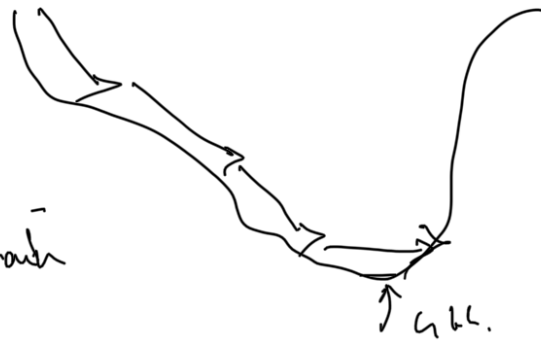


## Bias variance and regularisation

- loss - quantify.
- metrics - quantify.  $\rightarrow$  amount of slip  $\rightarrow$  Global optimum

Is this the final Stand

Performance on train



(1)

Risk Minimizer



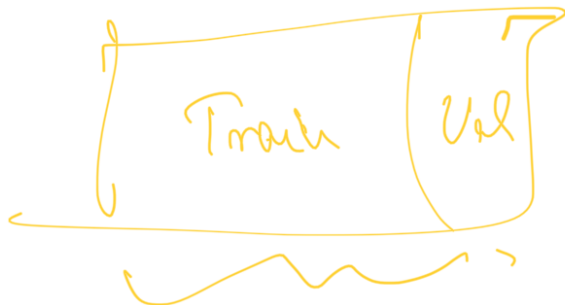
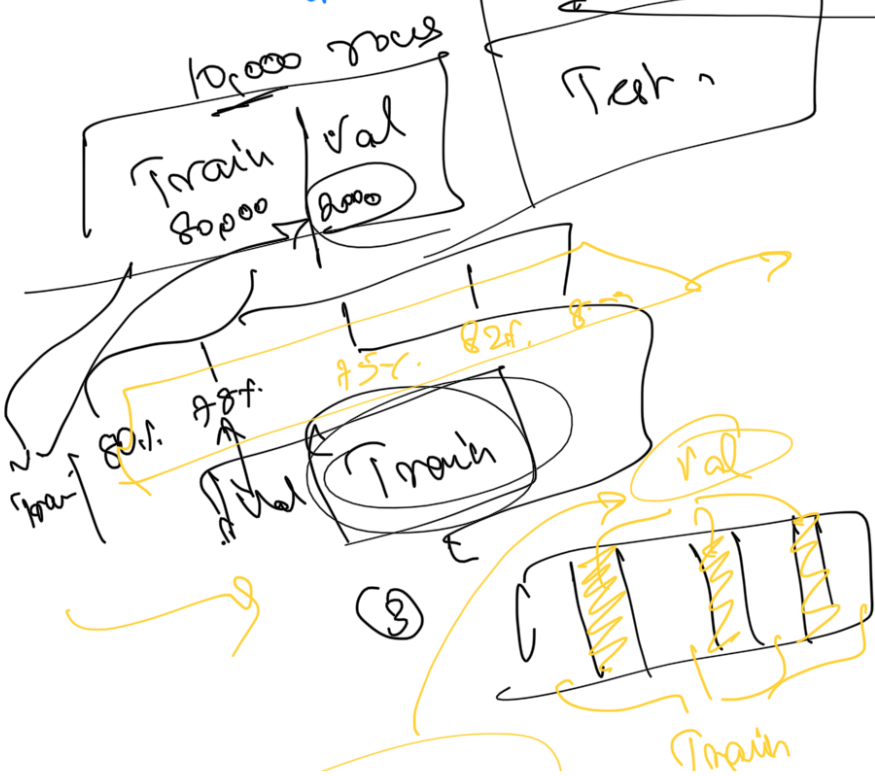
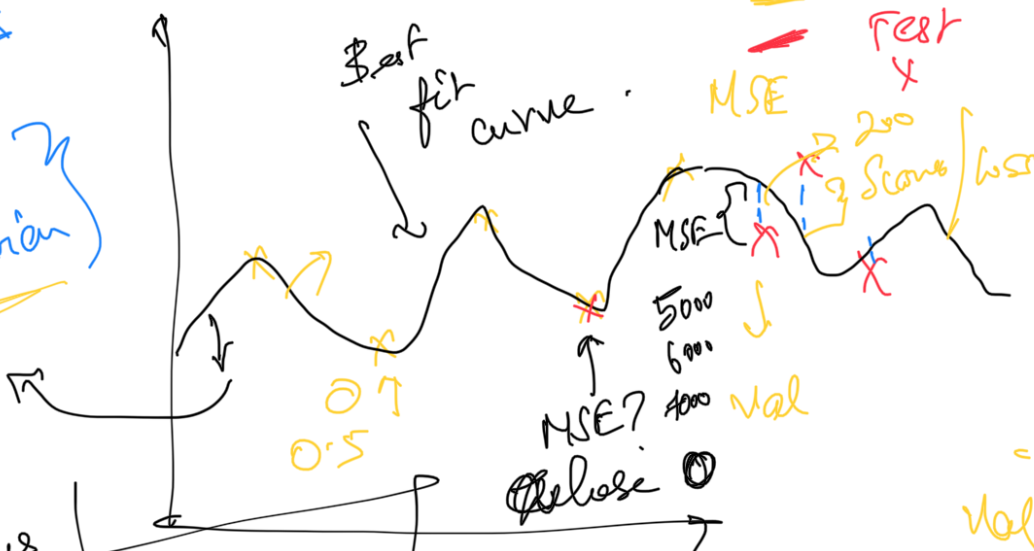
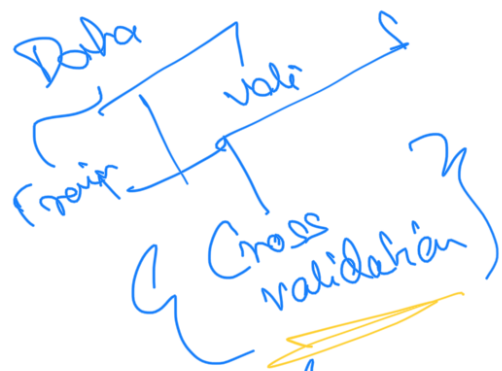
Mapping func.  
has to be compl.  
Perform well

