

Unsupervised Surrogate Anomaly Detection - Appendix

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A Importance of Learnable Shifts

Trivial solutions are a common problem also for DeepSVDD [18]. Namely when the last layer learns a zero multiplicative weight, but the learnable shift is equal to the desired c . To combat this, Ruff et. al. propose to remove the learnable shifts entirely. And while this certainly helps in making this shift impossible, it also limits how complicated a function can be learned by the neural network [14].

We show this in Figure 1, where we task neural networks to approximate a simple sinus curve. Here, we use neural networks with three layers of 100 nodes and relu activation in each hidden layer. The three networks differ only by the learnable shifts they use. While the network with learnable shifts (green) is clearly able to approximate the sinus curve, the version without learnable shifts (blue) is not able to do so. And since real anomaly representations can be much more complicated than such a simple sinus curve, we do not think that limiting the neural network complexity is a reasonable choice.

Instead, we use other methods to remove the trivial solution of a constant network. This also includes using learnable shifts in each hidden layer but not in the output layer. This setup is still able to approximate complicated functions, as is shown in orange in Figure 1.

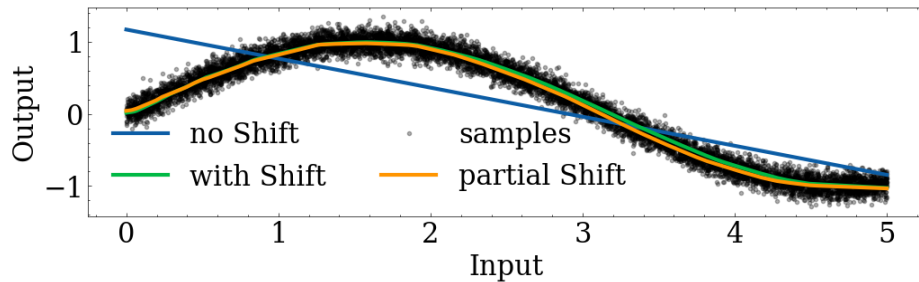


Fig. 1: Given complicated alinear data, the functions learned by three neural networks with relu activations are shown. The network without learnable shifts cannot capture the structure of the underlying data, while both a network with learnable shifts in each layer and a network with learnable shifts in all layers except the last can describe the alinearity.

B DEAN-Fair

To illustrate the adaptability of DEAN (see Section 6), we demonstrate its modification for improved fairness on a toy example using the COMPAS dataset [20]. In this context, we consider recidivism risk as the anomaly and employ fairness as a critical performance metric. The COMPAS dataset, which contains risk scores along with demographic and criminal history features, is widely used for evaluating such algorithmic fairness.

B.1 Setup

For our fairness evaluation, we compute the AUC-ROC separately for two subgroups defined by a protected attribute (age, binarized with a threshold at 25 years) and measure the deviation between them to showcase how DEAN can be guided towards equal treatment across different demographic groups in general. We chose the AUC-ROC since it is a metric invariant to the fraction of anomalous samples and also handles non-binary anomaly scores. An ideal fairness score is 0.5, indicating no performance difference between groups. For this, we propose three adaptation strategies to improve fairness.

1. Modified Loss Function: We add a fairness regularization term to the original loss:

$$L = \sum_{\mathbf{x} \in X_{\text{train}}} \|f(\mathbf{x}) - 1\| + \theta \cdot L_{\text{fair}} \quad (1)$$

where

$$L_{\text{fair}} = \frac{\|L_1 - L_0\|}{\|L_1\| + \|L_0\|} \quad (2)$$

and

$$L_{1/0} = \frac{1}{\|X_{(\text{un})\text{protected}}\|} \sum_{\mathbf{x} \in X_{(\text{un})\text{protected}}} f(\mathbf{x}) \quad (3)$$

Here, L_1 and L_0 denote the mean outputs for the unprotected and protected groups, respectively, and we set $\theta = 0.1$.

2. Submodel Pruning: In this approach, we iteratively remove the submodel that exhibits the greatest unfairness in a greedy manner. We test pruning rates of 1%, 5%, and 10% of the ensemble.

3. Non-uniform Weighting: We assign different weights to submodels in the ensemble to maximize fairness. Due to the non-continuous nature of this optimization, we employ an evolutionary algorithm to determine the optimal weights.

B.2 Results

Table 1 summarizes the AUC-ROC performance and fairness (measured as the deviation from 0.5) for each method. Each experiment is repeated five times to obtain uncertainty estimates.

Adjustment	AUC-ROC	Fairness
Baseline	0.583 ± 0.003	0.644 ± 0.020
Loss function	0.594 ± 0.012	0.453 ± 0.080
Pruning (1%)	0.583 ± 0.003	0.625 ± 0.019
Pruning (5%)	0.577 ± 0.003	0.555 ± 0.015
Pruning (10%)	0.574 ± 0.003	0.506 ± 0.014
Non-uniform weighting	0.566 ± 0.004	0.520 ± 0.011

Table 1: AUC-ROC performance and fairness deviation on the COMPAS dataset for various fairness adaptations of DEAN. Notice that the performance is better the higher the value is, while the fairness is optimal at 0.5.

The baseline model exhibits a fairness deviation of over 14%, indicating a significant bias. With as little as 1% pruning, fairness improves, and pruning 10% of the submodels nearly eliminates the bias (deviation of only 0.6%, within experimental uncertainty), albeit with a slight reduction in overall performance (approximately 1% drop). Non-uniform weighting yields a more pronounced performance drop (1.7%) and a moderate fairness improvement (2% deviation). Notably, the modified loss function further increases performance by about 1.1% but overshoots fairness slightly, resulting in a 4.7% deviation.

Overall, these experiments confirm that the DEAN framework can be effectively adapted to enhance fairness, demonstrating its versatility and potential for broader real-world applications.

C Performance Result Plots with AUC-PR

Since our results are very similar whether we use AUC-ROC or AUC-PR, we only state most of our results in AUC-ROC and add the alternative plots here.

Table 2 gives an overview of the performance for all evaluated algorithms across all datasets when using AUC-PR instead of AUC-ROC. Figure 2 shows the critical difference plot when we use AUC-PR instead of AUC-ROC to compare the performance of algorithms. Additionally, Figure 3 shows the AUC-PR score as a function of the submodels used.

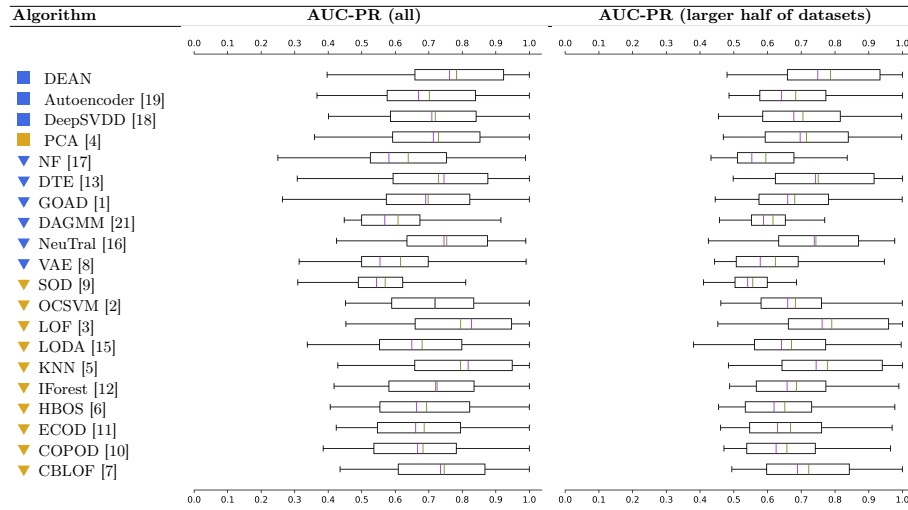


Table 2: Distribution of AUC-PR performance for all evaluated algorithms. Deep learning models (blue) and shallow models (yellow) are differentiated by surrogate status (squares for surrogates, triangles for non-surrogates). Mean and median values are shown in green and purple, respectively. Pendant to Table 1 in Section 5.2.

