
STAT 463: Homework 10

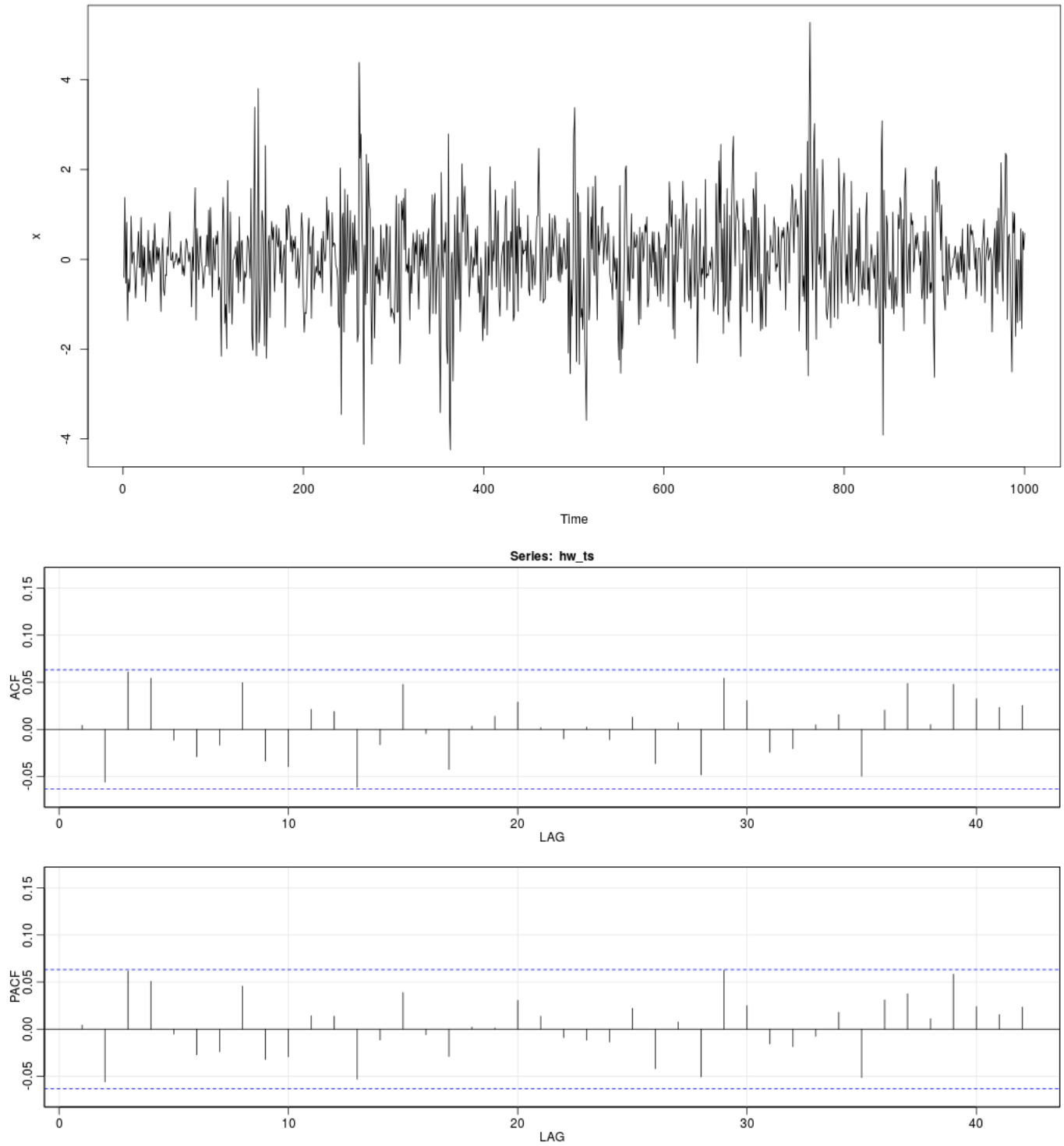
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April 25, 2018

