## NegativeWrites Theory: Handling Arithmetic Operations in Goal Attributes

## Approach:

- 1. Given IDB *I* defined by rule set with minimum cardinality 2 in which at least one rule, denoted *R*, possesses a goal attribute contains an arithmetic operation.
- 2. For all rules defining *I*, rewrite the rules to exhibit a uniform goal attribute variable schema, except for appearances of the universal variables in the body such that the variables also appear in head arithmetic expressions.
- 3. Decompose **R** into a series of separate rules.
- 4. Apply NegativeWrites algorithm to the rules defining *I* after establishing a uniform attribute variable list across the defining rules.

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Example:
P:
otherstuff(1,2);
b(1,2);
d(2);
e(2);
f(10,10);
stuff(X,Y):- otherstuff(X,Y), notin a(X,Y);
a(X,Y+1) :- b(X,Y), c(Y);
c(X) := d(X), e(X);
Rewrite 1:
Remove arith ops from heads of rule targeted for NegativeWrites if goal has multiple rule definitions.
a(X,Y+1) :- b(X,Y), c(Y);
≡
a(A0,A1) := a_b(A0,A1), a_c(A1);
a_b(X,Y+1) :- b(X,Y);
a_c(Y+1) :- c(Y);
}
Rewrite 3: Via NegativeWrites
not a(A0,A1): \neg a b(A0,A1), \neg f(A0,A1), dom stuff att0(A0), dom stuff att1(A1)
not_a(A0,A1) := \neg a_c(A0,A1), \neg f(A0,A1), dom_stuff_att0(A0), dom_stuff_att1(A1)
Rewrite 2: B/c a b, a c, and c are IDBs.
not_a_b(A0,A1+1) := dom_not_a_att0(A0), dom_not_a_att1(A1), \neg b(A0,A1);
not_a_c(A0+1) := dom_not_a_att1(A0), not_c(A0);
not_c(A0) := dom_not_a_c_att0(A0), \neg d(A0);
not_c(A0) := dom_not_a_c_att0(A0), \neg e(A0);
```

<sup>\*</sup>Observe the rule definitions for **not\_a\_b** and **not\_a\_c** do not need arithmetic op rewrites because **not\_a\_b** and **not\_a\_c** are defined only by single rules across the entire program. Therefore, rewrites from cross-rule schema uniformity are not necessary.

```
P':
otherstuff(1,2);
b(1,2);
d(2);
e(2);
f(10,10);
stuff(X,Y) :- otherstuff(X,Y), not_a(X,Y)
c(X) := d(X), e(X)
// arithmetic op rewrite
a(A0,A1) :- a_b(A0,A1), a_c(A1);
a_b(X,Y+1) :- b(X,Y);
a_c(Y+1) :- c(Y);
// negated a rewrite
not_a(A0,A1) := not_a_b(A0,A1), \neg f(A0,A1), dom_stuff_att0(A0), dom_stuff_att1(A1)
not_a(A0,A1) := not_a_c(A0,A1), \neg f(A0,A1), dom_stuff_att0(A0), dom_stuff_att1(A1)
// negated a_b and a_c rewrites
not_a_b(A0,A1+1):- dom_not_a_att0(A0), dom_not_a_att1(A1), not_b(A0,A1);
not_a_c(A0+1) := dom_not_a_att1(A0), not_c(A0);
// negated b rewrite
not_b(A0,A1) := dom_not_a_b_att0(A0), dom_not_a_b_att1(A1), \neg b(A0,A1);
// negated c rewrite
not_c(A0) := dom_not_a_c_att0(A0), \neg d(A0);
not_c(A0) := dom_not_a_c_att0(A0), \neg e(A0);
```

(domains from post-processing of evaluation not included for brevity)

## Provenance graph:

