

EN2550 Assignment 2 on Fitting and Alignment

Index: 190018V

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GitHub Link: https://github.com/KCSAbeywickrama/EN2550-Excercises/tree/master/Assignment_02

Only important code parts & results have been included. Full code with all function implementation is on [GitHub](#).

1) (a)

```
def get_circle(points,max_r): # find circle from 3 points
    ...
def fit_circle(points):      # find the best circle from a set of points algebraically
    ...
def get_inliers(points,thres): # find inliers using RANSAC
    point_count=len(points)
    max_inlier_count=0
    max_r=(np.max(points)-np.min(points))/2
    for ittr in range(ittrs_limit):
        init_points=points[np.random.choice(point_count,3)]
        circle=get_circle(init_points,max_r)

        if(circle):
            center,r=circle
            tmp_diff_sqr=(points-np.array(center))**2
            r_difs=np.abs(np.sqrt(tmp_diff_sqr[:,0])+tmp_diff_sqr[:,1])-r)
            inliers = points[r_difs<thres]
            inlier_count=len(inliers)
            if inlier_count>max_inlier_count:
                match_circle,match_samples,match_inliers=circle,init_points,inliers
                max_inlier_count=inlier_count

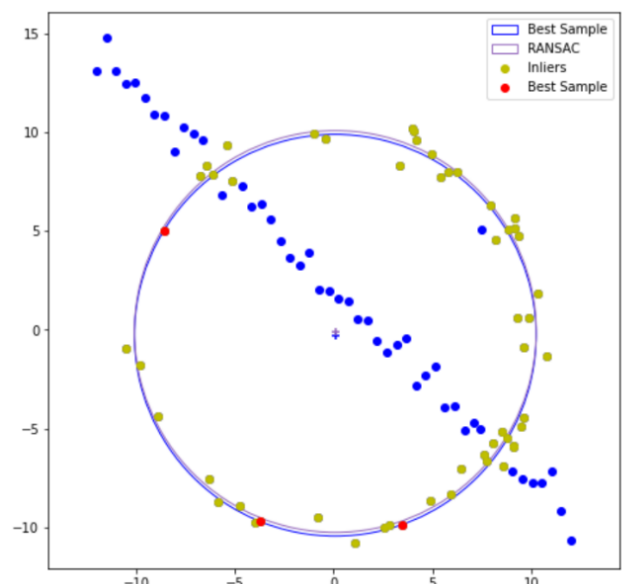
    return match_circle,match_samples,match_inliers

ittrs_limit=500
inlie_thres=1
(smpl_center,smpl_r),smpl_points,inliers=get_inliers(X,inlie_thres) #get inliers using RANSAC
ransac_center,ransac_r=fit_circle(inliers) #find best circle from inliers using algebraically
```

After getting the set of inliers, to get a better result the circle has been recalculated by considering all the inliers (removed function implementation available in the [notebook](#) on [GitHub](#))

1) (b)

There is a little difference between the circle from the best matching sample set & the recalculated circle by considering all inliers. The recalculated circle is more accurate because all inliers have been considered instead of considering only 3 sample points. (Clear large image is available in the [notebook](#) on [GitHub](#))



