

Let us assume  $P(z) = N(0, 1)$

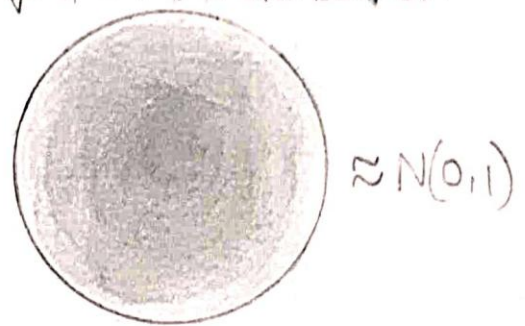
approx posterior

$$q(z|x) \approx p(z|x)$$

Gaussian distribution

$$q(z|x) = N(\mu, \sigma)$$

Variational Bayes



Optimization can be given by

Evidence lower bound (ELBO)

$$\mathcal{L}(x) = \underbrace{E_{q(z|x)} [\log p(x|z)]}_{\text{Data consistency follow } \ell_2} - \underbrace{KL(q(z|x) || P(z))}_{\text{Regularization term}}$$

Data consistency follow  $\ell_2$

Regularization term

Exp 11

## EXPERIMENTS USING VARIATIONAL AUTOENCODER

AIM

To implement a Variational Autoencoder (VAE) for the MNIST dataset learn probabilistic latent representation and evaluate.

OBJECTIVES

- \* To understand the architecture and concept of Variational Autoencoders (VAEs)
- \* To train a VAE on the MNIST dataset for unsupervised image generation and compression
- \* To compute reconstruction metrics such as MSE, PSNR, SSIM
- \* To visualize the training loss trend (Reconstruction + KL Divergence) and latent space.

PSEUDOCODE:

↳ Import necessary libraries

↳ Load MNIST Dataset

↳ Define Variational Autoencoder (VAE) model.

Encoder:

Input Image  $\rightarrow$  Flatten  $\rightarrow$  Dense  $\rightarrow \mu(\text{mean})$ ,  
 $\log \sigma^2$  ( $\log$  variance)

Sampling:

Reparameterise  $z = \mu + \sigma * \epsilon$   $\epsilon \sim N(0, 1)$

Decoder:

$z \rightarrow$  Dense  $\rightarrow$  Reconstruct image

↳ Define loss function

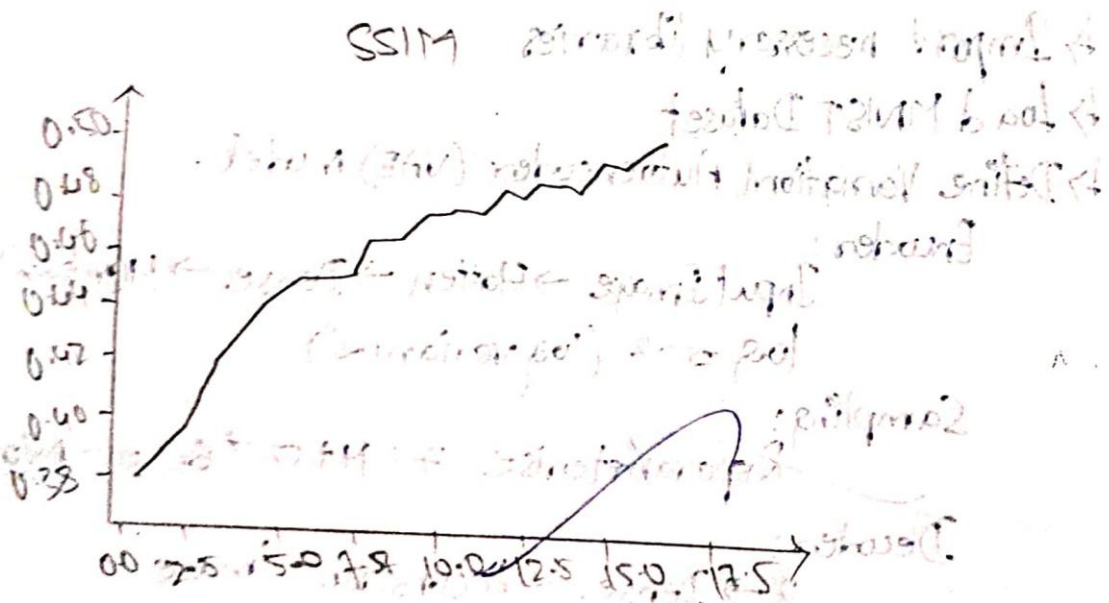
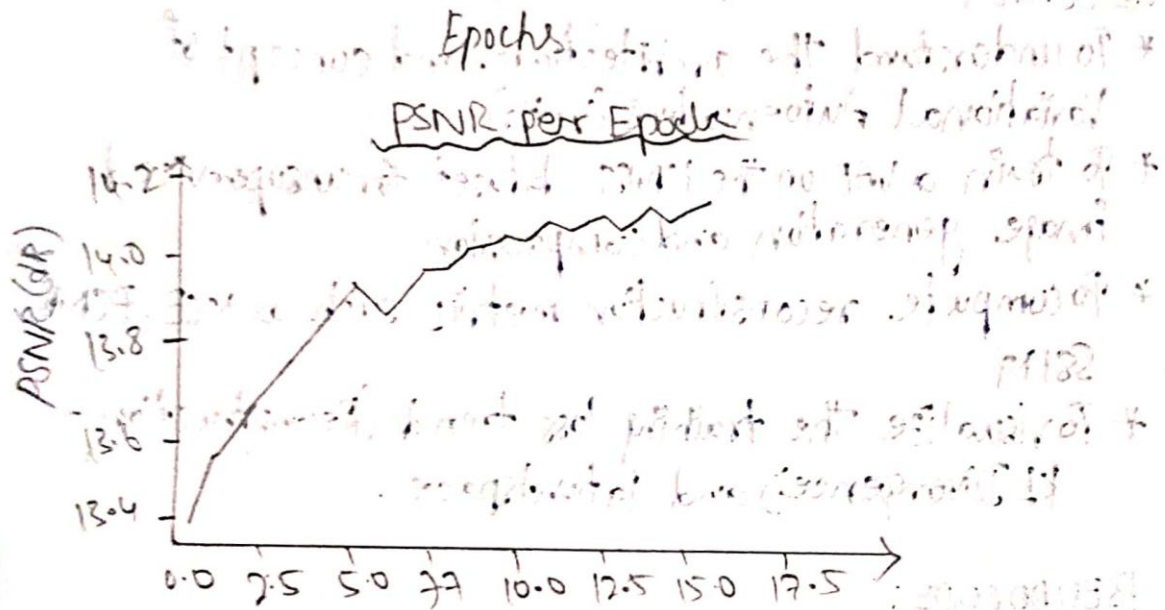
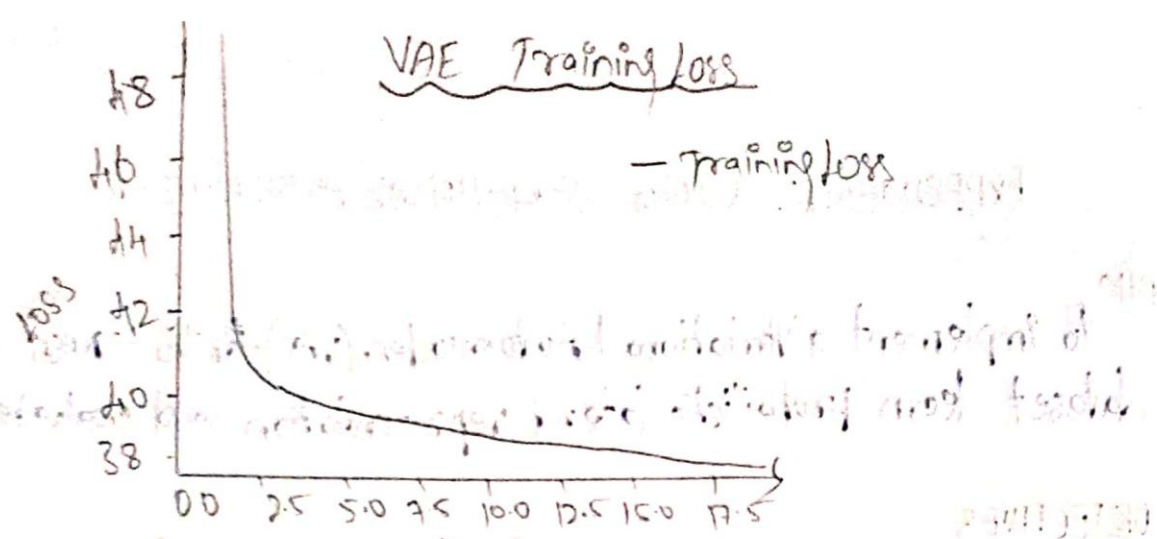
Reconstruction loss =  $MSE(x, x_{\text{reconstructed}})$

KL Divergence =  $0.5 * \sum (\mu^2 + \sigma^2 - \log \sigma^2 - 1)$

Total loss = Reconstruction +  $\beta * KL$  ( $\beta=1$ )

↳ Train for N epochs:





→ Evaluate performance:

\* Compute average MSE, PSNR, SSIM on test data.

