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# PENYELESAIAN KASUS 8-PUZZLE, 8- QUEEN MENGGUNAKAN BFS DAN DFS

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Anggota Kelompok :

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## BSF

Algoritma pencarian secara melebar dengan menggunakan queue untuk menyimpan node.

### Keuntungan :

- Tidak akan menemui jalan buntu.
- Jika ada satu solusi, maka BFS akan menemukannya. Dan jika ada lebih dari satu solusi, maka solusi minimum akan ditemukan.

### Kekurangan :

- Membutuhkan memori yang cukup banyak, karena menyimpan semua node dalam satu pohon.
- Membutuhkan waktu yang cukup lama, karena akan menguji  $n$  level untuk mendapatkan solusi pada level ke- $(n+1)$ .

## DFS

Algoritma pencarian secara mendalam dengan menggunakan stack untuk menyimpan node.

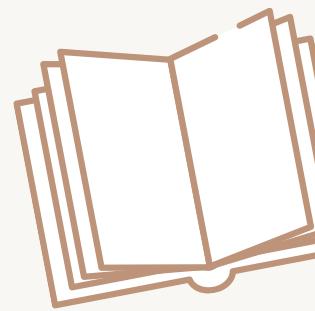
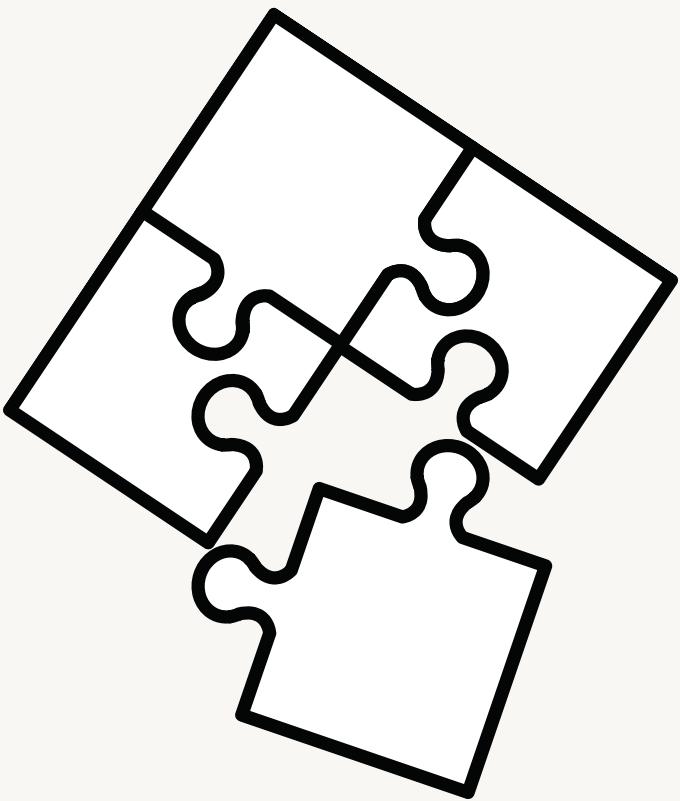
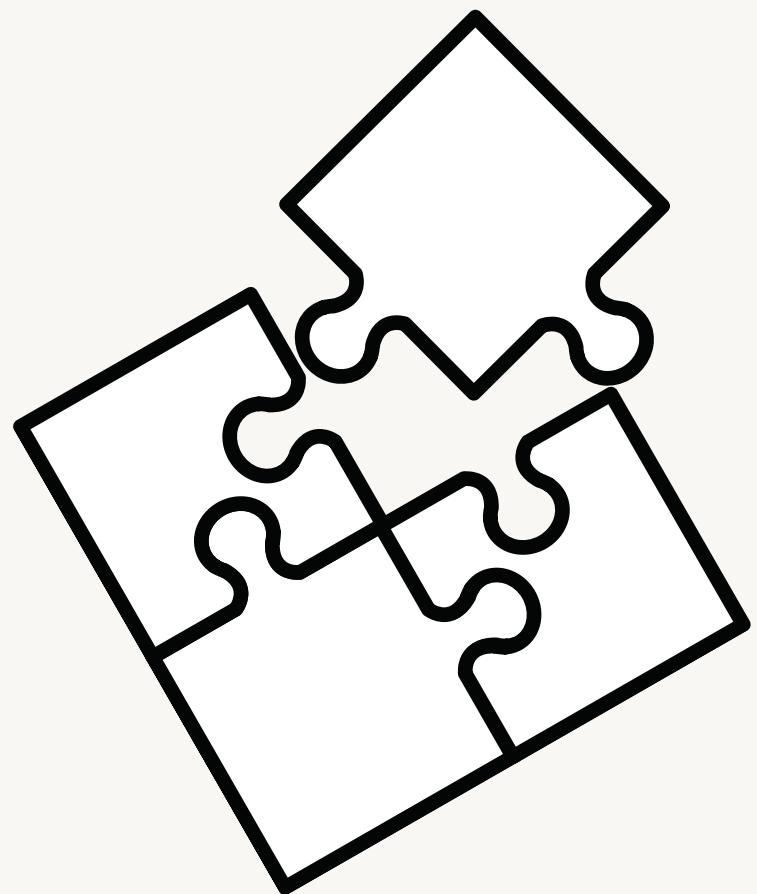
### Keuntungan :

- Pemakain memori hanya sedikit karena tidak menyimpan semua node yang pernah dibangkitkan.
- Jika solusi yang dicari berada pada level yang dalam dan paling kiri, maka DFS akan menemukannya secara cepat.

### Kekurangan :

- Jika pohon yang dibangkitkan mempunyai level yang dalam (tak terhingga), maka tidak ada jaminan untuk menemukan solusi (Tidak Complete).