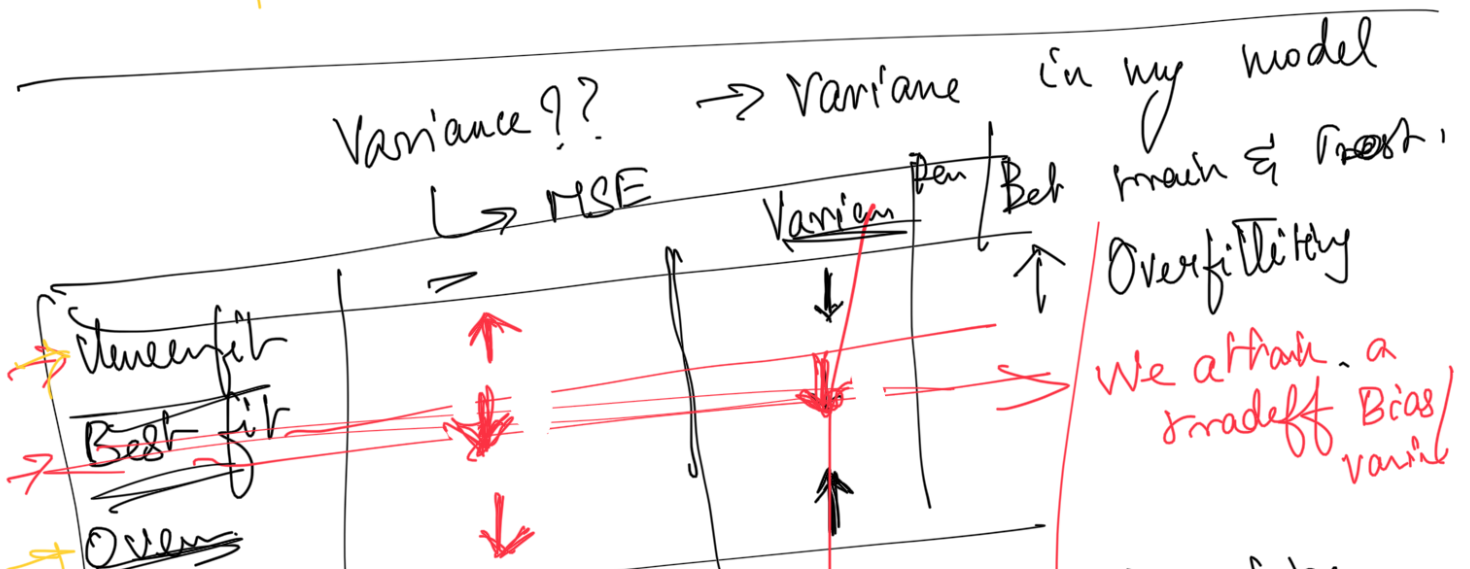
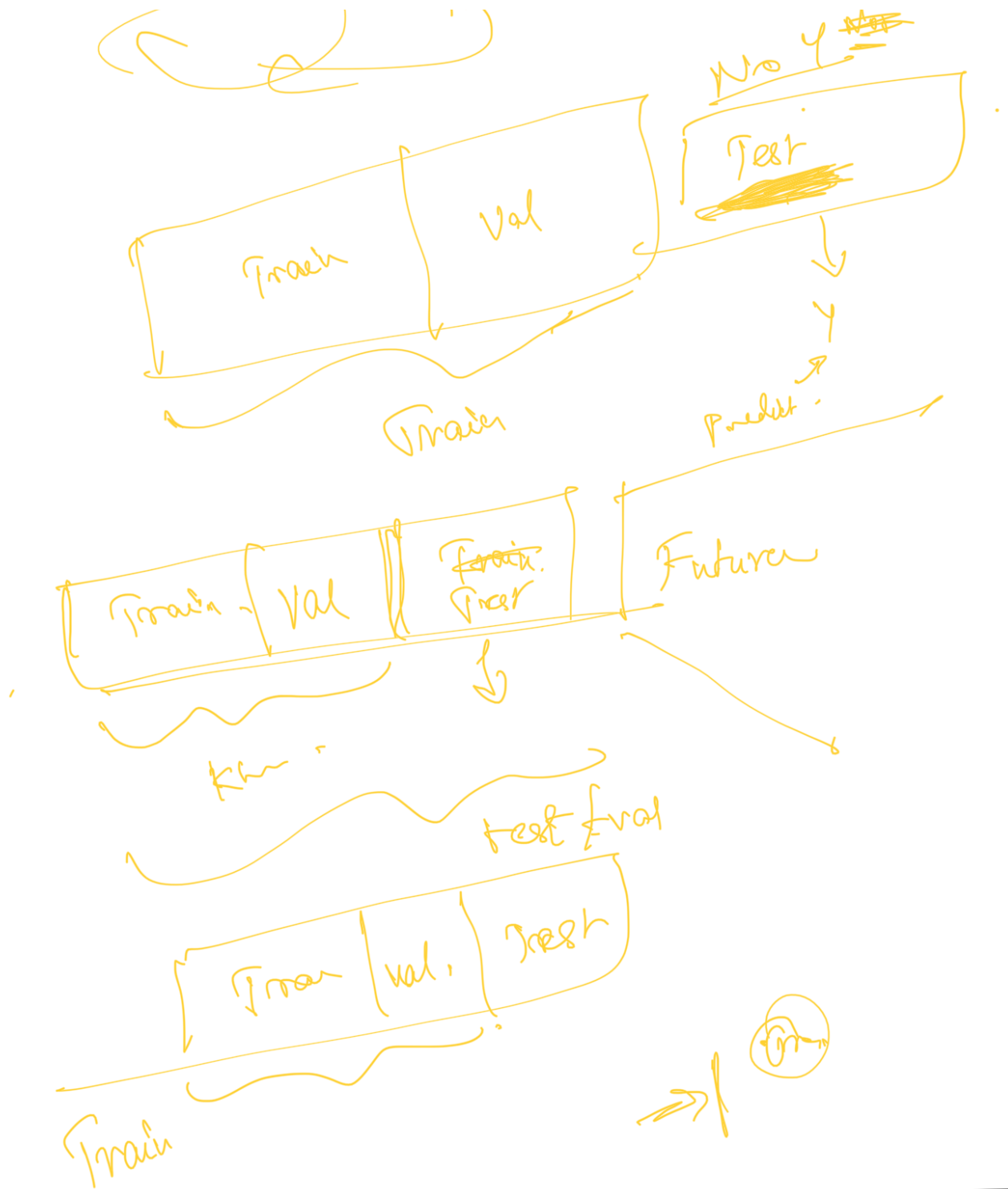