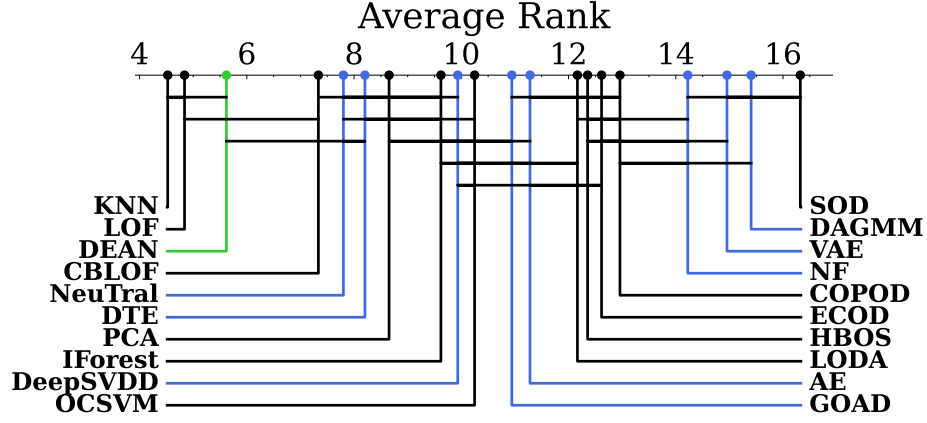


Fig. 2: Critical difference diagrams comparing the AUC-PR performance. A lower rank indicates better performance, while algorithms with no statistically significant differences are connected by a horizontal line. DEAN is depicted in green, other deep learning algorithms in blue. Pendant to Figure 2a in Section 5.2.

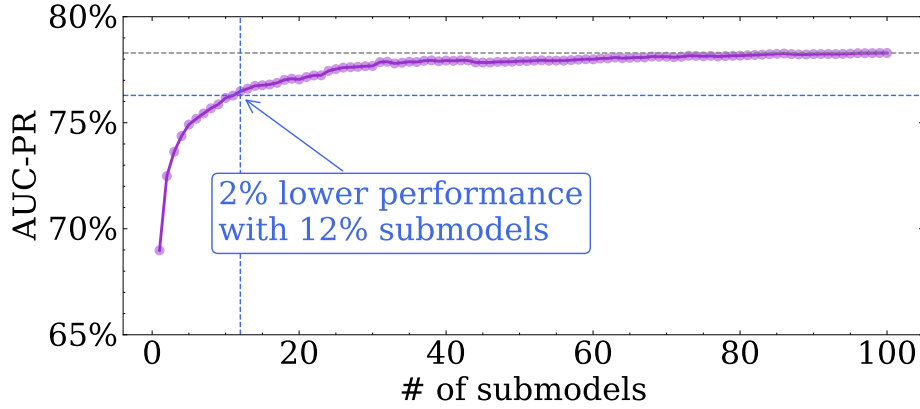


Fig. 3: AUC-PR performance changes with varying ensemble size, for DEAN. It reaches 2% less performance with the first 12% (instead of 13% for AUC-ROC) of submodels. Pendant to Figure 3b in Section 5.3.

D Individual Performance Scores

We state every performance in AUC-ROC in Tables 3, 4, 5, 6, 7 and 8. We also give the same performances in AUC-PR in Tables 9, 10, 11, 12, 13 and 14.

Table 3: AUC-ROC Scores for each datasets and algorithm (1/3|low performing algorithms)

Dataset	DEAN	HBOS	GOAD	ECOD	COPOD	LODA	NF	DAGMM	VAE	SOD
<i>20news</i> ²	56%	44%	44%	44%	43%	46%	49%	44%	54%	46%
<i>yeast</i>	59%	42%	68%	45%	38%	55%	48%	49%	41%	44%
<i>vertebral</i>	68%	38%	67%	41%	34%	26%	50%	50%	50%	38%
<i>MNISTC</i> ^{identity}	47%	49%	48%	48%	48%	48%	47%	49%	50%	46%
<i>speech</i>	59%	49%	50%	48%	50%	50%	47%	57%	49%	35%
<i>imdb</i>	53%	51%	54%	48%	53%	42%	53%	46%	42%	46%
<i>20news</i> ⁵	56%	49%	48%	48%	47%	55%	52%	48%	53%	44%
<i>WPBC</i>	54%	53%	45%	52%	54%	58%	49%	50%	48%	43%
<i>Wilt</i>	67%	36%	62%	38%	35%	37%	54%	70%	50%	32%
<i>20news</i> ⁴	59%	51%	53%	52%	50%	54%	42%	53%	48%	51%
<i>20news</i> ¹	64%	50%	52%	47%	50%	54%	51%	46%	44%	52%
<i>agnews</i> ⁰	63%	51%	53%	49%	52%	49%	50%	49%	50%	49%
<i>20news</i> ³	50%	56%	55%	55%	56%	61%	57%	49%	41%	51%
<i>MVTecAD</i> ^{screw}	60%	57%	52%	56%	56%	54%	47%	50%	57%	56%
<i>ALOI</i>	55%	54%	49%	54%	53%	52%	55%	53%	52%	54%
<i>amazon</i>	62%	57%	56%	55%	58%	61%	50%	50%	45%	54%
<i>SVHN</i> ⁶	65%	51%	64%	53%	52%	58%	54%	58%	52%	50%
<i>CIFAR10</i> ³	67%	48%	69%	52%	49%	59%	42%	54%	57%	51%
<i>CIFAR10</i> ⁵	67%	46%	69%	51%	47%	57%	52%	59%	53%	44%
<i>SVHN</i> ⁹	66%	51%	60%	54%	52%	54%	53%	55%	51%	56%
<i>SVHN</i> ³	65%	55%	60%	57%	56%	59%	46%	47%	50%	56%
<i>MNISTC</i> ^{rotate}	67%	56%	48%	55%	55%	50%	56%	53%	55%	51%
<i>CIFAR10</i> ²	61%	55%	59%	56%	55%	58%	54%	55%	55%	52%
<i>landsat</i>	77%	71%	61%	36%	42%	43%	45%	53%	57%	49%
<i>SVHN</i> ⁸	70%	50%	62%	53%	51%	56%	53%	55%	47%	56%
<i>yelp</i>	67%	60%	61%	58%	60%	59%	47%	59%	42%	56%
<i>agnews</i> ³	64%	56%	54%	56%	56%	53%	50%	56%	50%	55%
<i>SVHN</i> ⁰	76%	50%	65%	53%	51%	59%	40%	59%	54%	50%
<i>CIFAR10</i> ¹	75%	45%	73%	52%	47%	63%	47%	54%	53%	50%
<i>SVHN</i> ⁵	70%	57%	61%	59%	58%	64%	53%	57%	51%	57%
<i>MVTecAD</i> ^{pill}	62%	64%	52%	61%	65%	66%	51%	50%	50%	65%
<i>agnews</i> ¹	69%	58%	50%	58%	52%	58%	49%	52%	58%	50%
<i>SVHN</i> ⁴	66%	61%	54%	61%	61%	64%	52%	58%	62%	58%
<i>SVHN</i> ²	69%	58%	62%	60%	58%	64%	55%	50%	54%	61%
<i>census</i>	63%	66%	59%	66%	67%	55%	52%	61%	62%	58%
<i>fault</i>	75%	67%	69%	46%	45%	48%	57%	47%	52%	64%
<i>Hepatitis</i>	44%	82%	50%	73%	81%	74%	50%	50%	52%	52%
<i>SVHN</i> ⁷	66%	62%	62%	63%	62%	61%	51%	56%	62%	53%
<i>SVHN</i> ¹	68%	62%	68%	63%	61%	55%	47%	62%	63%	51%
<i>Pima</i>	65%	70%	61%	59%	65%	62%	49%	50%	50%	52%
<i>20news</i> ⁰	75%	62%	61%	60%	61%	61%	56%	56%	51%	64%
<i>CIFAR10</i> ⁷	69%	56%	71%	61%	57%	65%	54%	60%	65%	54%
<i>MNISTC</i> ^{translate}	85%	54%	54%	56%	56%	57%	51%	49%	50%	61%
<i>agnews</i> ²	74%	63%	61%	63%	63%	62%	54%	57%	48%	66%
<i>MVTecAD</i> ^{grid}	65%	61%	66%	62%	62%	59%	71%	50%	34%	60%
<i>MVTecAD</i> ^{capsule}	66%	67%	64%	66%	65%	65%	56%	50%	49%	70%
<i>MNISTC</i> ^{shear}	74%	64%	59%	64%	64%	60%	50%	54%	50%	60%
<i>letter</i>	90%	57%	51%	53%	51%	52%	56%	53%	49%	58%
<i>MVTecAD</i> ^{metal_nut}	67%	63%	69%	64%	62%	67%	55%	50%	46%	66%
<i>SpamBase</i>	68%	79%	44%	66%	69%	71%	71%	58%	50%	55%

Table 4: AUC-ROC Scores for each datasets and algorithm (1/3|high performing algorithms)