# 8 Puzzle (DFS)



Initial state:

1	2	-
3	4	5
6	7	8

Edit state

-	1	2
3	4	5
6	7	8

Edit state

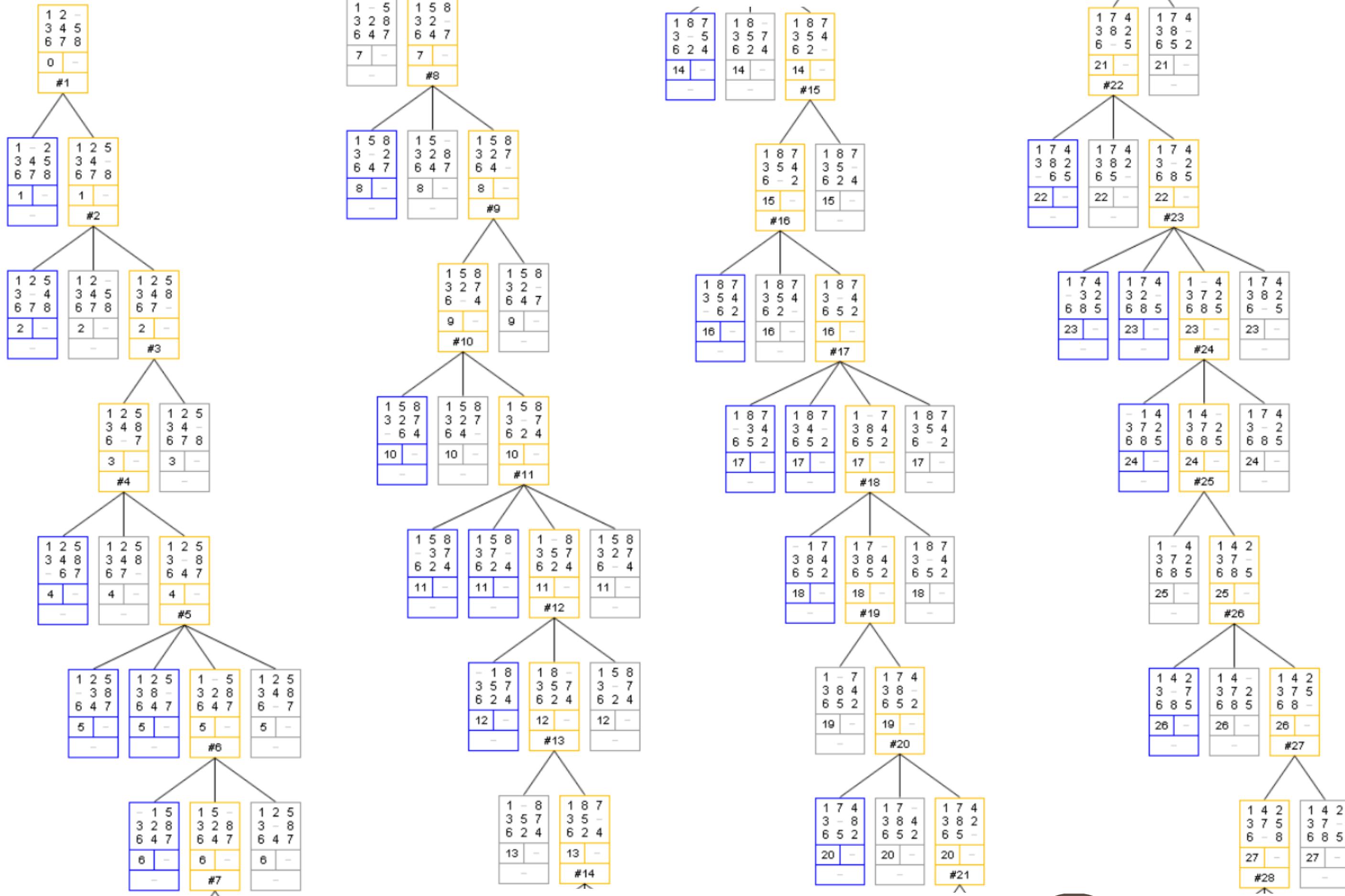
Goal state:

-	1	2
3	4	5
6	7	8

Edit state

Search algorithm:

Depth-first search



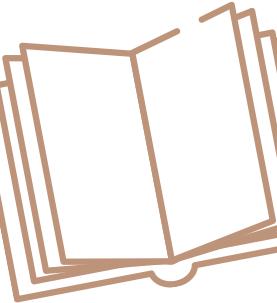
# Code DFS



```
#DFS
def dfs(startState):

    global GoalNode

    boardVisited = set()
    stack = list([PuzzleState(startState, None, None, 0, 0, 0)])
    while stack:
        node = stack.pop()
        boardVisited.add(node.map)
        if node.state == GoalState:
            GoalNode = node
            return stack
        #inverse the order of next paths for execution purposes
        possiblePaths = reversed(subNodes(node))
        for path in possiblePaths:
            if path.map not in boardVisited:
                stack.append(path)
                boardVisited.add(path.map)
```



```
7     class PuzzleState:
8         def __init__(self, state, parent, move, depth, cost):
9             self.state = state
10            self.parent = parent
11            self.move = move
12            self.depth = depth
13            self.cost = cost
14            if self.state:
15                self.map = ''.join(str(e) for e in self.state)
16        def __eq__(self, other):
17            return self.map == other.map
18        def __lt__(self, other):
19            return self.map < other.map
20        def __str__(self):
21            return str(self.map)
22
23 #Global variables
24 GoalState = [0, 1, 2, 3, 4, 5, 6, 7, 8]
25 GoalNode = None # at finding solution
26 NodesExpanded = 0 #total nodes visited
27 MaxSearchDeep = 0 #max deep
```

