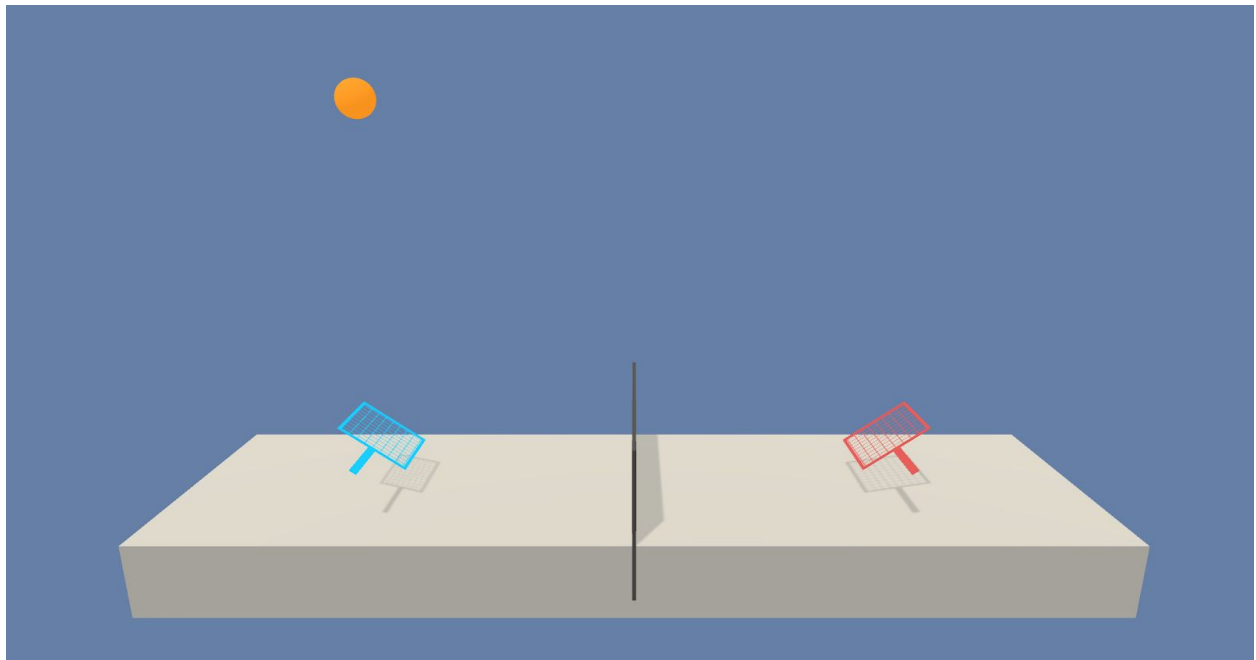


# Collaboration and Competition

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## Introduction

In this environment, the observation space consists of 8 variables corresponding to the position and velocity of the ball and racket. Each agent receives its own, local observation. Two continuous actions are available, corresponding to movement toward (or away from) the net, and jumping. The goal of each agent is to keep the ball in play. Two agents control rackets to bounce a ball over a net. If an agent hits the ball over the net, it receives a reward of +0.1. If an agent lets the ball hit the ground or hits the ball out of bounds, it receives a reward of -0.01. The task is episodic, and in order to solve the environment, the agent must get an average score of +0.5 (over 100 consecutive episodes, after taking the

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maximum over both agents). The environment is considered solved, when the average (over 100 episodes) of those scores is at least +0.5.

## Learning Algorithm Used - DDPG

DDPG is a type of actor-critic method which can be seen as an approximate Deep Q-Network (DQN). The critic in DDPG is used to predict the maximum Q-value for the next state similar to the DQN algorithms estimate function. The main advantage that DDPG has over DQN is that it can be used in a continuous state and action space.

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### Algorithm 1 DDPG algorithm

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Randomly initialize critic network  $Q(s, a|\theta^Q)$  and actor  $\mu(s|\theta^\mu)$  with weights  $\theta^Q$  and  $\theta^\mu$ .  
Initialize target network  $Q'$  and  $\mu'$  with weights  $\theta^{Q'} \leftarrow \theta^Q, \theta^{\mu'} \leftarrow \theta^\mu$   
Initialize replay buffer  $R$   
**for** episode = 1, M **do**  
    Initialize a random process  $\mathcal{N}$  for action exploration  
    Receive initial observation state  $s_1$   
    **for** t = 1, T **do**  
        Select action  $a_t = \mu(s_t|\theta^\mu) + \mathcal{N}_t$  according to the current policy and exploration noise  
        Execute action  $a_t$  and observe reward  $r_t$  and observe new state  $s_{t+1}$   
        Store transition  $(s_t, a_t, r_t, s_{t+1})$  in  $R$   
        Sample a random minibatch of  $N$  transitions  $(s_i, a_i, r_i, s_{i+1})$  from  $R$   
        Set  $y_i = r_i + \gamma Q'(s_{i+1}, \mu'(s_{i+1}|\theta^{\mu'}))|\theta^{Q'}$   
        Update critic by minimizing the loss:  $L = \frac{1}{N} \sum_i (y_i - Q(s_i, a_i|\theta^Q))^2$   
        Update the actor policy using the sampled policy gradient:  

$$\nabla_{\theta^\mu} J \approx \frac{1}{N} \sum_i \nabla_a Q(s, a|\theta^Q)|_{s=s_i, a=\mu(s_i)} \nabla_{\theta^\mu} \mu(s|\theta^\mu)|_{s_i}$$
  
        Update the target networks:  

$$\theta^{Q'} \leftarrow \tau \theta^Q + (1 - \tau) \theta^{Q'}$$
  

$$\theta^{\mu'} \leftarrow \tau \theta^\mu + (1 - \tau) \theta^{\mu'}$$
  
    **end for**  
**end for**

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Figure 1: DDPG Algorithm<sup>1</sup>

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<sup>1</sup> "Continuous control with deep reinforcement learning." <https://arxiv.org/abs/1509.02971>. Accessed 24 Jul. 2019.