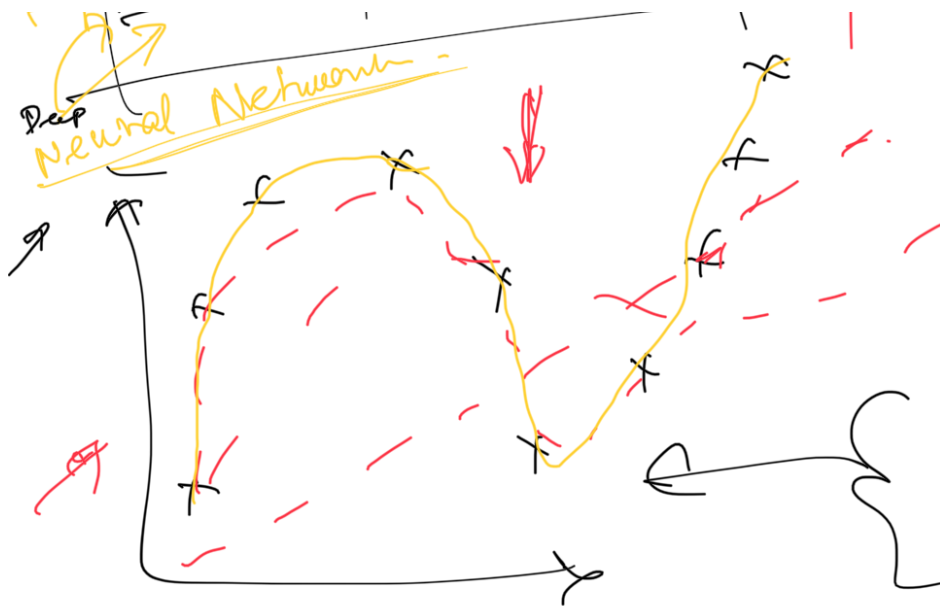
Bad M  
15/

complexity of the model is high.

