

Figure 1: The Exact solution compared to the numeric approximation of Problem 1.

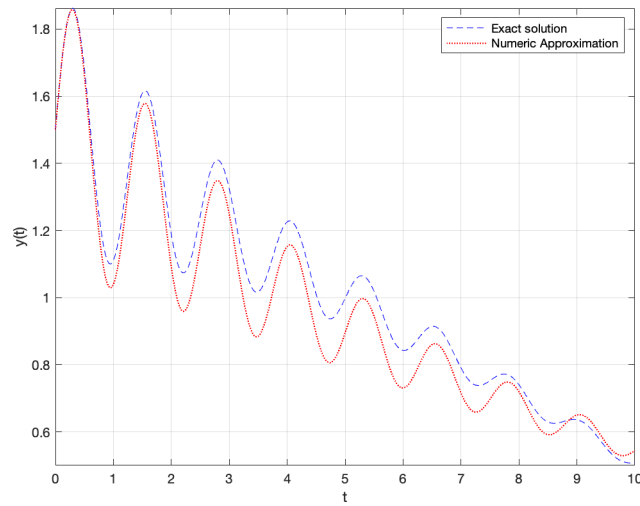


Figure 2: The Exact solution compared to the numeric approximation in Problem 2.

```

1  #include "main.h"
2
3  /*****
4   * Function Title: main
5   * Summary: This function facilitates the selection and calling of a problem
6   *           function and prints relevant error statements
7   *
8   * Inputs:
9   *   int argc: the amount of arguments passed to main
10  *   char** argv: the arguments passed as a string to main
11  * Outputs:
12  *   int: an error code to the operating system on program execution
13  *
14  * Compile Instructions: gcc main.c -o main
15  *****/
16  * Pseudocode
17  *   Begin

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18 *     if there was no number passed in the command line
19 *     prompt input for problem selection
20 *     else
21 *         convert command line input
22 *     call correct problem number 1,2, or 3
23 *     call function
24 *     if it returns error
25 *         print Error
26 *     else
27 *         print success
28 *     End
29 *****/
30 int main(int argc, char** argv) {
31     // Begin Program
32     int problem;
33     // If no arguments prompt and receive input
34     if (argc < 2) {
35         printf("Enter problem number: "); // Prompt user to select problem
36         scanf("%d", &problem);           // accept user input
37     } else {
38         // else use command line argument
39         problem = atoi(argv[1]); // Assign the value from the command line
40     }
41     // Do the selected problem
42     switch (
43         problem) { // if the problem fails to make a file print Error statement
44     case 1:
45         (problem_1() == 0) ? printf("Problem 1 success\n")
46                             : printf("Error in Problem 1\n");
47         break;
48     case 2:
49         (problem_2() == 0) ? printf("Problem 2 success\n")
50                             : printf("Error in Problem 2\n");
51         break;
52     case 3:
53         (problem_3() == 0) ? printf("Problem 3 success\n")
54                             : printf("Error in Problem 3\n");
55         break;
56     default:
57         printf("Error please choose 1-3.\n");
58     }
59     // End Program
60     return EXIT_SUCCESS;
61 }
62
63 // Problem 1 Code
64 int problem_1(void) {
65     FILE* fout = fopen("prog_sol_1.txt", "w");
66     if (fout == NULL) {
67         perror("output file failed");
68         return EXIT_FAILURE;
69     }
70     // Declare and Initialize variables
71     double y      = 3.0;
72     double delta_t = 0.001;
73     double time    = 0;
74     double a       = -2.5;
75     // This line doesn't change in the loop
76     a = (1 + a * delta_t);
77     // Do the math iteratively in a loop

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78     for (time = 0.0; time < 10.0; time += delta_t) {
79         // Print the t, y(t) coordinate
80         fprintf(fout, "%0.31f\t%0.101f\n", time, y);
81         // Do the calculation
82         y = a * y;
83     }
84     return EXIT_SUCCESS;
85 }
86
87 // Problem 2 Code
88 int problem_2(void) {
89     FILE* fout = fopen("prog_sol_2.txt", "w");
90     if (fout == NULL) {
91         perror("output file failed");
92         return EXIT_FAILURE;
93     }
94     double I[][3] = {{1, 0, 0}, {0, 1, 0}, {0, 0, 1}};
95     double A[][3] = {{0, 1, 0}, {0, 0, 1}, {-2.5063, -25.1125, -0.6}};
96     double x_t[3] = {1.5, 2, -1};
97     double delta_t = 0.001f;
98     double time;
99     // avoid unnecessary function calls in loop
100    mat_scale(delta_t, A, A);
101    mat_add(I, A, A);
102    // Do iterative math
103    for (time = 0.0; time < 10.0; time += delta_t) {
104        // print the result
105        fprintf(fout, "%.31f\t%.101f\n", time, x_t[0]);
106        // get next x_t value
107        mat_vec_mult(A, x_t, x_t);
108    }
109    return EXIT_SUCCESS;
110 }
111
112 // Problem 3 Code
113 int problem_3(void) {
114     FILE* fout = fopen("prog_sol_3.txt", "w");
115     if (fout == NULL) {
116         perror("output file failed");
117         return EXIT_FAILURE;
118     }
119
120     return EXIT_SUCCESS;
121 }
122
123 // scale matrix 'mat' by a and save in prod
124 void mat_scale(double scale, double mat[][3], double prod[][3]) {
125     int i, j;
126     for (i = 0; i < 3; ++i) {
127         for (j = 0; j < 3; ++j) {
128             prod[i][j] = scale * mat[i][j];
129         }
130     }
131 }
132
133 // subtract the right from the left and store in diff
134 void mat_sub(double left[][3], double right[][3], double diff[][3]) {
135     int i, j;
136     for (i = 0; i < 3; i++) {
137         for (j = 0; j < 3; j++) {

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138     diff[i][j] = left[i][j] - right[i][j];
139 }
140 }
141 }
142
143 // add the right and the left and store into sum
144 void mat_add(double left[][3], double right[][3], double sum[][3]) {
145     int i, j;
146     for (i = 0; i < 3; i++) {
147         for (j = 0; j < 3; j++) {
148             sum[i][j] = left[i][j] + right[i][j];
149         }
150     }
151 }
152
153 // Unsafe if used incorrectly!
154 // multiplies 3x3 matrix mat with 3x1 vector storing into 3x1 prod
155 void mat_vec_mult(double mat[][3], double* vector, double* prod) {
156     double sum;
157     int i, j;
158     for (i = 0; i < 3; i++) {
159         sum = 0;
160         for (j = 0; j < 3; j++) {
161             sum += mat[i][j] * vector[j];
162         }
163         prod[i] = sum;
164     }
165 }

```