Dataset	DEAN	LOF	KNN	CBLOF	NeuTral	AE	IFor	PCA	D.SVDD	OCSVM	DTE
<i>20news</i> ²	56%	50%	48%	48%	57%	44%	46%	43%	44%	46%	49%
<i>yeast</i>	59%	47%	45%	47%	57%	42%	42%	43%	45%	45%	47%
<i>vertebral</i>	68%	53%	41%	46%	59%	66%	43%	41%	62%	41%	39%
<i>MNISTC</i> ^{identity}	47%	49%	48%	50%	49%	50%	48%	48%	50%	47%	49%
<i>speech</i>	59%	53%	51%	49%	44%	49%	52%	49%	49%	48%	56%
<i>imdb</i>	53%	54%	52%	53%	48%	52%	49%	49%	48%	48%	56%
<i>20news</i> ⁵	56%	52%	50%	55%	57%	49%	46%	48%	51%	49%	55%
<i>WPBC</i>	54%	55%	55%	51%	43%	48%	55%	54%	49%	54%	47%
<i>Wilt</i>	67%	90%	82%	48%	80%	22%	45%	24%	44%	85%	35%
<i>20news</i> ⁴	59%	55%	50%	55%	62%	53%	53%	51%	51%	52%	46%
<i>20news</i> ¹	64%	60%	61%	51%	62%	57%	47%	48%	52%	50%	47%
<i>agnews</i> ⁰	63%	67%	61%	56%	59%	61%	54%	51%	48%	50%	54%
<i>20news</i> ³	50%	55%	66%	55%	69%	53%	54%	55%	58%	53%	48%
<i>MVTecAD</i> ^{screw}	60%	56%	59%	56%	58%	55%	58%	60%	60%	56%	47%
<i>ALOI</i>	55%	76%	70%	55%	54%	52%	56%	56%	56%	52%	54%
<i>amazon</i>	62%	59%	62%	57%	54%	58%	56%	56%	58%	55%	49%
<i>SVHN</i> ⁶	65%	61%	59%	55%	57%	55%	56%	56%	56%	59%	59%
<i>CIFAR10</i> ³	67%	66%	60%	62%	61%	59%	53%	56%	51%	60%	57%
<i>CIFAR10</i> ⁵	67%	63%	57%	60%	67%	57%	54%	57%	57%	60%	59%
<i>SVHN</i> ⁹	66%	64%	62%	58%	61%	60%	54%	57%	54%	57%	59%
<i>SVHN</i> ³	65%	66%	61%	58%	64%	56%	58%	59%	59%	56%	60%
<i>MNISTC</i> ^{rotate}	67%	75%	67%	59%	58%	59%	57%	56%	55%	54%	63%
<i>CIFAR10</i> ²	61%	65%	60%	60%	56%	58%	58%	59%	55%	59%	61%
<i>landsat</i>	77%	75%	77%	67%	83%	60%	61%	40%	49%	47%	58%
<i>SVHN</i> ⁸	70%	67%	64%	59%	62%	63%	55%	57%	65%	55%	58%
<i>yelp</i>	67%	67%	67%	63%	62%	65%	60%	59%	42%	57%	52%
<i>agnews</i> ³	64%	75%	65%	60%	66%	63%	60%	58%	59%	57%	60%
<i>SVHN</i> ⁰	76%	74%	69%	62%	68%	68%	55%	59%	61%	61%	59%
<i>CIFAR10</i> ¹	75%	76%	63%	63%	73%	58%	52%	62%	63%	62%	72%
<i>SVHN</i> ⁵	70%	66%	64%	63%	61%	65%	59%	62%	57%	58%	61%
<i>MVTecAD</i> ^{pill}	62%	66%	67%	64%	67%	53%	65%	64%	61%	61%	52%
<i>agnews</i> ¹	69%	83%	69%	61%	69%	65%	61%	60%	57%	57%	75%
<i>SVHN</i> ⁴	66%	65%	66%	63%	61%	64%	61%	60%	59%	61%	63%
<i>SVHN</i> ²	69%	69%	65%	62%	66%	65%	60%	62%	60%	60%	65%
<i>census</i>	63%	55%	67%	66%	54%	60%	66%	71%	69%	55%	61%
<i>fault</i>	75%	63%	80%	71%	73%	71%	66%	55%	54%	59%	72%
<i>Hepatitis</i>	44%	60%	53%	48%	55%	51%	82%	85%	70%	47%	83%
<i>SVHN</i> ⁷	66%	66%	64%	65%	61%	67%	64%	65%	65%	66%	67%
<i>SVHN</i> ¹	68%	63%	67%	66%	66%	66%	63%	65%	65%	67%	66%
<i>Pima</i>	65%	67%	69%	68%	58%	70%	74%	72%	64%	62%	70%
<i>20news</i> ⁰	75%	78%	72%	64%	69%	64%	63%	63%	67%	61%	53%
<i>CIFAR10</i> ⁷	69%	71%	65%	65%	63%	61%	62%	65%	62%	68%	66%
<i>MNISTC</i> ^{translate}	85%	91%	81%	66%	76%	69%	58%	61%	63%	55%	69%
<i>agnews</i> ²	74%	75%	74%	68%	64%	71%	65%	65%	61%	63%	53%
<i>MVTecAD</i> ^{grid}	65%	68%	72%	65%	73%	70%	65%	64%	67%	65%	76%
<i>MVTecAD</i> ^{capsule}	66%	67%	68%	71%	66%	64%	68%	66%	63%	65%	63%
<i>MNISTC</i> ^{shear}	74%	79%	74%	70%	68%	70%	65%	66%	65%	59%	75%
<i>letter</i>	90%	88%	88%	78%	76%	81%	64%	54%	50%	90%	77%
<i>MVTecAD</i> ^{metal_nut}	67%	71%	73%	72%	72%	73%	68%	71%	71%	68%	75%
<i>SpamBase</i>	68%	64%	75%	70%	42%	70%	82%	80%	83%	76%	67%

Table 5: AUC-ROC Scores for each datasets and algorithm (2/3|low performing algorithms)

Dataset	DEAN	HBOS	GOAD	ECOD	COPOD	LODA	NF	DAGMM	VAE	SOD
<i>celeba</i>	68%	77%	64%	76%	75%	58%	80%	62%	69%	44%
<i>CIFAR10</i> ⁹	77%	60%	76%	64%	61%	65%	48%	62%	62%	59%
<i>FashionMNIST</i> ⁶	82%	52%	68%	60%	55%	68%	55%	62%	66%	44%
<i>Waveform</i>	73%	69%	79%	58%	73%	69%	67%	55%	30%	49%
<i>optdigits</i>	99%	88%	52%	52%	60%	50%	55%	46%	44%	21%
<i>MNISTC</i> ^{scale}	89%	59%	56%	59%	57%	80%	53%	48%	61%	17%
<i>MVTecAD</i> ^{cable}	67%	72%	66%	71%	71%	71%	51%	50%	51%	69%
<i>CIFAR10</i> ⁸	74%	66%	78%	68%	66%	68%	58%	61%	65%	58%
<i>Cardiotocography</i>	84%	57%	76%	79%	66%	79%	50%	74%	60%	39%
<i>CIFAR10</i> ⁶	77%	70%	72%	71%	71%	70%	56%	56%	63%	65%
<i>InternetAds</i>	86%	55%	75%	69%	69%	57%	79%	61%	71%	41%
<i>CIFAR10</i> ⁰	76%	70%	76%	71%	69%	72%	74%	58%	65%	63%
<i>campaign</i>	73%	80%	70%	77%	78%	65%	73%	56%	69%	63%
<i>MNISTC</i> ^{brightness}	93%	64%	60%	64%	63%	67%	51%	46%	61%	45%
<i>MVTecAD</i> ^{carpet}	74%	75%	74%	71%	74%	74%	60%	50%	53%	64%
<i>satellite</i>	77%	87%	79%	59%	64%	71%	54%	72%	50%	54%
<i>MVTecAD</i> ^{hazelnut}	68%	74%	70%	69%	72%	71%	58%	65%	66%	70%
<i>annthyroid</i>	77%	71%	46%	81%	79%	60%	94%	67%	68%	62%
<i>MNISTC</i> ^{canny_edges}	93%	73%	48%	69%	68%	72%	43%	59%	83%	39%
<i>cover</i>	50%	65%	98%	92%	88%	95%	50%	69%	50%	10%
<i>magic.gamma</i>	83%	75%	76%	64%	68%	67%	70%	70%	68%	73%
<i>glass</i>	89%	85%	93%	65%	75%	67%	64%	50%	59%	68%
<i>MVTecAD</i> ^{toothbrush}	72%	81%	72%	77%	73%	59%	67%	50%	57%	83%
<i>MVTecAD</i> ^{wood}	74%	76%	75%	76%	76%	72%	78%	50%	76%	75%
<i>mnist</i>	53%	73%	92%	75%	78%	80%	49%	72%	50%	47%
<i>CIFAR10</i> ⁴	77%	76%	78%	76%	76%	74%	78%	57%	71%	71%
<i>MNISTC</i> ^{shot_noise}	93%	71%	69%	71%	70%	74%	44%	58%	66%	55%
<i>PageBlocks</i>	85%	88%	72%	90%	87%	76%	53%	92%	50%	45%
<i>FashionMNIST</i> ⁸	93%	70%	79%	73%	71%	74%	50%	67%	68%	52%
<i>MVTecAD</i> ^{transistor}	75%	80%	75%	78%	79%	80%	69%	50%	76%	73%
<i>backdoor</i>	94%	65%	78%	84%	79%	25%	89%	56%	90%	53%
<i>vowels</i>	94%	65%	90%	56%	45%	71%	91%	52%	58%	54%
<i>MVTecAD</i> ^{zipper}	77%	80%	77%	77%	80%	78%	67%	50%	59%	84%
<i>MVTecAD</i> ^{tile}	79%	82%	80%	79%	81%	81%	71%	50%	54%	75%
<i>FashionMNIST</i> ⁴	90%	70%	85%	77%	73%	80%	53%	62%	71%	54%
<i>wine</i>	99%	85%	92%	68%	84%	78%	50%	50%	99%	19%
<i>MNISTC</i> ^{zigzag}	95%	79%	66%	79%	77%	76%	47%	57%	67%	62%
<i>skin</i>	97%	77%	89%	49%	47%	82%	93%	90%	50%	55%
<i>MNISTC</i> ^{dotted_line}	95%	75%	68%	76%	74%	69%	66%	67%	78%	64%
<i>FashionMNIST</i> ²	92%	66%	85%	74%	70%	79%	80%	74%	65%	53%
<i>MNISTC</i> ^{spatter}	93%	81%	80%	79%	79%	82%	42%	76%	49%	69%
<i>MNISTC</i> ^{motion_blur}	98%	79%	78%	77%	77%	77%	44%	76%	45%	63%
<i>musk</i>	53%	100%	87%	97%	96%	99%	53%	89%	50%	4%
<i>FashionMNIST</i> ⁰	91%	77%	81%	81%	78%	84%	59%	72%	80%	62%
<i>donors</i>	100%	79%	50%	89%	82%	60%	67%	90%	84%	60%
<i>smtp</i>	92%	82%	84%	90%	92%	87%	96%	85%	21%	63%
<i>FashionMNIST</i> ³	93%	82%	83%	84%	82%	77%	67%	58%	82%	61%
<i>MNISTC</i> ^{fog}	100%	79%	83%	79%	78%	89%	66%	71%	49%	37%
<i>mammography</i>	84%	84%	86%	90%	90%	90%	78%	87%	50%	64%
<i>Ionosphere</i>	86%	72%	82%	71%	78%	79%	96%	50%	75%	88%