→ Visualize:

CONCLUSIONS/OBSERVATIONS:

Epoch [1/20] | Loss: 49.2570 | PSNR: 13.347 | SSIM: 0.381

Epoch [2/20] | Loss: 42.5184 | PSNR: 13.565 | SSIM: 0.403

Epoch [3/20] | Loss: 41.4425 | PSNR: 13.672 | SSIM: 0.422

Epoch [4/20] | Loss: 40.7862 | PSNR: 13.771 | SSIM: 0.441

Epoch [5/20] | Loss: 40.3012 | PSNR: 13.864 | SSIM: 0.449.

⋮

Epoch [18/20] | Loss: 38.0021 | PSNR: 14.197 | SSIM: 0.493

Epoch [20/20] | Loss: 37.9765 | PSNR: 14.172 | SSIM: 0.499.

Final Evaluation:

Average Training Loss: 39.9563

Final PSNR: 14.172

Final SSIM: 0.499

\*\* In The models Latent Space Representant (2D) The class '9' is more scattered So we got more number of '9' in reconstruction. \*\*

RESULTS:

We have implemented a Variational Autoencoder for MNIST with 0.499 SSIM. successfully

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Lab 11: Variational Autoencoder on MNIST

```
[ ] import torch
import torch.nn as nn
import torch.optim as optim
from torchvision import datasets, transforms
from torch.utils.data import DataLoader
import matplotlib.pyplot as plt
import numpy as np
from skimage.metrics import peak_signal_noise_ratio as psnr, structural_similarity as ssim

# Device
device = torch.device("cuda" if torch.cuda.is_available() else "cpu")

[ ] import kagglehub
path = kagglehub.dataset_download("arnavsharma45/mnist-dataset")
print("Path to dataset files:", path)

Using Colab cache for faster access to the 'mnist-dataset' dataset.
Path to dataset files: /kaggle/input/mnist-dataset

Dataset Preparation

[ ] transform = transforms.Compose([
    transforms.ToTensor()
])
```

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Using Colab cache for faster access to the 'mnist-dataset' dataset.  
Path to dataset files: /kaggle/input/mnist-dataset

Dataset Preparation

```
[ ] transform = transforms.Compose([
    transforms.ToTensor()
])

train_data = datasets.MNIST(root='./data', train=True, download=True, transform=transform)
test_data = datasets.MNIST(root='./data', train=False, download=True, transform=transform)

train_loader = DataLoader(train_data, batch_size=128, shuffle=True)
test_loader = DataLoader(test_data, batch_size=128, shuffle=False)
```

Define VAE Model

```
[ ] class VAE(nn.Module):
    def __init__(self, latent_dim=2):
        super(VAE, self).__init__()
        # Encoder
        self.fc1 = nn.Linear(28*28, 400)
        self.fc21 = nn.Linear(400, latent_dim) # Mean (μ)
        self.fc22 = nn.Linear(400, latent_dim) # Log variance (logσ²)
        # Decoder
        self.fc3 = nn.Linear(latent_dim, 400)
        self.fc4 = nn.Linear(400, 28*28)
```

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        self.fc21 = nn.Linear(400, latent_dim) # Mean (μ)
        self.fc22 = nn.Linear(400, latent_dim) # Log variance (logσ²)
        # Decoder
        self.fc3 = nn.Linear(latent_dim, 400)
        self.fc4 = nn.Linear(400, 28*28)
        self.relu = nn.ReLU()
        self.sigmoid = nn.Sigmoid()

    def encode(self, x):
        h1 = self.relu(self.fc1(x))
        return self.fc21(h1), self.fc22(h1) # μ and logσ²

    def reparameterize(self, mu, logvar):
        std = torch.exp(0.5 * logvar)
        eps = torch.randn_like(std)
        return mu + eps * std # z = μ + σ * ε

    def decode(self, z):
        h3 = self.relu(self.fc3(z))
        return self.sigmoid(self.fc4(h3))
```

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Loss Function

```
[ ] def vae_loss(recon_x, x, mu, logvar):
    MSE = nn.functional.mse_loss(recon_x, x.view(-1, 28*28), reduction='sum')
    KLD = -0.5 * torch.sum(1 + logvar - mu.pow(2) - logvar.exp())
    return MSE + KLD
```

Initialize Model & Optimizer