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## Improvements Added:

Soft Update mitigates the slow learning problem of early state Q-learning in noisy environments caused by hard optimization policy bias.<sup>2</sup>

Replay Buffer for Experience Replay allows previous states to be revisited later in the learning process using updated agent weights to help mitigate temporal biasing.

Leaky ReLU helps with initial learning to prevent the “dead ReLU” problem caused by encountering only negative rewards since ReLU removes negative rewards from the learning function.

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<sup>2</sup> "Taming the Noise in Reinforcement Learning via Soft Updates." 30 Mar. 2017, <https://arxiv.org/pdf/1512.08562>. Accessed 4 Aug. 2019.

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## Hyperparameters Used

`BUFFER_SIZE = int(1e5)` # replay buffer size

`BATCH_SIZE = 128` # minibatch size

`GAMMA = 0.99` # discount factor

`TAU = 1e-3` # for soft update of target parameters

`LR_ACTOR = 1e-5` # learning rate of the actor

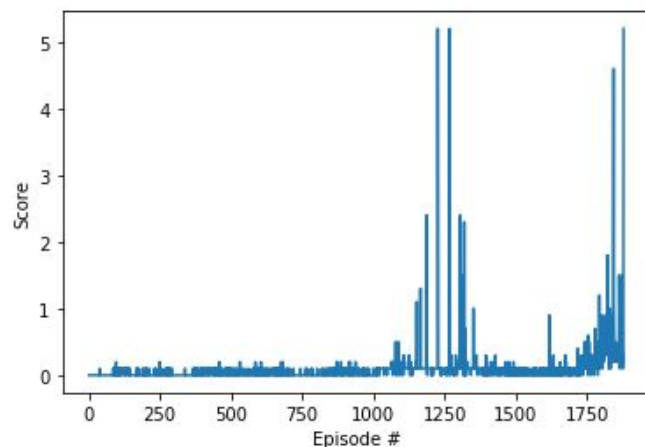
`LR_CRITIC = 1e-4` # learning rate of the critic

`WEIGHT_DECAY = 0` # L2 weight decay

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## Results - Plot of Rewards

Environment Solved! It took 1880 episodes!  
Average Score: 0.52



Episode 100	Average Score: 0.01
Episode 200	Average Score: 0.04
Episode 300	Average Score: 0.02
Episode 400	Average Score: 0.01
Episode 500	Average Score: 0.05
Episode 600	Average Score: 0.02
Episode 700	Average Score: 0.04
Episode 800	Average Score: 0.01
Episode 900	Average Score: 0.05
Episode 1000	Average Score: 0.04
Episode 1100	Average Score: 0.10
Episode 1200	Average Score: 0.15
Episode 1300	Average Score: 0.22
Episode 1400	Average Score: 0.17
Episode 1500	Average Score: 0.07
Episode 1600	Average Score: 0.04
Episode 1700	Average Score: 0.07
Episode 1800	Average Score: 0.18
Episode 1880	Average Score: 0.52

The figure above shows the agents average score throughout the training process which included 1880 episodes. The table to the right of the plot shows the average score over 100 hundred episodes for every 100 episodes throughout the training session. Based on these results, it appears the environment was solved in 1880 episodes.

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## Ideas for Future Work

### Trust Region Policy Optimization (TRPO)

TRPO is similar to natural policy gradient methods and is effective for optimizing large nonlinear policies such as neural networks.<sup>3</sup>

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**Algorithm 1** Policy iteration algorithm guaranteeing non-decreasing expected return  $\eta$

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Initialize  $\pi_0$ .

**for**  $i = 0, 1, 2, \dots$  until convergence **do**

    Compute all advantage values  $A_{\pi_i}(s, a)$ .

    Solve the constrained optimization problem

$$\pi_{i+1} = \arg \max_{\pi} [L_{\pi_i}(\pi) - CD_{\text{KL}}^{\max}(\pi_i, \pi)]$$

    where  $C = 4\epsilon\gamma/(1 - \gamma)^2$

$$\text{and } L_{\pi_i}(\pi) = \eta(\pi_i) + \sum_s \rho_{\pi_i}(s) \sum_a \pi(a|s) A_{\pi_i}(s, a)$$

**end for**

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**Figure 2: TRPO Algorithm**

### Truncated Natural Policy Gradient (TNPG)

By computing an ascent direction that approximately ensures a small change in the policy distribution TNPG improves upon the REINFORCE algorithm.<sup>4</sup>

### Distributed Distributional Deterministic Policy Gradients (D4PG)

D4DG adapts distributional reinforcement learning to the continuous control setting and combines it with distributed off-policy learning combined with improvement including N-step returns and prioritized experience replay.<sup>5</sup>

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<sup>3</sup> "Trust Region Policy Optimization." <https://arxiv.org/abs/1502.05477>. Accessed 4 Aug. 2019.

<sup>4</sup> "Benchmarking Deep Reinforcement Learning for Continuous Control." 22 Apr. 2016, <https://arxiv.org/abs/1604.06778>. Accessed 24 Jul. 2019.

<sup>5</sup> "distributed distributional deterministic policy gradients - OpenReview." <https://openreview.net/pdf?id=SyZipzbCb>. Accessed 24 Jul. 2019.

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