Table 6: AUC-ROC Scores for each datasets and algorithm (2/3|high performing algorithms)

Dataset	DEAN	LOF	KNN	CBLOF	NeuTral	AE	IFor	PCA	D.SVDD	OCSVM	DTE
<i>celeba</i>	68%	46%	62%	59%	48%	67%	69%	80%	78%	72%	84%
<i>CIFAR10</i> ⁹	77%	78%	71%	71%	74%	73%	65%	70%	62%	69%	75%
<i>FashionMNIST</i> ⁶	82%	82%	81%	74%	75%	78%	63%	71%	72%	65%	77%
<i>Waveform</i>	73%	80%	81%	83%	67%	70%	68%	64%	68%	84%	66%
<i>optdigits</i>	99%	100%	100%	89%	64%	98%	86%	52%	47%	100%	50%
<i>MNISTC</i> ^{scale}	89%	94%	91%	84%	80%	83%	66%	73%	82%	65%	68%
<i>MVTecAD</i> ^{cable}	67%	78%	81%	75%	71%	72%	72%	71%	62%	74%	72%
<i>CIFAR10</i> ⁸	74%	76%	72%	71%	74%	73%	69%	72%	67%	72%	70%
<i>Cardiotocography</i>	84%	77%	76%	72%	64%	82%	79%	82%	73%	83%	51%
<i>CIFAR10</i> ⁶	77%	77%	79%	75%	76%	76%	74%	74%	62%	68%	76%
<i>InternetAds</i>	86%	86%	82%	73%	87%	71%	47%	79%	76%	72%	73%
<i>CIFAR10</i> ⁰	76%	76%	75%	71%	76%	68%	71%	73%	65%	71%	74%
<i>campaign</i>	73%	59%	74%	68%	78%	69%	75%	77%	70%	69%	74%
<i>MNISTC</i> ^{brightness}	93%	98%	92%	80%	80%	87%	73%	72%	76%	66%	84%
<i>MVTecAD</i> ^{carpet}	74%	77%	78%	77%	74%	74%	76%	76%	75%	75%	71%
<i>satellite</i>	77%	83%	87%	84%	80%	62%	79%	66%	68%	87%	70%
<i>MVTecAD</i> ^{hazelnut}	68%	81%	80%	77%	74%	79%	73%	72%	71%	69%	73%
<i>annthyroid</i>	77%	78%	78%	68%	85%	63%	92%	84%	80%	57%	58%
<i>MNISTC</i> ^{canny_edges}	93%	98%	93%	84%	80%	83%	73%	76%	68%	70%	80%
<i>cover</i>	50%	100%	100%	69%	99%	50%	88%	94%	93%	52%	50%
<i>magic.gamma</i>	83%	83%	84%	76%	78%	76%	78%	71%	69%	73%	86%
<i>glass</i>	89%	80%	100%	100%	97%	63%	89%	65%	73%	46%	59%
<i>MVTecAD</i> ^{toothbrush}	72%	64%	87%	85%	88%	90%	87%	73%	76%	65%	85%
<i>MVTecAD</i> ^{wood}	74%	77%	80%	77%	80%	78%	79%	78%	77%	75%	72%
<i>mnist</i>	53%	96%	94%	87%	98%	96%	87%	91%	87%	50%	50%
<i>CIFAR10</i> ⁴	77%	76%	80%	79%	78%	73%	77%	77%	79%	76%	79%
<i>MNISTC</i> ^{shot_noise}	93%	95%	96%	90%	81%	86%	78%	79%	74%	76%	84%
<i>PageBlocks</i>	85%	91%	66%	64%	97%	52%	92%	93%	90%	61%	66%
<i>FashionMNIST</i> ⁸	93%	93%	92%	86%	72%	88%	77%	80%	72%	75%	90%
<i>MVTecAD</i> ^{transistor}	75%	85%	79%	81%	81%	74%	82%	81%	74%	81%	72%
<i>backdoor</i>	94%	95%	95%	83%	90%	86%	76%	64%	57%	87%	89%
<i>vowels</i>	94%	97%	97%	90%	98%	90%	76%	61%	79%	81%	98%
<i>MVTecAD</i> ^{zipper}	77%	88%	87%	84%	90%	79%	81%	81%	78%	79%	78%
<i>MVTecAD</i> ^{tile}	79%	85%	86%	83%	79%	79%	84%	80%	79%	80%	84%
<i>FashionMNIST</i> ⁴	90%	88%	88%	85%	87%	86%	78%	84%	84%	82%	82%
<i>wine</i>	99%	99%	99%	99%	84%	100%	85%	90%	89%	90%	2%
<i>MNISTC</i> ^{zigzag}	95%	96%	94%	85%	89%	89%	84%	85%	88%	78%	92%
<i>skin</i>	97%	93%	100%	91%	89%	89%	89%	60%	66%	90%	92%
<i>MNISTC</i> ^{dotted_line}	95%	97%	95%	84%	87%	87%	80%	82%	80%	80%	86%
<i>FashionMNIST</i> ²	92%	88%	91%	89%	90%	89%	79%	83%	81%	78%	90%
<i>MNISTC</i> ^{spatter}	93%	96%	93%	86%	88%	90%	83%	85%	82%	77%	92%
<i>MNISTC</i> ^{motion_blur}	98%	98%	97%	89%	93%	92%	85%	86%	84%	75%	97%
<i>musk</i>	53%	100%	100%	100%	100%	100%	97%	100%	100%	50%	46%
<i>FashionMNIST</i> ⁰	91%	91%	92%	88%	90%	90%	82%	86%	81%	81%	88%
<i>donors</i>	100%	99%	100%	93%	40%	85%	92%	89%	92%	87%	99%
<i>smtp</i>	92%	93%	95%	86%	78%	80%	90%	84%	78%	84%	90%
<i>FashionMNIST</i> ³	93%	93%	92%	89%	87%	91%	83%	88%	86%	84%	93%
<i>MNISTC</i> ^{fog}	100%	100%	100%	97%	98%	99%	89%	91%	87%	82%	99%
<i>mammography</i>	84%	84%	86%	87%	74%	91%	88%	90%	91%	88%	86%
<i>Ionosphere</i>	86%	91%	94%	93%	95%	88%	87%	87%	90%	80%	93%