2)

```
img_dst=cv.imread('imgs2/00x.jpg')
img_src=cv.imread('imgs2/flagx.png')

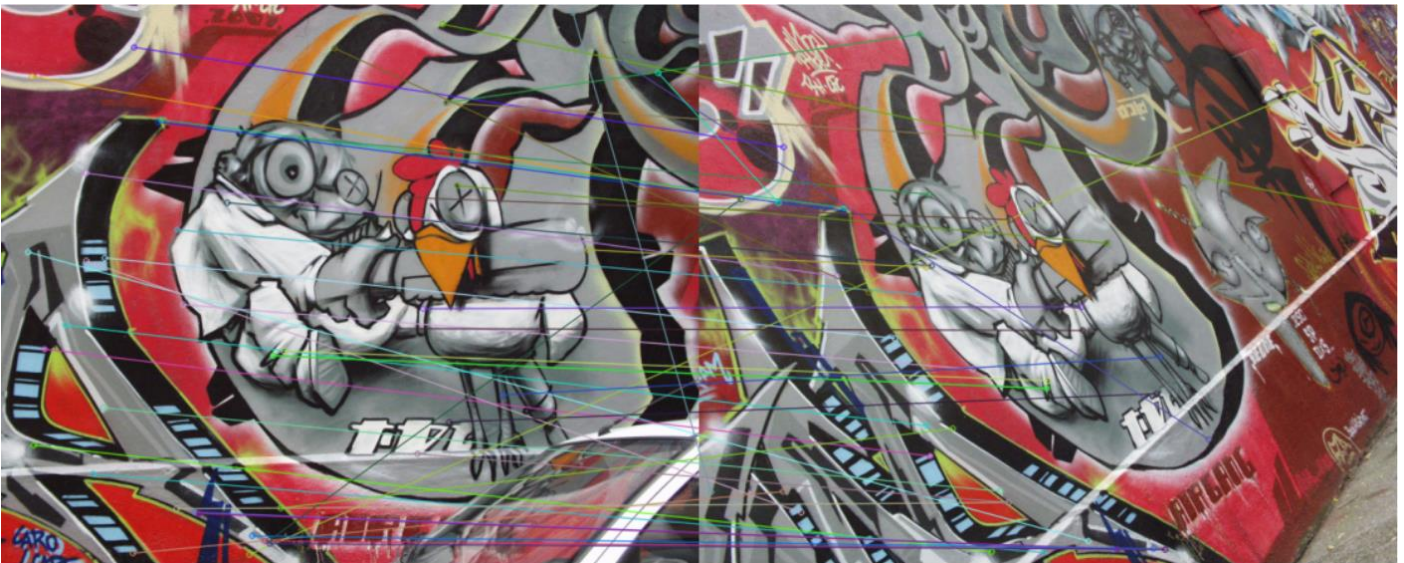
points_des=np.array(get_points(img_dst))
img_src_h=img_src.shape[0]
img_src_w=img_src.shape[1]
points_src=np.array([(0,0),(img_src_w,0),(img_src_w,img_src_h),(0,img_src_h)])
h,st=cv.findHomography(points_src,points_des)
img_warp=cv.warpPerspective(img_src,h,img_dst.shape[1::-1])
img_out=cv.addWeighted(img_warp,0.5,img_dst,1,0.0)
```

`get_points()` is a function that uses GUI options in OpenCV to find destination points of the flag image in the architectural image with mouse clicks (implementation available in the notebook on GitHub). Computing homography, warping & superimposing has done using inbuilt functions in OpenCV.



Images with large walls(flat surfaces) with linear edges have been selected as architectural images. Since flags are flat and rectangular shape superimposing these into walls with linear edges on the architectural images ends up with a nice result.

3) (a)



```
img1=cv.imread('imgs3/img1.ppm')
img2=cv.imread('imgs3/img4.ppm')

sift=cv.SIFT_create()
kp1,des1=sift.detectAndCompute(img1,None)
```

```

kp2,des2=sift.detectAndCompute(img2,None)
bf=cv.BFMatcher()
matches=bf.knnMatch(des1,des2,k=2)

good=[];pts1=[];pts2=[]
for m,n in matches:
    if m.distance<0.65*n.distance:
        pts1.append(kp1[m.queryIdx].pt);pts2.append(kp2[m.trainIdx].pt);good.append([m])

img_match=cv.drawMatchesKnn(img1,kp1,img2,kp2,good,None,flags=2)

```

Since the projective angle between img1 & img5 is very high it is very difficult to find a reasonable amount of matching features using SIFT. Because SIFT does not perform well in large changes in viewpoint angle. So img1 & img4 have been selected to continue the question workout. (workout of trying to match SIFT features between img1 & img5 has been included in the [notebook](#) on [GitHub](#) for the completion. But by limiting points to best points by reducing the threshold and then manually checking, it can be seen that those are incorrect matches)

3) (b)

```

def compute_H(pts1,pts2):
    A=[]
    for i in range(len(pts1)):
        xs,ys=pts1[i]
        xd,yd=pts2[i]
        A.append((xs,ys,1,0,0,0,-xd*xs,-xd*ys,-xd))
        A.append((0,0,0,xs,ys,1,-yd*xs,-yd*ys,-yd))

    A=np.array(A)
    L,V=np.linalg.eig(A.T @ A)
    l=np.argmin(np.abs(L))
    v=V[:,l]
    h33=v[-1]
    return v.reshape((3,3))/h33

max_inlier_count=0
for n in range(5000):
    smpl_idxxs=np.random.choice(len(pts1),4,replace=False)

    smpl_pts1=pts1[smpl_idxxs]
    smpl_pts2=pts2[smpl_idxxs]

    H=compute_H(smpl_pts1,smpl_pts2)

    Xs=np.vstack((pts1.T,np.ones(pts1.shape[0],dtype=int)))
    Xd=pts2.T
    XdH=H @ Xs

    XdH=XdH/XdH[2]
    XdH=np.delete(XdH,2,axis=0)
    tmp_diff_sqr=(XdH-Xd)**2
    dis_diff=np.sqrt(tmp_diff_sqr[0]+tmp_diff_sqr[1])
    thres=2
    inlier_idxxs=dis_diff<thres
    inliers=pts1[inlier_idxxs],pts2[inlier_idxxs]

