

$$K q_0 \left(\frac{R^2}{4L^2} - \frac{1}{LC} - \frac{R}{2L} \right) + R \left(-\frac{q_0 R}{2L} \right) + \frac{q_0}{C} = 0$$

$$0 = q_0 \left\{ \left(\frac{R^2}{4L} - \frac{1}{C} - \frac{R}{2} - \frac{R^2}{2L} + \frac{1}{C} \right) \right\} = \left(\frac{R^2}{4L} - \frac{R}{2} - \frac{R^2}{2L} \right)$$

$$0 = q_0 R \left\{ \frac{R}{4L} - \frac{R}{2L} - \frac{1}{2} \right\} = \frac{q_0 R}{2} \left\{ \frac{1}{2} \frac{R}{L} - \frac{R}{L} - 1 \right\}$$

$$\frac{R}{2L} - \frac{R}{L} = 1$$

$$\frac{R}{2} - R = L$$

$$-\frac{R}{2} = L$$

$$R = -2L = -10 \text{ H} \leftarrow \text{this doesn't make sense unit-wise}$$

$$f(R) = e^{-\frac{Rt}{2L}} \cos\left(\sqrt{\frac{1}{LC} - \left(\frac{R}{2L}\right)^2} t\right) - \frac{q}{q_0}$$

$$L = 5 \text{ H}, C = 10^{-4} \text{ F}, \frac{q}{q_0} = 0.01, t = 0.05$$

$$a = \frac{1}{2L} \quad b = \frac{1}{4L^2} \quad d = \frac{1}{LC}$$

$$f(R) = e^{-aR} \cos(\sqrt{d - bR^2} t) - \frac{q}{q_0}$$

$$f'(R) = -ae^{-aR} \cos(\sqrt{d - bR^2} t) + \frac{bRt}{\sqrt{d - bR^2}} e^{-aR} \sin(\sqrt{d - bR^2} t)$$

$$\left\{ \frac{d}{dR} \cos(\sqrt{d - bR^2} t) = -\sin(\sqrt{d - bR^2} t) \left(\frac{1}{\sqrt{d - bR^2}} \right) (-2bR) \right\}$$

$$= \frac{bRt}{\sqrt{d - bR^2}} \sin(\sqrt{d - bR^2} t)$$