

Logistic Regression

X variables

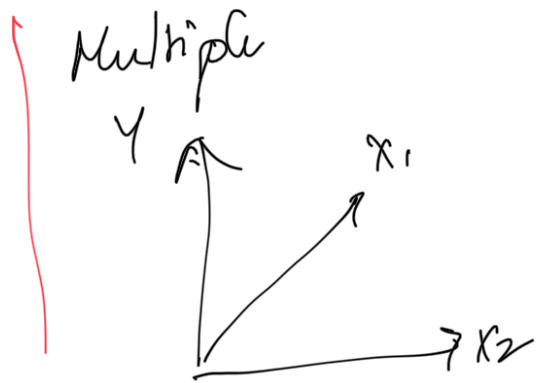
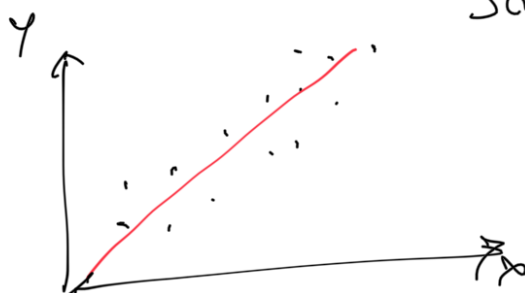
Y variables

Independent

Target

⇒ ① Simple linear regression

② Multiple regression



i) Nature of the algorithm

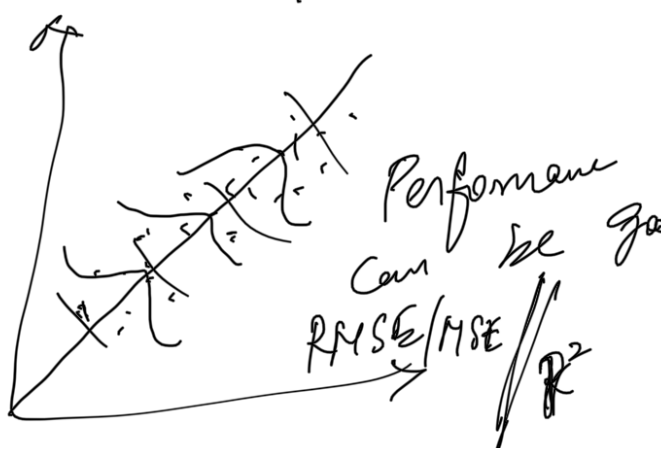
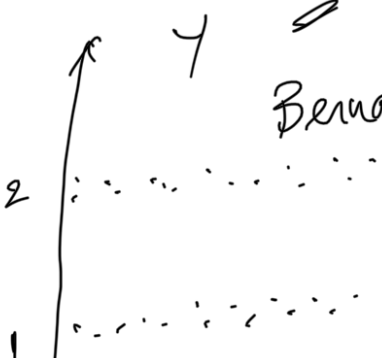
ii) Loss function

