

# Homework 3

## Automata

Version du September 20, 2020

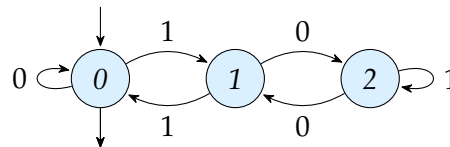
This homework has to be returned tomorrow, on Thursday, at the beginning of the tutorial.

**Exercise 1** (Translation of rational/regular expressions). *In this exercise, we assume that we have  $\Sigma = \{a, b, c\}$ .*

*For each following rational expression, you have to use the Thompson algorithm to build a finite nondeterministic automaton with spontaneous transitions, and then apply the building procedure seen during the lessons to get rid of spontaneous transitions, and finally the potentially useless states<sup>1</sup>. You will show the automata after each step.*

1.  $(a + b + cc)^* abab$
2.  $((ab + \varepsilon)^* c)^*$
3.  $(\emptyset(a + b))^*$

**Exercise 2** (Multiples of 3 and 7). *Let  $\mathcal{D}_3$  be the following deterministic automaton defined on the alphabet  $\Sigma = \{0, 1\}$ :*



1. *Execute  $\mathcal{D}_3$  on the words 101010, and 11111.*
2. *Prove that  $\mathcal{D}_3$  recognizes the binary representations of the natural integers multiple of 3. (Hint: give a meaning to the states numbers.)*
3. *Build  $\mathcal{D}_7$ , a deterministic automaton which recognizes the binary representations of the natural numbers which are multiple of 7.*

**Exercise 3** (Automaton for entry code). *You will have understood that the program of the entry code of yesterday (Homework 2, exercise 1) only executed an automaton. Today, we are going to modify the table `tab` of the program of Homework 2 to recognize another code.*

1. *Does the table `tab` of the preceding homework represent an NFA? a DFA?*
2. *How is the initial state indicated? And how about the final states?*
3. *We want to change the code in such a manner that the entry code only accepts the sequences of numbers which end by 747. Give a rational expression denoting the set  $L$  of these sequences.*
4. *Using the Thompson algorithm, build an  $\varepsilon$ -NFA which recognizes  $L$ . Then, delete the spontaneous transitions to obtain an NFA. Prune if necessary. Salt and pepper.*
5. *Build a DFA able to recognize  $L$ . You can proceed as you want; you are not been told how to. (Hint: you need only 4 states.)*
6. *Give a new implementation of the program of the entry code, able to recognize the words of  $L$  (followed by "E", as usual) based on the same principle as in Homework 2.*

1. see the section about *Unuseful states* in the course