# Code DFS

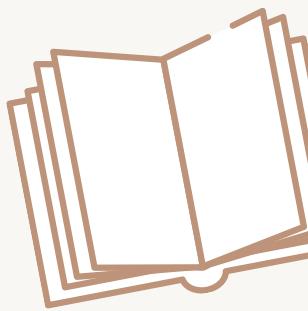
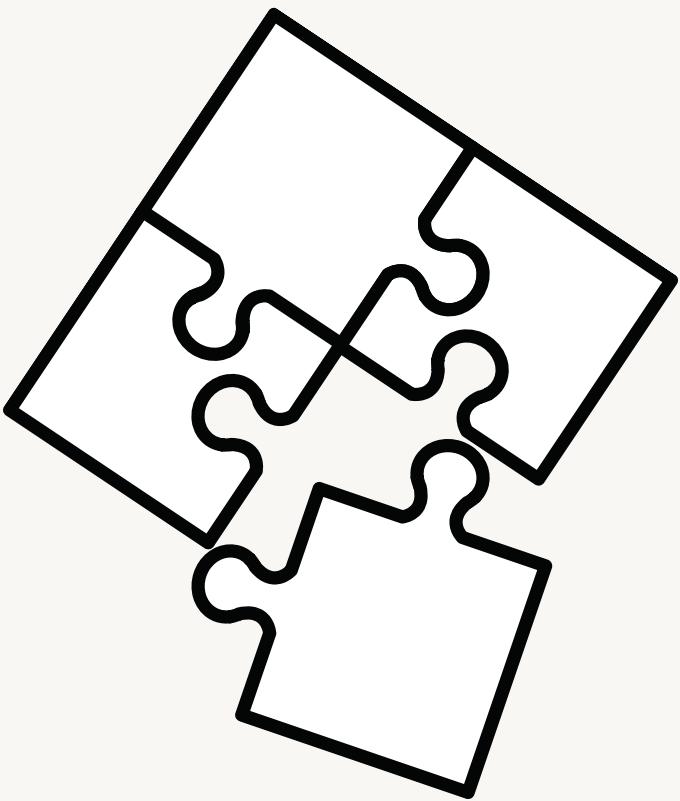
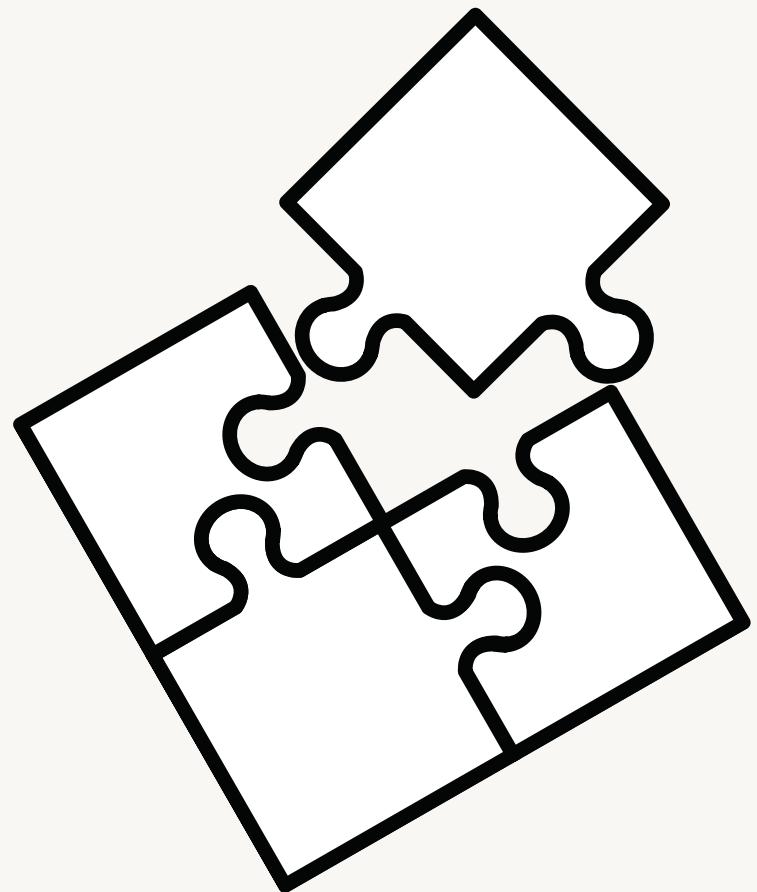


```
53 def subNodes(node):
54
55     global NodesExpanded
56     NodesExpanded = NodesExpanded+1
57
58     nextPaths = []
59     nextPaths.append(PuzzleState(move(node.state, 1), node, 1, node.depth + 1, node.cost + 1, 0))
60     nextPaths.append(PuzzleState(move(node.state, 2), node, 2, node.depth + 1, node.cost + 1, 0))
61     nextPaths.append(PuzzleState(move(node.state, 3), node, 3, node.depth + 1, node.cost + 1, 0))
62     nextPaths.append(PuzzleState(move(node.state, 4), node, 4, node.depth + 1, node.cost + 1, 0))
63     nodes=[]
64     for procPaths in nextPaths:
65         if(procPaths.state!=None):
66             nodes.append(procPaths)
67     return nodes
```

```
239 #Start operation
240 start = timeit.default_timer()
241
242 dfs(Initialstate)
243
244 stop = timeit.default_timer()
245 time = stop-start
246
247 #Save total path result
248 deep=GoalNode.depth
249 moves = []
250 while InitialState != GoalNode.state:
251     if GoalNode.move == 1:
252         path = 'Up'
253     if GoalNode.move == 2:
254         path = 'Down'
255     if GoalNode.move == 3:
256         path = 'Left'
257     if GoalNode.move == 4:
258         path = 'Right'
259     moves.insert(0, path)
260     GoalNode = GoalNode.parent
261
262 #Print results
263 print("path: ",moves)
264 print("cost: ",len(moves))
265 print("nodes expanded: ",str(NodesExpanded))
266 print("search_depth: ",str(deep))
267 print("MaxSearchDeep: ",str(MaxSearchDeep))
268 print("running_time: ".format(time, '.8f'))
```

```
PS C:\Users\abdur\Downloads\8puzzledfs\8puzzledfs> python 8puzzle_dfs.py 1,2,5,3,4,8,6,7,0
path: [ 'Up', 'Up', 'Left', 'Left' ]
cost: 4
nodes expanded: 181437
search_depth: 4
running_time: 2.23132810
```

# 8 Puzzle (BFS)





## N-Puzzle

Initial state:

3	1	2
4	-	5
6	7	8

Edit state

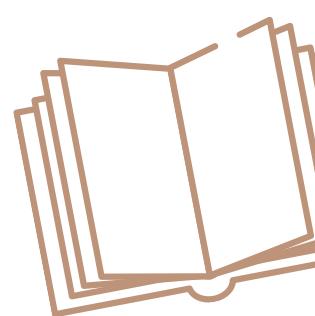
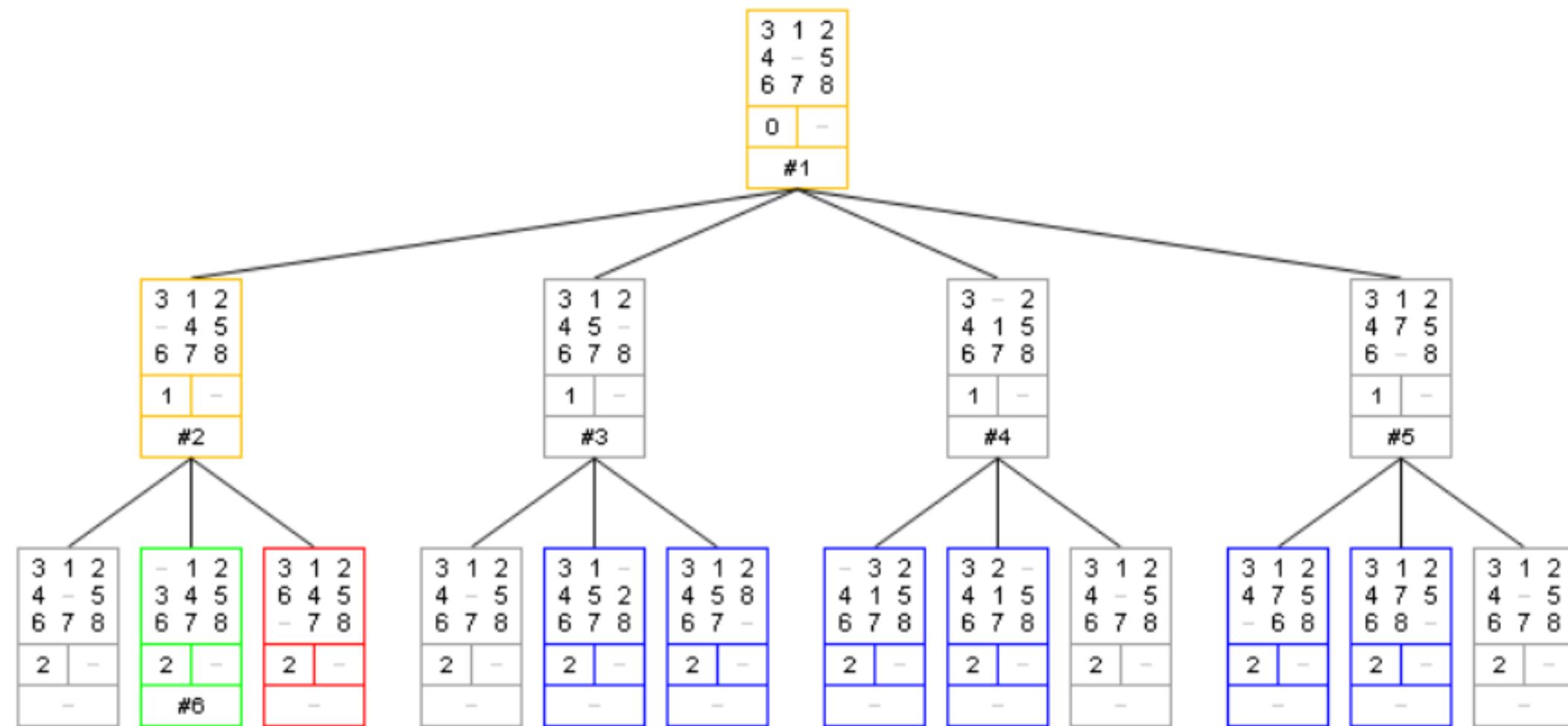
Goal state:

-	1	2
3	4	5
6	7	8

Edit state

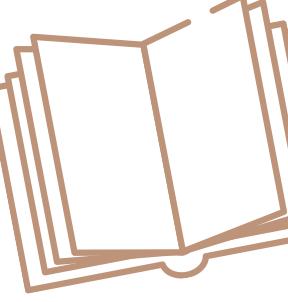
Search algorithm:

Breadth-first search

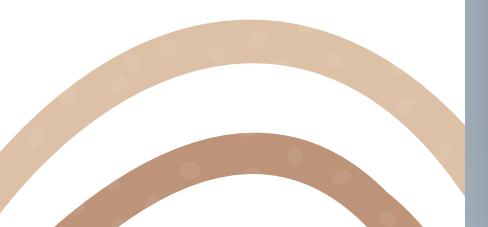




```
1 int main(void)
2 {
3
4     State initial; // initial board state
5     State goalState; // goal board configuration
6
7     // solution path of each search method
8     SolutionPath *bfs;
9
10    // input initial board state
11    printf("INITIAL STATE:\n");
12    inputState(&initial);
13
14    // input the goal state
15    printf("\nGOAL STATE:\n");
16    inputState(&goalState);
17
18    printf("INITIAL BOARD STATE:\n");
19    printBoard(initial.board);
20
21    printf("GOAL BOARD STATE:\n");
22    printBoard(goalState.board);
23
24    // perform breadth-first search
25    bfs = BFS_search(&initial, &goalState);
26    printf("\nBFS ALGORITHM\n");
27    printSolution(bfs);
28
29    return 0;
30 }
```



```
1 void inputState(State *const state)
2 {
3     state->action = NOT_APPLICABLE;
4     char row, col;
5     int symbol;
6
7     // flags for input validation
8     char isNumUsed[9] = {0};
9
10    for (row = 0; row < 3; ++row)
11    {
12        for (col = 0; col < 3; ++col)
13        {
14            printf("    board[%i][%i]: ", row, col);
```



```
1 printf("SOLUTION: \n");
2
3 // will use hash map to speed up the process a bit
4 char *move[4] = {"UP", "DOWN", "LEFT", "RIGHT"};
5 int counter = 1;
6
7 // will be skipping the first node since it represents the initial state with no action
8 for (path = path->next; path; path = path->next, ++counter)
9 {
10    printf("%i. Move %s\n", counter, move[path->action]);
11}
12
13 printf(
14 "DETAILS:\n"
15 " - Solution length : %i\n"
16 " - Nodes expanded : %i\n"
17 " - Nodes generated : %i\n"
18 " - Runtime         : %g milliseconds\n"
19 " - Memory used    : %i bytes\n", // only counting allocated 'Node's
20     solutionLength, nodesExpanded, nodesGenerated, runtime, nodesGenerated * sizeof(Node));
21 }
22 }
```

```
1 SolutionPath *BFS_search(State *initial, State *goal)
2 {
3     NodeList *queue = NULL;
4     NodeList *children = NULL;
5     Node *node = NULL;
6
7     // start timer
8     clock_t start = clock();
9
10    // initialize the queue with the root node of the search tree
11    pushNode(createNode(0, manhattanDist(initial, goal), initial, NULL), &queue);
12    Node *root = queue->head->currNode; // for deallocating the generated tree
13
14    // while there is a node in the queue to expand
15    while (queue->nodeCount > 0)
16    {
17        // pop the last node (tail) of the queue
18        node = popNode(&queue);
19
20        // if the state of the node is the goal state
21        if (statesMatch(node->state, goal))
22            break;
23
24        // else, expand the node and update the expanded-nodes counter
25        children = getChildren(node, goal);
26        ++nodesExpanded;
27        // add the node's children to the queue
28        pushList(&children, queue);
29    }
30
31    // determine the time elapsed
32    runtime = (double)(clock() - start) / CLOCKS_PER_SEC;
33}
```

```
1
2     // get solution path in order from the root, if it exists
3     SolutionPath *pathHead = NULL;
4     SolutionPath *newPathNode = NULL;
5
6     while (node)
7     {
8         newPathNode = malloc(sizeof(SolutionPath));
9         newPathNode->action = node->state->action;
10        newPathNode->next = pathHead;
11        pathHead = newPathNode;
12
13        // update the solution length and move on the next node
14        ++solutionLength;
15        node = node->parent;
16    }
17
18    --solutionLength; // uncount the root node
19    return pathHead;
20}
```



```
1 Node *createNode(unsigned int d, unsigned int h, State *s, Node *p)
2 {
3     Node *newNode = malloc(sizeof(Node));
4     if (newNode)
5     {
6         newNode->depth = d;
7         newNode->hCost = h;
8         newNode->state = s;
9         newNode->parent = p;
10        newNode->children = NULL;
11        ++nodesGenerated; // update counter
12    }
13    return newNode;
14 }
```



```
1 int totalCost(Node *const node)
2 {
3     return node->depth + node->hCost;
4 }
```



```
1 NodeList *getChildren(Node *parent, State *goalState)
2 {
3     NodeList *childrenPtr = NULL;
4     State *testState = NULL;
5     Node *child = NULL;
6     // attempt to create states for each moves, and add to the list of children if true
7     if (parent->state->action != DOWN && (testState = createState(parent->state, UP)))
8     {
9         child = createNode(parent->depth + 1, manhattanDist(testState, goalState), testState, parent);
10        pushNode(child, &parent->children);
11        pushNode(child, &childrenPtr);
12    }
13    if (parent->state->action != UP && (testState = createState(parent->state, DOWN)))
14    {
15        child = createNode(parent->depth + 1, manhattanDist(testState, goalState), testState, parent);
16        pushNode(child, &parent->children);
17        pushNode(child, &childrenPtr);
18    }
19    if (parent->state->action != RIGHT && (testState = createState(parent->state, LEFT)))
20    {
21        child = createNode(parent->depth + 1, manhattanDist(testState, goalState), testState, parent);
22        pushNode(child, &parent->children);
23        pushNode(child, &childrenPtr);
24    }
25    if (parent->state->action != LEFT && (testState = createState(parent->state, RIGHT)))
26    {
27        child = createNode(parent->depth + 1, manhattanDist(testState, goalState), testState, parent);
28        pushNode(child, &parent->children);
29        pushNode(child, &childrenPtr);
30    }
31    return childrenPtr;
32 }
```

```

1 #define BLANK_CHARACTER '0'

2

3 typedef enum Move {
4     UP, DOWN, LEFT, RIGHT,
5     NOT_APPLICABLE
6 } Move;

7

8 typedef struct State {
9     Move action;
10    char board[3][3];
11 } State;

```

```

1 State* createState(State *state, Move move) {
2     State *newState = malloc(sizeof(State));
3
4     char i, j;
5     char row, col;
6
7     for(i = 0; i < 3; ++i) {
8         for(j = 0; j < 3; ++j) {
9             if(state->board[i][j] == BLANK_CHARACTER) {
10                 row = i;
11                 col = j;
12             }
13             newState->board[i][j] = state->board[i][j];
14         }
15     }
16
17     if(move == UP && row - 1 >= 0) {
18         char temp = newState->board[row - 1][col];
19         newState->board[row - 1][col] = BLANK_CHARACTER;
20         newState->board[row][col] = temp;
21         newState->action = UP;
22         return newState;
23     }
24     else if(move == DOWN && row + 1 < 3) {
25         char temp = newState->board[row + 1][col];
26         newState->board[row + 1][col] = BLANK_CHARACTER;
27         newState->board[row][col] = temp;
28         newState->action = DOWN;
29         return newState;
30     }
31     else if(move == LEFT && col - 1 >= 0) {
32         char temp = newState->board[row][col - 1];
33         newState->board[row][col - 1] = BLANK_CHARACTER;
34         newState->board[row][col] = temp;
35         newState->action = LEFT;
36         return newState;
37     }
38     else if(move == RIGHT && col + 1 < 3) {
39         char temp = newState->board[row][col + 1];
40         newState->board[row][col + 1] = BLANK_CHARACTER;
41         newState->board[row][col] = temp;
42         newState->action = RIGHT;
43         return newState;
44     }
45     free(newState);
46     return NULL;
47 }