```
[ ] model = VAE(latent_dim=2).to(device)
optimizer = optim.Adam(model.parameters(), lr=1e-3)

epochs = 20
train_losses, psnr_history, ssim_history = [], [], []
```

Training & Metric Evaluation per Epoch

```
[ ] for epoch in range(epochs):
    model.train()
    train_loss = 0

    for data, _ in train_loader:
        data = data.to(device)
        optimizer.zero_grad()
        recon_batch, mu, logvar = model(data)
        loss = vae_loss(recon_batch, data, mu, logvar)
```

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```
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train_losses, psnr_history, ssim_history = [], [], []

Training & Metric Evaluation per Epoch

for epoch in range(epochs):
    model.train()
    train_loss = 0

    for data, _ in train_loader:
        data = data.to(device)
        optimizer.zero_grad()
        recon_batch, mu, logvar = model(data)
        loss = vae_loss(recon_batch, data, mu, logvar)
        loss.backward()
        train_loss += loss.item()
        optimizer.step()

    avg_train_loss = train_loss / len(train_loader.dataset)
    train_losses.append(avg_train_loss)

    # --- Validation ---
    model.eval()
    mse_list, psnr_list, ssim_list = [], [], []
    with torch.no_grad():
        for data, _ in test_loader:
            data = data.to(device)
            recon_batch, mu, logvar = model(data)
            x_orig = data.cpu().numpy()
            x_recon = recon_batch.view(-1, 1, 28, 28).cpu().numpy()
```

```
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# --- Validation ---
model.eval()
mse_list, psnr_list, ssim_list = [], [], []
with torch.no_grad():
    for data, _ in test_loader:
        data = data.to(device)
        recon_batch, mu, logvar = model(data)
        x_orig = data.cpu().numpy()
        x_recon = recon_batch.view(-1, 1, 28, 28).cpu().numpy()

        for i in range(len(x_orig)):
            orig = x_orig[i, 0]
            rec = x_recon[i, 0]
            mse_val = np.mean((orig - rec) ** 2)
            mse_list.append(mse_val)
            psnr_list.append(psnr(orig, rec, data_range=1))
            ssim_list.append(ssim(orig, rec, data_range=1))

        psnr_history.append(np.mean(psnr_list))
        ssim_history.append(np.mean(ssim_list))

    print(f"Epoch [{epoch+1}/{epochs}] | Loss: {avg_train_loss:.4f} | "
          f"PSNR: {np.mean(psnr_list):.3f} | SSIM: {np.mean(ssim_list):.3f}")

Epoch [1/20] | Loss: 49.2570 | PSNR: 13.347 | SSIM: 0.381
Epoch [2/20] | Loss: 42.5184 | PSNR: 13.565 | SSIM: 0.483
Epoch [3/20] | Loss: 41.4425 | PSNR: 13.672 | SSIM: 0.422
Epoch [4/20] | Loss: 40.7862 | PSNR: 13.771 | SSIM: 0.441
Epoch [5/20] | Loss: 40.3012 | PSNR: 13.864 | SSIM: 0.449
Epoch [6/20] | Loss: 39.9422 | PSNR: 13.836 | SSIM: 0.451
Epoch [7/20] | Loss: 39.6417 | PSNR: 13.836 | SSIM: 0.455
```

```
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print(f"Epoch [{epoch+1}/{epochs}] | Loss: {avg_train_loss:.4f} | "
      f"PSNR: {np.mean(psnr_list):.3f} | SSIM: {np.mean(ssim_list):.3f}")

Epoch [1/20] | Loss: 49.2570 | PSNR: 13.347 | SSIM: 0.381
Epoch [2/20] | Loss: 42.5184 | PSNR: 13.565 | SSIM: 0.403
Epoch [3/20] | Loss: 41.4425 | PSNR: 13.672 | SSIM: 0.422
Epoch [4/20] | Loss: 40.7862 | PSNR: 13.771 | SSIM: 0.441
Epoch [5/20] | Loss: 40.3012 | PSNR: 13.864 | SSIM: 0.449
Epoch [6/20] | Loss: 39.9422 | PSNR: 13.836 | SSIM: 0.451
Epoch [7/20] | Loss: 39.6417 | PSNR: 13.935 | SSIM: 0.465
Epoch [8/20] | Loss: 39.4002 | PSNR: 13.942 | SSIM: 0.465
Epoch [9/20] | Loss: 39.1871 | PSNR: 13.978 | SSIM: 0.473
Epoch [10/20] | Loss: 39.0195 | PSNR: 14.015 | SSIM: 0.474
Epoch [11/20] | Loss: 38.8723 | PSNR: 14.014 | SSIM: 0.479
Epoch [12/20] | Loss: 38.7233 | PSNR: 14.031 | SSIM: 0.477
Epoch [13/20] | Loss: 38.6062 | PSNR: 14.093 | SSIM: 0.487
Epoch [14/20] | Loss: 38.4940 | PSNR: 14.084 | SSIM: 0.485
Epoch [15/20] | Loss: 38.3804 | PSNR: 14.108 | SSIM: 0.489
Epoch [16/20] | Loss: 38.2775 | PSNR: 14.130 | SSIM: 0.490
Epoch [17/20] | Loss: 38.2031 | PSNR: 14.103 | SSIM: 0.489
Epoch [18/20] | Loss: 38.0947 | PSNR: 14.181 | SSIM: 0.497
Epoch [19/20] | Loss: 38.0021 | PSNR: 14.147 | SSIM: 0.493
Epoch [20/20] | Loss: 37.9765 | PSNR: 14.172 | SSIM: 0.499

Evaluation

print("\n Final Evaluation:")
print(f"Average Training Loss: {np.mean(train_losses):.4f}")
print(f"Final PSNR: {psnr_history[-1]:.3f}")
print(f"Final SSIM: {ssim_history[-1]:.3f}")
```

```
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Evaluation

print("\n Final Evaluation:")
print(f"Average Training Loss: {np.mean(train_losses):.4f}")
print(f"Final PSNR: {psnr_history[-1]:.3f}")
print(f"Final SSIM: {ssim_history[-1]:.3f}")

Final Evaluation:
Average Training Loss: 39.7563
Final PSNR: 14.172
Final SSIM: 0.499

Visualizations

# (a) Loss Curve
plt.figure(figsize=(6,4))
plt.plot(train_losses, label="training loss", color='tab:red', linewidth=2)
plt.xlabel("epochs"); plt.ylabel("loss")
plt.title("VAE Training Loss")
plt.legend(); plt.grid(True)
plt.show()

# (b) PSNR Curve
plt.figure(figsize=(6,4))
plt.plot(psnr_history, label="PSNR", color='tab:blue', marker='o')
plt.xlabel("epochs"); plt.ylabel("PSNR (db)")
```



