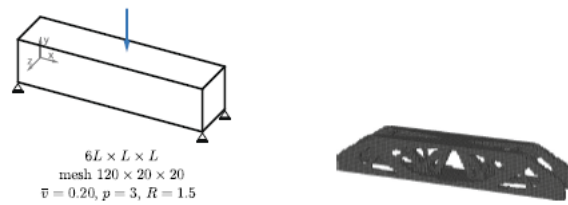
Case Description

The MBB structure is considered with one Newtown load at the middle point in its top surface. The material has a modulus of elasticity of 100 MPa and the Poisson's ratio of 0.3. The 3D SIMP topology optimization method is conducted for the minimization of the strain energy function c , defined as:

$$c(\tilde{x}) = F^T U(\tilde{x})$$

where \tilde{x} is the physical densities, F is the nodal force vector and $U(\tilde{x})$ is the vector of nodal displacements. The nodal force vector F is independent of the design variables and the nodal displacement vector $U(\tilde{x})$ is the solution of $K(\tilde{x}) U(\tilde{x}) = F$

The detail problem can be described as follows: MBB beam is supported at the four corners in its bottom surface. The support is a three-dimensional planar joint. The unit force (1 Newtown) is exerted at the middle point in its top surface and heading to downward directly. The coordinate origin is placed at the left-bottom-back corner. The Cartesian coordinate system follows the right-hand rule with its x axis follow the longitude direction. The design domain has the scale $6L \times L \times L$ with L equals to 1.0cm i.e. the domain is a cuboid with the size of $60\text{mm} \times 10\text{mm} \times 10\text{mm}$. The mesh is $120 \times 20 \times 20$. The volume fraction is set as 0.2 and penalization factor is set as 3.



Methodology

A 3D SIMP topology optimization code written in MATLAB called Top3d is given at <https://top3dapp.com>. The method is described in the paper *K. Liu and A. Tovar, "An efficient 3D topology optimization code written in Matlab", Struct Multidisc Optim, 50(6): 1175-1196, 2014, doi:10.1007/s00158-014-1107-x*. It is written intending for engineering education. The state variables and boundary condition are defined in the Matlab code. They are modified to this case by the author.

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Alternative Filters Study-Searching for the most black-and-white solution

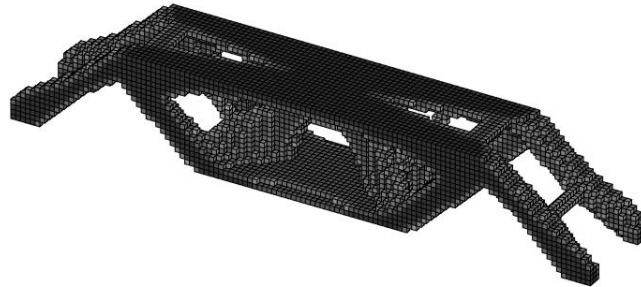
To avoid numerical instabilities like checkerboard different kinds of filters have been introduced. Different filtering techniques can result different discreteness of final solutions and eventually cause different topologies. In this case study, three different kinds of filters are implemented individually or combined. They are (i) density filter, (ii) sensitivity filter, and (iii) gray scale filter. Density filter and sensitivity filter have been studied in the Mid-term project report. Here we briefly discuss about gray scale filter and then compare the results.

Gray scale filter is a simple non-linear gray-scale filter proposed by Groenwold and Etman ^[1] to further achieve black-and-white topologies. The implementation of the gray scale filter is by changing the OC update scheme as the following

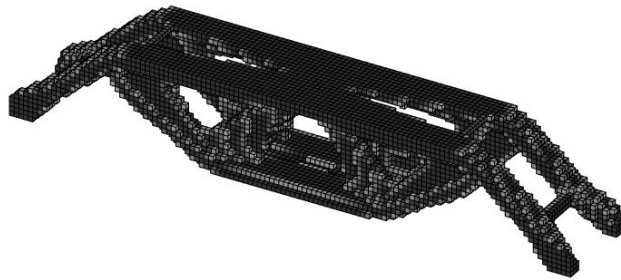
$$x_i^{new} = \begin{cases} \max(0, x_i - m), & \text{if } x_i B_i^\eta \leq \max(0, x_i - m) \\ \min(1, x_i + m), & \text{if } x_i B_i^\eta \geq \min(1, x_i + m) \\ (x_i B_i^\eta)^q, & \text{otherwise} \end{cases}$$

The standard OC updating method is a special case with $q = 1$. For the SIMP-based topology optimization the value of q is $q = 2$. The factor q should be increased gradually from a small value 1 to 2. In the program, the first fifteen loops use q equals to 1. After the fifteenth loop, q is increased by 1 percent in each loop until it equals to 2.