```

```

inlier_count=len(inliers[0])
if(inlier_count>max_inlier_count):
    match_inliers=inliers
    max_inlier_count=inlier_count

```

```

H=compute_H(*match_inliers)

```

H=

```

[[ 6.56816848e-01  6.80640096e-01 -3.08528938e+01]
 [-1.51582999e-01  9.69920508e-01  1.49997446e+02]
 [ 4.09138545e-04 -1.06392211e-05  1.00000000e+00]]

```

the square root of sum of squared differences between calculated H & given H in the data set is **1.280**

RANSAC is used to remove incorrect matches (outliers) and get set of accurate matches (inliers) before calculate Homography(H). Above H computation is for img1 & img4. Due to the issue mentioned in 3 (a) can't calculate H between img1 & img5 only using SIFT matches directly. But applying the above same procedure to img1 & img3 and then img3 & img5, H1to3 & H3to5 can be obtained. Then using,

```

H1to5= H3to5 @ H1to3

```

relationship, **H1to5** can be calculated.

the square root of sum of squared differences between calculated H1to5 & given H1to5 in the data set is **1.881**

So calculated Homographies and given Homographies are almost equal. So Homography calculation is very accurate. (Reading the given H and the calculating differences & rest of the code is available in the [notebook](#) on [GitHub](#))

3) (c)

```

T=np.array([[1,0,50],[0,1,50],[0,0,1]],dtype=float)

```

```

img1_mask=np.ones(img1.shape)

```

```

canvas1=cv.warpPerspective(img1,T @ H1to5,(900, 850))

```

```

canvas1_mask=cv.warpPerspective(img1_mask,T @ H1to5,(900, 850))==1

```

```

canvas5=cv.warpPerspective(img5,T,(900, 850))

```

```

canvas_out=np.array(canvas5)

```

```

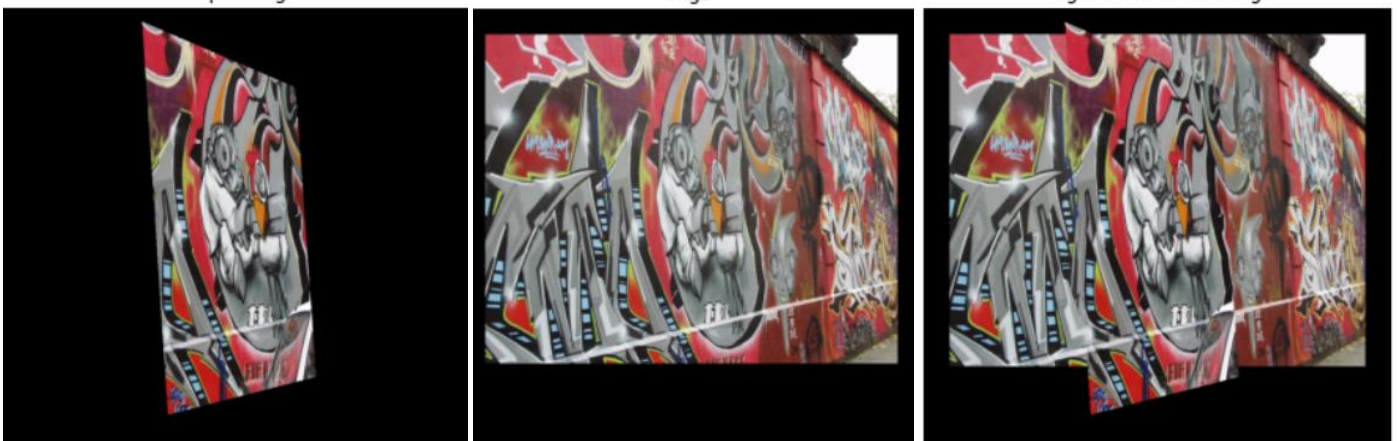
canvas_out[canvas1_mask]=canvas1[canvas1_mask]

```

Warped img1

img5

img1 stitched on to img5



Translation(using T matrix) has been given to img1 & img5 for better results without cropping parts after stitching. Translation & projection has given to img1 at once by multiplying the Translation matrix and Homography. Mask of warped img1 has been used to place warped img1 on top of img5.