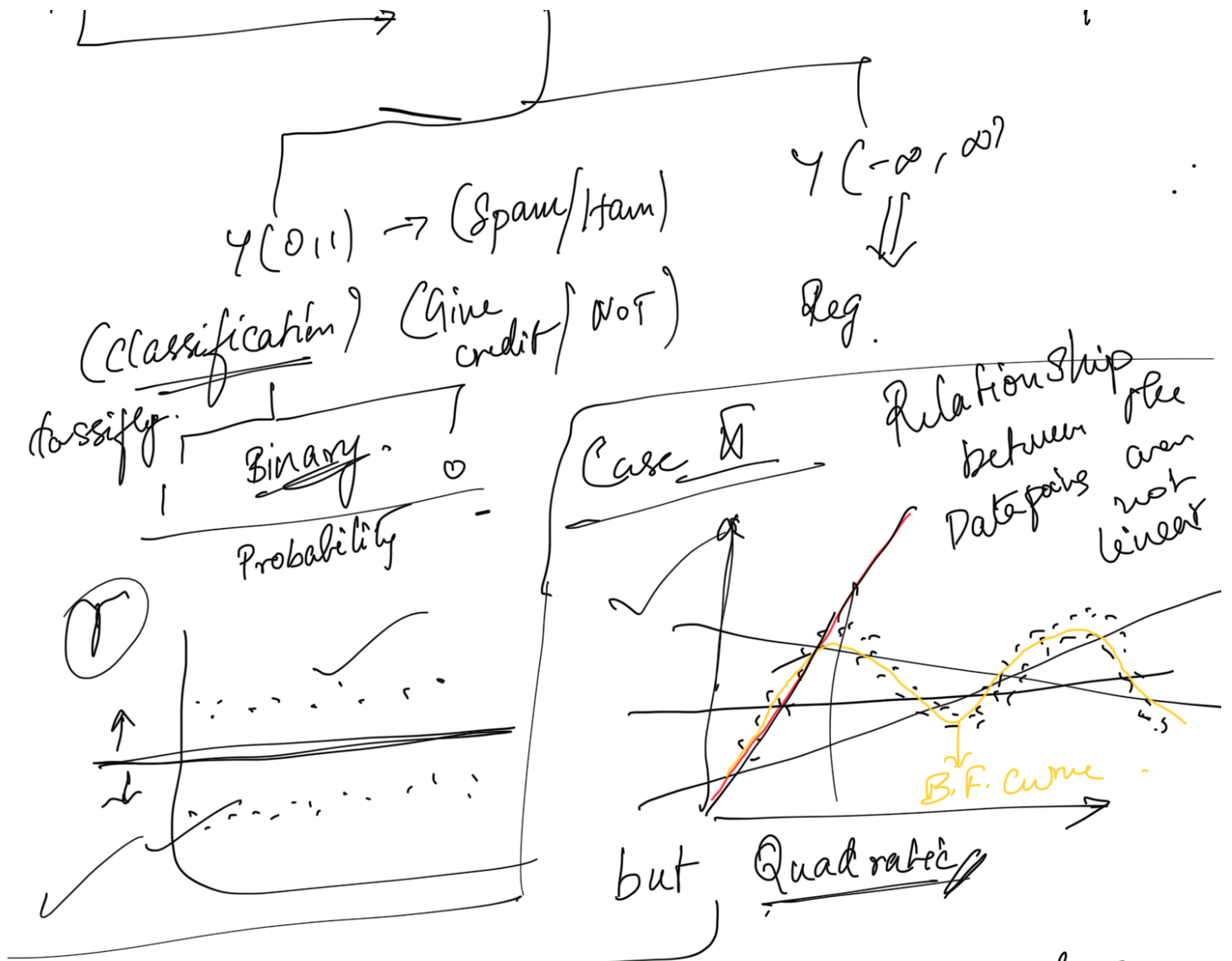
⇒ Linear Regression

abs() Independent var $Y \in \mathbb{R}^n$

Linear Regress
↓
Line
↓
Bernouli distribut.

* Cases where linear Reg. fail
Normal





In these cases ① My LR is incapable & I will need a more Complex Model.

In order to fit non-linear data pts we will need more Complexity in the model.

$y = mx + c$
 Slope / Intercept
 $y = (\uparrow \text{Complexity}) \rightarrow n \text{ indepen}$
 Mapping function to be more complex
Classification
 Not see today