```

```

INITIAL STATE:
board[0][0]: 1
board[0][1]: 2
board[0][2]: 3
board[1][0]: 4
board[1][1]: 0
board[1][2]: 5
board[2][0]: 6
board[2][1]: 7
board[2][2]: 8

GOAL STATE:
board[0][0]: 0
board[0][1]: 1
board[0][2]: 2
board[1][0]: 3
board[1][1]: 4
board[1][2]: 5
board[2][0]: 6
board[2][1]: 7
board[2][2]: 8

USING BFS ALGORITHM
SOLUTION: (Relative to the space character)
1. Move LEFT
2. Move UP
3. Move RIGHT
4. Move RIGHT
5. Move DOWN
6. Move LEFT
7. Move UP
8. Move LEFT
9. Move DOWN
10. Move RIGHT
11. Move RIGHT
12. Move UP
13. Move LEFT
14. Move LEFT

INITIAL BOARD STATE:
+---+---+---+
| 1 | 2 | 3 |
+---+---+---+
| 4 | 0 | 5 |
+---+---+---+
| 6 | 7 | 8 |
+---+---+---+

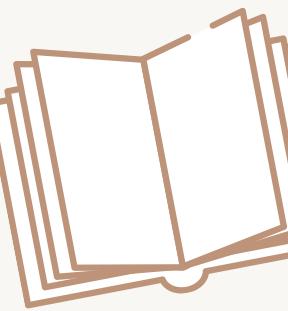
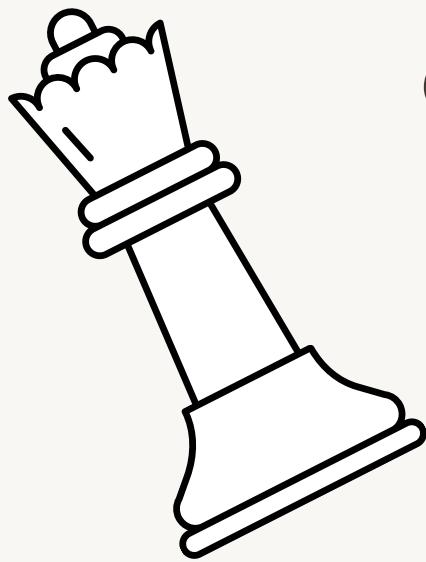
GOAL BOARD STATE:
+---+---+---+
| 0 | 1 | 2 |
+---+---+---+
| 3 | 4 | 5 |
+---+---+---+
| 6 | 7 | 8 |
+---+---+---+

DETAILS:
- Solution length : 14
- Nodes expanded : 8706
- Nodes generated : 14732
- Runtime : 0.006 milliseconds
- Memory used : 471424 bytes
PS C:\Users\Kartika Diva\Documents\8-Puzzle-Solver

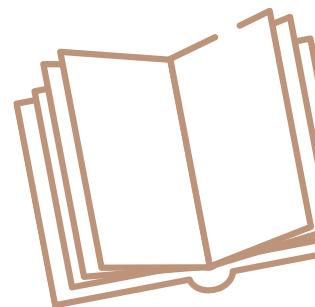
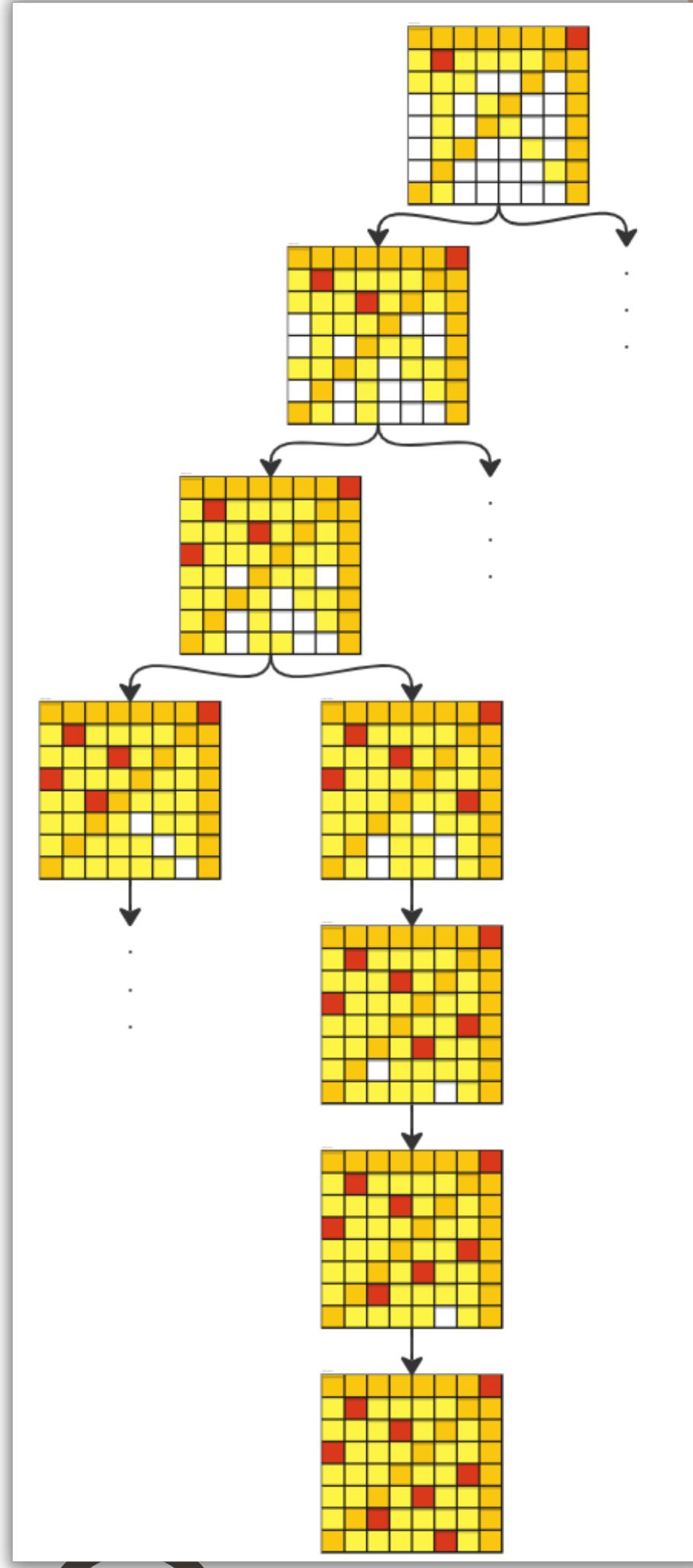
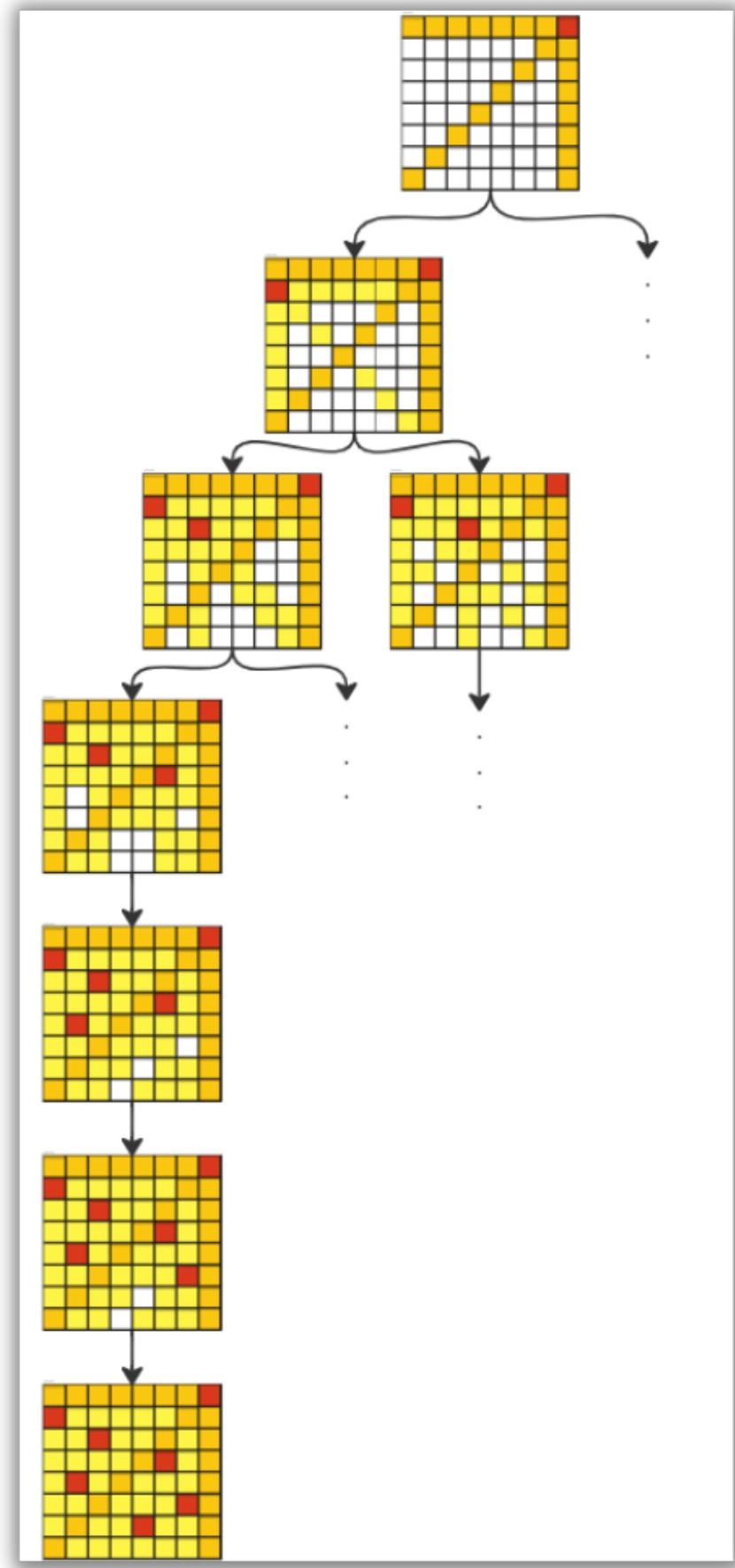
```