Table 7: AUC-ROC Scores for each datasets and algorithm (3/3|low performing algorithms)

Dataset	DEAN	HBOS	GOAD	ECOD	COPOD	LODA	NF	DAGMM	VAE	SOD
<i>shuttle</i>	100%	98%	82%	99%	99%	82%	9%	95%	50%	31%
<i>pendigits</i>	99%	94%	90%	92%	90%	88%	67%	64%	89%	21%
<i>MNISTC^{glass_blur}</i>	100%	90%	92%	89%	88%	90%	74%	62%	52%	54%
<i>cardio</i>	89%	84%	95%	93%	91%	95%	90%	69%	95%	45%
<i>http</i>	100%	99%	1%	97%	99%	43%	99%	99%	100%	40%
<i>MVTecAD^{bottle}</i>	96%	96%	92%	92%	96%	95%	91%	50%	7%	97%
<i>Stamps</i>	89%	90%	88%	90%	91%	91%	89%	72%	91%	52%
<i>satimage2</i>	100%	98%	92%	97%	98%	99%	61%	99%	50%	46%
<i>WDBC</i>	100%	99%	93%	97%	100%	100%	50%	82%	50%	79%
<i>Lymphography</i>	100%	100%	100%	100%	100%	58%	69%	50%	94%	58%
<i>WBC</i>	99%	99%	99%	100%	100%	99%	85%	50%	99%	75%
<i>FashionMNIST⁵</i>	96%	92%	96%	92%	91%	94%	73%	67%	79%	78%
<i>MNISTC^{stripe}</i>	100%	99%	90%	97%	97%	98%	40%	66%	87%	52%
<i>fraud</i>	94%	96%	91%	95%	95%	93%	92%	93%	95%	67%
<i>thyroid</i>	98%	99%	74%	98%	94%	93%	99%	83%	86%	66%
<i>FashionMNIST¹</i>	99%	92%	96%	94%	93%	95%	80%	73%	93%	76%
<i>FashionMNIST⁹</i>	98%	94%	97%	95%	94%	94%	68%	83%	91%	83%
<i>MVTecAD^{leather}</i>	99%	99%	99%	97%	98%	98%	92%	50%	72%	98%
<i>MNISTC^{impulse_noise}</i>	100%	99%	100%	98%	98%	100%	73%	98%	94%	41%
<i>FashionMNIST⁷</i>	98%	95%	96%	96%	95%	95%	91%	89%	92%	89%
<i>breastw</i>	100%	99%	99%	99%	100%	99%	97%	50%	100%	91%
Average	78%	71%	71%	70%	70%	69%	61%	61%	61%	56%
Rank	5.64	12.12	11.08	12.83	12.86	12.05	15.26	15.81	15.37	16.47

Table 8: AUC-ROC Scores for each datasets and algorithm (3/3|high performing algorithms)

Dataset	DEAN	LOF	KNN	CBLOF	NeuTral	AE	IFor	PCA	D.SVDD	OCSVM	DTE
<i>shuttle</i>	100%	100%	100%	99%	100%	100%	100%	99%	99%	100%	50%
<i>pendigits</i>	99%	99%	100%	97%	62%	89%	98%	93%	94%	94%	98%
<i>MNISTC^{glass_blur}</i>	100%	99%	100%	98%	96%	99%	95%	96%	97%	92%	99%
<i>cardio</i>	89%	93%	91%	92%	86%	91%	93%	95%	92%	94%	92%
<i>http</i>	100%	93%	100%	99%	100%	99%	99%	100%	100%	100%	99%
<i>MVTecAD^{bottle}</i>	96%	96%	96%	97%	96%	96%	97%	96%	96%	96%	95%
<i>Stamps</i>	89%	93%	95%	93%	99%	90%	92%	92%	93%	91%	92%
<i>satimage2</i>	100%	99%	100%	100%	100%	99%	100%	98%	97%	97%	50%
<i>WDBC</i>	100%	100%	100%	100%	96%	100%	100%	100%	100%	100%	40%
<i>Lymphography</i>	100%	97%	100%	100%	72%	100%	100%	100%	97%	100%	94%
<i>WBC</i>	99%	92%	99%	100%	72%	99%	99%	99%	93%	99%	40%
<i>FashionMNIST⁵</i>	96%	93%	96%	96%	96%	95%	93%	94%	94%	94%	95%
<i>MNISTC^{stripe}</i>	100%	100%	100%	100%	100%	100%	99%	100%	100%	97%	100%
<i>fraud</i>	94%	74%	97%	96%	92%	95%	96%	96%	94%	95%	96%
<i>thyroid</i>	98%	98%	97%	94%	99%	95%	99%	98%	97%	88%	93%
<i>FashionMNIST¹</i>	99%	98%	99%	97%	97%	99%	95%	97%	95%	96%	99%
<i>FashionMNIST⁹</i>	98%	98%	97%	96%	98%	97%	95%	96%	96%	96%	97%
<i>MVTecAD^{leather}</i>	99%	98%	99%	99%	99%	99%	99%	99%	99%	99%	99%
<i>MNISTC^{impulse_noise}</i>	100%	100%	100%	100%	100%	100%	100%	100%	100%	100%	100%
<i>FashionMNIST⁷</i>	98%	97%	97%	96%	97%	97%	95%	96%	96%	96%	96%
<i>breastw</i>	100%	96%	100%	100%	86%	99%	100%	99%	99%	99%	91%
Average	78%	80%	80%	76%	75%	75%	74%	73%	72%	72%	71%
Rank	5.64	5.00	4.33	7.13	7.35	8.31	8.93	9.00	10.45	10.81	9.20

Table 9: AUC-PR Scores for each datasets and algorithm (1/3|low performing algorithms)

Dataset	DEAN	GOAD	HBOS	ECOD	COPOD	LODA	NF	VAE	DAGMM	SOD
<i>20news</i> ²	56%	45%	44%	45%	44%	44%	44%	52%	45%	45%
<i>imdb</i>	53%	50%	48%	46%	49%	48%	54%	44%	46%	46%
<i>WPBC</i>	54%	46%	48%	47%	49%	50%	49%	49%	50%	45%
<i>MNISTC^{identity}</i>	47%	49%	49%	49%	49%	49%	48%	50%	50%	48%
<i>vertebral</i>	68%	58%	42%	43%	39%	37%	75%	50%	50%	41%
<i>yeast</i>	59%	61%	49%	50%	46%	54%	49%	45%	53%	45%
<i>20news</i> ¹	64%	50%	49%	47%	49%	45%	47%	45%	47%	50%
<i>speech</i>	59%	50%	50%	50%	52%	48%	52%	50%	55%	39%
<i>20news</i> ⁵	56%	50%	50%	50%	48%	49%	51%	56%	47%	49%
<i>20news</i> ⁴	59%	52%	51%	51%	50%	52%	45%	52%	53%	48%
<i>20news</i> ³	50%	51%	54%	51%	56%	49%	59%	42%	48%	50%
<i>Wilt</i>	67%	57%	41%	43%	39%	42%	57%	50%	59%	38%
<i>agnews</i> ⁰	63%	51%	52%	50%	52%	46%	50%	49%	50%	50%
<i>amazon</i>	62%	54%	55%	53%	56%	49%	51%	47%	50%	52%
<i>census</i>	63%	52%	57%	58%	59%	39%	48%	54%	56%	53%
<i>CIFAR10</i> ²	61%	57%	52%	53%	53%	59%	53%	54%	58%	50%
<i>MVTecAD^{screw}</i>	60%	53%	59%	58%	58%	55%	47%	59%	50%	55%
<i>ALOI</i>	55%	50%	54%	54%	52%	57%	56%	55%	55%	54%
<i>MNISTC^{rotate}</i>	67%	49%	54%	53%	53%	55%	53%	56%	55%	50%
<i>CIFAR10</i> ⁵	67%	67%	47%	50%	47%	61%	55%	54%	62%	48%
<i>agnews</i> ³	64%	53%	54%	54%	54%	54%	52%	50%	53%	54%
<i>landsat</i>	77%	59%	68%	42%	45%	44%	45%	52%	53%	49%
<i>SVHN</i> ³	65%	59%	53%	55%	54%	56%	68%	49%	46%	54%
<i>CIFAR10</i> ³	67%	67%	50%	53%	51%	53%	47%	56%	51%	53%
<i>agnews</i> ¹	69%	48%	53%	55%	49%	50%	48%	57%	51%	50%
<i>SVHN</i> ⁹	66%	58%	52%	54%	53%	51%	54%	51%	55%	58%
<i>yelp</i>	67%	58%	59%	56%	59%	54%	50%	45%	59%	54%
<i>SVHN</i> ⁸	70%	60%	50%	53%	52%	49%	56%	49%	54%	59%
<i>CIFAR10</i> ¹	75%	68%	45%	49%	47%	58%	49%	52%	56%	50%
<i>SVHN</i> ⁶	65%	63%	53%	55%	54%	64%	57%	53%	57%	54%
<i>SVHN</i> ⁰	76%	62%	52%	53%	52%	56%	44%	55%	60%	54%
<i>SVHN</i> ⁵	70%	61%	56%	58%	57%	56%	57%	50%	58%	58%
<i>SVHN</i> ¹	68%	66%	60%	60%	59%	59%	49%	63%	63%	48%
<i>20news</i> ⁰	75%	57%	59%	58%	59%	60%	55%	53%	55%	59%
<i>SVHN</i> ²	69%	62%	59%	61%	59%	57%	57%	55%	52%	60%
<i>Hepatitis</i>	44%	55%	74%	60%	67%	66%	75%	50%	50%	50%
<i>SVHN</i> ⁴	66%	54%	62%	62%	62%	63%	56%	63%	60%	56%
<i>Pima</i>	65%	59%	67%	61%	67%	60%	25%	50%	50%	55%
<i>fault</i>	75%	65%	66%	47%	46%	49%	60%	54%	49%	62%
<i>MNISTC^{translate}</i>	85%	55%	52%	54%	54%	59%	50%	51%	53%	57%
<i>SVHN</i> ⁷	66%	60%	64%	63%	63%	67%	55%	63%	60%	51%
<i>MVTecAD^{pill}</i>	62%	57%	65%	64%	66%	63%	60%	53%	50%	67%
<i>CIFAR10</i> ⁷	69%	70%	58%	61%	59%	64%	55%	64%	58%	57%
<i>agnews</i> ²	74%	62%	63%	61%	63%	64%	56%	50%	59%	64%
<i>MNISTC^{scale}</i>	89%	51%	53%	53%	52%	60%	53%	55%	46%	34%
<i>MNISTC^{shear}</i>	74%	61%	64%	64%	64%	67%	51%	52%	57%	60%
<i>FashionMNIST</i> ⁶	82%	68%	49%	55%	51%	61%	53%	61%	61%	47%
<i>letter</i>	90%	51%	54%	55%	53%	50%	58%	49%	58%	57%
<i>MVTecAD^{capsule}</i>	66%	69%	68%	69%	68%	63%	59%	54%	50%	72%
<i>MVTecAD^{grid}</i>	65%	68%	61%	64%	64%	70%	77%	44%	50%	64%