Very complex -

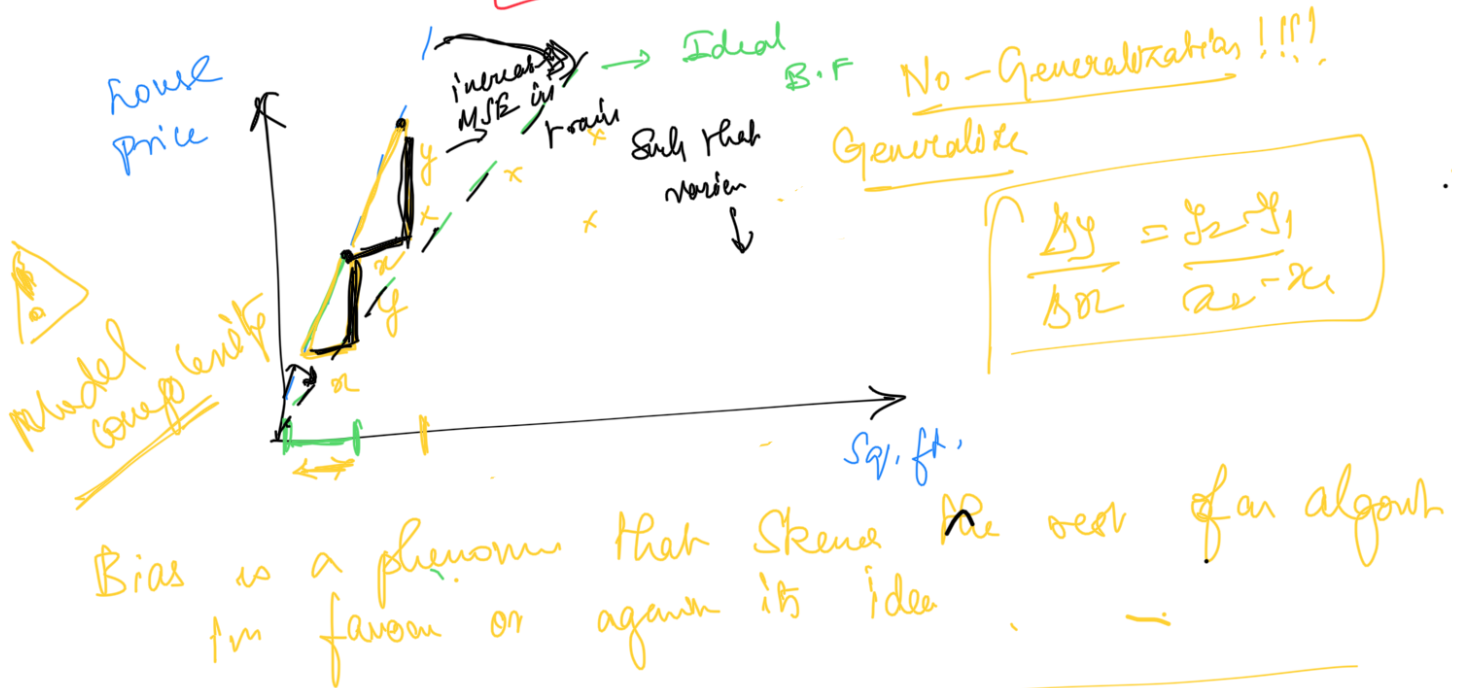






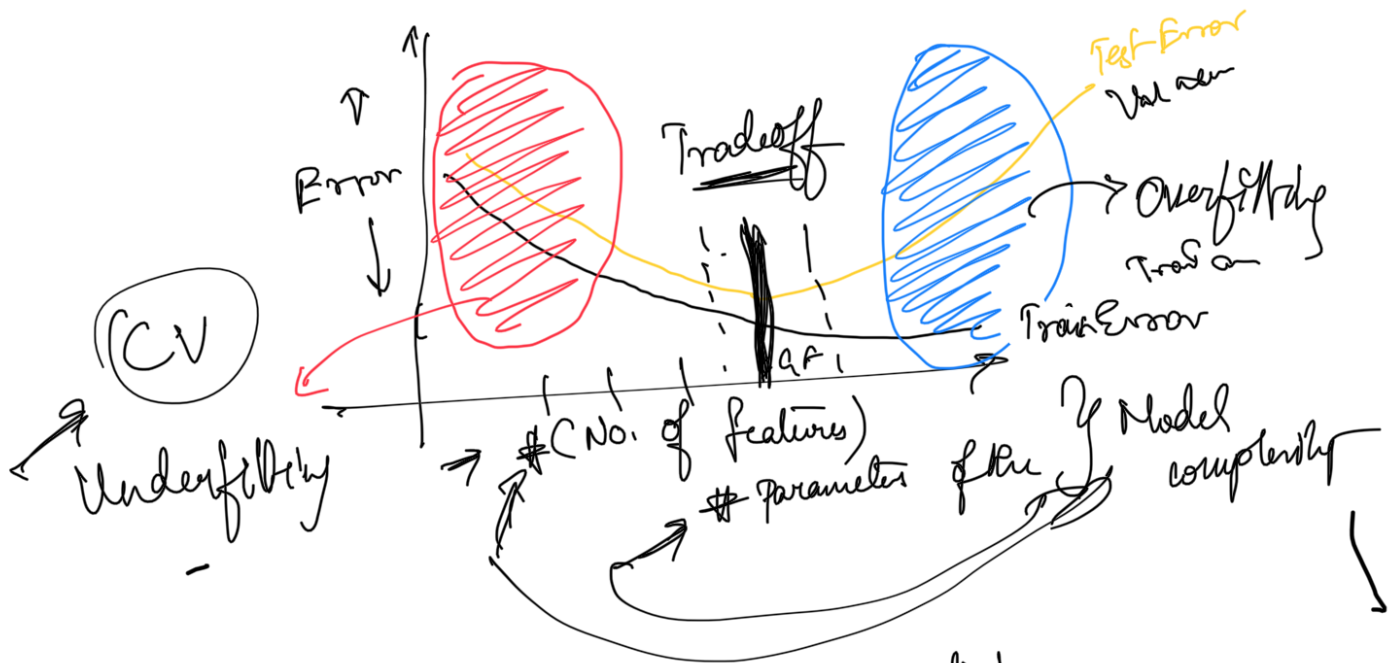
Inductive bias  
 ↓  
 combination of  
 a learning algorithm  
 ↓  
 set of assumptions  
 the learner sees

Bias → Prejudice → ↑ occurs when a model produces  
 ops that are prejudiced due to its assumptions  
 ↓  
 systematic errors  
 does not work in favor of learner as well  
 (variance)  
 Variance → Differs in the Error Bet train & Test