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Final PSNR: 19.172  
Final SSIM: 0.499

Visualizations

```
[ ] # (a) Loss Curve
plt.figure(figsize=(6,4))
plt.plot(train_losses, label="training loss", color='tab:red', linewidth=2)
plt.xlabel("Epochs"); plt.ylabel("Loss")
plt.title("VAE training loss")
plt.legend(); plt.grid(True)
plt.show()

# (b) PSNR Curve
plt.figure(figsize=(6,4))
plt.plot(psnr_history, label="PSNR", color='tab:blue', marker='o')
plt.xlabel("Epochs"); plt.ylabel("PSNR (dB)")
plt.title("PSNR per Epoch")
plt.legend(); plt.grid(True)
plt.show()

# (c) SSIM Curve
plt.figure(figsize=(6,4))
plt.plot(ssim_history, label="SSIM", color='tab:green', marker='s')
plt.xlabel("Epochs"); plt.ylabel("SSIM")
plt.title("SSIM per Epoch")
plt.legend(); plt.grid(True)
plt.show()
```

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```
[ ] # (c) SSIM Curve
plt.figure(figsize=(6,4))
plt.plot(ssim_history, label="SSIM", color='tab:green', marker='s')
plt.xlabel("Epochs"); plt.ylabel("SSIM")
plt.title("SSIM per Epoch")
plt.legend(); plt.grid(True)
plt.show()

# (d) Reconstruction Visualization
test_iter = iter(test_loader)
test_imgs, _ = next(test_iter)
test_imgs = test_imgs.to(device)
reconstructed, _ = model(test_imgs)
reconstructed = reconstructed.view(-1, 1, 28, 28).cpu().detach()

fig, axes = plt.subplots(2, 10, figsize=(12, 3))
for i in range(10):
    axes[0, i].imshow(test_imgs[i, 0].cpu(), cmap='gray')
    axes[0, i].axis('off')
    axes[1, i].imshow(reconstructed[i, 0], cmap='gray')
    axes[1, i].axis('off')
axes[0, 0].set_title("Original")
axes[1, 0].set_title("Reconstructed")
plt.suptitle("VAE Reconstruction Results")
plt.show()

# (e) Latent Space Visualization
with torch.no_grad():
    mu_vals, labels = [], []
```

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