Table 10: AUC-PR Scores for each datasets and algorithm (1/3|high performing algorithms)

Dataset	DEAN	LOF	KNN	NeuTral	CBLOF	PCA	DTE	IFor	OCSVM	D.SVDD	AE
<i>20news</i> ²	56%	49%	47%	57%	44%	44%	51%	44%	45%	43%	47%
<i>imdb</i>	53%	52%	48%	50%	49%	47%	53%	49%	46%	45%	49%
<i>WPBC</i>	54%	50%	50%	46%	47%	51%	48%	52%	52%	51%	48%
<i>MNISTC^{identity}</i>	47%	50%	49%	50%	51%	49%	50%	50%	48%	49%	54%
<i>vertebral</i>	68%	51%	43%	60%	47%	42%	40%	42%	53%	44%	68%
<i>yeast</i>	59%	50%	49%	57%	48%	47%	49%	47%	48%	45%	48%
<i>20news</i> ¹	64%	60%	61%	63%	50%	48%	48%	49%	48%	52%	53%
<i>speech</i>	59%	55%	53%	46%	51%	51%	58%	48%	51%	58%	51%
<i>20news</i> ⁵	56%	53%	51%	58%	53%	50%	54%	50%	51%	55%	47%
<i>20news</i> ⁴	59%	54%	49%	62%	52%	52%	48%	51%	52%	52%	51%
<i>20news</i> ³	50%	52%	67%	67%	52%	54%	50%	55%	50%	52%	51%
<i>Wilt</i>	67%	89%	70%	78%	47%	36%	39%	47%	85%	40%	37%
<i>agnews</i> ⁰	63%	65%	60%	60%	55%	52%	51%	54%	50%	51%	58%
<i>amazon</i>	62%	54%	56%	57%	55%	55%	51%	55%	54%	52%	56%
<i>census</i>	63%	50%	59%	55%	53%	65%	56%	55%	50%	65%	53%
<i>CIFAR10</i> ²	61%	62%	58%	56%	59%	56%	58%	53%	56%	55%	56%
<i>MVTecAD^{screw}</i>	60%	55%	59%	59%	54%	63%	52%	60%	57%	61%	50%
<i>ALOI</i>	55%	74%	71%	55%	56%	56%	55%	54%	55%	56%	55%
<i>MNISTC^{rotate}</i>	67%	74%	67%	58%	56%	56%	62%	54%	52%	55%	56%
<i>CIFAR10</i> ⁵	67%	66%	59%	68%	59%	58%	59%	52%	60%	53%	50%
<i>agnews</i> ³	64%	75%	64%	66%	58%	55%	58%	55%	54%	57%	56%
<i>landsat</i>	77%	80%	75%	82%	64%	45%	58%	62%	48%	42%	56%
<i>SVHN</i> ³	65%	66%	60%	64%	57%	58%	61%	57%	54%	58%	52%
<i>CIFAR10</i> ³	67%	68%	63%	64%	62%	56%	59%	56%	59%	54%	59%
<i>agnews</i> ¹	69%	83%	66%	70%	57%	55%	71%	55%	54%	56%	57%
<i>SVHN</i> ⁹	66%	66%	65%	62%	59%	59%	63%	55%	55%	59%	60%
<i>yelp</i>	67%	63%	63%	62%	59%	59%	52%	61%	57%	58%	60%
<i>SVHN</i> ⁸	70%	68%	66%	64%	60%	60%	60%	56%	54%	61%	59%
<i>CIFAR10</i> ¹	75%	76%	61%	73%	59%	60%	71%	51%	59%	54%	55%
<i>SVHN</i> ⁶	65%	62%	61%	59%	63%	59%	63%	56%	59%	63%	51%
<i>SVHN</i> ⁰	76%	72%	69%	67%	64%	60%	62%	57%	58%	59%	61%
<i>SVHN</i> ⁵	70%	66%	65%	63%	63%	62%	63%	60%	57%	62%	59%
<i>SVHN</i> ¹	68%	58%	64%	66%	66%	61%	62%	62%	66%	56%	58%
<i>20news</i> ⁰	75%	75%	71%	69%	61%	59%	52%	61%	58%	58%	62%
<i>SVHN</i> ²	69%	66%	65%	67%	62%	62%	65%	61%	60%	63%	58%
<i>Hepatitis</i>	44%	64%	50%	57%	50%	76%	87%	63%	60%	67%	58%
<i>SVHN</i> ⁴	66%	61%	66%	61%	66%	60%	63%	61%	62%	62%	58%
<i>Pima</i>	65%	65%	69%	59%	68%	68%	67%	69%	71%	66%	68%
<i>fault</i>	75%	60%	76%	71%	70%	57%	71%	64%	60%	61%	72%
<i>MNISTC^{translate}</i>	85%	89%	77%	75%	61%	60%	70%	57%	55%	62%	60%
<i>SVHN</i> ⁷	66%	64%	64%	61%	64%	62%	67%	62%	67%	61%	62%
<i>MVTecAD^{pill}</i>	62%	69%	68%	68%	67%	65%	60%	66%	64%	65%	60%
<i>CIFAR10</i> ⁷	69%	73%	67%	63%	65%	66%	67%	61%	66%	61%	57%
<i>agnews</i> ²	74%	74%	73%	65%	67%	64%	53%	66%	63%	60%	62%
<i>MNISTC^{scale}</i>	89%	91%	89%	81%	77%	70%	66%	66%	60%	69%	72%
<i>MNISTC^{shear}</i>	74%	80%	75%	67%	69%	67%	77%	65%	62%	67%	62%
<i>FashionMNIST</i> ⁶	82%	86%	82%	74%	71%	68%	77%	59%	62%	73%	68%
<i>letter</i>	90%	89%	86%	75%	78%	56%	79%	58%	89%	54%	78%
<i>MVTecAD^{capsule}</i>	66%	70%	71%	67%	73%	69%	68%	69%	68%	68%	55%
<i>MVTecAD^{grid}</i>	65%	73%	77%	74%	69%	67%	78%	69%	67%	67%	57%