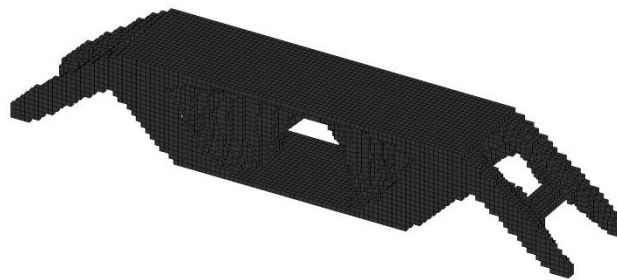
- a. Density filter only;



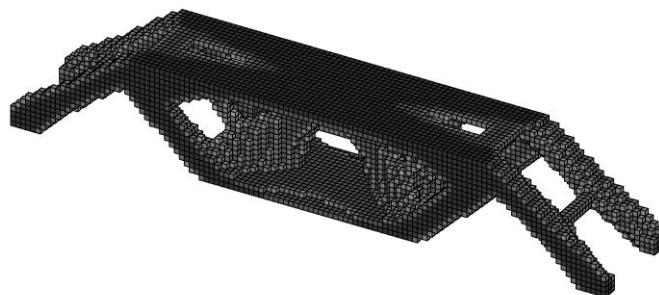
- b. Sensitivity filter only;



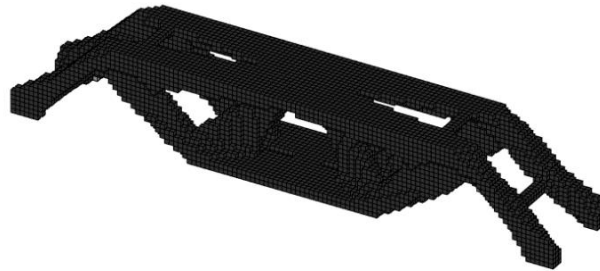
c. Grey scale filter only;



d. Density filter and grey scale filter;



Iteration:55 Volume fraction:0.2 Change: 0.008
e. Sensitivity filter and grey scale filter.



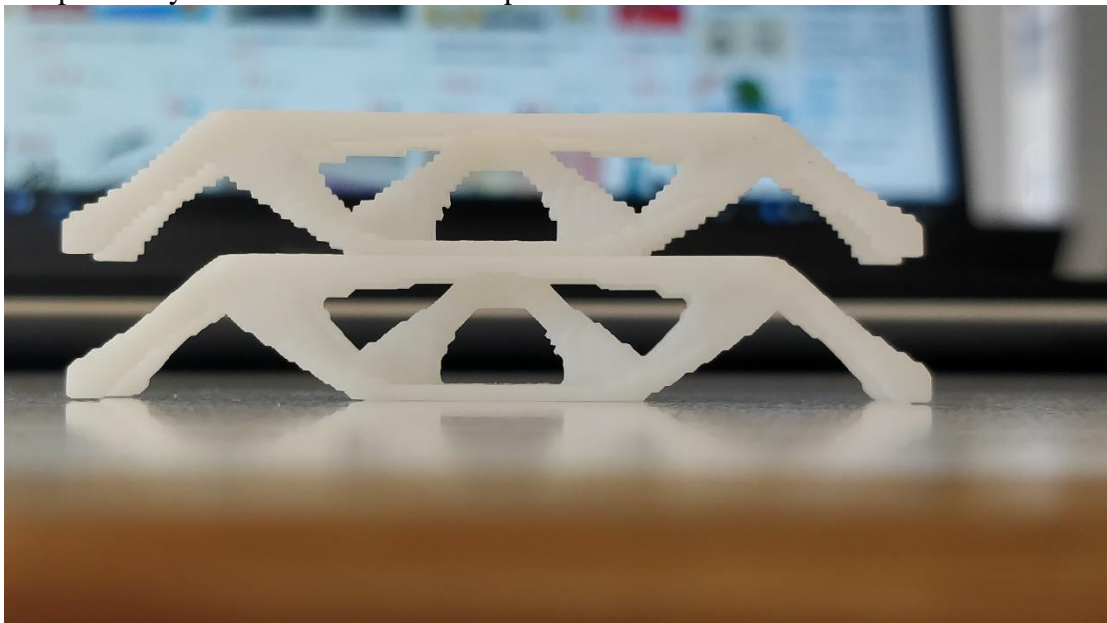
Iteration:156 Volume fraction: 0.2 Change: 0.004

According to the result figure, the Sensitivity filter and grey scale filter provides the most black-and-white solution.

