

a)

	m	f
str	○ ○ ○	△ △ △
end	○ ○ ○	△ △ △
cross	○ ○ ○	△ △ △

This is a crossed design

$$y_{ijt} = \alpha_i + \beta_j + (\alpha\beta)_{ij} + \epsilon_{ijt} \quad \epsilon \sim N(0, \sigma^2)$$

$i = m, f$   
 $j = \text{str, end, cross}$   
 $t = 1, \dots, 5$

b)

Stats: 1, 2, 3  
 Humanities: 1, 2, 3

This is a nested design (but actually a random-effects)

$$y_{ijt} = \alpha_i + \beta_{j(i)} + \epsilon_{ijt} \quad \epsilon \sim N(0, \sigma^2)$$

$i = \text{stats, humanities}$   
 $j = 1, 2, 3$   
 $t = 1, 2, 3$

c)

This is a nested design where head is nested in machine

$$y_{ijt} = \mu + \alpha_i + \beta_{j(i)} + \epsilon_{ijt}$$

$i = M_1, \dots, M_5$   
 $j = H_1, \dots, H_4$   
 $t = 1, \dots, 4$   
 $\epsilon_{ijt} \sim N(0, \sigma^2)$