

Problem Set 10

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STAT 100, SECTION 0221

PROBLEM #1

A.

$$\mu_1 = \mu_2$$

$$\mu_1 \neq \mu_2$$

B.

This is a two-sided test because it specifically states “to determine whether there is a **difference** between the mean number of correct identifications.”

C.

$$t = \frac{37.56 - 36.21}{\sqrt{\frac{(6.34)^2}{195} + \frac{(5.97)^2}{195}}}$$

$$t = 2.165$$

D.

$$p - \text{value} = 2[1 - P(Z < |t|)]$$

$$2.165 \rightarrow -2.17 \rightarrow 0.0150 \rightarrow 0.0150 \times 2 = 0.0300$$

E.

Since $p - \text{value} = 0.03 < 0.05 = \alpha$, we reject H_0 .

PROBLEM #2

A.

$$\mu_1 = \mu_2$$

$$\mu_1 > \mu_2$$

B. This is a one-sided test because it specifically states “to determine whether the mean gain in SAT Verbal scores is **higher** for students who were coached after their first attempt.”

C.

$$t = \frac{26.53 - 24.38}{\sqrt{\frac{(9.77)^2}{152} + \frac{(9.81)^2}{158}}}$$

$$t = 1.933$$

D.

$$p - \text{value} = [1 - P(Z < |t|)]$$

$$1.933 \rightarrow 1.93 \rightarrow 0.9732 \rightarrow 1 - 0.9732 = 0.0268$$

E.

Since $p - \text{value} = 0.0268 > 0.01$, we cannot reject H_0 .

F.

Since $p - \text{value} = 0.0268 < 0.05$, we reject H_0 .

G.

We can reject H_0 at both $\alpha = 0.01$ and $\alpha = 0.05$.

$$p - \text{value} < 0.01 \text{ and } p - \text{value} < 0.05$$

$$p - \text{value} < 0.01$$

$$p - \text{value} = P(Z > t_o) = 1 - P(Z < t_o) < 0.01$$

$$1 - 0.01 = 0.99 = \text{using the } Z - \text{table} = P(Z < 2.33)$$

$$t_o \geq 2.33 \rightarrow \text{any value} \geq 2.33, \text{ for it to satisfy both conditions.}$$