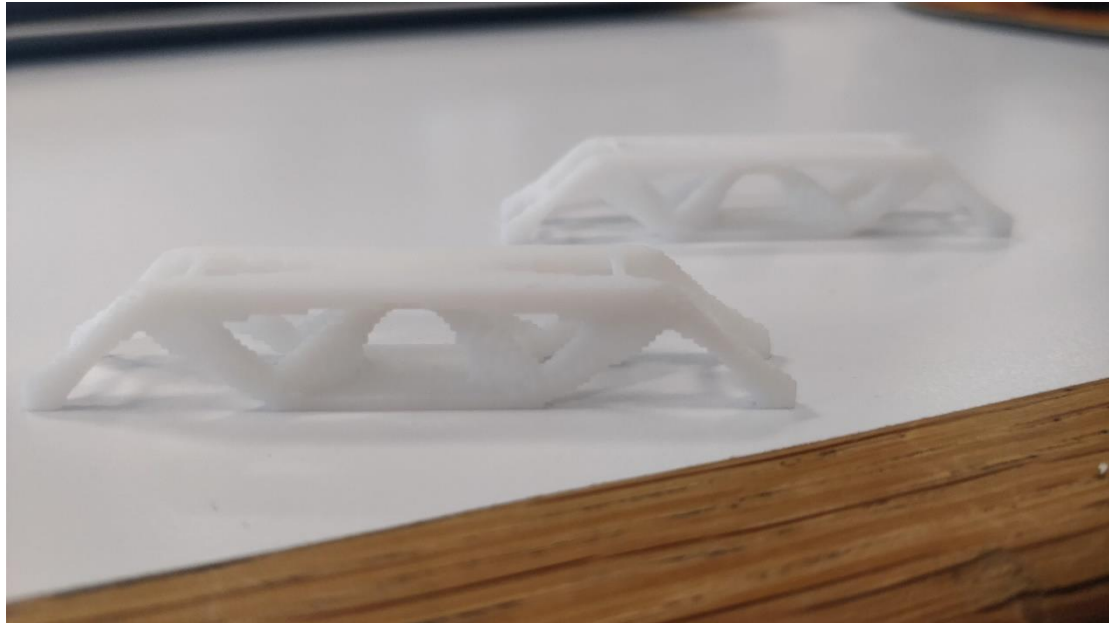
3D Printing

The model is the optimization result using the sensitivity filter and grey scale filter, which is the most black-and-white solution from the analysis above. The STL writing program use the UNITLENGTH of [0.5 0.5 0.5] since the mesh is $120 \times 20 \times 20$ and the design domain is $60\text{mm} \times 10\text{mm} \times 10\text{mm}$ which means the element unit length should be 0.5mm. The file is written in 'binary' for machine-readable. The density cutoff value leaves as 0.5.

There are two facet representations cubic and ISO. Both should be studied independently. Two models have been printed.



Top: Cubic Bottom: ISO



Left: Cubic Right: ISO

As we can see from the pictures, the ISO representation has much smoother surface. The border changes slightly. The border of cubic representation is zigzag. Almost all the angles are 90 degree.

Printing method: SLA

The printer uses stereolithography(SLA) method to print this model. SLA is a form of 3D printing technology. It creates models, prototypes, patterns and production of parts in a layer by layer fashion using photopolymerization. Photopolymerization is a process by which light causes chains of molecules to link, forming polymers. Those polymers then make-up the body of a three-dimensional solid.

3D Printer: UnionTech Lite 600 3D Printer^[2]

Manufacturing accuracy: ± 0.1 mm

Layer thickness: 0.05 - 0.25 mm

Z axis positioning accuracy: $\leq \pm 8$ μ m



UnionTech Lite 600 3D Printer

Resin material: DSM Somos® 14120

DSM's Somos® 14120^[3] is a low-viscosity liquid photopolymer that produces strong, tough and water-resistant parts. Parts created with Somos® 14120 have a white, opaque appearance similar to production plastics.

This ABS-like photopolymer is used in solid imaging processes, like stereolithography, to build three-dimensional parts. Somos® 14120 offers many properties that mimic traditional engineering plastics, including ABS and PBT. This makes the material ideal for many applications in the automotive, medical and consumer electronics markets and include functional prototypes, water-resistant applications, appearance models with minimal finishing, durable concept models, high humidity environment applications and RTV patterns

Reference

1. Groenwold AA, Etman LFP (2009) A simple heuristic for gray-scale suppression in optimality criterion-based topology optimization. Struct Multidiscip Optim 39(2):217–225
2. UnionTech Lite 600 3D Printer <http://www.uniontech3d.cn/product/download/13>
3. Somos® 14120 Datasheet.indd - DSM
https://www.dsm.com/content/dam/dsm/somos/en_US/documents/somos-14120-datasheet.pdf