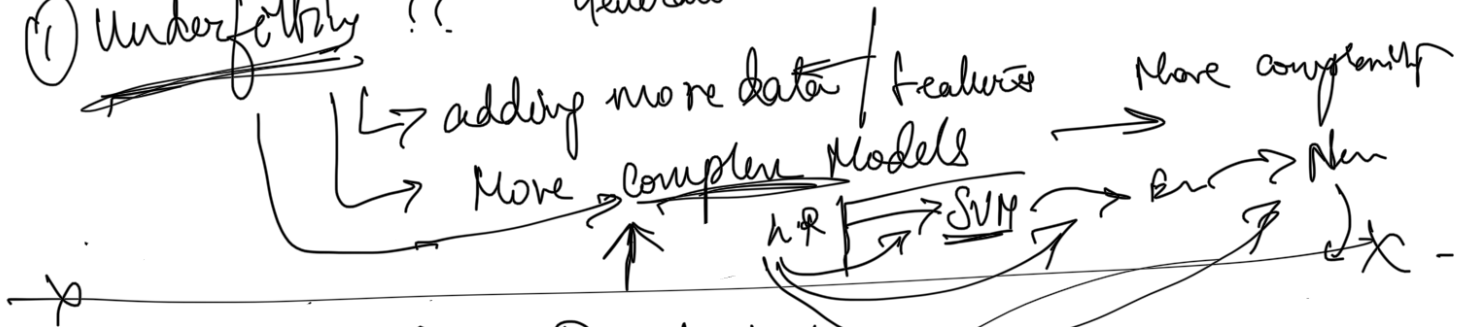


How do we quantify the

⇒ Now



① Underfitting ?? Generalization can be added



② Overfitting ?? → Regularization

My descent is too good on my train.

introduce a bias in my error term

GAD smooth

→ MSE in train ↑  
→ Variance in MSE Bet  
2 Train & Test is down.

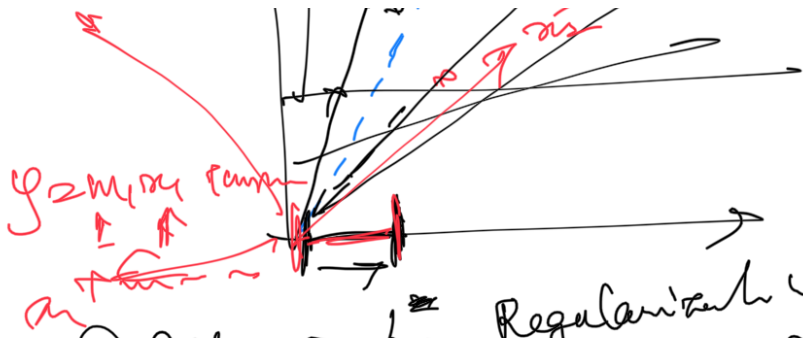
Gradient Descent

loss  $\Rightarrow \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y})^2$



$$\frac{1}{n} \sum_{i=1}^n (y_i - \hat{y})^2 + \lambda \left[ \right]$$





- ① Lasso
- ② Ridge
- ③ Elastic Net

① Ridge  $\rightarrow L_2$  Regularization

$$MSE = \frac{1}{N} \sum_{i=1}^N (y_i - (mx_i + b))^2$$

Penalizing our cost term  
Generalizes

$$\frac{1}{N} \sum_{i=1}^N (y_i - (mx_i + b))^2 + \lambda \sum_{i=1}^p (mx_i + b)^2$$

For Ridge  $\lambda$  is parameter to control  
 $\downarrow$  Training Score  $\uparrow$  Train Test Loss  
 $\downarrow$  Variance  $\downarrow$  Bias (MSE)  $\downarrow$   $T_r$  &  $T_v$

$\rightarrow$  Slopes  $\neq 0$  Ridge!!!  
asymptotically close to 0

Lasso  $|L_1$  Regularization  $L_1$  Regular.

$$\frac{1}{N} \sum_{i=1}^N (y_i - (mx_i + b))^2 + \lambda \sum_{i=1}^p |mx_i + b|$$

The big difference: Ridge vs Lasso Regularization  
 Ridge: Can reduce the slope  
 Lasso: Can shrink the slope to zero

Only useful columns will be retained /  
 Useless columns will be discarded  
 in Lasso



~~Elastic Net~~

$$MSE + \lambda_1(Ridge) + \lambda_2(Lasso)$$

$\lambda_1$   $\lambda_2$   
 $R_1$  /  $R_2$

log-loss

Hinge loss

$L_{\text{ass}}$   
 $L_2$   
 $L_1$   
 $L_2$   
 $\downarrow$   
Ridge