USING BFS ALGORITHM  
SOLUTION: (Relative to the space character)  
1. Move LEFT

# 8 Queen (DFS)



# Skema (column = 8)



```
1 #include<iostream>
2
3 using namespace std;
4
5 int N = 8;
6 int board[8][8];
7 int numQueens = 0;
8 int sols = 0;
9
10 void searchCol(int col) {
11     // base case
12     if(numQueens >= N) {
13         // print solution and exit
14         for(int i = 0; i < N; i++) {
15             for(int j = 0; j < N; j++) {
16                 if(board[i][j] < 1)
17                     cout << "0" << "\t";
18                 else
19                     cout << board[i][j] << "\t";
20             }
21             cout << "\n";
22         }
23         cout << "\n";
24         sols++;
25     }
26 }
```

```
64
65
66
67
68 }
```

```
int main() {
    searchCol(0);
    cout << sols << "\n";
    return 0;
```

```
27
28     // for each row
29     for(int i = 0; i < N; i++) {
30         // if cell is not attacked
31         if(board[i][col] > -1) {
32             // set queen and mark all cells in cross and diagonal
33             board[i][col] = 1;
34             for(int j = 0; j < N; j++) {
35                 if(j != col) board[i][j]--;
36                 if(j != i) board[j][col]--;
37             }
38             for(int j = 1; j < N; j++) {
39                 if(i - j >= 0 && col - j >= 0) board[i - j][col - j]--;
40                 if(i + j < N && col + j < N) board[i + j][col + j]--;
41                 if(i - j >= 0 && col + j < N) board[i - j][col + j]--;
42                 if(i + j < N && col - j >= 0) board[i + j][col - j]--;
43             }
44
45             numQueens++;
46             searchCol(col + 1);
47             // remove queens and markers
48             board[i][col] = 0;
49             for(int j = 0; j < N; j++) {
50                 if(j != col) board[i][j]++;
51                 if(j != i) board[j][col]++;
52             }
53             for(int j = 1; j < N; j++) {
54                 if(i - j >= 0 && col - j >= 0) board[i - j][col - j]++;
55                 if(i + j < N && col + j < N) board[i + j][col + j]++;
56                 if(i - j >= 0 && col + j < N) board[i - j][col + j]++;
57                 if(i + j < N && col - j >= 0) board[i + j][col - j]++;
58             }
59             numQueens--;
60         }
61     }
62 }
```