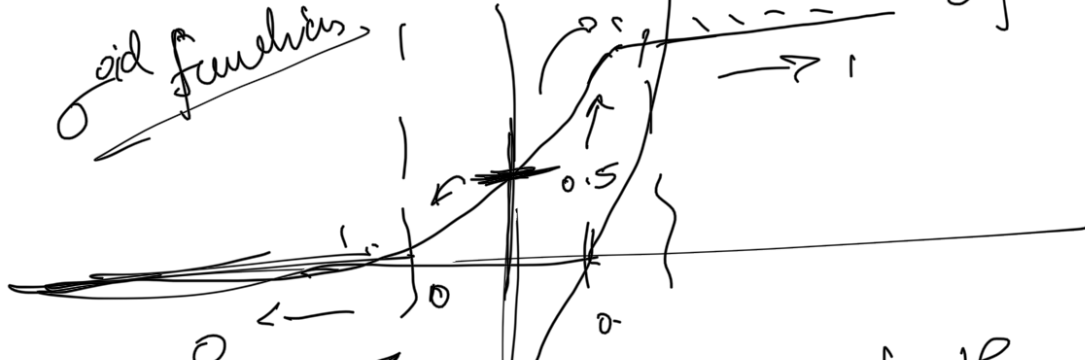
Linear Regression

Squish

0 \longleftrightarrow 1
(Betw.) $\nearrow \infty \searrow$

SIGMOID

oid function

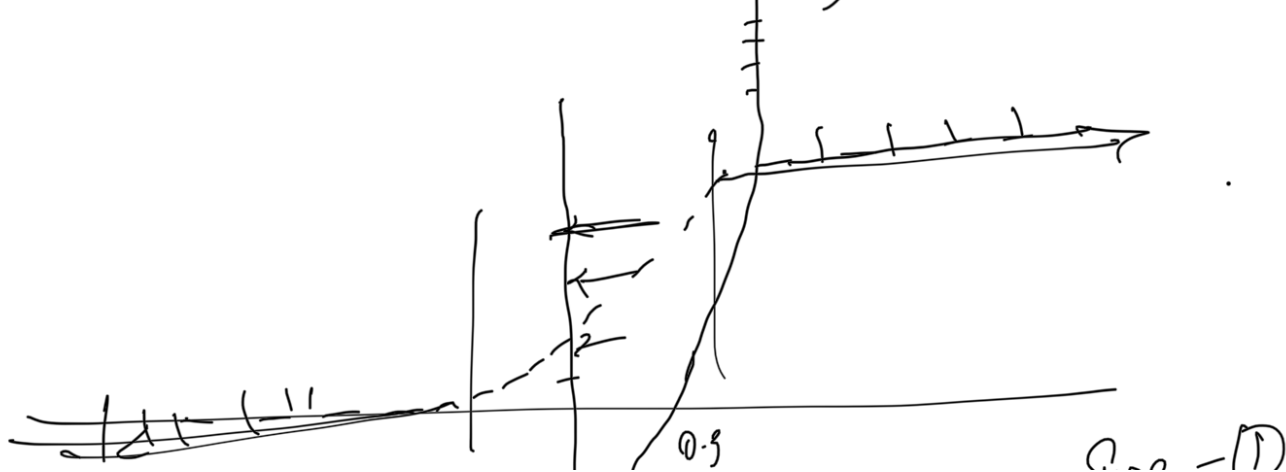


Pass it through
a function called
"Sigmoid fun"
where $y \rightarrow$

$$P = \frac{1}{1 + e^{-y = (mx + c)}}$$

probability
value

$$\frac{1}{1 + e^{-(mx + c)}}$$



y - datapoint \Leftrightarrow probability
 $\frac{P(\text{sure})}{P(\text{total})} \rightarrow$ \rightarrow desired probability
 continuous prediction

sure \rightarrow 0 \rightarrow 1
 $-\infty \rightarrow 0 \rightarrow \infty$

Stock price prediction
 $y \Rightarrow$ Tomorrow stock price
~~5806.23785~~

Given the data should
 & buy tomorrow
 or not

Yes / No.
 0.8 / 0.2
 0.5 / 0.5

Continuous values

Logistic Regression
0 - 1

Where

- (i) Linear Regression would fail
- (ii) Linear Regression would fail in places where continuous o/p's
- (iii) Sigmoid function which maps any L.R o/p from $-\infty \rightarrow \infty$ \rightarrow 0 to 1 probability

→ loss function ???
MSE / SSE → Predict o/p → Expect o/p

I will need a loss fun.
 Blows up when prediction is wrong (∞) → $0 \leftrightarrow 1$
 → would make gradient descent think we are in optimal place already

Case 1 / actual = 0 / predicted value = 0 / Error = 0
 $(1-y) \log(1-\hat{y})$
 $(1-0) \log(1-0)$
 $-\log(1) = 0$

Case 2 / actual = 0 / $\hat{y} = 1$
 $+(1-y) \log(1-\hat{y})$
 $\Rightarrow -1 \log(0) = \infty$

~~$+(1-y) \log(1-\hat{y})$~~ ← $y=1$ $\hat{y}=0$
 Part 1 is working fine for $y=0$ case 0
 $y(\log(\hat{y}))$

Case 3: $y(\log(\hat{y}))$ all $y=1$

$$y=1, \hat{y}=1$$

$$-\log(1) = 0$$

Case 4:

$$y=1, \hat{y}=0$$

$$-\log(0) \Rightarrow \infty$$

$$\Rightarrow -\frac{1}{N} \sum_{i=1}^N \left[y_i \cdot \log(p(\hat{y}_i)) + (1-y_i) \log(1-p(\hat{y}_i)) \right]$$

| actual y | \hat{y} | Error |
|------------|-----------|--------------------------------|
| 0 | 0 | 0 |
| 0 | 1 | ∞ |
| 1 | 1 | 0 |
| 1 | 0 | ∞ |

Probability

$$(1-y) \log(1-\hat{y})$$

$$(y) \log \hat{y}$$

Indicator of how close the predicted probability is to the corresponding original value.

\uparrow higher $\rightarrow \uparrow$ deviation
 \downarrow value $\rightarrow \downarrow$ deviation

(0 or 1) Binary

$x_1 \quad x_2 \quad x_3 \quad x_4 \quad x_5$



$$\frac{0}{1} \bigg/ \frac{1}{0.8} \bigg/ \frac{0.4}{0.4}$$

decision Boundary

Log-loss !!!