Table 11: AUC-PR Scores for each datasets and algorithm (2/3|low performing algorithms)

Dataset	DEAN	GOAD	HBOS	ECOD	COPOD	LODA	NF	VAE	DAGMM	SOD
<i>MVTecAD^{metal_nut}</i>	67%	74%	60%	62%	60%	71%	56%	48%	50%	68%
<i>SpamBase</i>	68%	54%	76%	61%	63%	72%	77%	50%	55%	53%
<i>celeba</i>	68%	66%	78%	77%	76%	58%	73%	69%	59%	42%
<i>optdigits</i>	99%	48%	84%	47%	52%	46%	64%	46%	45%	35%
<i>CIFAR10⁹</i>	77%	75%	62%	65%	63%	71%	53%	64%	63%	59%
<i>CIFAR10⁸</i>	74%	78%	63%	65%	64%	75%	56%	65%	62%	57%
<i>CIFAR10⁶</i>	77%	72%	65%	66%	65%	62%	60%	61%	56%	61%
<i>Waveform</i>	73%	74%	64%	58%	68%	65%	77%	39%	59%	51%
<i>MNISTC^{brightness}</i>	93%	57%	60%	60%	59%	65%	51%	58%	51%	47%
<i>CIFAR10⁰</i>	76%	75%	69%	69%	68%	66%	73%	64%	57%	61%
<i>MVTecAD^{cable}</i>	67%	70%	72%	72%	71%	80%	56%	54%	50%	74%
<i>MNISTC^{canny_edges}</i>	93%	44%	67%	63%	62%	65%	47%	81%	60%	41%
<i>skin</i>	97%	80%	66%	45%	44%	64%	85%	50%	76%	50%
<i>campaign</i>	73%	72%	80%	77%	78%	66%	74%	70%	54%	59%
<i>Cardiotocography</i>	84%	74%	63%	76%	67%	76%	75%	59%	72%	46%
<i>annthyroid</i>	77%	49%	77%	79%	72%	57%	93%	69%	70%	61%
<i>cover</i>	50%	97%	65%	89%	85%	89%	25%	50%	70%	32%
<i>MVTecAD^{carpet}</i>	74%	77%	77%	73%	76%	75%	66%	59%	50%	71%
<i>MVTecAD^{hazelnut}</i>	68%	69%	78%	73%	76%	77%	58%	70%	64%	69%
<i>InternetAds</i>	86%	80%	60%	75%	75%	43%	86%	78%	64%	43%
<i>MNISTC^{shot_noise}</i>	93%	63%	66%	67%	66%	82%	52%	64%	56%	52%
<i>CIFAR10⁴</i>	77%	79%	75%	76%	75%	76%	78%	71%	56%	69%
<i>FashionMNIST⁸</i>	93%	74%	67%	69%	68%	76%	74%	64%	67%	52%
<i>MVTecAD^{toothbrush}</i>	72%	75%	85%	80%	75%	54%	70%	63%	50%	87%
<i>backdoor</i>	94%	67%	58%	78%	73%	38%	94%	93%	61%	62%
<i>MNISTC^{zigzag}</i>	95%	59%	73%	73%	71%	73%	49%	65%	57%	60%
<i>vowels</i>	94%	90%	67%	62%	45%	65%	86%	58%	51%	50%
<i>donors</i>	100%	46%	71%	84%	78%	39%	67%	71%	85%	62%
<i>satellite</i>	77%	82%	89%	67%	71%	81%	55%	50%	82%	55%
<i>FashionMNIST⁴</i>	90%	84%	65%	73%	68%	77%	57%	68%	60%	54%
<i>MNISTC^{dotted_line}</i>	95%	59%	70%	71%	69%	72%	62%	78%	67%	61%
<i>FashionMNIST²</i>	92%	83%	58%	66%	61%	77%	77%	60%	73%	53%
<i>mnist</i>	53%	91%	68%	68%	73%	81%	56%	50%	72%	50%
<i>PageBlocks</i>	85%	74%	84%	87%	83%	75%	66%	50%	91%	55%
<i>magic.gamma</i>	83%	81%	76%	67%	71%	73%	76%	73%	73%	75%
<i>MVTecAD^{zipper}</i>	77%	75%	79%	77%	79%	75%	74%	65%	50%	82%
<i>MVTecAD^{wood}</i>	74%	79%	79%	80%	80%	76%	82%	80%	50%	76%
<i>glass</i>	89%	90%	86%	71%	79%	64%	69%	68%	50%	82%
<i>MVTecAD^{transistor}</i>	75%	79%	83%	83%	83%	76%	71%	80%	50%	76%
<i>wine</i>	99%	89%	85%	59%	71%	61%	75%	99%	50%	35%
<i>MNISTC^{spatter}</i>	93%	78%	76%	75%	75%	79%	43%	48%	77%	66%
<i>MNISTC^{motion_blur}</i>	98%	73%	76%	73%	73%	82%	53%	47%	72%	58%
<i>MVTecAD^{tile}</i>	79%	84%	86%	84%	86%	82%	79%	58%	50%	81%
<i>FashionMNIST⁰</i>	91%	78%	73%	77%	74%	82%	58%	78%	71%	61%
<i>MNISTC^{fog}</i>	100%	81%	73%	74%	73%	78%	61%	45%	71%	41%
<i>FashionMNIST³</i>	93%	83%	77%	79%	78%	82%	68%	79%	62%	62%
<i>http</i>	100%	26%	86%	75%	85%	34%	90%	100%	87%	32%
<i>Stamps</i>	89%	89%	76%	82%	77%	78%	82%	84%	71%	48%
<i>Ionosphere</i>	86%	80%	62%	74%	76%	69%	96%	79%	50%	92%
<i>mammography</i>	84%	89%	82%	92%	92%	89%	72%	50%	88%	58%

Table 12: AUC-PR Scores for each datasets and algorithm (2/3|high performing algorithms)