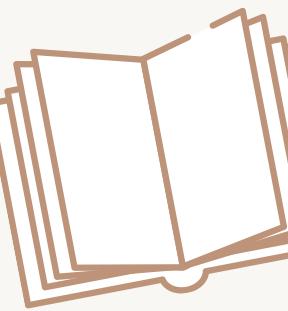
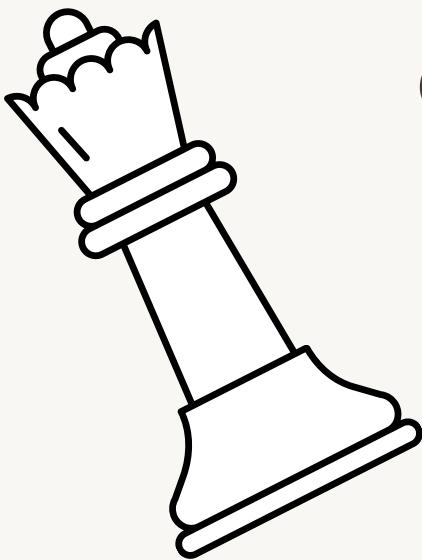


# Output:

1	0	0	0	0	0	0	0
0	0	0	0	0	0	1	0
0	0	0	0	1	0	0	0
0	0	0	0	0	0	0	1
0	1	0	0	0	0	0	0
0	0	0	1	0	0	0	0
0	0	0	0	0	1	0	0
0	0	1	0	0	0	0	0
1	0	0	0	0	0	0	0
0	0	0	0	0	0	1	0
0	0	0	1	0	0	0	0
0	0	0	0	0	1	0	0
0	0	0	0	0	0	0	1
0	1	0	0	0	0	0	0
0	0	0	0	1	0	0	0
0	0	1	0	0	0	0	0
1	0	0	0	0	0	0	0
0	0	0	0	0	1	0	0
0	0	0	0	1	0	0	0
0	0	1	0	0	0	0	0
0	0	0	0	0	0	1	0
0	0	0	1	0	0	0	0
0	1	0	0	0	0	0	0
0	0	0	0	0	0	0	1
0	0	0	0	0	1	0	0
0	0	0	0	1	0	0	0
1	0	0	0	0	0	0	0
0	1	0	0	0	0	0	0

0	0	1	0	0	0	0	0
0	0	0	0	0	0	0	1
0	0	0	0	0	0	1	0
1	0	0	0	0	0	0	0
0	0	1	0	0	0	0	0
0	0	0	0	0	0	0	0
0	1	0	0	0	0	0	0
0	0	0	0	0	0	0	1
0	0	0	0	0	0	1	0
0	0	0	0	0	1	0	0
0	0	0	0	1	0	0	0
0	0	0	1	0	0	0	0
0	0	1	0	0	0	0	0
0	1	0	0	0	0	0	0
0	0	0	0	0	0	0	1
0	0	0	0	0	0	1	0
0	0	0	0	0	1	0	0
1	0	0	0	0	0	0	0
0	1	0	0	0	0	0	0

# 8 Queen (BFS)



```
4  class Queens:
5      def __init__(self, size):
6          self.size = size
7
8      def solve_bfs(self):
9          solutions = []
10         queue = Queue()
11         queue.put([])
12         while not queue.empty():
13             solution = queue.get()
14             if self.conflict(solution):
15                 continue
16             row = len(solution)
17             if row == self.size:
18                 solutions.append(solution)
19                 continue
20             for col in range(self.size):
21                 queen = (row, col)
22                 queens = solution.copy()
23                 queens.append(queen)
24                 queue.put(queens)
25
26         return solutions
27
28     def conflict(self, queens):
29         for i in range(1, len(queens)):
30             for j in range(0, i):
31                 a, b = queens[i]
32                 c, d = queens[j]
33                 if a == c or b == d or abs(a - c) == abs(b - d):
34                     return True
35
36     def print(self, queens):
37         for i in range(self.size):
38             print('---' * self.size)
39             for j in range(self.size):
40                 p = 'Q' if (i, j) in queens else ' '
41                 print('| %s |' % p, end=' ')
42             print('|')
43             print('---' * self.size)
```

```
1 from queens import Queens  
2  
3  
4 def main():  
5     size = 8  
6     queens = Queens(size)  
7     bfs_solutions = queens.solve_bfs()  
8     for i, solution in enumerate(bfs_solutions):  
9         print('BFS Solution %d:' % (i + 1))  
10        queens.print(solution)  
11    print('Total BFS solutions: %d' % len(bfs_solutions))  
12  
13  
14 if __name__ == '__main__':  
15     main()
```

```
BFS Solution 1:  
-----  
| Q | | | | | | | |  
-----  
| | | | | Q | | | |  
-----  
| | | | | | | | Q |  
-----  
| | | | | | Q | | |  
-----  
| | | Q | | | | | |  
-----  
| | | | | | | | Q |  
-----  
| | Q | | | | | | |  
-----  
| | | | Q | | | | |  
-----  
| | | | | | | | Q |  
-----  
| | | | | | Q | | |  
-----  
| | | | | | | | | Q |  
-----  
  
BFS Solution 2:  
-----  
| Q | | | | | | | |  
-----  
| | | | | | Q | | |  
-----  
| | | | | | | | Q |  
-----  
| | | Q | | | | | |  
-----  
| | | | | | Q | | |  
-----  
| | | | | | | | Q |  
-----  
| | Q | | | | | | |  
-----  
| | | | Q | | | | |  
-----  
| | | | | | Q | | |  
-----  
| | | | | | | | Q |  
-----  
  
BFS Solution 3:  
-----
```

```
BFS Solution 92:  
-----  
| | | | | | | | Q |  
-----  
| | | | | | | | | Q |  
-----  
| | | | | | | | | | Q |  
-----  
| | | | | | | | | | | Q |  
-----  
| | | | | | | | | | | | Q |  
-----  
| | | | | | | | | | | | | Q |  
-----  
| | | | | | | | | | | | | | Q |  
-----  
| | | | | | | | | | | | | | | Q |  
-----  
| | | | | | | | | | | | | | | | Q |  
-----  
| | | | | | | | | | | | | | | | | Q |  
-----  
| | | | | | | | | | | | | | | | | | Q |  
-----  
| | | | | | | | | | | | | | | | | | | Q |  
-----  
| | | | | | | | | | | | | | | | | | | | Q |  
-----  
  
Total BFS solutions: 92
```

# TERIMA KASIH