

## GAUSS THEOREM MEMO

- Identify the coordinate system
  - ex: spherical distribution
    - ↳ spherical coordinate system
  - cylindrical distribution of charge
    - ↳ cylindrical coordinate system
- Determine the invariance of the electric field
  - perform the study of the symmetry created by the charge on different receiver points in the space
  - identify  $\vec{E}$  direction and orientate → identify the unit vector related in the basis of coordinate
- Choose the Gauss surface ( $\Sigma_g$ )
  - choose the <sup>appropriate</sup> shape with the electric field symmetries
  - $\Sigma_g$  closed
  - $M \in \Sigma_g$ ,  $M$  being a receiver point. It can have  $\neq$  possible locations
  - $Q_{int} \in \Sigma_g$
  - Several  $\Sigma_g$  can be chosen if we want to determine  $\vec{E}$  everywhere in the space (inside and outside the shape)
- Identify the  $d\vec{S}_g$ :
  - > unity vector that is carrying  $dS$  (or the projection)
  - >  $\|d\vec{S}_g\| = dS$  expression (if it is needed)
- Calculate the charge  $\in \Sigma_g$ :  $Q_{int}$ 
  - $\lambda$  if 1D
  - $\sigma$  if 2D
  - $\rho$  if 3D
  - △ choose the good  $R$  to consider
- Calculate  $\oint \vec{E} \cdot d\vec{S}$  expression, using if needed the  $\neq$  parts of  $\Sigma_g$ 
  - △ Don't forget the scalar product of the unit vectors of  $d\vec{S}$  and  $\vec{E}$
- $\oint \vec{E} \cdot d\vec{S} = \frac{Q_{int}}{\epsilon_0}$ 
  - extract the expression of  $E$  from the equation
- $\vec{E} = E \cdot \text{unit vector}$
- Potential computation  $V$  from  $\vec{E} = -\vec{\text{grad}}(V)$ 
  - take into account the boundary conditions
  - $\alpha, \beta \dots$