Dataset	DEAN	LOF	KNN	NeuTral	CBLOF	PCA	DTE	IFor	OCSVM	D.SVDD	AE
<i>MVTecAD^{metal_nut}</i>	67%	77%	78%	72%	77%	68%	80%	68%	70%	71%	59%
<i>SpamBase</i>	68%	64%	75%	45%	70%	79%	66%	80%	76%	79%	72%
<i>celeba</i>	68%	45%	62%	49%	67%	81%	77%	74%	73%	76%	67%
<i>optdigits</i>	99%	100%	100%	66%	72%	46%	75%	79%	100%	43%	97%
<i>CIFAR10⁹</i>	77%	78%	72%	75%	70%	70%	73%	67%	69%	68%	63%
<i>CIFAR10⁸</i>	74%	76%	70%	74%	69%	70%	68%	66%	72%	66%	66%
<i>CIFAR10⁶</i>	77%	76%	75%	75%	71%	70%	75%	67%	66%	72%	68%
<i>Waveform</i>	73%	84%	83%	68%	85%	62%	67%	73%	85%	51%	76%
<i>MNISTC^{brightness}</i>	93%	98%	90%	81%	77%	70%	84%	66%	62%	73%	72%
<i>CIFAR10⁰</i>	76%	74%	73%	76%	70%	72%	74%	68%	70%	74%	64%
<i>MVTecAD^{cable}</i>	67%	81%	82%	71%	74%	70%	75%	76%	74%	65%	63%
<i>MNISTC^{canny_edges}</i>	93%	97%	91%	80%	78%	72%	79%	69%	63%	84%	68%
<i>skin</i>	97%	83%	100%	90%	79%	52%	80%	76%	76%	60%	51%
<i>campaign</i>	73%	53%	74%	76%	70%	77%	75%	73%	72%	71%	68%
<i>Cardiotocography</i>	84%	75%	74%	64%	75%	81%	55%	77%	82%	78%	84%
<i>annthyroid</i>	77%	81%	78%	83%	70%	84%	59%	91%	57%	84%	61%
<i>cover</i>	50%	100%	100%	98%	59%	90%	75%	78%	76%	78%	51%
<i>MVTecAD^{carpet}</i>	74%	81%	81%	73%	80%	78%	74%	78%	78%	76%	67%
<i>MVTecAD^{hazelnut}</i>	68%	85%	82%	75%	80%	76%	79%	78%	73%	77%	60%
<i>InternetAds</i>	86%	89%	86%	86%	80%	82%	76%	45%	78%	82%	77%
<i>MNISTC^{shot_noise}</i>	93%	94%	95%	79%	87%	77%	86%	72%	73%	80%	74%
<i>CIFAR10⁴</i>	77%	77%	80%	78%	78%	78%	79%	76%	76%	76%	64%
<i>FashionMNIST⁸</i>	93%	93%	89%	73%	81%	76%	88%	73%	70%	73%	78%
<i>MVTecAD^{toothbrush}</i>	72%	64%	88%	87%	86%	80%	88%	89%	72%	79%	56%
<i>backdoor</i>	94%	96%	96%	91%	72%	58%	92%	67%	78%	61%	77%
<i>MNISTC^{zigzag}</i>	95%	96%	93%	88%	81%	84%	93%	77%	72%	82%	73%
<i>vowels</i>	94%	96%	96%	98%	80%	63%	96%	78%	82%	69%	89%
<i>donors</i>	100%	99%	100%	42%	83%	82%	97%	84%	76%	68%	89%
<i>satellite</i>	77%	88%	90%	79%	89%	78%	70%	85%	89%	77%	71%
<i>FashionMNIST⁴</i>	90%	90%	89%	86%	84%	84%	86%	72%	79%	84%	74%
<i>MNISTC^{dotted_line}</i>	95%	96%	94%	86%	81%	81%	87%	73%	75%	78%	71%
<i>FashionMNIST²</i>	92%	90%	90%	90%	86%	83%	92%	73%	73%	83%	78%
<i>mnist</i>	53%	96%	94%	96%	86%	90%	75%	84%	75%	88%	96%
<i>PageBlocks</i>	85%	92%	70%	96%	63%	91%	74%	90%	71%	88%	58%
<i>magic.gamma</i>	83%	85%	86%	79%	79%	74%	88%	78%	77%	72%	79%
<i>MVTecAD^{zipper}</i>	77%	88%	86%	89%	84%	81%	82%	80%	80%	78%	70%
<i>MVTecAD^{wood}</i>	74%	83%	84%	79%	83%	83%	80%	82%	80%	84%	60%
<i>glass</i>	89%	88%	100%	96%	100%	71%	61%	88%	61%	67%	72%
<i>MVTecAD^{transistor}</i>	75%	88%	83%	81%	83%	84%	78%	86%	84%	79%	66%
<i>wine</i>	99%	99%	99%	83%	99%	85%	31%	74%	92%	86%	100%
<i>MNISTC^{spatter}</i>	93%	97%	94%	87%	87%	85%	93%	84%	76%	85%	77%
<i>MNISTC^{motion_blur}</i>	98%	98%	96%	91%	86%	85%	97%	80%	72%	85%	83%
<i>MVTecAD^{tile}</i>	79%	88%	88%	77%	88%	80%	87%	87%	83%	79%	58%
<i>FashionMNIST⁰</i>	91%	91%	92%	91%	86%	84%	88%	78%	78%	80%	81%
<i>MNISTC^{fog}</i>	100%	100%	100%	97%	95%	90%	98%	81%	81%	85%	93%
<i>FashionMNIST³</i>	93%	93%	92%	87%	87%	88%	93%	79%	81%	89%	78%
<i>http</i>	100%	59%	100%	99%	91%	99%	93%	79%	100%	99%	99%
<i>Stamps</i>	89%	89%	91%	98%	90%	85%	84%	79%	83%	89%	86%
<i>Ionosphere</i>	86%	91%	94%	94%	95%	89%	94%	86%	84%	85%	88%
<i>mammography</i>	84%	86%	88%	74%	85%	91%	86%	90%	89%	91%	92%

Table 13: AUC-PR Scores for each datasets and algorithm (3/3|low performing algorithms)

Dataset	DEAN	GOAD	HBOS	ECOD	COPOD	LODA	NF	VAE	DAGMM	SOD
<i>musk</i>	53%	74%	100%	97%	95%	99%	76%	50%	92%	31%
<i>pendigits</i>	99%	84%	92%	90%	87%	96%	58%	88%	56%	37%
<i>smtp</i>	92%	89%	88%	91%	93%	92%	96%	36%	89%	65%
<i>MNISTC^{glass_blur}</i>	100%	89%	86%	84%	83%	93%	79%	49%	63%	52%
<i>cardio</i>	89%	94%	85%	90%	89%	89%	91%	91%	69%	48%
<i>shuttle</i>	100%	87%	99%	99%	100%	90%	32%	50%	95%	42%
<i>WBC</i>	99%	99%	99%	100%	100%	94%	71%	99%	50%	70%
<i>satimage2</i>	100%	86%	98%	98%	98%	99%	53%	50%	99%	53%
<i>MVTecAD^{bottle}</i>	96%	95%	97%	93%	97%	96%	93%	31%	50%	97%
<i>WDBC</i>	100%	93%	99%	98%	100%	100%	75%	50%	77%	79%
<i>thyroid</i>	98%	73%	99%	98%	90%	91%	99%	86%	83%	58%
<i>FashionMNIST⁵</i>	96%	97%	93%	94%	93%	96%	77%	82%	68%	76%
<i>MNISTC^{stripe}</i>	100%	86%	98%	96%	96%	99%	55%	86%	65%	51%
<i>Lymphography</i>	100%	100%	100%	100%	100%	96%	82%	94%	50%	49%
<i>FashionMNIST¹</i>	99%	93%	91%	92%	91%	95%	75%	92%	73%	74%
<i>fraud</i>	94%	94%	97%	97%	96%	97%	95%	97%	95%	67%
<i>FashionMNIST⁹</i>	98%	97%	94%	95%	94%	95%	78%	93%	84%	81%
<i>breastw</i>	100%	99%	99%	99%	100%	99%	94%	100%	50%	88%
<i>MVTecAD^{leather}</i>	99%	99%	99%	97%	98%	91%	95%	82%	50%	98%
<i>MNISTC^{impulse_noise}</i>	100%	100%	98%	97%	96%	100%	84%	95%	97%	44%
<i>FashionMNIST⁷</i>	98%	97%	96%	96%	96%	97%	94%	93%	91%	90%
Average	78%	70%	69%	69%	68%	68%	64%	62%	61%	57%
Rank	5.72	10.90	12.34	12.62	12.95	12.14	14.19	14.95	15.38	16.28

Table 14: AUC-PR Scores for each datasets and algorithm (3/3|high performing algorithms)

Dataset	DEAN	LOF	KNN	NeuTral	CBLOF	PCA	DTE	IFor	OCSVM	D.SVDD	AE
<i>musk</i>	53%	100%	100%	99%	100%	100%	43%	96%	75%	100%	100%
<i>pendigits</i>	99%	98%	100%	61%	98%	90%	98%	96%	91%	78%	84%
<i>smtp</i>	92%	95%	95%	77%	90%	89%	92%	80%	88%	87%	65%
<i>MNISTC^{glass_blur}</i>	100%	99%	100%	94%	97%	95%	99%	91%	89%	95%	93%
<i>cardio</i>	89%	91%	90%	85%	89%	94%	90%	93%	91%	97%	91%
<i>shuttle</i>	100%	100%	99%	98%	98%	99%	75%	100%	100%	99%	99%
<i>WBC</i>	99%	92%	99%	73%	99%	99%	45%	99%	99%	97%	98%
<i>satimage2</i>	100%	99%	100%	97%	100%	99%	75%	99%	97%	83%	99%
<i>MVTecAD^{bottle}</i>	96%	97%	97%	93%	97%	97%	97%	97%	97%	97%	87%
<i>WDBC</i>	100%	100%	100%	95%	100%	100%	40%	100%	100%	100%	100%
<i>thyroid</i>	98%	98%	97%	98%	92%	98%	93%	99%	88%	98%	85%
<i>FashionMNIST⁵</i>	96%	95%	97%	96%	96%	96%	96%	95%	96%	95%	90%
<i>MNISTC^{stripe}</i>	100%	100%	100%	98%	100%	100%	100%	99%	97%	100%	99%
<i>Lymphography</i>	100%	97%	100%	71%	100%	100%	94%	100%	100%	100%	100%
<i>FashionMNIST¹</i>	99%	98%	98%	98%	94%	96%	98%	94%	94%	96%	96%
<i>fraud</i>	94%	71%	98%	92%	97%	97%	97%	96%	97%	96%	97%
<i>FashionMNIST⁹</i>	98%	98%	98%	96%	97%	96%	98%	95%	96%	96%	92%
<i>breastw</i>	100%	92%	100%	83%	100%	99%	89%	100%	99%	98%	99%
<i>MVTecAD^{leather}</i>	99%	98%	99%	97%	99%	99%	99%	99%	99%	98%	97%
<i>MNISTC^{impulse_noise}</i>	100%	100%	100%	98%	100%	100%	100%	99%	100%	100%	100%
<i>FashionMNIST⁷</i>	98%	98%	98%	95%	97%	97%	97%	97%	97%	96%	90%
Average	78%	80%	80%	75%	75%	73%	73%	72%	72%	72%	70%
Rank	5.72	4.88	4.57	7.87	7.33	8.62	8.19	9.61	10.24	9.91	11.31

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