PROBLEM 1

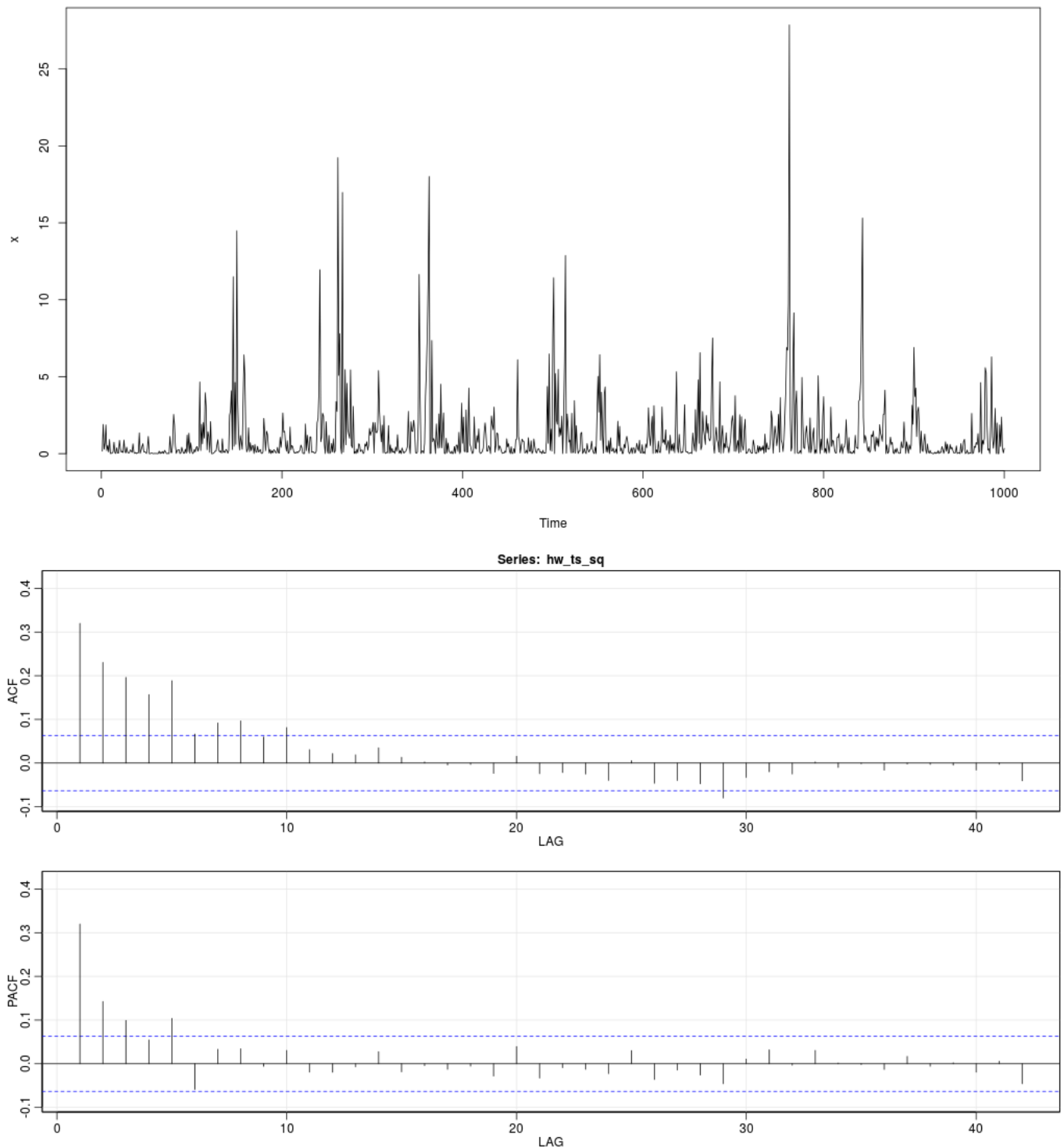
a)

Based on the time series and both the ACF and PACF plots, it appears that the entire time series is random noise.



b)

Using the squared series values, the ACF and PACF Possibly suggest an AR(1) or ARMA(1,1).



c)

Based on the ARCH and GARCH models, the GARCH had a lower AIC, BIC, SIC, and HQIC.

Normality tests show that the residuals have a normal distribution

Standardised Residuals Tests:

			Statistic	p-Value
Jarque-Bera Test	R	Chi^2	1.822259	0.4020699
Shapiro-Wilk Test	R	W	0.9985522	0.5890539

Ljung-Box Test	R	Q(10)	10.24976	0.4188616
Ljung-Box Test	R	Q(15)	14.32952	0.5006984
Ljung-Box Test	R	Q(20)	17.56494	0.6160438
Ljung-Box Test	R^2	Q(10)	3.469898	0.9681106
Ljung-Box Test	R^2	Q(15)	10.28095	0.801705
Ljung-Box Test	R^2	Q(20)	11.20095	0.9408438
LM Arch Test	R	TR^2	5.638083	0.9332166

Information Criterion Statistics :

AIC	BIC	SIC	HQIC
2.673371	2.688095	2.673353	2.67896

d)

$$y = \sigma_t \epsilon_t$$

$$\sigma_t = \sqrt{0.09622 + 0.31894y_{t-1}^2 + 0.60802\sigma_{t-1}^2}$$

$$\epsilon \stackrel{iid}{\sim} N(0, 1)$$

e)

	meanForecast	meanError	standardDeviation
1	0	0.8140121	0.8140121
2	0	0.8428764	0.8428764
3	0	0.8687765	0.8687765
4	0	0.8921136	0.8921136
5	0	0.9132138	0.9132138
6	0	0.9323465	0.9323465
7	0	0.9497377	0.9497377
8	0	0.9655789	0.9655789
9	0	0.9800345	0.9800345
10	0	0.9932465	0.9932465

PROBLEM 2

a)

Looking at the 'none', 'both', 'trend', and 'constant' models, the 'none' produced the highest adjusted R^2 values for all models. These are the resulting models:

$$\hat{B}_t = 1.05330B_{t-1} - 0.30720M_{t-1} + 0.24882K_{t-1}$$

$$\hat{M}_t = 0.14485B_{t-1} + 0.56676M_{t-1} + 0.27974K_{t-1}$$

$$\hat{K}_t = 0.2423B_{t-1} - 0.4384M_{t-1} + 1.1886K_{t-1}$$

b)

Again, for the VAR(2) models, including neither the intercept or constant produced the best model based on adjusted R^2 value.

$$\hat{K}_t = -0.09426t - 0.19763B_{t-1} + 0.59703M_{t-1} + 0.81700K_{t-1} + 1.13432B_{t-2} - 1.67339M_{t-2} + 0.33416K_{t-2}$$

c)

The BIC values are as follows:

- BIC1: 8.417481
- BIC2: 8.492818

Based on these values the BIC for the VAR(1) model indicates that it is the better option.

d)

Based on the ACF of the residuals for the 3 cities, all values are within the lines of significance.

